Nucleation of Ge quantum dots on the Si(001) surface

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A direct observation of nucleation of Ge hut clusters formed by ultrahigh-vacuum molecular-beam epitaxy is reported. The nuclei of the pyramidal and wedgelike clusters have been observed on the wetting layer blocks and found to have different structures. The growth of the clusters of both species goes on following different scenarios: Formation of the second atomic layer of the wedgelike cluster results in rearrangement of its first layer. Its ridge structure does not replicate the structure of the nucleus. The pyramidal cluster grows without phase transitions. The structure of its vertex copies the structure of the nucleus. The wedgelike clusters contain point defects on the triangular faces and have preferential directions of growth along the ridges.

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Arrays of densely packed self-assembled Ge quantum dots (QDs) on the $Si(001)$ $Si(001)$ $Si(001)$ surface (Fig. 1) (Refs. 1 and [2](#page-4-2)) due to the phenomenon of quantum confinement of carriers are currently considered as a basis for development of pro-spective devices of photoelectronics.^{3,[4](#page-4-4)} Extensive investigations carried out for the last two decades (see, e.g., Refs. $5-12$ $5-12$) resulted in the technological achievements of the recent years that enabled the controllable formation of Ge QD arrays with the desired cluster densities (up to 10^{12} cm⁻², Refs. [1](#page-4-1) and [2](#page-4-2)). However, the problems of uniformity of cluster types in the arrays and the dispersion of cluster sizes are still far from solution. That is why the intensive investigations of the cluster morphology and growth process with view of reproducible formation of uniform and defectless QD arrays are strongly required. This is an issue of special importance for the ordered QD arrays¹² taking into account extremely exacting restrictions imposed on the uniformity by

FIG. 1. STM images of Ge (a) pyramidal and (b) wedgelike clusters, (c) Ge QD dense array $(h_{\text{Ge}} = 10 \text{ \AA})$ on the Si (001) surface, and (d) a fraction of wedges (\blacksquare) and pyramids (\square) in the arrays vs Ge coverage $(T_{\text{gr}}=360 \text{ °C})$.

the aim of development of such arrays. Nonuniform ordered array composed of clusters of different types and sizes would not operate as three-dimensional crystal of artificial atoms or even would not reproduce regularity in successive QD layers if containing defects such as large and extended clusters or depleted regions.¹³

Recently we showed that the ${105}$ faceted clusters usually referred to as hut clusters⁵ are subdivided into two main *morphologically different* species—pyramids and wedges $(Fig. 1)²$ $(Fig. 1)²$ $(Fig. 1)²$ $(Fig. 1)²$ $(Fig. 1)²$ In the literature, both species of hut clusters are traditionally considered as structurally identical and geneti-cally connected types.^{5[,11](#page-4-8)} Explanations of transitions from square shaped to elongated islands (from pyramids to wedges in our terminology) are discussed^{7-[9](#page-4-10)} although no clear observations of such phenomenon have been described anywhere. Different models from simple coalescence of neighboring square shaped clusters⁷ to more sophisticated kinetic model of growth 8 have been brought forward which are in satisfactory agreement with observations. We found that at moderate growth temperatures the densities of clusters of both species are equal at the initial stage of the array formation [Fig. $1(d)$ $1(d)$]. Then, as the Ge coverage is increased, the wedges become dominating in the arrays whereas the pyramids exponentially rapidly disappear. $2,14$ $2,14$ Lately we investigated by scanning tunnel microscope (STM) the structure of the ${105}$ cluster facets together with the structure of apexes (ridges and vertices) of the clusters and built structural models of both species of huts. 15 We found the structure of the ridges of the wedgelike clusters to be different from the structure of the vertices of the pyramidal ones, therefore a wedgelike cluster cannot arise from a pyramidal one and vice versa[.2](#page-4-2)[,15](#page-4-13) Transitions between the shapes of the hut clusters are prohibited.¹⁶ One can find additional evidences of the above strong statement investigating the cluster nucleation and the initial stage of its growth by *in situ* STM with high enough resolution.

