Magnetic properties of the geometrically frustrated $S = \frac{1}{2}$ antiferromagnets, La₂LiMoO₆ and Ba₂YMoO₆, with the B-site ordered double perovskite structure: Evidence for a collective spin-singlet ground state

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Two B-site ordered double perovskites, La₂LiMoO₆ and Ba₂YMoO₆, based on the $S=\frac{1}{2}$ ion, Mo⁵⁺, have been investigated in the context of geometric magnetic frustration. Powder neutron diffraction, heat capacity, susceptibility, muon-spin relaxation (μ SR), and ⁸⁹Y NMR-including magic-angle spinning (MAS) NMR data have been collected. La₂LiMoO₆ crystallizes in $P2_1/n$ with a=5.59392(19) Å, b=5.69241(16) Å, c=7.88029(22) Å, and $\beta=90.2601(30)^{\circ}$ at 299.7 K, while Ba₂YMoO₆ is cubic, Fm3m, with a = 8.39199(65) Å at 297.8 K. Ba₂YMoO₆ shows no distortion from cubic symmetry even at 2.8 K in apparent violation of the Jahn-Teller theorem for a t_{2g}^1 ion. ⁸⁹Y NMR MAS data indicate about a 3% level of Y/Mo site mixing. La₂LiMoO₆ deviates strongly from simple Curie-Weiss (C-W) paramagnetic behavior below 150 K and zero-field-cooled/field-cooled (ZFC/FC) irreversibility occurs below 20 K with a weak, broad susceptibility maximum near 5 K in the ZFC data. A Curie-Weiss fit shows a reduced $\mu_{eff}=1.42\mu_{B}$, (spin only = 1.73 $\mu_{\rm B}$) and a Weiss temperature, $\theta_{\rm C}$, which depends strongly on the temperature range of the fit. Powder neutron diffraction and heat capacity show no evidence for long-range magnetic order to 2 K. On the other hand oscillations develop below 20 K in µSR indicating at least short-range magnetic correlations. Susceptibility data for Ba₂YMoO₆ also deviate strongly from the C-W law below 150 K with a nearly spin only $\mu_{\text{eff}}=1.72\mu_{\text{B}}$ and $\theta_{\text{C}}=-219(1)$ K. There is no discernible ZFC/FC irreversibility to 2 K. Heat capacity, neutron powder diffraction, and μ SR data show no evidence for long-range order to 2 K but a very broad, weak maximum appears in the heat capacity. The ⁸⁹Y NMR paramagnetic Knight shift shows a remarkable local spin susceptibility behavior below about 70 K with two components from roughly equal sample volumes, one indicating a singlet state and the other a strongly fluctuating paramagnetic state. Further evidence for a singlet state comes from the behavior of the relaxation rate, $1/T_1$. These results are discussed and compared with those from other isostructural $S = \frac{1}{2}$ materials and those based on S = 3/2 and S = 1.

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I. INTRODUCTION

Geometric magnetic frustration (GMF) generally originates if spins, constrained by an antiferromagnetic (AF) nearest-neighbor exchange coupling, are situated on lattices with a topology of triangles or tetrahedra. Magnetic properties of GMF compounds have been studied intensively in recent years due to their exotic ground states, such as spin glasses, spin ices, and spin liquids.¹ Since the theoretical proposal by Anderson of one possible model for the spin liquid for frustrated antiferromagnets with $S=\frac{1}{2}$, researchers have been inspired to seek experimental evidence for the existence of spin-liquid states.² In this model the spins form a collective singlet ground state and the dynamics of singlets is normally retained down to low temperature. The pyrochlore compound $Tb_2Ti_2O_7$ (Ref. 3) and the so-called hyperkagome compound,⁴ Na₄Ir₃O₈,⁵ have been proposed as spinliquid compounds or candidates.

B-site ordered double perovskites with chemical formula $A_2BB'O_6$, where magnetic ions reside on the B' site, present a face-centered-cubic (fcc) symmetry, which is a threedimensional lattice based on edge sharing tetrahedra and is, thus, geometrically frustrated. In previous work, double perovskites with S=3/2 and S=1 spins and both cubic and monoclinic lattice symmetries have been studied in detail from the perspective of geometric frustration.^{6,7} Unit cells for the two crystallographic symmetries are shown in Fig. 1. For the S=3/2 materials it was found that, while frustration was clearly important, both Ba₂YRuO₆ and La₂LiRuO₆ did eventually show long-range antiferromagnetic order, even in the case of the former where a 1% level of Y/Ru site mixing was detected by ⁸⁹Y magic-angle spinning (MAS) NMR. In the case of the S=1 phases, long-range order was clearly quenched for both symmetries. La2LiReO6 showed a very unusual singlet ground state, while Ba₂YReO₆, which retains cubic symmetry in apparent violation of the Jahn-Teller (J-T)

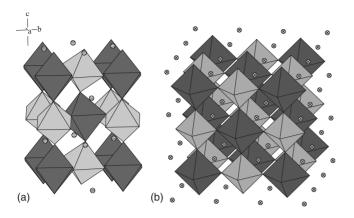


FIG. 1. (a) Crystal structure of La₂LiMoO₆, $P2_1/n$. Dark gray octahedra represent MoO₆ and light gray octahedral, LiO₆. Dashed circles represent the La ions. (b) Crystal structure of Ba₂YMoO₆, Fm3m. Dark gray octahedra represent MoO₆ and light gray octahedra, YO₆. The small crossed spheres represent the Ba ions.

theorem, undergoes spin freezing. Paradoxically, Y/Re site mixing was undetectable via ⁸⁹Y MAS NMR. In this work, two $S = \frac{1}{2}$ double perovskites, the cubic Ba₂YMoO₆ and monoclinic La₂LiMoO₆, have been studied in detail using a wide range of probes including powder neutron diffraction, bulk magnetic susceptibility, heat capacity, muon-spin relaxation, and ⁸⁹Y NMR, both MAS and paramagnetic Knightshift measurements. Ba₂YMoO₆ had been reported previously to remain paramagnetic to 2 K while no magnetic properties studies exist for La₂LiMoO₆.^{8,9} The results are compared with other isostructural $S = \frac{1}{2}$ B-site ordered double perovskites such as the monoclinic spin glass, Sr₂CaReO₆, the cubic ferromagnet, Ba₂NaOsO₆, and the cubic antiferromagnet, Ba₂LiOsO₆.^{10,11}

II. EXPERIMENTAL

Polycrystalline samples of La₂LiMoO₆ and Ba₂YMoO₆ were prepared using conventional solid-state reactions. For La₂LiMoO₆, a stoichiometric mixture of prefired La₂O₃, Li₂MoO₄, and MoO₂ were ground and sealed in a Mo crucible, heated to 1100 °C in an Ar atmosphere, and kept for 48 h. For Ba₂YMoO₆, BaCO₃, prefired Y₂O₃ and MoO₃, were weighed out stoichiometrically and the mixture was fired at 950 °C for 12 h, reground, then heated to 1300 °C in 5% H₂/Ar and held for 48 h.

