Nitrogen composition dependence of electron effective mass in GaAs1−*x***N***^x*

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We have investigated the N composition, *x*, and temperature, *T*, dependence of the electron effective mass, m^* , of GaAs_{1−*x*}N_{*x*} films with sufficiently low carrier concentration that carriers are expected to be confined to near the bottom of the conduction-band edge (CBE). Using Seebeck and Hall measurements, in conjunction with assumptions of parabolic bands and Fermi-Dirac statistics, we find a nonmonotonic dependence of m^* on x and an increasing T dependence of m^* with x . These trends are not predicted by the two-state band anticrossing model but instead are consistent with the predictions of the linear combination of resonant nitrogen states model, which takes into account several N-related states and their interaction with the GaAs CBE.

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I. INTRODUCTION

Dilute nitride alloys such as GaAsN and InGaAsN are promising for a wide range of applications including laser diodes, high-efficiency solar cells, and high performance bipolar transistors. Earlier studies have shown that the electron mobility of (In)GaAs_{1-*x*}N_{*x*} decreases significantly with N composition, x ^{1-[6](#page-3-2)} presumed to be partly due to the influence of N incorporation on the effective mass, *m* . [3](#page-3-3)[,4](#page-3-4)[,7](#page-3-5)[,8](#page-3-6) There have been conflicting experimental^{3[,7](#page-3-5)[–9](#page-3-7)} and theoretical^{8,[10](#page-3-8)[,11](#page-3-9)} reports on the *x* and temperature, *T*, dependences of *m* . For $x \le 0.005$, m^* was reported to either decrease⁴ or rapidly increase^{3,[7](#page-3-5)[,9](#page-3-7)} with increasing *x*. For $x > 0.005$, m^* is predicted to either increase monotonically, according to the simple band anticrossing (BAC) model,¹¹ or to vary nonmonotonically with a minimum around $x=0.01$ and a maximum around $x=0.02$, according to the linear combination of reso-nant nitrogen states (LCINS) model.^{[10](#page-3-8)} However, experimentally, a *x*-dependent saturation in m^* was reported.⁷ In terms of the *T* dependence, one group has reported measurements showing that m^* decreases monotonically with increasing T^8 T^8 . Here, we have determined the x dependence of m^* , using a combination of *T*-dependent Seebeck and Hall measurements, interpreted in the framework of parabolic conduction bands and Fermi-Dirac statistics. We find a nonmonotonic behavior of m^* with x . Our results are in contrast to the prediction of a simple BAC model¹¹ of a monotonic decrease in m^* with increasing x , but they are very similar to the predicted minimum at $x=0.01$ of the LCINS model¹⁰ and to the experimental values for $x=0.016$ of Ibáñez *et al.*^{[3](#page-3-3)} In addition, our data suggest a more significant *T* dependence with m^* decreasing by \sim 30% from 150 to 300K.

II. EXPERIMENTS

For these studies, GaAs_{1−*x*}N_{*x*} alloy films were grown on (001) GaAs substrates by molecular-beam epitaxy, using Ga, As, GaTe, and a N_2 radio-frequency plasma source with ultrahigh-purity N_2 gas, as described elsewhere.^{5,[12](#page-3-11)} For all samples, a 500-nm-thick buffer layer was grown at 580 °C

on GaAs (001) substrates using a growth and annealing sequence described elsewhere.¹³ Next, an electronically active layer of GaAs(N) was grown at 400 \degree C with targeted Te doping concentrations of $5-13\times10^{17}$ cm⁻³. The buffer and active layers were grown with As to Ga incorporation rate ratios of 1.5[.14](#page-3-13) In all cases, the surface reconstruction was monitored *in situ* with reflection high-energy electron diffraction.

Following growth, *x* in the GaAs_{1−*x*}N_{*x*} films was determined using x-ray rocking curves, interpreted with an interstitial model, as discussed elsewhere.¹⁵ For Hall and magnetotransport measurements, Hall bars $(1050 \times 150 \ \mu m^2)$ were prepared using standard lithography and lift-off processes. For thermoelectric measurements, 5 mm \times 15 mm rectangles were cleaved and In-Sn contacts were applied, and subsequently annealed at 410 °C for 2 min in N_2 atmosphere.