At present, nucleation of Ge clusters on the $Si(001)$ surface is still very little studied. Probably only two direct observations of this phenomenon were reported by Goldfarb *et al.*[7](#page-4-9)[,17](#page-4-15) and Vailionis *et al.*[18](#page-4-16) Those comprehensive *in situ* STM studies explored gas-source-molecular-beam-epitaxy $(GS-MBE)$ growth of Ge on $Si(001)$ in the atmosphere of GeH₄ (Refs. [7](#page-4-9) and [17](#page-4-15)) or Ge_2H_6 .^{[18](#page-4-16)} The chemistry of GS-MBE is obviously strongly different from that of ultrahigh-

FIG. 2. (a) STM empty-state image of Ge QD array $(h_{\text{Ge}}=6 \text{ Å}, T_{\text{gr}}=360 \text{ °C})$ on the Si(001) surface; (b) $p(2\times 2)$ structure within the WL block, upper Ge atoms of the tilted dimers are resolved in the rows; (c) pyramid (left) and wedge nuclei (1 ML) on the neighboring WL blocks, both nuclei reconstruct the WL surface, a nucleus never exceeds the bounds of a single WL block.

vacuum (UHV) MBE which is usually employed for Ge deposition on Si substrates[.4](#page-4-4) Unfortunately, experimental and especially direct high-resolution UHV STM investigations of Ge cluster nucleation and early stages of the cluster growth on $Si(001)$ by UHV MBE have not been described in the literature thus far. No data are available on the morphology of nuclei and the beginning of cluster growth. Now we shall try to fill up this gap.

In this paper, we investigate the nucleation and very beginning of growth of Ge hut clusters composing dense QD arrays formed by UHV MBE at moderate temperatures. The atomic structure of cluster nuclei as well as the structures of very little clusters-as small as a few monolayers (MLs) high over the wetting layer (WL)—are the issues of this study.¹⁹

The results reported in the paper evidence that there are two different types of nuclei on Ge wetting layer which evolve in the process of Ge deposition to pyramidal and wedgelike hut clusters. It might seem that solid proofs of this statement can be only obtained from STM measurements during growth.^{7[,8](#page-4-11)} Unfortunately, such experiment is hardly possible now. STM operating at the growth temperatures cannot assure atomic resolution which is necessary to reveal an atomic structure of clusters and smaller objects on WL. We have made a different experiment. Having assumed that nuclei emerge on WL as combinations of dimer pairs and/or longer chains of dimers in epitaxial configuration²⁰ and correspond to the known structure of apexes specific for each hut species^{2[,15](#page-4-13)} we have investigated WL patches, 1 ML high formations on them and clusters of different heights (number of steps) over WL. This approach exactly simulates the above experiment ensuring the required high resolution. As a result, we succeeded to select two types of formations different in symmetry and satisfying the above requirements, which first appear at a coverage of \sim 5 Å (T_{gr} =360 °C) and then arise on WL during the array growth. We have interpreted them as hut nuclei, despite their sizes are much less than those predicted by the first-principles calculations, $2¹$ and traced their evolution to huts.²²

The experiments were carried out using an ultrahighvacuum instrument consisting of the UHV MBE chamber coupled with high-resolution STM which enables the sample study at any stage of processing sequentially investigating the surface and giving additional treatments to the specimen; the samples never leave UHV ambient during experiments.

Silicon substrates (*p*-type, $\rho = 12 \Omega$ cm) were completely deoxidized as a result of short annealing at the temperature of \sim 925 °C.^{[23](#page-4-21)} Germanium was deposited directly on the atomically clean $Si(001)$ surface from the source with the electron-beam evaporation.² The rate of Ge deposition was \sim 0.1 A/s and the Ge coverage (h_{Ge}) (Ref. [24](#page-4-22)) was varied from 3 to 14 Å. The substrate temperature T_{gr} was 360 °C during Ge deposition. The rate of the sample cooling down to the room temperature was $\sim 0.4 \degree C/s$ after the deposition. The temperature was monitored with tungsten-rhenium thermocouple mounted in vacuum near the rear side of the samples and *in situ* graduated beforehand against the IMPAC IS 12-Si pyrometer which measured the sample temperature through the chamber window. Specimens were scanned at room temperature in the constant tunneling current (I_t) mode. The STM tip was zero biased while a sample was positively or negatively biased (U_s) . The details of the sample preparation as well as the experimental techniques can be found elsewhere[.2,](#page-4-2)[23,](#page-4-21)[25](#page-4-23)

FIG. 3. Nuclei of Ge hut clusters: [(a) and (c)] STM empty-state images and $[(b)$ and $(d)]$ atomic structures of the $[(a)$ and $(b)]$ pyramid and $[(c)$ and $(d)]$ wedge nuclei, 1 is WL.

FIG. 4. (a) STM empty-state micrograph of the 5 ML Ge pyramid $(h_{Ge} = 6 \text{ Å}, T_{gr} = 360 \text{ °C})$, (b) a top view of the pyramidal QD and (c) a contrasted image of its vertex; (d) STM empty-state topograph $(h_{\text{Ge}}=6 \text{ Å}, T_{\text{gr}}=360 \text{ °C})$ of the 2 ML Ge wedgelike cluster, (e) a top view of the wedgelike QD and (f) an empty-state image of the ridge of the 3 ML Ge wedgelike cluster; 1, 2, and 3 designate WL, the first and the second layers of QD, respectively, d marks a defect arisen because of one translation uncertainty of the left dimer pair position.