Phase purity was assessed using a focusing Guinier-Hägg camera and PanAlytical X-Pert x-ray diffraction apparatus. Thermal gravimetric analysis (TGA) was carried out on Ba_2YMoO_6 by heating in air to determine the oxidation state of Mo. The weight gain was 1.45% compared to the expected 1.44% indicating the Mo⁵⁺ state to better than 1%.

dc magnetic susceptibility as a function of temperature was measured in 0.01–0.05 T applied fields within the temperature range of 2–300 K and isothermal magnetization data were collected for La₂LiMoO₆ in the field range from –5 to 5 T at 5 and 20 K using Quantum Design magnetic properties measurement system (MPMS) superconducting quantum in-

terference device (SQUID) magnetometer at McMaster University.

The powder neutron-diffraction measurements were carried out on the C2 diffractometer at the Canadian Neutron Beam Centre, NRC, Chalk River Laboratories. The measurements were performed at 3.3 and 299.7 K with neutron wavelengths, λ =1.32873 and λ =2.36937 for La₂LiMoO₆, and λ =1.33052 and 2.37192 Å at 2.8 and 297.8 K for Ba₂YMoO₆. Additionally, higher-resolution diffraction data at 2.8 K with λ =1.33052 Å was collected for this compound. Refinements were done either with the GSAS or FULL-PROF software packages.^{12,13}

Heat-capacity measurements were carried out using an Oxford MagLab calorimeter at McMaster University and a Quantum Design physical properties measurement system (PPMS) at Florida State University. The lattice match compounds La_2LiIrO_6 and Ba_2YNbO_6 were prepared using solid-state reactions as well. The synthesis method for La_2LiIrO_6 is described in Ref. 14. For Ba_2YNbO_6 a stoichiometric mixture of $BaCO_3$, prefired Y_2O_3 and Nb_2O_5 was heated at 1300 °C for 36 h in air.

Muon-spin relaxation (μ SR) measurements were carried out on the M20 beamline at TRIUMF in Vancouver. The zero-field μ SR (ZF- μ SR) data were collected at various temperatures between 1.66 and 25 K for La₂LiMoO₆, and at 2, 5, 10, and 20 K for Ba₂YMoO₆. For La₂LiMoO₆, longitudinal field μ SR (LF- μ SR) was also collected at 1.66 K for the field of 100, 400, 800, 1200, and 1600 G.

⁸⁹Y MAS NMR was carried out at the University of Manitoba using a Varian ^{UNITY}*Inova* 600 (B_0 =14.1 T) spectrometer operating at a Larmor frequency of 29.36 MHz. Ba₂YMoO₆ powder was packed in a ZrO₂ MAS rotor with a 22 µl fill volume and spun at 20000±6 Hz in a 3.2 mm double-resonance Varian-Chemagnetics probe. Acquisition was carried out using a 20° tip angle (v_{rf} =42 kHz), 270 000 coadded transients, and a recycle delay of 0.8 s. Frequency shifts are referenced with respect to 2M Y(NO₃)₃ at 0.0 ppm.

⁸⁹Y NMR (nuclear spin I=1/2, nuclear gyromagnetic ratio ${}^{89}\gamma_n/2\pi = 2.0859$ MHz/T), Knight-shift measurements were carried out at McMaster University in a fixed magnetic field of $B_0=7.7$ T. The NMR line shape was obtained by applying the standard fast Fourier transform (FFT) technique for the spin-echo envelope at ~ 100 K or higher. However, gradual line broadening was observed and the linewidth exceeded the bandwidth of our rf excitations at lower temperature. Accordingly, it was needed to convolute multiple FFT envelopes to obtain the entire line shape below ~ 100 K down to ~ 63 K. Below ~ 63 K, due to the extremely broad line shape, the line shape was measured point by point by integrating the spin-echo intensity. It was confirmed that the point-by-point measurements agree well with the convolution of the multiple FFT envelopes at 63 K. The ⁸⁹Y nuclear spin-lattice relaxation rate, $1/T_1$, was measured by applying saturation comb pulses prior to a regular spin-echo sequence, and varying the delay time between them. The single exponential fit of the recovery of nuclear magnetization was good, as expected for a nuclear spin I=1/2 nucleus.

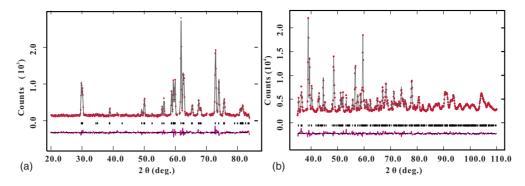


FIG. 2. (Color online) Rietveld refinement of neutron-diffraction data collected with two wavelengths, 2.37 Å (a) and 1.33 Å (b) at 297 K for La₂LiMoO₆. The vertical tick marks locate the Bragg peak positions and the lower horizontal line represents the difference between the data (crosses) and the model (solid line). A weak impurity peak near 70° was excluded for the 2.37 Å pattern.

