Location of gap nodes in the organic superconductors κ -(ET)₂Cu(NCS)₂ and κ -(ET)₂Cu[N(CN)₂]Br determined by magnetocalorimetry

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We report specific-heat measurements of the organic superconductors κ -(ET)₂Cu(NCS)₂ and κ -(ET)₂Cu[N(CN)₂]Br. When the magnetic field is rotated in the highly conducting planes at low temperature ($T \approx 0.4$ K), we observe clear oscillations of specific heat which have a strong fourfold component. The observed strong field and temperature dependence of this fourfold component identifies it as originating from nodes in the superconducting energy gap which point along the in-plane crystal axes (d_{xy} symmetry).

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I. INTRODUCTION

The organic charge-transfer salts with general formula κ -(ET)₂X [where ET stands for bis(ethylenedithio)tetrathiafulvalene] have attracted considerable interest because of their unconventional properties. Like the high- T_c cuprates this family of quasi-two-dimensional materials exhibit a low-temperature superconducting ground state which is in close proximity to an antiferromagnetically ordered Mott insulating state. The position of the various members of the series in the phase diagram is determined by the "chemical pressure" exerted by the anion X. There is considerable evidence that the superconductivity is unconventional.¹ Power-law temperature dependencies observed in thermal conductivity, NMR, magnetic penetration depth, and recently specific-heat measurements⁵ point strongly to there being nodes in the superconducting energy gap in certain directions of k space. In order to gain a better insight into the mechanism for the superconductivity it is important to know the location of these nodes.

The two most widely studied organic superconductors are κ -(ET)₂Cu(NCS)₂ and κ -(ET)₂Cu[N(CN)₂]Br (which we abbreviate to κ -NCS and κ -Br, respectively) as these have the highest superconducting transition temperatures (T_c) of \sim 9.5 K and \sim 12.5 K, respectively) at ambient pressure. Angle-dependent magnetothermal conductivity⁶ measurements indicate that in κ -NCS the gap symmetry is $d_{x^2-y^2}$ (i.e., with nodes at 45° to crystal axis). This conclusion is also supported by angle-dependent tunneling measurements,⁷ however it is at odds with most theories of superconductivity such as that of Schmalian⁸ based on spin-fluctuation mediated pairing (for a review see Ref. 9) which predict a d_{xy} pairing state (i.e., with nodes along the crystal axes). In this case the nodes are in the same location with respect to the dominant nearest-neighbor antiferromagnetic coupling direction, as in the high T_c cuprates. However, Kuroki et al. 9,10 calculate that a $d_{x^2-y^2}$ pairing state is often close in energy to the d_{xy} and can dominate for certain model parameter values.

Here we report an investigation of the location of the nodes in the order parameter of both κ -NCS and κ -Br using angle-dependent magnetocalorimetry as a probe. The magnetic field was rotated in the highly conducting plane of the sample and oscillations of the specific heat were observed.

The location of the maxima and minima of the fourfold component of these oscillations points to the order parameter having d_{xy} symmetry. This appears to contradict the thermal-conductivity results but recent sophisticated theories of magneto-oscillatory specific heat and thermal conductivity predict rather complicated phase diagrams with the phase of the oscillations with respect to the nodes changing in distinct regions of field and temperature space. Hence, the interpretation of the experimental data is not straightforward and indeed these two seemingly opposite conclusions are not necessarily incompatible.

Angle-dependent magnetospecific-heat oscillations were first used successfully to locate the minima in the superconducting energy gap of YNi₂B₂C.¹¹ Subsequently, experiments were performed in several heavy fermion superconductors: Sr₂RuO₄, ¹² CeColn₅, ¹³ CeIrIn₅, ¹⁴ PrOs₄Sb₁₂, ¹⁵ and URu₂Si₂ (Ref. 15) as well as the strongly anisotropic s-wave superconductor CeRu₂. ¹⁵ In the simplest case, the oscillations arise from the field-induced "Doppler" shift of the energies of the quasiparticle states, $^{16} \delta E \propto v_s \cdot k$, where v_s is the velocity of the screening currents ($\propto H$) and k is the quasiparticle momentum. Close to a node or deep gap minimum, this field-induced shift can cause a substantial change in the population of the quasiparticle energy levels. In the case of a simple two-dimensional d-wave superconductor, if the field is applied along a node then only two nodes will contribute to the change in the density of states as the field is perpendicular to the other two. However, if the field is applied at 45° to this direction all four nodes will contribute, leading to an increase in the angle averaged density of states. Hence, at sufficiently low temperature and field, the direction of the maxima in the density of states should indicate the antinodal directions. 17 Although several experimental quantities are sensitive to these oscillations, the specific heat is perhaps the most direct and simplest to interpret. For example, to interpret the oscillations in the thermal conductivity, scattering of the quasiparticles from the vortex lattice needs to be taken into account.17