Figure $2(a)$ $2(a)$ presents an STM image of an array of small Ge clusters grown at $T_{\text{gr}}=360$ °C and $h_{\text{Ge}}=6$ Å. WL is seen to have a block $(M \times N)$ patched) structure. The blocks are usually $p(2 \times 2)$ $p(2 \times 2)$ $p(2 \times 2)$ reconstructed [Fig. 2(b)].^{[26](#page-4-24)} We suppose that the process of the cluster nucleation consists in formation of new structures on the WL blocks. These 1 ML high structures are well resolved in Fig. $2(c)$ $2(c)$ on the neighboring WL blocks: the left feature is assumed to be a nucleus of the pyramid whereas the right one is considered as a nucleus of the wedgelike cluster. A good few of such structures are observed in the long shot of the array [Fig. $2(a)$ $2(a)$]. STM images of the nuclei and their schematic plots are given in Fig. [3.](#page-1-1) The further growth of the clusters is shown in Fig. [4.](#page-2-0) Figure $4(a)$ $4(a)$ presents an STM image of the 5 ML high pyramid. It is commonly adopted that the hut clusters grow by successive filling the (001) terraces of the $\{105\}$ faces by the dimer rows.⁸ A schematic plot of the 2 ML pyramid based on this assumption [Fig. $4(b)$ $4(b)$] demonstrates its atomic structure [even number of layers is shown in both (a) and (b) pictures, so the diagram reproduces the entire structure of the dot except for its height]. It is seen comparing Figs. $3(a)$ $3(a)$ and $4(c)$ $4(c)$ that the vertex repeats the structure of the nucleus drawn in Fig. $3(b)$ $3(b)$.^{[28](#page-4-25)} The characteristic distances exactly match. The (100) direction of the base sides is predetermined by the nucleus structure, thus the pyramids grow without phase transition when the second and subsequent layers are added. Only nucleuslike structures of their apexes are rotated 90°

with respect to the rows on previous terraces to form the correct epitaxial configuration when the heights are increased by 1 ML but this rotation does not violate the symmetry of the previous layers of the cluster.

A different scenario of growth of the wedgelike clusters have been observed. Figures $4(d)$ $4(d)$ and $4(e)$ show an image and a schematic of the 2 ML wedgelike cluster. The ridge structure is seen to be different from the nucleus structure presented in Figs. $3(c)$ $3(c)$ and $3(d)$. The structure of the ridge is well resolved in the image of the 3 ML cluster [Fig. $4(f)$ $4(f)$] filtered to contrast the uppermost layer of atoms. In this image, the dimer pairs of the ridge are 90° rotated compared to the 2 ML wedge that is in full agreement with the proposed atomic model[.29](#page-4-26) This structure of the wedgelike cluster arise due to rearrangement of rows of the first layer in the process of the second layer formation (Fig. [5](#page-3-0)). The phase transition in the first layer generates the base with all sides directed along the $\langle 100 \rangle$ axes which is necessary to give rise to the $\{105\}$ faceted cluster [it is seen from Figs. [3](#page-1-1)(c) and 3(d) that only one pair of sides of a wedge nucleus runs along the (100) direction]. After the transition, the elongation of the elementary structure is possible only along a single axis which is determined by the symmetry and clearly seen when comparing Figs. $4(e)$ $4(e)$ and $5(b)$ $5(b)$ [along the arrows in Fig. $5(b)$]. This preferential growth direction determines the rapid growth on the triangular facets (short edges). The growth on these facets does not change the orientation of the dimer

FIG. 5. Rearrangement of the (a) first layer of a forming wedge during addition of dimer pairs of the (b) second layer; labels are the same as in Fig. [4.](#page-2-0) FIG. 6. Schematic drawing of the $\{105\}$ facet superimposed on

pairs forming the ridge. It is obviously also that it cannot increase the cluster height but only its length. The increase in the cluster height is governed by the completion of the trapezoidal facet. 30 The latter process is accompanied by the change in direction of the dimer pairs on the ridge when the apex terrace is completed. Note that the phenomenon of the wedge height limitation described in Ref. [2](#page-4-2) differs from the process of its length self-limitation. The former is mainly controlled by the growth temperature and the later is governed by either the area of the trapezoidal faces or the number and/or sizes of the WL blocks covered by the elongating cluster, as well as the competition of the processes of the in-height and longitudinal growth. In general, the cause of the wedge elongation is still unclear now.