III. RESULTS AND DISCUSSION

A. La₂LiMoO₆

1. Crystal structure

The crystal structure of La₂LiMoO₆ was confirmed by both x-ray diffraction and neutron-diffraction measurements to be monoclinic with space group $P2_1/n$, consistent with the previous x-ray single-crystal diffraction result of Tortelier and Gougeon.9 The unit-cell constants refined from the data collected at 300 K are a=5.5939(2) Å, b=5.6924(2) Å, c=7.8803(2) Å, and β =90.260(3)°. The overall refinement results are shown in Fig. 2 and Table I where both data sets were refined simultaneously using GSAS. The model assumes full ordering of the B-site cations (Li and Mo). This is consistent with the empirical study of B-site ion ordering in the double perovskites by Anderson et al.¹⁵ which shows that for a formal charge difference of 4, full B-site ordering is found, regardless of the difference in radii, Δr . For this compound even Δr is significant as the radii for Mo⁵⁺ (0.61 Å) and Li⁺ (0.76 Å) differ by almost 25%.¹⁶ Moreover, the isostructural compound, La2LiRuO6, was shown to have no detectable Li/Ru disorder using ⁷Li MAS NMR.¹⁷ There is no indication from the B-site atomic displacement parameters that this is not correct. The crystal structure of this compound at 3.3 K was also refined and the monoclinic structure, $P2_1/n$ was retained.

Note that in spite of the overall monoclinic symmetry, the nearest-neighbor environments of both B-site ions are those of a nearly perfect octahedron with a weak tetragonal compression. Especially for the Mo-O polyhedron, the O-Mo-O angles are either 90° or 180° to within a few tens of a degree. The weak tetragonal compression will split the nominally t_{2g}^1 configuration into a lower orbital singlet (d_{xy}) and a higher doublet (d_{xz}, d_{yz}) .

2. Magnetic properties

The susceptibility of this compound is shown in Fig. 3. Note the deviation from the Curie-Weiss (C-W) law below ~ 150 K. Data were fitted to the Curie-Weiss law, $\chi = C/(T-\theta)$ for the range T > 150 K, yielding, $\theta = -45(2)$ K and C = 0.253(1) (emu/mol K) corresponding to $\mu_{eff} = 1.42\mu_B$, compared to the spin only value of $1.73\mu_B$. A zero-field-cooled/field-cooled (ZFC/FC) divergence was observed at 20 K and a broad peak around 5 K. It should be noted that there was some sample to sample variability for this material, especially in terms of the derived θ value which varied from \sim -10 to -45 K. Nonetheless, robust observations for all samples include the deviation from the C-W law below 150 K, the ZFC/FC divergence at 20 K and the broad maximum near 5 K. Thus, an average frustration index, *f*

TABLE I. (a) The results for a Rietveld refinement using GSAS (Ref. 12) of neutron powder data for La₂LiMoO₆ (299.7 K) in $P2_1/n$. a=5.5939(2) Å, b=5.6924(2) Å, c=7.8803(2) Å, and $\beta =90.260(3)^{\circ}$. $R_{\rm wp}=0.0519$ and $\chi^2=2.47$. (b) Selected interatomic distances (angstrom) and angles (degree) for La₂LiMoO₆ at 299.7 K.

				U _{iso}
(a) Atom	x	У	Z	(Å ²)
La	-0.0098(6)	0.05034(35)	0.2516(4)	0.0106(5)
Li	0.5	0	0	0.029(5)
Mo	0.5	0	0.5	0.0119(10)
01	0.1917(8)	0.2159(8)	-0.0460(6)	0.0137(12)
O2	0.2855(7)	-0.3077(8)	-0.0421(6)	0.0105(11)
03	0.0836(7)	-0.5207(5)	0.2387(5)	0.0108(8)
(b) Bond	Dis./angle			
Mo-O1(x2)	1.975(4)			
Mo-O1(x2)	1.966(4)			
Mo-O3(x2)	1.940(4)			
Li-O1(x2)	2.148(4)			
Li-O2(x2)	2.148(4)			
Li-O3(x2)	2.117(4)			
01-Mo-01	180.0			
O1-Mo-O2	89.02(23)			
O1-Mo-O3	90.03(15)			
O2-Mo-O2	179.96			
O2-Mo-O3	89.72(18)			
O3-Mo-O3	180.0			
Li-O1-Mo	150.93(24)			
Li-O2-Mo	151.86(25)			
Li-O3-Mo	152.42(20)			

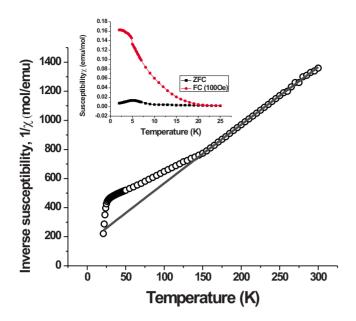


FIG. 3. (Color online) The inverse magnetic susceptibility of La_2LiMoO_6 showing Curie-Weiss behavior below 150 K. (Inset) The susceptibility below 25 K at an applied field of 100 Oe. Note the ZFC/FC divergence below ~20 K and the broad maximum at 5 K in the ZFC data.

 $= |\theta|/T^*$, falls in the range $\sim 1-2$ taking the divergence temperature as T^* , in stark contrast to the isostructural S=3/2 and S=1 materials, La₂LiRuO₆ and La₁LiReO₆, where $f \sim 7$ for each.^{6,7} Thus, from the bulk susceptibility there is no evidence for magnetic frustration, at least from the frustration index. The field dependence of the susceptibility shown in Fig. 4 discloses a weak hysteresis at 5 K, which disappears at 20 K, indicating the presence of a weak spontaneous moment below 20 K.

3. Magnetic neutron diffraction

There is no sign of long-range order in the neutron powder-diffraction data, Fig. 5, where the difference plot, 3.3-25 K is shown. Of course, the intensities of magnetic

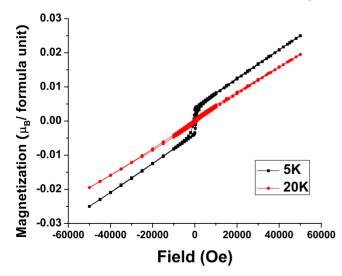


FIG. 4. (Color online) Hysteresis loops for La_2LiMoO_6 at 5 and 20 K.

