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# **Oxygen/noble gas binary phase diagrams at 296 K and high pressures**

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The binary phase diagrams of  $O_2$ /rare gas (He, Ne, Ar, and Xe) mixtures have been measured at 296 K up to 20 GPa in a diamond-anvil cell. The boundary lines were determined by visual observation and by the Raman frequency of the  $O_2$  vibron mode. The  $O_2$ -He phase diagram is of eutectic type with a liquid-liquid miscibility gap and complete immiscibility in the solid phase. The  $O_2$ -Ne phase diagram is of eutectic type with partial immiscibility in the solid phase. The  $O_2$ -Ar phase diagram is of azeotrope type and three different structures of  $Ar/O<sub>2</sub>$  solid solutions have been identified. The  $O<sub>2</sub>$ -Xe phase diagram is of peritectic with eutectic type. The stoichiometric compound  $Xe(O_2)_2$  is observed and characterized as a laves phase with a cubic structure isomorphous to  $MgCu<sub>2</sub>$ . A qualitative understanding of these various diagrams is reached by the comparison of the effective hard-sphere diameters of the various species in the 10 GPa range. Some of the usefulness of the knowledge of these binary phase diagrams is highlighted: as a reference data set to test theoretical calculations on mixtures; to grow single crystal of  $O_2$  in a rare-gas pressure medium; and to synthesize rare-gas oxides at high pressure.

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#### **I. INTRODUCTION**

We present here an extensive high-pressure study of the binary phase diagrams of  $O_2$  with rare gases (He, Ne, Ar, and Xe) at 296 K. Up to now, the study of the thermodynamical and structural properties of the mixtures of  $O_2$  with rare gases has been limited essentially to  $Ar_xO_{2(1-x)}$  systems at ambient pressure and low temperature.<sup>1</sup> In particular, many authors have contributed to the understanding of the properties of the  $Ar/O<sub>2</sub>$  cryosolid solutions that exist over the entire concentration range. $2-4$  $2-4$  The essential issues discussed have been the structural changes in the end-component solids, Ar or  $O_2$ , under the gradual dissolution of the other components. Turning on the pressure parameter for the study of molecular binary mixtures reveals a rich class of new phenomena, such as a possible stability of stoichiometric compounds or an increase influence of the pressure-induced chemical changes in the species. Specifically addressed in the present study: does a van der Waals compounds exist in any mixture of  $O_2$ with a rare gas, as observed for  $H_2$ , with  $Ar(H_2)_2$  (Ref. [5](#page-7-3)) and  $Xe(H_2)$ <sub>7</sub> (Ref. [6](#page-7-4)), and N<sub>2</sub>, with  $He(N_2)_{11}$  (Ref. [7](#page-7-5))? How does the molecular association of  $O_2$  into  $O_8$ , observed above 10 GPa in the solid phase, $8.9$  $8.9$  influence the binary phase diagrams of  $O_2$  with rare gases? It is still formidably challenging to address these issues theoretically. Hence, the present measurements should constitute a reference data set to test improved theoretical methods for computing dense molecular alloys.<sup>10</sup> The present study was also motivated by two applications. First, the search for a topology of phase separation which could give a single crystal of  $O_2$  embedded in a rare-gas pressure medium. Second, the search for stable  $O_2$ /Xe alloys that could favor the synthesis of xenon oxide at high pressure from a topochemical principle. The outline of the paper is the following: in Sec. [II,](#page-0-0) experimental details are presented; the binary phase diagram of  $O_2$  with He, Ne, Ar, and Xe are constructed in Sec. [III;](#page-1-0) and the x-ray measurements of the three structures of the  $Ar-O<sub>2</sub>$  solid solutions and of the  $Xe(O_2)_2$  van der Waals compounds are presented in

Sec. [IV;](#page-3-0) Interpretations and usefulness of this data set are discussed in Sec. [V.](#page-4-0)