II. EXPERIMENTAL DETAILS

Our samples were grown using a standard electrochemical method¹⁸ and weighed $\sim 500 \ \mu g$. The crystal orientation

was determined by x-ray diffraction. Specific heat was measured using a purpose built calorimeter⁵ based on a bare chip Cernox¹⁹ thin-film resistor. The samples were cooled slowly (~0.2 K/min) to avoid any stress-induced separation.²⁰ The Cernox was used as both heater and thermometer. Two different methods of measurement were used. To measure the temperature dependence of C the longrelaxation technique was used.^{5,21} For the rotation studies. where much smaller temperature excursions from the base temperature are required, a thermal-modulation technique was used. 22,23 An ac current ($\omega \simeq 3-6$ Hz) was passed through the Cernox and the signals at ω and 3ω detected with lock-in amplifiers. The 3ω signal is inversely proportional to the specific heat provided that ω is selected appropriately.^{22,23} The thermometers were calibrated in field using a ³He vapor-pressure thermometer (below 4 K) and a capacitance thermometer at higher temperature. The angle dependence of the thermometer magnetoresistance was measured directly and was found to be negligibly small. Any angle dependence of the addenda specific heat was checked by measuring a pure Ag sample at our base temperature and in fields up to 14 T. No change was detected to within a precision of 0.2%. The thermal-modulation method has the advantage of high resolution at the expense of a small $(\sim 10\%)$ systematic error in the absolute values.

For measurements as a function of field angle the calorimeter was mounted on a mechanical rotator whose rotation plane was parallel to the field. Sample alignment was done by eye and was checked using optical images. Using this arrangement we estimate that the field was kept parallel to planes to within a few (\leq 5) degrees. Experiments were done either by rotating the sample at low temperature or by heating the sample above T_c after each rotation. In general, the two methods gave very similar results however there were occasional reproducible jumps in the data in certain field directions when the sample was not heated above T_c after each rotation, presumably because of vortex pinning effects.

III. RESULTS AND DISCUSSION

For $B^{\perp}=14$ T (applied along the interlayer direction) both samples are in the normal state and the data follow $C/T=\gamma+\beta_3T^2+\beta_5T^4$ with $\gamma=29\pm1$ mJ K $^{-2}$ mol $^{-1}$ for κ -Br and 33 ± 1 mJ K $^{-2}$ mol $^{-1}$ for κ -NCS in good agreement with previous measurements. We do not observe any Schottky-type upturns even at high field so the $B^{\perp}=14$ T data is likely to be very close to the normal-state C at zero field. The zero-field data with the 14 T data subtracted shown in Fig. 1 shows the superconducting anomalies of each sample with midpoints of 9.6 K and 12.5 K for κ -NCS and κ -Br, respectively.

We now discuss the data with the field rotating in the basal plane. Figure 2 shows the raw $C(\phi)$ data for κ -Br at several temperatures and $B^{\parallel}=3$ T which is $\sim 10\%$ of H_{c2} for this field orientation²⁴ (ϕ is the angle measured relative to the in-plane c axis). Focusing on the lowest temperature data T=0.4 K, we see that the total change in C with angle is around 33% of the total (minus addenda) or around 55% of the electronic term at this field (the phonon contribution at

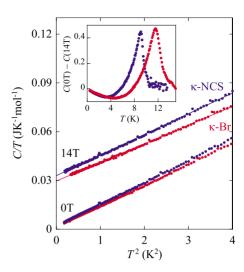


FIG. 1. (Color online) The temperature of the heat capacity in zero field and $B^{\perp}=14$ T for samples of κ -Br and κ -NCS plotted versus T^2 . The inset shows zero-field specific-heat data (with normal-state contribution at $B^{\perp}=14$ T subtracted).