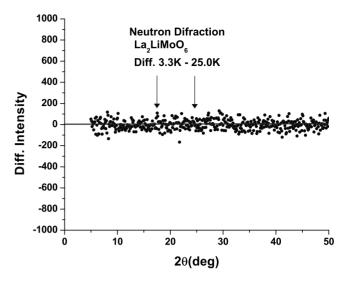


FIG. 5. The difference neutron-diffraction pattern for La_2LiMoO_6 , 3.3–25.0 K. The arrows show the positions expected for magnetic reflections assuming a type 1 fcc magnetic structure as found for La_2LiRuO_6 (Ref. 17).

Bragg peaks for $S = \frac{1}{2}$ spins is expected to be approximately ten times weaker than those from the S=3/2 analog, La₂LiRuO₆, where such peaks were readily visible above background.¹⁷

4. Heat capacity

Heat-capacity data, Fig. 6, show only broad features at 20 and 5 K, consistent with the bulk susceptibility and supportive of the absence of long-range magnetic order. Unfortunately, the chosen lattice match material, La₂LiIrO₆ was not useful here as its heat capacity actually exceeded that for LaLiMoO₆ above 20 K. The entropy removal from 7–2 K, including the peak at 5 K, is 0.25 J/mol K² or 4.4% of that expected for $S = \frac{1}{2}$.

 μ SR is a local probe of magnetism and is therefore complementary to the bulk techniques just described. ZF μ SR data are shown in Fig. 7(a). Although one observes only weak, paramagnetic relaxation at 25 K, well-defined oscillations are observed at 5 K. The latter indicates that each muon senses a static, unique field in the low-temperature regime. A FFT of the data at 6 K detects three peak frequencies, and this is consistent with the presence of three magnetically inequivalent oxygen sites in the crystal structure (see Table I). As a result, the data was fit to the following function:

$$A_0 P(t) = A_1 \exp(-\omega_1 t) \cos(\omega_1 t + \theta) + A_2 \exp(-\omega_2 t)$$
$$\times \cos(\omega_2 t + \theta) + A_3 \exp(-\omega_3 t) \cos(\omega_3 t + \theta)$$
$$+ A_{totil} \exp(-\lambda_{totil} t) + A_C G_{VT},$$

The three frequencies are given by ω_1 , ω_2 , and ω_3 , respectively, and their temperature dependences are plotted in Fig. 7(b). The onset of these frequencies is around 20 K, in line with the susceptibility and heat-capacity data. The A_{tail} term accounts for the volume fraction of the sample that is ordered but with a local field parallel to the muon spin. Finally, the Gaussian Kubo-Toyabe term (temperature-independent

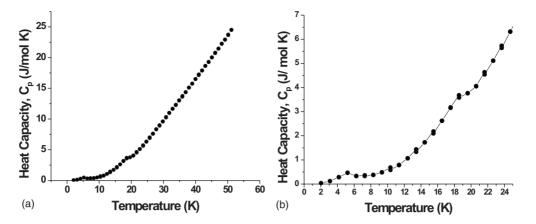


FIG. 6. (a) The heat capacity C_p as a function of temperature for La₂LiMoO₆. (b) The region below 25 K showing two broad peaks at ~18 and 5 K.

relaxation rate was assumed in this analysis) accounts for the volume fraction of the sample that is not ordered. Note that the amplitude of this component quickly dropped to zero below ~ 20 K, and so 100% of the volume fraction was found to be ordered at low temperatures.

For the data collected below 5 K, an additional frequency peak was observed in the FFTs at ~ 2 MHz shown in the inset of Fig. 7(b). This is likely related to the broad 5 K peak in the susceptibility and heat capacity and may signify a change in the local magnetic structure. As well, longitudinal field data (not shown) at 1.7 K show that decoupling occurs for an applied field of 800 Oe, indicating a static spin ground state.

While the behavior seen for La₂LiMoO₆ could be taken as evidence for long-range magnetic order, the evidence from heat capacity and neutron diffraction indicate otherwise. Of course it is not possible to measure a correlation length for the magnetic order sensed by a local probe such as μ SR and it is thus not possible to distinguish between true long-range order and order on a finite but significant length scale. A similar situation was encountered with Li₂Mn₂O₄ for which strong oscillations were detected by μ SR, whereas, the length scale of the magnetic correlations is known to be finite but on the order 90 Å.¹⁸

B. Ba₂YMoO₆

1. Crystal structure

The neutron-diffraction data collected at 2.7 and 298 K with $\lambda = 1.33$ and 2.37 Å were refined and the results are shown in Fig. 8 and Table II. The results are in excellent agreement with those of Cussen *et al.*⁸ According to the refinement, the compound retains cubic symmetry with space group *Fm3m*, and the lattice constant was determined to be 8.3827(7) Å at 2.7 K.

Surprisingly, even at 2.7 K, there is no clear distortion observed this compound although one could expect to see Jahn-Teller distortion arising from d^1 electronic configuration of Mo⁵⁺. Additionally, no distortion was observed with higher-resolution data, $(\Delta d/d \sim 2 \times 10^{-3})$ collected at 2.7 K, Fig. 8 (bottom). While the symmetry consequences of a J-T distortion in this material are not clear, certainly a lowering of the *m*3*m* site symmetry at the Mo site must occur. This will likely result in a lowering of the space-group symmetry. Such an effect was not observed in our data but a very subtle distortion below the resolution of the data cannot of course be ruled out. It is important to note that room-temperature x-ray diffraction data of much better resolution, $\Delta d/d \sim 1 \times 10^{-3}$, also did not show any distortion from *Fm*3*m* symmetry.

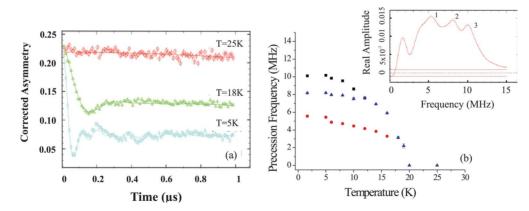


FIG. 7. (Color online) (a) μ SR results for La₂LiMoO₆. Corrected asymmetry at selected temperatures. (b) Temperature dependence of the amplitudes of the three frequencies (1–3) obtained from a fast Fourier transform (see text) of the data. The inset shows the result at 1.7 K where a fourth, low amplitude frequency at ~2 MHz is seen. This feature disappears above 5 K.