### **II. EXPERIMENTS**

<span id="page-0-0"></span>The binary phase diagram is the locus of boundary surfaces in the three-dimensional thermodynamical space, pressure  $(P)$ , temperature  $(T)$ , and the  $O_2$  molar concentration  $(X)$ . In the present study, the temperature is fixed at 296 K. The boundary lines in the  $(P, X)$  diagram have been investigated by measuring changes in the properties of the sample by varying pressure. A membrane diamond-anvil cell has been used, allowing very controlled and smooth variations in pressure, with a sensitivity of 0.02 GPa. The pressure range of the present study is 0.2–20 GPa. The membrane diamondanvil cell equipped with 500  $\mu$ m flat culet anvils was loaded at room temperature in a high-pressure vessel, typically under a pressure of 20 MPa to avoid the use of a compressor. Mixtures were directly made in the pressure vessel. The initial concentration of the mixture was fixed from the partial pressures of the gases, corrected with the virial coefficients. The loading of the diamond anvil cell was done after sufficient time for homogenization (12 h). The error bar on the concentration is less than 1 mol %. Inox 301 or rhenium gaskets were used. The sample chamber was typically around 80  $\mu$ m in diameter at 10 GPa. The pressure was measured with the ruby luminescence technique using the quasihydrostatic ruby scale.<sup>11</sup> The error bar in pressure is  $\pm 0.05$  GPa. Depending on the system, 7–20 different initial concentrations have been studied and measurements at some concentrations have been repeated to test reproducibility.

Three different kinds of measurements have been performed to probe phase transitions in a given mixture under pressure. Phase boundaries have been clearly detected by visual observation through a microscope apparatus associated with the pressure measurement. The sample was observed at each point from a few minutes (in helium-oxygen

<span id="page-1-1"></span>

FIG. 1. Experimental binary phase diagram of the  $He-O<sub>2</sub>$  system. The black circles are experimental points of the liquidus. Triangles correspond to the pressure of the triple points measured for different concentrations. The inset corresponds to a zoom around the second triple point at 11.9 GPa and 0.25%.

or neon-oxygen mixtures) to several hours (in xenon-oxygen mixtures) to test for equilibration. Solid-fluid equilibrium could easily be observed. The transition points were the most finely detected by working with a single crystal in equilibrium with a fluid. The liquidus line was then delimited by the locus of the  $P(X)$  points where the single crystal was seen to disappear. The solidus line corresponds to the locus of  $P(X)$ points where the single crystal is seen to fill the whole sample chamber. Solid-solid transitions could be detected visually as well. Raman spectroscopy of the vibron mode of  $O_2$ has been used to quantify the solubility of  $O_2$  in the rare-gas matrix, to precisely confirm the phase transitions by looking at discontinuities of the vibron frequency with pressure, to determine the number of sites in  $O_2$ -Ar solid solutions (usually associated with different vibron frequencies), and to prove the existence of the  $Xe(O_2)_2$  compound. Finally, the structures of the  $O_2$ /rare gas alloys have been determined by x-ray diffraction at the ESRF using angle dispersive monochromatic x-ray diffraction at  $0.3738$  Å (on ID30 or ID27) and at 0.3304 and 0.4180  $\AA$  (on ID09). The diffracted signal has been recorded on a MAR345 image plate.

#### **III. BINARY PHASE DIAGRAMS**

#### **A. Helium-oxygen mixtures**

<span id="page-1-0"></span>The  $He-O<sub>2</sub>$  binary phase diagram has been determined mainly by visual observation. Sixteen different concentrations have been investigated at 296 K. The binary phase diagram is plotted in Fig. [1.](#page-1-1) The phase diagram is of eutectic type with a liquid-liquid miscibility gap. It has two triple points: one corresponding to an equilibrium  $F_1 + F_2 + S_{O_2}$  at 6.7 GPa and 52 mol %  $O_2$  and the other one corresponding to the equilibrium  $S_{He} + F_1 + S_{O_2}$  at 11.9 GPa and 0.25 mol %  $O_2$ . The inset of Fig. [1](#page-1-1) shows more finely the measurements

<span id="page-1-2"></span>

FIG. 2. Experimental binary phase diagram of the  $Ne-O<sub>2</sub>$  system. Black circles are experimental points of the liquidus. Triangles correspond to the pressure of the triple point measured for each concentration. Black diamonds correspond to the neon solubility in solid  $S_2$  measured by x-ray diffraction.

around the second triple point. Complete immiscibility in the solid phase is observed. Above 11.9 GPa, at any concentration, a solid-solid phase separation is observed. One phase is pure solid helium and the other is pure solid oxygen. From the volume of solid  $O_2$  phase separated from solid helium at the concentration 0.25 mol %  $O_2$  and from the absence of Raman  $O_2$  vibron signal in solid helium, we estimated that the solubility of  $O_2$  in solid helium should be less than 0.01 mol %  $O_2$ . For the 98.5 mol %  $O_2$  mixture, a solidsolid phase separation has been observed. From the ratio between the volumes of the two solid phases in equilibrium, the solubility of He in solid oxygen is estimated to be smaller than 1 mol %  $O_2$ . X-ray diffraction measurements on a single crystal of  $O_2$  grown in helium have shown no effect of a possible residual solubility of He in solid  $O_2$  on the equation of state nor on the structural changes. Finally, since  $O<sub>2</sub>$ and  $N_2$  systems under pressure have very similar intermolecular interactions, the existence of a van der Waals compound, similar to the observed  $(N_2)_{11}$ He,<sup>7</sup> was seen to be probable. The reason for the absence of a similar compound in  $O_2$ -He mixture is probably due to the exchange term in the interaction between  $O_2$  molecules.