It is necessary to remark here that the nuclei are always observed to arise on sufficiently large WL patches. There must be enough room for a nucleus on a single patch. A nucleus cannot be housed on more than one patch. So, cluster nucleation is impossible on little (too narrow or short) patches [Fig. $2(a)$ $2(a)$].

It should be noted also that according to the proposed model the wedgelike clusters always contain point defects on the triangular (short) facets. The defects are located in the upper corners of the facets and caused by uncertainty of one translation in the position a dimer pair which forms the penultimate terrace of the triangular facet [Figs. $4(d) - 4(f)$ $4(d) - 4(f)$]. The predicted presence of these defects removes the degeneracy of the facets and hence an issue of the symmetry violation which occur if the pyramid-to-wedge transition is assumed (this issue was discussed in detail in Ref. 2). These defects are absent on the facets of the pyramidal huts. Their triangular facets are degenerate. Therefore, as it follows from our model, the trapezoidal and triangular facets of the wedge are not degenerate with respect to one another even at very beginning of cluster growth. The wedges can easily elongate by growing on the triangular facets faster than on trapezoidal ones, whereas pyramids, having degenerate facets, cannot elongate and grow only in height outrunning wedges. This explains greater heights of pyramids.²

The proposed models being applied to draw the clusters by filling terrace by terrace (like it is done in Fig. [4](#page-2-0)) allowed us to deduce a model of the ${105}$ facets. This model resulting from the above simple crystallographic consideration corresponds to the⁵ paired dimers (PDs) rather than more recent rebonded step (RS) model^{10[,11](#page-4-8)} which is now believed

its STM image $(4.3 \times 4.4 \text{ nm}^2, U_s = +3.0 \text{ V}, I_t = 100 \text{ pA})$, the cluster base side is parallel to the $[100]$ direction, the steps rise from the lower right to the upper left corner.

to improve the previous PD model by Mo *et al.* Being superposed with the empty-state STM image of the cluster 105 facet it demonstrates an excellent agreement with the experiment (Fig. [6](#page-3-1)). Dangling bonds of the derived in such a way ${105}$ -PD facets in reality may stimulate Ge atom addition and cluster growth. Less stability of the ${105}$ -PD facets compared to the $Ge(105)/Si(105)$ -RS plane may cause fast completion of hut terraces during epitaxy.

It should be noticed also that, as it follows from the reported models, the growth of the wedge second layer requires reconstruction of the buried previous layer. This phenomenon has been discussed theoretically before as "critical epinucleation" on reconstructed surface.²⁰ In particular, the atomic models drawn in Figs. $4(e)$ $4(e)$ and [5](#page-3-0) show the ad-dimer rows unreconstructing the surface layer that can only happen beyond a critical number of ad-dimers defined as "epinucleus." So, the presented data could be one of the first experimental evidence of the epinucleus. The critical epinucleation appears to be a basic phenomenon for hut formation on $(M \times N)$.

In conclusion, we have reported the direct observation of nucleation of Ge hut clusters formed by UHV MBE on the Si surface. The nuclei of the pyramidal and wedgelike clusters have been observed on the wetting layer $(M \times N)$ patches and found to have different structures. The atomic models of nuclei of both species of the hut clusters have been built as well as the models of the clusters at the early stage of growth. The growth of the clusters of each species has been demonstrated to follow generic scenarios. The formation of the second atomic layer of the wedgelike cluster results in rearrangement of its first layer. Its ridge structure does not repeat the structure of the nucleus. The pyramidal cluster grows without phase transitions. The structure of its vertex copies the structure of the nucleus. The cluster of one species cannot turn into the cluster of the other species. The wedgelike clusters contain point defects in the upper corners of the triangular faces and have preferential directions of growth along the ridges. The derived structure of the $\{105\}$ facet corresponds to the PD model. The critical epinucleation phenomenon may be responsible for hut formation on $(M \times N)$ patched WL.

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- 29A complete set of ridge configurations arising during the wedge height growth can be easily obtained when drawing schematic plots of a growing wedge by serial—layer by layer from bottom to top—completion of its terraces.
- 30 Of course, the triangular facets also grow by the same number of layers as trapezoidal ones in the process of the in-height growth of a wedge, otherwise the whole crystalline structure of the cluster would be disturbed. As distinct from the in-height growth, rapid growth of the triangular facets, which is responsible for cluster elongation, does not cause the growth of the trapezoidal facets.