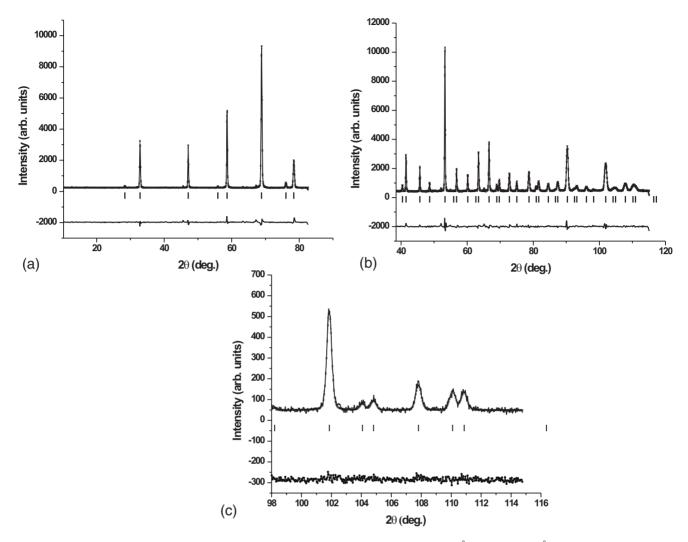


FIG. 8. The refinement result of neutron-diffraction pattern for two wavelengths, 2.37 Å (a) and 1.33 Å (b), collected at 2.7 K for Ba₂YMoO₆. (c) Higher resolution ($\Delta d/d \sim 2 \times 10^{-3}$), high angle data showing that cubic symmetry is retained. The vertical tick marks locate the Bragg peaks and the lower horizontal line is the difference between the data (circles) and the fit (solid line).

This compound has a charge difference of 2 for the B site ions which differ by 0.29 Å in ionic radius,¹² thus locating it near the B-site order/disorder boundary in the phase diagram of Anderson et al.¹⁵ and the issue of Y/Mo site disorder should be investigated. This discussion follows closely that already presented for Ba₂YRuO₆.⁶ Woodward et al.¹⁹ have studied B-site ordering in a number of double perovskites of the type $A_2BB'O_6$ with the combination B^{3+}/B'^{5+} , which is relevant here.²⁰ The extent of B/B' site order was determined quantitatively by a constrained refinement of neutron powder-diffraction data and by monitoring the relative widths of the hkl all-odd supercell reflections to the hkl alleven subcell reflections. In all cases of partial B-site order, the *hkl* all-odd reflections were significantly broader than the hkl all-even reflections. To summarize some of their findings, for $\Delta r > 0.260$ Å, 100% B/B'-site order is always found. For example, among the Fm3m phases studied, Ba₂YNbO₆ is judged to be 100% ordered, $\Delta r = 0.260$ Å, while Ba₂ScNbO₆ and Ba₂ScTaO₆, with Δr =0.105 Å, show only about 50% order. Thus, one would expect 100% B-site order in Ba₂YMoO₆.

First, the neutron-diffraction data were examined. The contrast in neutron-scattering lengths between Mo(6.715 fm) and Y(7.75 fm) is ~15%, about twice the contrast for x-ray scattering. There is no indication from the atomic displacement parameters, U, Table II, for obvious Y/Mo site disorder nor from the derived interatomic Y-O and Mo-O distances, which agree well with those of Cussen *et al.*⁸ and the sum of the ionic radii.¹⁶ As well, the full width at half maximum (FWHM) of several *hkl*-odd/*hkl*-even pairs were examined and no significant differences were found. For example, the odd/even width ratio for the (551,711)/(624) pair is 1.04(8) and that for the (553,731)/(642) pair is 1.01(8). Thus, from the neutron powder-diffraction data, there is no detectable Y/Mo site disorder.

Hence, ⁸⁹Y MAS NMR data were collected for this compound. Previous studies on Ba₂YRuO₆ which also showed no evidence for B-site disorder from neutron data disclosed a $\sim 1\%$ Y/Ru mixing.⁶ Figure 9 shows the spectrum obtained for Ba₂YMoO₆ at 288 K and there are two distinct peaks located at -1391 ppm and -1334 ppm with an area ratio of 81%/19%, respectively. The uncertainty in these areas is

TABLE II. (a) The results for a Rietveld refinement using FULLPROF (Ref. 13) of neutron powder data for Ba₂YMoO₆ in *Fm3m* at 297.8 and 2.7 K. *a*=8.3920(6) Å (297.8 K) and *a*=8.3784(6) Å (2.7 K). Agreement indices at 297.8 K: R_{wp} =0.063[0.076], χ^2 =2.51[2.08], R_B =0.031[0.021] and at 2.7 K: R_{wp} =0.067[0.054], χ^2 =3.00[9.45], R_B =0.035[0.011]. Numbers in [] are those from refinement of the λ =2.37 Å data and the others from λ =1.33 Å data. (b) Selected bond lengths and comparison with the sum of the ionic radii (Ref. 19).

() 207.0 V				$U_{\rm iso}$			
(a) 297.8 K	x	У	Z	$(Å^2)$	U_{11}	U_{22}	U_{33}
Ba	0.25	0.25	0.25	0.0072	0.0020(2)	0.0020(2)	0.0020(2)
Y	0.5	0.5	0.5	0.0043	0.0012(4)	0.0012(4)	0.0012(4)
Mo	0	0	0	0.0044	0.0012(4)	0.0012(4)	0.0012(4)
О	0.2347(2)	0	0	0.0123	0.0017(4)	0.0043(3)	0.0043(3)
2.7 K	x	У	Z	$U_{\rm iso}$ (Å ²)	U_{11}	<i>U</i> ₂₂	<i>U</i> ₃₃
Ba	0.25	0.25	0.25	0.0015	0.0005(3)	0.0005(3)	0.0005(3)
Y	0.5	0.5	0.5	0.0023	0.0006(4)	0.0006(4)	0.0006(4)
Mo	0	0	0	0.0008	0.0002(1)	0.0002(1)	0.0002(1)
0	0.2341(2)	0	0	0.0069	0.0005(4)	0.0026(3)	0.0026(3)
(b) Bond (Å)	297.8 K	2.7 K	$r_{\rm B} + r_{\rm O} \ (r_{\rm B'} + r_{\rm O})$				
Mo-O x6	1.969(3)	1.963(2)	1.96				
Y-O x6	2.227(3)	2.226(2)	2.25				

+/-3%. This is a considerably greater site mixing than found in Ba₂YRuO₆ or Ba₂YReO₆.^{6,7} Following the previous analysis⁶ the more negatively shifted peak is assigned to a Y-(O-Mo)₆ local environment and the other to Y-(O-Mo)₅(O-Y). Taking into account the coordination number of 6 at the Y site, an estimate of the mixing level is \sim 3%, too small to be detected in the neutron-diffraction data.⁶ Note that these results imply that a finite concentration of "defect" clusters of composition [Mo-(O-Mo)₆] will exist and this will likely be reflected in both the bulk and especially the local susceptibility.