#### **B. Neon-oxygen mixtures**

The Ne- $O_2$  binary phase diagram has been determined at room temperature, mainly by visual observation. Seventeen different initial concentrations have been studied. Raman spectroscopy measurements and x-ray diffraction experiments were performed to characterize the solid phases. The  $Ne-O<sub>2</sub>$  binary diagram is plotted in Fig. [2.](#page-1-2) It is of eutectic type with partial immiscibility in the solid phase below 10 GPa and complete immiscibility above. The eutectic point is at 6.7 GPa and 62.5 mol %  $O_2$ . There is a small oxygen miscibility (4 mol %  $O_2$ ) below 6.7 GPa in the neon-rich

<span id="page-2-0"></span>

FIG. 3. Isothermal (296 K) equation of state of  $S_{Ne}$  and  $S_2$ . The equations of state of pure neon (Ref.  $12$ ) and pure oxygen (Refs. [8,](#page-7-6) [13,](#page-7-11) and [14](#page-7-12)) are plotted as reference.

solid  $(S_1)$ . Above this pressure, an oxygen release from solid  $S_1$  is observed and the solubility of  $O_2$  is estimated to fall below 1 mol %  $O_2$ . From visual observation, the solubility of neon in oxygen-rich solid  $(S_2)$  has been estimated to be smaller than 6 mol %. But, it was not possible to follow the change in this solubility either from visual observation or Raman measurement (no measurable Raman  $O<sub>2</sub>$  vibron frequency shift is associated with this Ne solubility).

X-ray diffraction measurements have been performed on the  $S_1 + S_2$  phase separation obtained in an O<sub>2</sub>/Ne mixture of 53 mol  $\%$  O<sub>2</sub> initial concentration. The sequence of phase transitions observed in  $S_2$  is identical to pure solid  $O_2$ , namely  $(\beta-\delta_2, R\bar{3}m)$ , above 9.3 GPa  $(\delta-\delta_2, Fmmm)$  and above 13.5 GPa ( $\varepsilon$ -O<sub>2</sub>,  $C2/m^{13}$ ). The volume of S<sub>1</sub> and S<sub>2</sub> is compared in Fig. [3](#page-2-0) to the equation of state of pure solid Ne and pure solid  $O_2$ . The  $S_1$  solid has the same face-centeredcubic (fcc) structure and the same molar volume as pure solid neon which confirms the visual observations of a complete immiscibility of oxygen in solid neon above 7 GPa. The volume of  $S_2$  is seen to be smaller than the one of pure solid O<sub>2</sub>. Under ideal mixing assumption, the molar concentration of Ne in  $S_2$  is estimated to be 5 mol %. Above 8.5 GPa, the molar volume of  $S_2$  falls on the equation of state of  $O_2$ , implying that the solubility of Ne in  $S_2$  drops below 1 mol %.

#### **C. Argon-oxygen mixtures**

The  $Ar-O<sub>2</sub>$  binary phase diagram has been measured at 296 K, mainly by visual observation. A total of 40 samples have been prepared to cover finely the whole concentration range. The  $Ar-O_2$  binary phase diagram is plotted in Fig. [4.](#page-2-1) It is of the azeotrope type, with a congruent melting at 75 mol %  $O_2$ . For oxygen concentrations above 93% there is a solid-solid phase separation above 5.6 GPa. The solidus line has a strong discontinuity at 75 mol  $\%$  O<sub>2</sub>, indicative of a structural change in  $Ar/O<sub>2</sub>$  alloys at this concentration.

<span id="page-2-1"></span>

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FIG. 4. Experimental binary phase diagram of the Ar-O<sub>2</sub> system. Black circles and open squares are experimental points of, respectively, the liquidus and the solidus lines. Open triangles and dashed lines indicate the stability limits of the  $S_1$  (hcp),  $S_2$  (*Pm3n*), and  $S_3$  (*I*-42*d*) solid solutions. Below 5 mol %  $O_2$ , the solid has the fcc structure of argon.