To determine the carrier concentration, we measured the parallel resistivity, ρ_{xx} , and the transverse resistivity, ρ_{xy} , as a function of T (1.6 to 300 K) and magnetic field $(-8 \text{ to } 8 \text{ T})$. For measurements of the Seebeck coefficient, $S = \Delta V / \Delta T$, a current-driven heater and a copper block were attached to each end of the cleaved rectangles. The thermally induced *T* gradients were measured with thermocouples attached to the In-Sn contacts.

III. RESULTS AND DISCUSSION

Figure [1](#page-1-0) shows a plot of *S* as function of *T*, from 2 to 300 K, for GaAs and GaAsN layers. At the lowest *T*, *S* decreases monotonically to a minimum (maximum absolute value) at 12 K, followed by a corresponding monotonic increase up to \sim 100 K. The significant enhancement of *S* in the low-*T* regime is attributed to increased electron-phonon coupling, often termed the "phonon drag" component of *S*. [16](#page-3-15) For GaAs_{1−*x*}N_{*x*} with *x*=0, the maximum |S| is 1000 μ V K⁻¹, and increases with *x*, from 1800 to 3050 μ V K⁻¹ for *x*=0.01 to *x*=0.017.

For $T > 140$ K, for both GaAs and GaAsN, *S* decreases monotonically with *T*, due to electron diffusion driven by the

FIG. 1. (Color online) Seebeck coefficient, *S*, as a function of temperature, *T*, from 2 to 300 K. The significant enhancement in $|S|$ in the low-*T* regime is attributed to increased electron-phonon coupling, often termed phonon drag. For the *T* range from 140 to 300 K, $|S|$ decreases monotonically with T , due to electron diffusion driven by the *T* gradient.

T gradient. To consider the influence of *x* on *S* in this socalled "diffusion" regime, we examine *S* in the *T* range from 140 to 300 K, shown in Fig. $2(a)$ $2(a)$. For GaAs, *S* is negative and decreases monotonically with increasing *T*, consistent with reported values for n -type GaAs.¹⁷ In the GaAsN alloys, *S* is also negative and decreases monotonically with increasing *T*. However, the absolute values of *S* are larger than those of GaAs and the *T* dependence is less significant. In Fig. $2(a)$ $2(a)$, linear least-squares fits to $S(T)$ are shown. For each value of *x* in GaAs_{1−*x*}N_{*x*}, the electron diffusion regime is identified within this *T* range. Interestingly, the low-*T* bound of the electron diffusion regime increases with *x*, from 140 K for GaAs to nearly 200 K for $GaAs_{1-x}N_x$ with $x=0.017$. Since *S* consists of a phonon drag, S_{Ph} , and a electron diffusion, S_{el} , component, the total is $S = S_{Ph} + S_{el}$. With increasing x , the phonon drag component, S_{Ph} , increases, and the S_{Ph} tail extends to higher *T*, presumably due to a shift of the electron diffusion regime to higher *T*.

As shown in Fig. $2(b)$ $2(b)$, the GaAs free carrier concentration, n_s , is *T* independent. For GaAsN alloys grown with nominally identical doping concentration, n_s is approximately an order of magnitude lower than that of GaAs, presumably due to electron trapping at native N-related defect states, e.g., N interstitials.^{12[,18,](#page-3-17)[19](#page-3-18)} In addition, for all the GaAsN alloys, n_s exhibits a gradual monotonic increase with temperature, suggesting the presence and thermal activation of deep-level donors related to N interstitials.¹⁸ In all cases, n_s is sufficiently low that carriers are expected to be confined to near the bottom of the conduction-band edge (CBE). Indeed, the Fermi level, derived using Eq. (2) (2) (2) (below), is within ± 20 meV of the CBE, varying from $+20$ meV (x) $= 0.001$) to -20 meV $(x=0.019)$. Therefore, any nonparabolicity of the CBE is expected to be negligible.