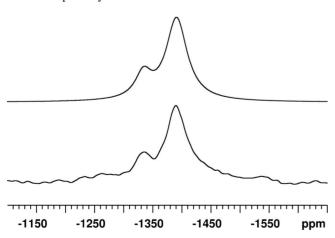


FIG. 9. ⁸⁹Y magic-angle spinning (MAS) NMR of Ba_2YMoO_6 at 288 K. The top is a simulation and the bottom are the data. The relative intensities of the two peaks are 19%/81% with an error of +/-3%.

2. Magnetic properties

Ba₂YMoO₆ shows only apparent bulk paramagnetic behavior down to 2 K, Fig. 10, which is consistent with the result previously reported by Cussen *et al.*⁸ The result of Curie-Weiss fitting above 150 K shows $\theta = -219(1)$ K, and an effective moment of $1.72(1)\mu_{\rm B}$ which is essentially the spin only value for $S = \frac{1}{2} (1.73\mu_{\rm B})$. These values are somewhat larger than those reported by Cussen *et al.* The frustration index, $f = |\theta_{\rm cw}|/T_{\rm N}$ for this compound is thus >100, indicative of extremely frustrated behavior. In order to verify any ordering/spin dynamics, we have conducted low-

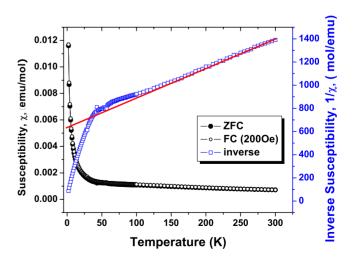


FIG. 10. (Color online) The susceptibility and inverse susceptibility of Ba_2YMoO_6 at an applied field of 200 Oe.

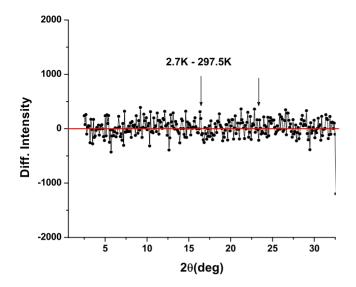


FIG. 11. (Color online) Neutron-diffraction difference pattern, 2.7–297.5 K for Ba_2YMoO_6 . The arrows show the expected positions of magnetic reflections assuming a type 1 fcc magnetic structure as found for Ba_2YRuO_6 (Ref. 6).

temperature neutron diffraction, heat capacity, muon-spin relaxation, and ⁸⁹Y NMR investigations.

3. Magnetic neutron diffraction

From the difference powder neutron-diffraction pattern (2.8–297.8 K), Fig. 11, no magnetic Bragg peaks were detected in the diffraction pattern. As in the case for La_2LiMoO_6 , while this observation is evidence against long-range magnetic order in this system, it is not necessarily conclusive given the small *S* value and other corroborating data are needed.

4. Heat capacity

Heat-capacity data for Ba_2YMoO_6 and Ba_2YNbO_6 , the lattice match phase, are shown in Fig. 12. Note the absence of a λ -type peak which again is evidence against long-range order. The magnetic heat capacity shows a very broad peak around 50 K. The entropy lost in this temperature range (<50 K) was calculated to be 51.9% of the theoretical value (*R* ln 2).

5. μSR

 μ SR data, collected at various temperatures, are shown in Fig. 13. One can see that the relaxation functions indicate dynamic spin behavior down to 2 K with a weak slowing down at 2 K but no indication of spin freezing or order on any length scale. The relaxation functions were fitted with the equation for dynamic behavior, $P(t)=A \exp(-\lambda t)$. Overall, the spins in this compound show persistent fluctuating spin behavior within the μ SR time window.

6. 89Y NMR

Ba₂YMoO₆ magnetic properties and spin dynamics were also studied through ⁸⁹Y NMR, measuring the linewidth of resonance peaks and paramagnetic Knight shifts. NMR is an extremely useful probe to uncover the distinctive temperature dependences of the local magnetic susceptibility which is different from the overall bulk average. For example, earlier ³⁵Cl and ¹⁷O NMR measurements uncovered the presence of vanishingly small spin susceptibility in a kagome antiferromagnet ZuCu₃(OH)₆Cl₂, although the bulk susceptibility data grows monotonically down to 2 K.^{21,22} In Fig. 14(a), representative ⁸⁹Y NMR line shapes at 295, 185, and 75 K are presented. A sharp peak with FWHM less than 10 kHz is evident near 295 K with however, a broad hump at the higher frequency side, and hence the overall line shape is tapered toward higher frequency. In addition, a small side peak on the higher frequency side of the main peak is observed which is most distinctly visible at 185 K near 16.03 MHz. The main sharp peak broadens gradually with decreasing temperature and masks the presence of this side peak which is no longer distinguishable at 75 K. The entire line shape is shifted to the lower frequency side compared with the expected position of the resonance in 7.7 T, ${}^{89}f_0 = {}^{89}\gamma_n B = 16.061$ MHz (shown by gray dotted line). For example, the peak frequency at 295 K, ${}^{89}f=16.041$ MHz, is shifted from ${}^{89}f_{o}$ by $\Delta f = {}^{89}f_{o} = -0.020$ MHz. This shift Δf is caused by the paramagnetic *Knight shift*, as defined by

$${}^{89}K = \Delta f / {}^{89}f_0. \tag{1}$$

 ^{89}K is represented in terms of percent, by applying a factor of 100, following the common convention in condensed-matter physics. (Note that 0.01% of the Knight shift corresponds to

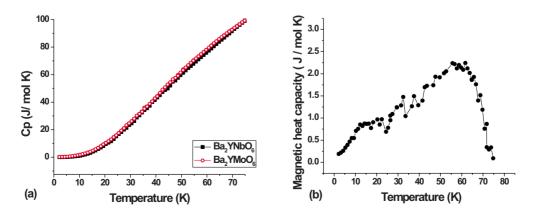


FIG. 12. (Color online) (a) The heat capacity of Ba₂YMoO₆ and Ba₂YNbO₆. (b) Magnetic heat capacity of Ba₂YMoO₆.