Above 9.5 GPa, the alloys completely phase separate into almost pure fcc Ar and  $\varepsilon$ -O<sub>2</sub>, identified by x-ray diffraction. For  $O_2$  concentrations smaller than 5 mol %, no phase separation is observed; the amount of  $O_2$  dissolved in solid Ar above 9.5 GPa is thus estimated to be around 5 mol %  $O_2$ . From Raman measurements of the  $O_2$  vibron, three Ar/ $O_2$ alloys—S<sub>1</sub>, S<sub>2</sub>, and S<sub>3</sub>—have been identified. Their boundary lines are plotted in Fig. [4.](#page-2-1) Raman frequencies measured in these alloys are reported in Fig.  $5$ . In  $S_1$ , only one vibron peak is observed; in addition, x-ray diffraction measurements showed that  $S_1$  has the hcp structure. In  $S_2$  and  $S_3$ , two vibron peaks are measured, which have a 1.5 intensity ratio independent of the  $O_2$  concentration. This implies that  $S_2$  and  $S_3$  are solid solutions of Ar and  $O_2$  with random distribution on the sites and that they have a structure with two different sites at least. From x-ray diffraction data, the  $S_2$  structure is identified as  $Pm3n$ . The S<sub>3</sub> structure has not been fully resolved but is probably a tetragonal distortion of the  $S_2$  with possible space group *I*-42*d*. Both structures allow the random substitution of  $O_2$  molecules by Ar atoms on the  $\gamma$ -O<sub>2</sub> structure. It is very similar to what has been obtained for  $Ar-O<sub>2</sub>$  cryosolid solutions.<sup>4</sup> The gamma phase of oxygen is quite stable to the dissolution of argon in it, up to 50 mol % Ar. Above 7 GPa the symmetry is reduced and a doubling of the cell obtained. That is described in more detail in Sec. [IV.](#page-3-0)

#### **D. Xenon-oxygen mixtures**

Seven  $Xe-O<sub>2</sub>$  samples with various initial concentrations have been studied at 296 K. The liquidus line has been determined by visual observation. The stability domains in the solid phase have been determined by the combination of visual observation, Raman spectroscopy and x-ray diffraction.

<span id="page-3-1"></span>

FIG. 5. (Color online) Oxygen vibron frequency measured for different concentrations of  $Ar-O_2$  mixtures. The vertical dashed line corresponds to the fluid-S<sub>2</sub> transition observed at 77 mol %  $O_2$ . The vertical dotted line represents the  $S_1-S_2$  transition observed at 50 mol  $\%$  O<sub>2</sub>. The vertical straight line corresponds to the phase separation observed above 8.5 GPa in  $S_1$  and  $S_3$ .

The  $Xe-O_2$  binary phase diagram is plotted in Fig. [6.](#page-3-2) It is of peritectic with eutectic type. The eutectic point is at 5.95 GPa and approximately 98 mol  $\%$  O<sub>2</sub> and the peritectic point around 75 mol %  $O_2$  at 3.1 GPa. The presence of a peritectic point reveals the stability of a  $Xe/O<sub>2</sub>$  compound. The  $O<sub>2</sub>$  vibron frequencies versus pressure, for various initial concentrations, are plotted in Fig. [7.](#page-3-3) This indicates the existence of three stable solid phases in  $Xe/O<sub>2</sub>$  mixtures: a solid rich in Xe,  $S_1$ , a stoichiometric compound and pure oxygen. Both  $S_1$  and the compound have only one  $O_2$  vibron Raman

<span id="page-3-2"></span>

FIG. 6. Binary phase diagram of the Xe-O<sub>2</sub> system. Black symbols represent experimental points and lines interpolations between these points.

<span id="page-3-3"></span>

FIG. 7. (Color online) Evolution of the frequencies of the intramolecular  $O_2$  vibron with pressure measured for different concentrations of Xe-O<sub>2</sub> mixtures. The frequencies measured in  $S_1$  and  $Xe(O_2)_2$  are lower than the frequency in pure  $O_2$  (Ref. [15](#page-7-14)).

frequency, lower than the one measured in pure oxygen. The solubility of Xe in solid  $O_2$  is estimated to be lower than 1 mol % from the lever rule applied to the volumes of the two solid phases separated in the mixture of initial concentration 96 mol %  $O_2$ . The solubility of  $O_2$  in solid Xe was seen to increase with pressure, starting from about 1 mol %  $O<sub>2</sub>$  at the solidification pressure of Xe, 0.42 GPa, to approximately 15 mol  $\%$  O<sub>2</sub> above 4 GPa. This leads to a gradient of concentration in solid  $S_1$ . X-ray diffraction shows that the structure of  $S_1$  is fcc as pure solid Xe. The fcc structure of Xe is thus remarkably stable upon the dissolution of up to 15 mol %  $O_2$  in it up 10 GPa. As presented in more detail in the next paragraph, the x-ray study of the stoichiometric compound was used to determine its exact formula. We found that it is  $Xe(O_2)_2$ , with the MgCu<sub>2</sub>-type Laves phase structure.<sup>16</sup> It is assumed that the  $O_2$  and Xe entities occupy, respectively, the Cu and Mg sites. The fact that only one site is occupied by  $O_2$  molecule matches the observation of only one Raman vibron mode, as reported in Fig. [7.](#page-3-3)