To determine the values of m^* , S is defined in terms of the reduced Fermi level, $\eta = E_F/k_B T$, where E_F is the Fermi level with respect to the CBE, and the electron momentum relaxation time τ_m , as follows:

FIG. 2. (Color online) Electronic properties as a function of temperature, T , are shown from 135 to 300 K. (a) Seebeck coefficient, *S*, for $GaAs_{1-x}N_x$ (left axis) and $GaAs$ (right axis). Linear least-square fits to the data are shown. The low-*T* bound of the electron diffusion regime increases with *x*, from 140 K for GaAs to nearly 200 K for $GaAs_{1-x}N_x$ with $x=0.017$. (b) Free carrier concentration, n_s , for GaAs_{1-*x*}N_{*x*}, and (c) m^* determined from *S* and n_s using assumptions of parabolic bands and Fermi-Dirac statistics. a See Ref. [33.](#page-3-22)

$$
S = \frac{k_B}{e} \left(\frac{\langle \tau_m \eta \rangle}{\langle \tau_m \rangle} - \eta \right). \tag{1}
$$

In general, τ_m is a function of the reduced Fermi level $\tau_m = \tau_0 \eta^r$, where $r = 3/2$ for ionized impurity scattering (GaAs) (Ref. [20](#page-3-19)) and $r=-1/2$ for localized N scattering $(GaAsN)$.^{[5](#page-3-10)} We note that the introduction of N into GaAs has been reported to lead to an order of magnitude decrease in electron mobility.^{2,[3,](#page-3-3)[5](#page-3-10)[,8,](#page-3-6)[18](#page-3-17)[,21](#page-3-21)} Since the majority of N is incorporated substitutionally, it is thus assumed that electrons in GaAsN are primarily scattered by localized states associated with N atoms. Furthermore, LO phonon scattering in GaAs has been reported to be insignificant at room temperature (RT) and to decrease with decreasing temperature;^{22[,23](#page-3-24)} therefore, it is not expected to be significant in GaAsN at low *T*. *S* is then simplified to

$$
S = \frac{k_B}{e} \left[\frac{(r + 5/2)}{(r + 3/2)} \frac{F_{r+3/2}(\eta)}{F_{r+1/2}(\eta)} - \eta \right],
$$
 (2)

where $F_j(\eta)$ is the *j*th Fermi integral given as

$$
F_j(\eta) = \frac{1}{j!} \int_0^{\infty} \frac{E^j}{e^{(E - E_F)/k_B T} + 1} dE.
$$
 (3)

Using Fermi-Dirac statistics, the free carrier concentration is written as

$$
n = 2\left(\frac{m^*k_BT}{2\pi\hbar^2}\right)^{3/2} F_{1/2}(\eta)
$$
 (4)

and the effective mass becomes

$$
m^* = \frac{2\pi\hbar^2}{k_B T} \left[\frac{n}{2F_{1/2}(\eta)} \right]^{2/3}.
$$
 (5)

For GaAs, using the values of *S* and *n*, shown in Figs. $2(a)$ $2(a)$ and $2(b)$ $2(b)$, and solving for η in Eqs. (2) and ([5](#page-2-1)), we find a RT value of m^* of 0.048 ± 0.019 times the free-electron mass (m_e) and a monotonic decrease in m^* with increasing $T(19\%$ from 140 to 300 K), as shown in Fig. $2(c)$ $2(c)$. Similar RT values of m^* were obtained by other groups using indirect experimental methods, including analysis of electric susceptibility and Shubnikov de Haas measurements. $24-26$ However, a larger RT m^* value, 0.067 m_e , was observed via direct experimental methods, such as cyclotron resonance, Faraday rota-tion, and Faraday oscillation.^{27[–30](#page-3-28)} In addition, a significantly smaller gradient in the monotonic *T*-dependent decrease in m^* is typically observed,^{27[,30–](#page-3-28)[32](#page-3-29)} consistent with the calculations of the dilatational change in the energy gap in GaAs by Stradling and Wood.³³ Overall, at room temperature, our GaAs m^* is within 20% of literature values, and the estimated error in m^* , $\pm 0.019m_e$, is negligible compared to the variations in the GaAsN m^* (from 0.084 m_e to 0.164 m_e).

For GaAsN, m^* is larger than that of GaAs, and decreases monotonically with increasing *T*. Similar low-*T* values for *m*^{*} in GaAsN were reported in Refs. [7](#page-3-5) and [9.](#page-3-7) The significant *T* dependence of m^* in GaAsN is likely due to a nonparabolic perturbation in the electron dispersion relation, leading to a local increase in m^* . In PbTeTl, 34 a similar temperature dependence of *S* and m^* were reported, and attributed to an isolated Tl energy level in close proximity to the PbTe CBE. In addition, a maximum of m^* was observed at 230 K and attributed to a resonance between the Tl state and the PbTe CBE.