100 ppm.) ⁸⁹K is related to the paramagnetic susceptibility of Mo magnetic moments χ by

$$^{89}K = A\chi + K_{\rm chem},\tag{2}$$

where A is the hyperfine coupling constant, and K_{chem} is a small chemical shift (typically, $|K_{\text{chem}}| < 0.02\%$, or equivalently, <200 ppm).

Upon cooling, the overall line shape shifts further to lower frequency. In view of the observed increase in the bulk susceptibility data χ at lower temperatures presented earlier in Fig. 10, we can understand the observed temperaturedependent shift of the NMR line shapes as the consequence of a negative hyperfine coupling with magnetic moments, i.e., A < 0. The observed linewidth at 75 K, FWHM ~ 9 kHz, is typical for a paramagnetic insulator of a large bulk magnetic susceptibility. However, below \sim 75 K, qualitatively different NMR line shapes emerge, as shown in Fig. 14(b) in the form of two distinct peaks, clearly seen at 50 K, with one shifted to higher frequency. At 50 K the main peak is narrower than the higher frequency component only by a factor of ~ 2 and below 50 K the low-frequency component becomes very broad with decreasing temperature while shifting dramatically to lower frequencies. The proximity between the two peaks and the asymmetric line shape makes it difficult to estimate the intensity ratio accurately. Recalling that the hyperfine coupling constant A < 0, the ⁸⁹Y nuclear spins represented by the low-frequency peak sense a growing hyperfine field with decreasing temperature. In contrast the broader peak at the higher frequency shifts to higher frequency with decreasing temperature reaching a constant value at ~ 40 K. Thus, the local magnetic susceptibility near these ⁸⁹Y nuclear spins decreases with decreasing temperature.

In Fig. 15(a) the contrasting behavior of local magnetic susceptibility for the two distinctive ⁸⁹Y environments in the sample is demonstrated by plotting the temperature dependence of ${}^{89}K$, plotted as $-{}^{89}K$ to reflect the fact that A < 0, defined for different components of the NMR line shape. First, consider $-{}^{89}K_{CG}$, defined for the center of gravity of the whole line shape (open triangles). In essence, $-\frac{89}{CG}$ is a bulk average of local magnetic susceptibility at the nuclear spin of each ⁸⁹Y site, although the nonlocal nature of the hyperfine coupling makes the direct comparison somewhat nontrivial. Nonetheless, notice that the observed temperature dependence of $-{}^{89}K_{CG}$ is qualitatively similar to the SQUID data in Fig. 10. $-{}^{89}K_{CG}$, monotonically increases from 295 to ~ 100 K, levels off, then increases rapidly as $T \rightarrow 0$. The Knight shift $-{}^{89}K_{Main}$ defined for the low-frequency peak exhibits analogous behavior down to ~ 50 K, where the sharp feature becomes no longer observable in the NMR line shape. In contrast, the local magnetic susceptibility at the location of ⁸⁹Y nuclear spins involved in the higher frequency peak, as represented by $-{}^{89}K_{Singlet}$, begins to decrease below ~ 100 K down to ~ 40 K. The very small magnitude, $-^{89}K \sim 0.02\%$, observed at 40 K suggests that the *local mag*netic susceptibility is vanishingly small at these sites. Recalling that the integrated intensity of the higher frequency peak is roughly half of the overall NMR line shape, we conclude that about half of the magnetic moments at Mo sites become vanishingly small.

Further analysis of the $-^{89}K$ data can yield values of the hyperfine coupling constant, A, and an estimate of the separate contributions to the bulk susceptibility, $\chi = \chi_{spin} + \chi_{VV} + \chi_{dia}$, where χ_{VV} and χ_{dia} are the Van Vleck and diamagnetic contributions, respectively. In Fig. 16, $-^{89}K$ is plotted as a function of the bulk-averaged SQUID susceptibility, χ , by choosing temperature as the implicit parameter. Note the linear relations between $-^{89}K$ and χ above ~100 K. From the slope, one obtains the hyperfine coupling constant A=-23.4 kOe/ $\mu_{\rm B}$ using the results of $-^{89}K_{CG}$. The magnitude of A is ~5% greater (smaller) for $-^{89}K_{Main}$ $(-^{89}K_{Singlet})$. By extrapolating the linear fit to $-^{89}K_{CG}=0$, we find that $\chi_{\rm VV} + \chi_{\rm dia} \sim 2.2 \times 10^{-4}$ emu/mol in the temperature range above ~100 K.

Finally, the nuclear spin-lattice relaxation rate $1/T_1$ in Fig. 15(b) provides additional evidence for the presence of a collective singletlike ground state of Mo magnetic moments. $1/T_1$ measures the spectral weight at the NMR frequency ⁸⁹ f of the fluctuating hyperfine magnetic fields at the location of nuclear spins and may be written as

$$\frac{1}{T_1} \propto T \sum_{\vec{q} \in 1st \text{ BZ}} |A(\vec{q})|^2 \chi''(\vec{q}, f)$$

where χ'' is the imaginary part of the dynamical susceptibility, **q** is the wave vector, $f(\sim 16 \text{ MHz})$ is the resonance frequency, $A(\mathbf{q})$ is the hyperfine form factor, and the summation over **q** should be taken over the first Brillouin zone.