T=0.4 K $C_{\rm Phonon}$ =0.85 mJ mol $^{-1}$ K $^{-1}$ which is 60% of the total). The largest component has twofold symmetry, however to get a good fit we need also to include a fourfold term. We find the data are best fitted by the function

$$C(\phi) = C_0 + |C_2 \cos(\phi + \delta_2)| + C_4 \cos(4\phi + \delta_4),$$
 (1)

which fits the data perfectly within the noise as shown by the residuals displayed in the figure. The fit parameters are C_2 =0.54 mJ mol⁻¹ K⁻¹, δ_2 =13±2°, C_4 =0.04 mJ mol⁻¹ K⁻¹, and δ_4 =0±2°.

The C_2 twofold term likely originates from a combination of sample misalignment and the anisotropy of the Fermi sur-

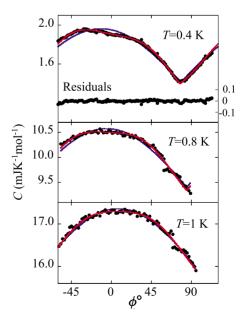


FIG. 2. (Color online) Raw data for κ -Br taken at three temperatures 0.4, 0.8, and 1 K. The blue lines are a fit to a twofold angle dependence whereas the red lines include the additional fourfold term as described in the text.

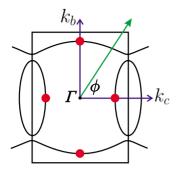


FIG. 3. (Color online) Sketch of the Fermi surface of κ -NCS (Ref. 27) along with the definition of ϕ . The red dots show the position of the nodes for the d_{xy} pairing state.

face of these compounds. If the sample is misaligned by an angle φ to the plane of rotation, then there will be a component of magnetic field B^{\perp} perpendicular to the planes given by $B^{\perp}/B_0 = \cos \phi \sin \varphi$, where B_0 is the applied field and ϕ is the in-plane rotation angle. As H_{c2} is much lower for fieldapplied perpendicular rather than parallel to the planes there will be a induced component to $C(\phi)$ which will depend on B^{\perp} . For a pure d-wave superconductor at low field we would expect that at low fields $\Delta C(B) \sim (B/B_{c2})^{1/2}$, however in general the functional dependence may not be a square root (for example, if the field is less than a scale set by the impurity scattering bandwidth then $\Delta C \simeq -B/B_{c2} \ln(B/B_{c2})$ Ref. 25). Experimentally, for these compounds for $B^{\perp} \gtrsim 0.1$ T, $\Delta C(B)$ is close to linear. Given that this misalignment term must be even with respect to B, the simplest form is then $\Delta C(\phi)$ $=A\mathcal{F}[\cos(\phi+\delta)]$, where A is constant which depends on the misalignment angle and the form of the function \mathcal{F} and δ is a constant which depends on the misalignment angle. For simplicity we took \mathcal{F} to be a simple power law so the misalignment term is $\Delta C(\phi) = A |\cos(\phi + \delta)|^n$. A least-squares fit to the data with this in place of the C_2 term in Eq. (1) gives $n=1.1\pm0.1$ so we fixed n=1 for all temperatures and fields.

The crystal structures of κ -Br and κ -NCS are orthorhombic and monoclinic, respectively. The Fermi surface of κ -NCS has been determined by both tight-binding²⁶ and first-principles²⁷ calculations and quantum oscillation measurements²⁶ and is sketched in Fig. 3. The quasi-two-dimensional Fermi surface would have a near ellipsoidal cross-section if all the ET-dimers were equivalent. However, the difference in the interdimer hopping integrals causes a gap to appear where the ellipse crosses the Brillouin-zone boundary. The Fermi surface of κ -Br is very similar to that of κ -NCS except that there are twice the number of Fermi-surface sheets because the unit cell contains twice the number of formula units due to the doubling of the c axis.²⁸

Theoretical calculations based on spin-fluctuation pairing suggest that the pairing state has either d_{xy} or $d_{x^2-y^2}$ symmetry. For the case of d_{xy} pairing as the gap has nodes along the crystal axes^{8,9} so the angle between these nodes remains 90° even in the presence of the orthorhombic distortion and maxima in $C(\phi)$ with fourfold symmetry as in Eq. (1) are expected. In the semiclassical theory the field dependence of the specific heat depends on the Fermi velocity and gradient of the superconducting energy gap Δ near the nodes

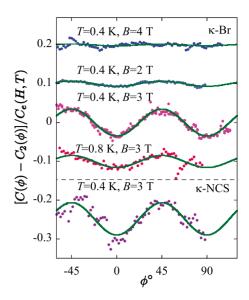


FIG. 4. (Color online) Angle-dependent heat capacity data with the twofold terms subtracted. The angle-dependent changes $[C(\phi) - C_2(\phi)]$ are divided by the angle-averaged electronic-specific heat at each temperature and field $C_e(H,T)$. The solid lines are fits to $C_4 \cos(4\phi + \delta_4)$.