## <span id="page-3-0"></span>**IV. STRUCTURAL DETERMINATION OF ArO<sub>2</sub> AND Ar(O2)3 ALLOYS AND Xe(O2)2 VAN DER WAALS COMPOUND**

The three different structures of  $Ar/O<sub>2</sub>$  solid solutions have been characterized by x-ray diffraction under pressure of three mixtures of different initial concentrations. At 25 mol %  $O_2$  and 50 mol %  $O_2$ , the mixture solidifies into the  $S_1$  phase and easily forms a single crystal. The observed diffraction peaks could be indexed and correlated with a hexagonal unit cell with two molecular entities in it (space group  $P63/mmc$ ). In the 75 mol % O<sub>2</sub> mixture, a single crystal S<sub>2</sub> is grown from the melt. The diffraction peaks could be in-

<span id="page-4-1"></span>

FIG. 8. (Color online) X-ray diffraction pattern collected in a mixture of 50 mol % Ar-50 mol %  $O_2$  at 6.9 GPa. The dots correspond to the measured pattern and the line to the calculated pattern after a Rietveld refinement. The inset shows a schematic view of the  $S<sub>2</sub>$  crystal with argon and oxygen atoms, respectively, in dark and light gray.

dexed and correlated with a cubic *Pm*3*n* space group with eight molecular entities in the unit cell. The structure is thus very similar to the gamma phase of  $\text{cryo-Ar-O}_2$  solid solutions.<sup>4</sup> From Raman measurements showing that the intensity ratio between the two oxygen vibrons is independent of concentration, we assume that there is a random substitution of  $O_2$  by Ar on the (2*a*) and (6*c*) sites of the gamma phase of oxygen[.17](#page-7-15) Yet, we cannot completely rule out the existence of a preferential substitution. That would require a full refinement of the atomic positions using single-crystal x-ray diffraction data. In the 50 mol %  $O_2$  mixture, the  $S_1$ transforms into the  $S_2$  phase at 5.5 GPa. The transition breaks the single crystal. A powder pattern of the  $S_2$  phase obtained in the 50 mol %  $O_2$  mixture at 6.9 GPa is presented in Fig. [8.](#page-4-1) The data are well indexed using *Pm*3*n* space group with  $a = 5.7828$  Å. The Rietveld analysis program GSAS  $(Ref. 18)$  $(Ref. 18)$  $(Ref. 18)$  was used for the structure refinement. The structural parameters are presented in Table [I.](#page-4-2)

Finally the  $S_2$  phase transforms into the  $S_3$  phase at 7 GPa. This transition, observed by x-ray diffraction in the 50 and 75 mol  $\%$  O<sub>2</sub> mixture, is expected to occur regardless of the concentration in  $S_2$ . The powder patterns of  $S_3$  obtained in the 50 mol %  $O_2$  mixture at 7.5 GPa is presented in Fig.

<span id="page-4-2"></span>TABLE I. Refined structural parameters of the  $S_2$  crystal (space group  $Pm3n$ ) for a 50 mol %  $O_2$  structure at 6.9 GPa and 296 K.

Unit cell $a_{\text{cub}} = 5.7828$ Å				
Label	$\mathcal{X}$	ν	Z.	Occ
$A_{R}1$	0.0000	0.0000	0.0000	0.500
O <sub>1</sub>	0.05988	0.05988	0.05988	0.125
$A_{R}2$	0.2500	0.5000	0.0000	0.500
O <sub>2</sub>	0.2367	0.4869	0.1020	0.125

<span id="page-4-3"></span>

FIG. 9. (Color online) X-ray diffraction pattern collected in a mixture of 50 mol % Ar-50 mol %  $O_2$  at 7.5 GPa (top). The dots correspond to the measured pattern and the line to the calculated pattern after a Lebail refinement.