In both GaAs and GaAsN, it appears that the phonon drag component of *S* (for $T < 150$ K), shown in Fig. [1,](#page-1-0) contributes to a small artificial increase in *m* . Indeed, significant decreases in *S* are observed for $T < 150$ K with the most significant decreases for $T < 100$ K. The lower *S* value leads to an increase in E_f , and a subsequently smaller m^* [see Eqs. (2) (2) (2) and (5) (5) (5)].

FIG. 3. (Color online) Effective mass, m^* , vs N composition, x , for as-grown bulk GaAs1−*x*N*x*. "This work" values are given at RT; Ibáñez *et al.* are extracted by Raman spectroscopy at 80 K; Masia *et al.* from magnetophotoluminescence at 20 K; Young *et al.* from magnetotransport at RT; Lindsay *et al.* from the LCINS model at low *T*; and Shan et al. (dashed line) from the two-state BAC model at low *T*. ^bSee Ref. [3.](#page-3-3) ^cSee Ref. [7.](#page-3-5) ^dSee Ref. [4.](#page-3-4) ^eSee Ref. [10.](#page-3-8) ^fSee Ref. [11.](#page-3-9)

The influence of x on m^* is shown in Fig. [3.](#page-2-2) For $x \le 0.005$, an increase in the m^* with increasing x up to $x=0.04$,^{[3,](#page-3-3)[7](#page-3-5)} and subsequent saturation beyond $x=0.005$ (Ref. [7](#page-3-5)) have been reported experimentally. The rapid increase up to *x*=0.004 is in good agreement with the predictions of the LCINS model.^{7,[10](#page-3-8)} For $x > 0.005$, the LCINS model predicts nonmonotonic behavior of m^* with increasing x , with a minimum at $x=0.010$ and a maximum at $x=0.018$. The oscillatory dependence of m^* on x was explained by a strong hybridization of states arising from N clusters near the CBE of GaAs,^{[10](#page-3-8)} leading to a large locally increased m^* in GaAsN.

Our RT *m*^{*} values for GaAs_{1−*x*}N_{*x*} films are in good agreement with low-temperature values predicted by the LCINS model¹⁰ and those from other experimental reports.^{3,[7](#page-3-5)} For a limited composition range $(x=0.010-0.015)$, our RT m^* values are also in agreement with those predicted by the BAC model.¹¹ Indeed, the temperature dependence of m^* is apparently negligible. As the temperature is reduced from 300 to 0 K, the relative energies of the nitrogen-induced localized states and the CBE are shifted by approximately 36 meV.⁶ Since the *x* values investigated range from 0.001 to 0.019, a negligible temperature dependence of the *x* values at which the localized state-CBE resonance induced increase in effective mass is expected.

For the lowest *x* values, $x=0.001$ and $x=0.006$ $(m^*=0.114m_e)$ is consistent with the maximum at $x=0.005$ $(m^*=0.15m_e)$, predicted by the LCINS model. In addition, we find a local minimum at $x=0.013$ $(m^*=0.084m_e)$, which agrees very well with the LCINS-predicted minimum at $x=0.010$ ($m^*=0.1m_e$). We also find a local maximum at $x=0.017$ ($m^*=0.164m_e$) which is in very good agreement with the LCINS-predicted maximum at *x*=0.018 $(m^*=0.18m_e)$. Indeed, our observed nonmonotonic increase in m^* with *x* agrees very well with the *x* dependence (maxima at $x=0.004$ and $x=0.018$, minimum at $x=0.010$)

predicted by the LCINS model. Our m^* values are also in good agreement with experimental values from Masia *et al.*[7](#page-3-5) for $x=0.014$ but are significantly lower for $x=0.011$. The discrepancy for $x=0.011$ can be resolved with corrections for *x* from the interstitial model by Reason *et al.*^{[15](#page-3-14)} shifting m^* values by Masia *et al.* to higher *x*. In the very dilute limit, the decrease in *m* , reported by Young *et al.*, [4](#page-3-4) is likely to be an artifact of the parabolic band-structure assumption for highly doped GaAsN.

IV. CONCLUSION

In summary, we have determined the *T* dependence of *m* for a set of $GaAs_{1-x}N_r$ alloy films with *x* values ranging from 0 to 0.018. We observe a nonmonotonic dependence of *m on* x and an increasing m^* *T* dependence with *x*, both of which cannot be explained by a simple two-state BAC model. Instead, the data is in good agreement with the LCINS model, which takes into account several N-related states and their interaction with the GaAs CBE.

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