 $d\Delta/d\phi|_{\rm node}$. ¹⁶ So an orthorhombic distortion of the Fermi surface can produce a twofold $|\cos\phi|$ dependence of C(B) similar to the case of field misalignment. Indeed, in the field-angle dependent thermal-conductivity measurements of κ -NCS a twofold term around two times larger than the fourfold term was observed at T=0.43 K (Ref. 6) even though the field was aligned to better than 0.01°.

As the phase of the twofold term in our measurements implies symmetry far from a crystal-symmetry direction, this suggests that a sizeable fraction of it originates from misalignment, however the thermal-conductivity results suggest that the intrinsic contribution is not negligible. In principle, in situ adjustment of the crystal orientation (using, for example, a vector magnet as in Ref. 6) and angle detection using the magnetoresistance of the sample would allow us to distinguish between these two contributions however this was not possible with our current set up.

In Fig. 4 we show the κ -Br data with the twofold term subtracted and normalized to the angle-averaged value of the electronic-specific heat at the relevant temperature and field $C_e(H,T)$. At T=0.4 K the fourfold term is now clearly evident. It has a relatively large peak to peak amplitude of $\sim 7\%$ of $C_e(H,T)$. Note that the in-plane shape of this sample is an irregular polygon and so the fourfold term cannot result from shape-dependent vortex pinning effects. The phase of this term is $\delta_4 = 0 \pm 2^\circ$ so that the minima occur when the field is along the a and c crystal axes (equivalent to the b and c axes for κ -NCS in Fig. 3). Hence, we conclude that the nodes in the gap function are located along the crystal axes, i.e., the energy gap has d_{xy} symmetry.

As the temperature is increased the relative size of the fourfold term compared to the angle average decreases rapidly and is barely discernible in the T=1 K data. This strong decrease with increasing temperature points strongly to the origin of the fourfold oscillation being from nodal quasipar-

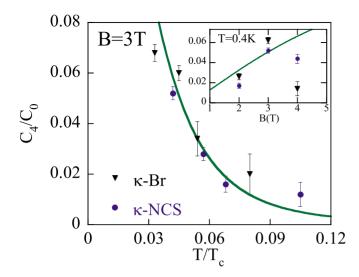


FIG. 5. (Color online) The normalized amplitude of the fourfold component for both κ -NCS and κ -Br as a function of temperature at B=3 T. The inset show the field dependence at fixed T=0.4 K. The solid lines in both parts of the figure are fits to the nodal-approximation theory (see text).

ticles, rather than, for example, v_F anisotropy which would have a much weaker T dependence. For CeRu₂, which has a strongly anisotropic s-wave gap $(\Delta_{\max}/\Delta_{\min} = 5-10)$, it is found that C_4/C_e increases with increasing T up to a maximum at $T/T_c = 0.16$. Fig. 4 also shows that the magnitude of the fourfold term depends strongly on the applied field. It is maximal at B=3 T and is significantly reduced for B=2 and 4 T.

Data for κ -NCS are also shown in Fig. 4. The magnitude of the fourfold term is comparable to that found for κ -Br and importantly the maxima/minima are at the same angles so we expect the symmetry of the gap functions to be the same. For this sample we had to introduce an additional term $C_1 \cos(\phi + \delta_1)$ which is comparable in magnitude to the C_2 term to fully fit the background, the origin of which is unclear. The temperature and field dependence of the fourfold component C_4 for both samples is shown in Fig. 5. As for κ -Br, C_4/C_e in κ -NCS decreases strongly with increasing temperature and decreasing field. However, for κ -NCS C_4/C_e decreases significantly less as the field is increased from B=3 T to B=4 T than in κ -Br.