[9.](#page-4-3) The diffraction pattern indicates a tetragonal distortion of the cubic phase. The situation is thus similar to what has been observed in pure solid nitrogen at the  $\delta-\delta'$  phase transition<sup>19</sup> but the *P*4<sub>2</sub>/*ncm* space group proposed for  $\delta^*$ does not fit all the diffraction lines. The present diffraction pattern is correctly indexed by a tetragonal unit cell with the lattice parameters  $a=11.6606$  Å and  $c=11.1970$  Å. This corresponds to a doubling of the lattice parameters of the gamma phase as already reported at low temperature.<sup>4</sup> Therefore, the structure of  $S_3$  is assumed to be an analog of the structure of the low-temperature  $\delta$  phase of Ar-O<sub>2</sub> solutions (symmetry group *I*-43*d*) with possible space group *I*-42*d*. The Rietveld refinement of the data to determine the exact atomic positions was unsuccessful.

The diffraction pattern of the  $Xe(O_2)_2$  compound has been collected on a polycrystalline solid in equilibrium with a O<sub>2</sub>-rich fluid at 3.7 GPa, in a mixture of 75 mol % O<sub>2</sub> concentration. The integrated diffraction pattern is presented in Fig. [10.](#page-5-0) The pattern can be best indexed by an *Fd*3*m* cubic unit cell. The volume of the unit cell almost matches 8  $\times V_{Xe} + 16 \times V_{O_2}$  at the same pressure.<sup>20,[21](#page-7-19)</sup> We propose that the  $Xe(O_2)_2$  adopts the MgCu<sub>2</sub>-type Laves phase structure,<sup>16</sup> with  $O_2$  and Xe occupying, respectively, the Cu and Mg sites. As discussed in the next section, based on the molecular size ratio, an  $AB_2$  Laves phase was expected in the  $Xe/O_2$ mixture, as observed for Ne(He)<sub>2</sub> (Ref. [22](#page-7-20)) and  $Ar(H_2)_2$ .<sup>[5](#page-7-3)</sup> The  $Xe(O_2)_2$  compound has been drawn in Fig. [10.](#page-5-0) The orientation of the molecules could not be refined by a Rietveld refinement of the powder spectra because of the too small number of crystallites in the x-ray beam. The orientation of the  $O_2$  molecules has been drawn to optimize a quadrupolar order, as in  $\varepsilon$ -N<sub>2</sub>.<sup>[23](#page-7-21)</sup> At higher pressure, the volume of  $Xe(O_2)_2$  remains close to the ideal mixing value of as shown in Fig. [11.](#page-5-1)

#### **V. DISCUSSION**

<span id="page-4-0"></span>An important conclusion from studies on metallic alloys is that the solid-state solubility is governed mainly by geo-

<span id="page-5-0"></span>

FIG. 10. (Color online) X-ray diffraction pattern obtained in a mixture of 25 mol % Xe-75 mol %  $O_2$  at 3.7 GPa and 296 K. A picture of the bidimensional pattern is presented together with the circularly integrated pattern. It is compared with a theoretical diffraction pattern for a  $Xe(O_2)_2$  solid with the MgCu<sub>2</sub> Laves phase structure and a lattice parameter of 9.20 Å [space group  $Fd3m$  $(Ref. 16)$  $(Ref. 16)$  $(Ref. 16)$ ]. The sample chamber is filled with numerous crystals of  $Xe(O_2)_2$ , in equilibrium with a  $O_2$ -rich fluid. Inset: picture of  $Xe(O_2)_2$  with the MgCu<sub>2</sub> structure. Xenon atoms and oxygen molecules are, respectively, drawn in white and red.

metrical effects, as expressed by the well-known Hume-Rothery rule.<sup>25</sup> This rule was shown to explain the shape of the phase diagrams of helium with other rare gases under pressure. This empirical rule applied here would state that solid solutions should exist if the effective molecular diameter of the two species do not differ by more than 15%. The effective diameter of a molecular species at a given pressure

<span id="page-5-1"></span>

FIG. 11. (Color online) Isothermal (296 K) equations of state of  $Xe(O_2)_2$  compound,  $ArO_2$  and  $Ar(O_2)_3$  alloys. The compression curves for ideal solutions of 33% Xe-67%  $O_2$ , 50% Ar-50%  $O_2$ , and 25% Ar-75%  $O_2$ , as calculated from the EOS of pure  $O_2$  (Refs. [13,](#page-7-11) [14,](#page-7-12) and [20](#page-7-18)), pure Ar (Ref. [21](#page-7-19)), and pure Xe (Ref. [24](#page-7-26)), are also plotted.

<span id="page-5-2"></span>

FIG. 12. Evolution of atomic/molecular radii ratios with pres-sure for the studied rare gases and oxygen (Refs. [12](#page-7-10)[–14,](#page-7-12) [20,](#page-7-18) [21,](#page-7-19) [24,](#page-7-26) and [26](#page-7-27)). The ideal ratios for Laves phases with compositions  $RGS(O_2)_2$  and  $O_2(RGS)_2$  (respectively, 1.225 and 0.816) are represented as continuous gray lines.

is proportional to the cubic root of its molar volume. The ratio of the rare-gas effective diameter over that of  $O_2$  versus pressure is plotted in Fig. [12.](#page-5-2) The ratio is almost unity for  $Ar/O<sub>2</sub>$  so a large concentration range of solid solutions is expected, as observed. For all the other rare gases, the difference is larger than 15%: slightly larger than 15% for Xe, explaining the partial miscibility—up to 15 mol %  $O_2$  in solid Xe; about 20% difference for Ne, explaining the small miscibility of Ne in  $O_2$  and vice versa and more than 30% difference for He, explaining the complete immiscibility in the solid phase. Furthermore, for a large difference, a fluidfluid miscibility gap is expected, as observed in the  $He/O<sub>2</sub>$ case.

In addition to substitutional alloys, various stoichiometric compounds can be formed. For hard-sphere systems, several types of stoichiometric compounds have been proposed, which optimize packing. By increasing small to large hardsphere diameter ratios  $\alpha$ , compounds of type *AB* ( $\alpha \le 0.4$ ),  $AB_2$  ( $\alpha \approx 0.5$ ), and  $AB_{13}$  ( $\alpha \approx 0.6$ ) have been predicted.<sup>27</sup> However none of these compounds have been observed so far in molecular mixtures under pressure. For  $\alpha \approx 0.8$ , a class of  $AB_2$  compounds are expected,<sup>28</sup> usually referred to as Laves phases. These phases have been first observed in metallic binary systems; the most efficient packing is obtained for  $\alpha$ =0.816. The Laves phases crystallize in one of the three closely related structures, $16$  isomorphous with the compound  $MgCu<sub>2</sub>$  (cubic cell, 8 f.u.),  $MgZn<sub>2</sub>$  (hexagonal cell, 4 f.u.), or  $MgNi<sub>2</sub>$  (hexagonal cell, 8 f.u.). As seen in Fig. [12,](#page-5-2) the effective diameter of  $O_2$  is 0.84 times that of Xe, close to the ideal value of 0.816 and indeed a  $Xe(O_2)_2$  compound is observed. On the other hand, the effective diameter of Ne is 0.8 times that of  $O_2$  but the compound  $O_2(Ne)_2$  has not been observed. Hence, consideration of efficient packing is certainly not the only parameter explaining the formation of Laves phases in molecular systems. As it was shown previously on the  $Ne(He)_2$  case, the formation of the Laves phase is driven by both entropy and energy.<sup>29</sup> An elaborate Gibbs energy calcu-

lation to fully explain the stability of the  $Xe(O_2)_2$  compound is beyond the scope of the present work.

Ne, Ar, and Xe rare-gas solids have a fcc structure. At least up to  $200$  GPa for Ne (Ref. [12](#page-7-10)) and Ar (Ref. [21](#page-7-19)) whereas a sluggish transition from fcc to hcp is observed in Xe over the pressure range 14 GPa–75 GPa[.30](#page-7-28) It is well known that the dissolution of small impurities in cryoraregas solids tend to favor the hcp structure. For example, the dissolution of no more than  $1\%$  O<sub>2</sub> in fcc cryo-Ar stabilizes the hcp structure.<sup>31</sup> It was thus expected that the fcc structure would be destabilized by the addition of oxygen. It is observed here that the fcc structure is more resistant to the dissolution of  $O_2$  at high pressure since up to 5 mol %  $O_2$ can be mixed with fcc Ar and fcc Ne before the solid solution adopts the hcp structure. More surprisingly,  $Xe-O<sub>2</sub>$  solid solutions with up to 15 mol  $\%$  O<sub>2</sub> retain the fcc structure. The fact that the rare gas with the least stable fcc structure under pressure is the one that can dissolve the larger amount of  $O_2$  without changing to the hcp structure is thus counterintuitive and should motivate detailed calculations.

The dramatic change in  $Ar/O<sub>2</sub>$  mixtures from full miscibility above the solidus line to complete immiscibility above 9 GPa is striking. The Hume-Rothery rule is highly violated here. The explanation originates from the sharp phase transition that occurs in pure solid  $O_2$  above 10 GPa. The nature of this phase transition has been recently elucidated as the molecular association of  $4 O<sub>2</sub>$  molecules into a rhombohedral  $(O_2)_4$  unit.<sup>8,[9](#page-7-7)</sup> The presence of this new chemical bond between  $O_2$  molecules affects the miscibility in the  $O_2$ /Ar mixture. That also explains the opening of the miscibility gap in  $Ne/O<sub>2</sub>$  mixtures above 9 GPa. This implies that the computation of the  $Ar/O<sub>2</sub>$  binary phase diagram above 10 GPa would have to be treated at the *ab initio* level. That is still a formidable challenge.