In Fig. 5 we compare our experimental data to quantitative predictions of the magnitude of this effect for a d-wave superconductor. For simplicity we use the nodal approximation of the Doppler-shift theory which gives the following expression for the field/angle dependence of the density of states: 16,29,30

$$\frac{N(\boldsymbol{\omega}, \boldsymbol{H}, T)}{N_0} = \frac{1}{2} \left[\frac{E_1}{\Delta_0} F\left(\frac{\boldsymbol{\omega}}{E_1}\right) + \frac{E_2}{\Delta_0} F\left(\frac{\boldsymbol{\omega}}{E_2}\right) \right],\tag{2}$$

where the field scale E_H =0.5 $a\hbar v_F \gamma_{\lambda}^{-(1/2)} \sqrt{\pi \mu_0 H/\Phi_0}$, E_1 = E_H |sin($\pi/4-\phi$)|, E_2 = E_H |cos($\pi/4-\phi$)|, and

$$F(y) = \begin{cases} y[1 + 1/(2y^2)] & \text{if } y \ge 1\\ [(1 + 2y^2)\arcsin y + 3y\sqrt{1 - y^2}]/y\pi & \text{if } y \le 1. \end{cases}$$

In this approximation, which was shown to be in good agreement with more sophisticated treatments in the low-temperature/field limit, ¹⁷ only quasiparticles in the nodal directions are included. This density of states was used to calculate the entropy S then numerically differentiated to give the heat capacity $C = T \partial S / \partial T$. For the curve in the figure we set $E_H = 0.13 \sqrt{\mu_0 H k_B T_c}$.

The theory and experiment show reasonable agreement considering this contains just one-fitting parameter E_H . In particular, the theory explains the rapid decrease in signal with increasing temperature. For κ -NCS, using the in-plane Fermi velocity $v_F = 1.1 \times 10^5$ m/s,³¹ and penetration depth anisotropy $\gamma_{\lambda} \simeq 100$, this gives $E_H \simeq 0.17 \sqrt{\mu_0 H} k_B T_c$ (setting the numerical constant a=1). This agreement with the experimental value is probably fortuitous as a and the effective value of γ_{λ} depend on the details of the vortex lattice. ¹⁶ The increase in field between 2 and 3 T is similar to that predicted but the theory does not explain the observed decrease in higher field. However, more sophisticated treatments 17,30 actually predict that the oscillations in C change sign for $T \ge 0.1T_c$ or for $H \ge (0.2-0.4)H_{c2}$ and so a strong decrease in C_4 with increasing field is expected near these transition points.

IV. CONCLUSIONS

In summary, the magnetic field angle dependence of the heat capacity of κ -Br and κ -NCS shows a clear fourfold oscillation. These oscillations are shown to arise from nodes in the superconducting gap situated along the crystal axis. These results imply a d_{yy} order parameter that is consistent with the spin-fluctuation mediated pairing theory of Schmalian⁸ and others.⁹ At first sight these results seem to contradict the angular thermal conductivity κ experiments performed on κ -NCS,⁶ which showed that the small fourfold component ($\sim 0.1\%$ of the total κ) was 45° out of phase with the one observed in this experiment (i.e., a maximum of κ was observed with the field along the b or c axes whereas a minimum is observed here). A similar discrepancy between the C and κ measurements was found for CeCoIn₅. ^{13,32} Vorontsov and Vekhter¹⁷ have shown that the oscillations in C and κ both change sign as a function of H and T and so the CeCoIn₅ results could be explained because the measurements of C and κ were conducted in different regions of the (H,T) phase diagram. According to the phase diagrams in Ref. 33 our C measurements should be well within the low (T,H) limit so the minima are along the nodal directions. The κ measurements were made at similar H and T and also should be in the low (H,T) limit with minima along the nodal directions, however in this case they are much closer to the sign switching-phase boundary. Hence the previous thermal conductivity and the present data are not necessarily inconsistent and might be explained if there were small material-dependent changes to the global phase diagrams of Ref. 33. Further work will be required to understand this.