We have selected here below some applications of the present determination of the  $O_2$ /rare gas binary phase diagrams, one for each diagram: (1) the growth of  $O_2$  single crystals in a helium pressure medium. $8,14$  $8,14$  At 10 GPa, i.e., at the  $\delta$ - $\varepsilon$  transition, solid oxygen undergoes significant changes in its properties. The  $\varepsilon$  phase remains stable up to 96 GPa, above which the solid becomes metallic  $(\zeta$  phase). The structures of the  $\varepsilon$  and  $\zeta$  phases remained unsolved for decades, partly because of the low quality of the diffraction patterns obtained with pure oxygen powders. By exploiting the topology of the complete solid immiscibility in  $O_2$ /He mixtures, very good quality  $\varepsilon$  single crystals could be grown in helium. Practically, the crystal is grown in a  $O_2$ /He mixture with an initial 2.5 mol %  $O_2$  concentration and occupies one third of the full sample thicknesses at 20 GPa. But, at this concentration, the phase separation appears at 8 GPa at room temperature, i.e., below the  $\beta$ - $\delta$ - $\varepsilon$  sequence of transition. To directly phase separate in the stability domain of the  $\varepsilon$  phase, the single crystals were slowly grown at 450 K and 22.5 GPa.

(2) Formation of fine  $O_2$  powder in Ne.<sup>14</sup> In  $O_2$ /Ne mixtures, by rapidly increasing pressure from the fluid phase, a mixed powder of  $O_2$  and Ne crystals is obtained, with grains less than  $1 \mu m$  in diameter. Such a powder could be useful

to perform Rietveld refinement in the metallic phase of solid oxygen and thus complement x-ray diffraction measurement on single crystal.

(3) Recrystallization from a fine-grained polycrystalline mixture of pure solid  $O_2$  and solid Ar. The opening of a large miscibility gap in  $Ar/O<sub>2</sub>$  mixtures above 9 GPa transforms the  $Ar(O_2)$ <sub>3</sub> solid solution single crystal into a fine-grained polycrystalline mixture of Ar and  $O_2$ . Upon decreasing pressure below 9 GPa, a recrystallization of this powder into a single crystal of  $Ar(O_2)_3$  is observed within few hours. That implies great mobility of atoms and molecules, unexpected when vacancy mechanisms are excluded. A more detailed analysis will be the subject of a future publication.

(4) Reactivity of  $Xe-O<sub>2</sub>$  mixture at high pressure. The topochemical principle implies that  $Xe(O_2)_2$ , where xenon atoms and oxygen molecules lie close to each other, is an ideal reactant to synthesize xenon oxides under high pressure.

### **VI. CONCLUSIONS**

A series of  $O_2$ /rare gas binary phase diagrams at 296 K is presented here. The large range of differences in binary interactions explains the various types of binary phase diagrams observed, from an azeotrope type to an eutectic type with complete immiscibility in the solid phase and a liquidliquid miscibility gap. Two salient results of the present work are the discovery of the  $Xe(O_2)_2$  Laves phase compounds and the rich structural polymorphism in  $Ar/O<sub>2</sub>$  solid mixtures. A partial understanding of the various phase diagrams can be obtained, at a first level, from geometrical considerations. However, it is shown that this can be misleading at high pressure. The dramatic opening of an almost complete immiscibility gap in  $Ar/O_2$  solid solutions above 9 GPa is understood by the chemical change in the  $O_2$  molecules under pressure. That is the first observation of the effect of pressure-induced chemical changes on a binary phase diagram. *Ab initio* calculations seem to be the suited method for a microscopic investigation of the  $Ar/O<sub>2</sub>$  binary phase diagram. Yet remain a great challenge. Consequently, we believe that the present data set of  $O_2$ /rare gas mixtures should provide a useful corpus for testing calculations of mixture properties in molecular systems at high pressure. This is particularly important because there is a current great interest in the synthesis of new molecular materials by pressure. Part of the strategy for new molecular crystal engineering at high pressure is to control the ordering of the molecular entities in the reactant solid phase so as to preorganize the molecules in such a way to favor the reaction and the final product. Accurate predictions of the structural changes in binary mixtures will be an important step.

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