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- ¹M. Lang and J. Müller, *The Physics of Superconductors*, edited by K. H. Bennemann and J. B. Ketterson (Springer-Verlag, Berlin, 2003), Vol. 2.
- ²S. Belin, K. Behnia, and A. Deluzet, Phys. Rev. Lett. **81**, 4728 (1998).
- ³S. M. De Soto, C. P. Slichter, A. M. Kini, H. H. Wang, U. Geiser, and J. M. Williams, Phys. Rev. B **52**, 10364 (1995).
- ⁴ A. Carrington, I. J. Bonalde, R. Prozorov, R. W. Giannetta, A. M. Kini, J. Schlueter, H. H. Wang, U. Geiser, and J. M. Williams, Phys. Rev. Lett. **83**, 4172 (1999).
- ⁵O. J. Taylor, A. Carrington, and J. A. Schlueter, Phys. Rev. Lett. 99, 057001(R) (2007).
- ⁶ K. Izawa, H. Yamaguchi, T. Sasaki, and Y. Matsuda, Phys. Rev. Lett. **88**, 027002 (2001).
- ⁷T. Arai, K. Ichimura, K. Nomura, S. Takasaki, J. Yamada, S. Nakatsuji, and H. Anzai, Phys. Rev. B **63**, 104518 (2001).
- ⁸J. Schmalian, Phys. Rev. Lett. **81**, 4232 (1998).
- ⁹K. Kuroki, J. Phys. Soc. Jpn. **75**, 051013 (2006).
- ¹⁰K. Kuroki, T. Kimura, R. Arita, Y. Tanaka, and Y. Matsuda, Phys. Rev. B **65**, 100516(R) (2002).
- ¹¹T. Park, M. B. Salamon, E. M. Choi, H. J. Kim, and S. I. Lee, Phys. Rev. Lett. **90**, 177001 (2003).
- ¹²K. Deguchi, Z. Q. Mao, H. Yaguchi, and Y. Maeno, Phys. Rev. Lett. **92**, 047002 (2004).
- ¹³ H. Aoki, T. Sakakibara, H. Shishido, R. Settai, Y. Onuki, P. Miranovic, and K. Machida, J. Phys.: Condens. Matter 16, L13 (2004).
- ¹⁴ Y. Kasahara, T. Iwasawa, Y. Shimizu, H. Shishido, T. Shibauchi, I. Vekhter, and Y. Matsuda, Phys. Rev. Lett. **100**, 207003 (2008).
- ¹⁵T. Sakakibara, A. Yamada, J. Custers, K. Yano, T. Tayama, H. Aoki, and K. Machida, J. Phys. Soc. Jpn. **76**, 051004 (2007).
- ¹⁶I. Vekhter, P. J. Hirschfeld, J. P. Carbotte, and E. J. Nicol, Phys. Rev. B **59**, R9023 (1999).

- ¹⁷ A. Vorontsov and I. Vekhter, Phys. Rev. Lett. **96**, 237001 (2006).
- ¹⁸ A. M. Kini, U. Geiser, H. H. Wang, K. D. Carlson, J. M. Williams, W. K. Kwok, K. G. Vandervoort, J. E. Thompson, D. L. Stupka, D. Jung, and M. H. Whangbo, Inorg. Chem. 29, 2555 (1990).
- ¹⁹Lakeshore Cryotronics, Inc., 575 McCorkle Blvd., Westerville, OH 43082, U.S.A.
- ²⁰O. J. Taylor, A. Carrington, and J. A. Schlueter, Phys. Rev. B 77, 060503 (2008).
- ²¹ Y. X. Wang, T. Plackowski, and A. Junod, Physica C 355, 179 (2001).
- ²²P. F. Sullivan and G. Seidel, Phys. Rev. **173**, 679 (1968).
- ²³Y. Kraftmakher, Phys. Rep. **356**, 1 (2002).
- ²⁴ Y. Shimojo, A. E. Kovalev, S. Kamiya, E. Ohmichi, T. Ishiguro, H. Yamochi, G. Saito, A. Ayari, and P. Monceau, Physica B 294-295, 427 (2001).
- ²⁵ Y. Barash, A. Svidzinskii, and V. Mineev, JETP Lett. **65**, 638 (1997).
- ²⁶ K. Oshima, T. Mori, H. Inokuchi, H. Urayama, H. Yamochi, and G. Saito, Phys. Rev. B **38**, 938 (1988).
- ²⁷ Y.-N. Xu, W. Y. Ching, Y. C. Jean, and Y. Lou, Phys. Rev. B 52, 12946 (1995).
- ²⁸ W. Y. Ching, Y.-N. Xu, Y. C. Jean, and Y. Lou, Phys. Rev. B 55, 2780 (1997).
- ²⁹C. Kübert and P. Hirschfeld, Solid State Commun. 105, 459 (1998).
- ³⁰G. R. Boyd, P. J. Hirschfeld, I. Vekhter, and A. B. Vorontsov, Phys. Rev. B **79**, 064525 (2009).
- ³¹J. Wosnitza, G. W. Crabtree, H. H. Wang, U. Geiser, J. M. Williams, and K. D. Carlson, Phys. Rev. B 45, 3018 (1992).
- ³²K. Izawa, H. Yamaguchi, Y. Matsuda, H. Shishido, R. Settai, and Y. Onuki, Phys. Rev. Lett. 87, 057002 (2001).
- ³³ A. B. Vorontsov and I. Vekhter, Phys. Rev. B **75**, 224502 (2007).