If $1/T_1$ is dominated by fluctuating hyperfine magnetic fields from localized magnetic moments at temperatures much greater than the energy scales of interactions between themselves, we expect $1/T_1 \sim \text{constant.}^{23}$ On the other hand, if the magnetic moments develop short-range order, $1/T_1$ generally increases with decreasing temperature near a magnetic instability. These results for $1/T_1$ measured at the main sharp peak show only a mild increase from 295 K down to ~ 50 K. The absence of a pronounced peak or divergent behavior rules out the presence of any magnetic long-range order. However, $1/T_1$ measured at the singletlike peak begins to deviate from the behavior of the main sharp peak below ~ 100 K and rapidly tends toward zero. This implies that the low-energy excitations of magnetic moments are nearly nonexistent, as expected for a collective singlet ground state. In

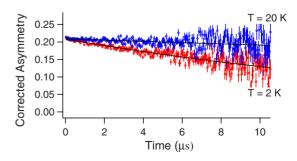


FIG. 13. (Color online) ZF μ SR data for Ba₂YMoO₆ for two temperatures. The lines are fits to a single exponential relaxation function, see text.

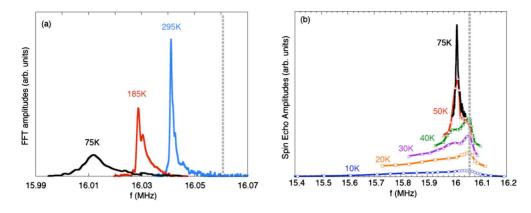


FIG. 14. (Color online) ⁸⁹Y NMR line shape at various temperatures. (a) Representative line shapes at selected temperatures for Ba_2YMoO_6 . (b) Evolution of the line shape below 75 K.

order to characterize this singletlike spin state, we model the overall temperature dependence as $1/T_1 \sim C/T \exp(-\Delta/k_{\rm B}T)$, where *C* is a constant. We found that the behaviors of the singletlike peak below 150 K as well as the main peak above 150 K can be reproduced well by choosing the gap size as $\Delta/k_{\rm B} \sim 140$ K. Recall, however, that the singletlike peak accounts for only about a half of all ⁸⁹Y nuclear spins in the sample the other half being in the broad tail of the NMR line shape below ~50 K, as shown in Fig. 14(b). $1/T_1$ measured for these ⁸⁹Y nuclear spins does *not* show any suppression below ~50 K, as shown by data points represented by open triangles. In other words, approximately half of ⁸⁹Y nuclear spins continue to sense the same level of fluctuating hyperfine magnetic fields arising from low-energy excitations of magnetic moments even below 50 K.

It is of considerable interest to return to the bulk susceptibility at this stage to look for evidence for the singlet state. In Fig. 17, the bulk data are plotted following the subtraction of a Curie-Weiss plus TIP tail obtained by fitting the data below 40 K. The constants for this fit are: C=0.0338 emu K/mol, θ =-1.07 K, and χ (TIP)=5.6 $\times 10^{-4}$ emu/mol. Note the similarity to the data of either Fig. 15 and 17, bringing the bulk and local susceptibility results into at least qualitative agreement. However, the Curie constant for the tail part of the bulk data, 0.0338 emu K/mol, is much smaller than that found from fitting the high-temperature bulk data, C=0.36 emu K/mol, and does not approach 50% as might be expected from the analysis of the local susceptibility via NMR.

Before continuing, it is important to consider a possible role for single ion physics in this system, as the Mo⁵⁺ ion, $5d^1$, t_{2g}^1 , has been shown to reside at a site of rigorously octahedral symmetry. This problem was first addressed by Kotani²⁴ and a detailed discussion can be found as well from other sources.²⁵ The basic result is that the perturbation of spin-orbit coupling on the ${}^{2}T_{2}$ crystal-field term of the t_{2g}^{1} configuration results in an unusual "nonmagnetic quartet" (NMQ) ground state which arises due to an accidental cancellation of the spin moment by the unquenched orbital moment. This is not a singlet state in the sense that this term is normally used but the result is that the ground-state magnetic moment is in fact zero. This NMQ state is separated from a magnetic doublet by an energy gap $\Delta = 3\lambda/2$, where λ is the single ion spin-orbit coupling constant. For Mo^{5+} , λ =1030 cm⁻¹ or 1481 K, thus, a gap of $\Delta/k_{\rm B}$ ~2200 K would be expected on this basis. Even considering a reduction in λ due to orbital delocalization effects of 20–30 % or even more, the single ion energy scale is more than one order of magnitude larger than anything seen in the data presented above. Thus, while the single ion effects should be consid-

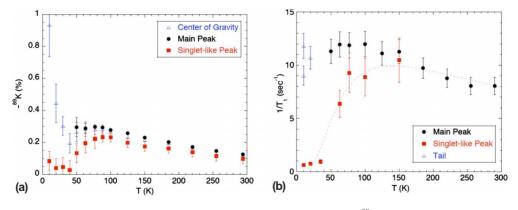


FIG. 15. (Color online) Temperature dependence of the paramagnetic Knight shift, $-{}^{89}K$ (a) and the relaxation rate, $1/T_1$ (b) for the "main" (lower frequency) peak and the singletlike (higher frequency) peak of Fig. 14(b). The dotted line is an empirical fit $1/T_1 \sim C/T \exp(-\Delta/k_B T)$ with $\Delta/k_B \sim 140$ K. Integrated intensities of the two are roughly equal.

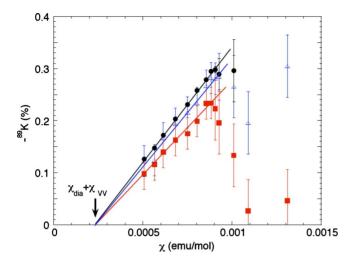


FIG. 16. (Color online) Scaling of the paramagnetic Knight shift $(-^{89}K)$ with the bulk susceptibility for Ba₂YMoO₆. The derived hyperfine coupling constant, A = -23.4 kOe/ $\mu_{\rm B}$. The intercept gives the sum of the Van Vleck and diamagnetic susceptibility components.

ered in any detailed theory for this material, it seems highly doubtful that the observed singlet state is of single ion origin and strengthens the case for a collective singlet state.

IV. SUMMARY AND COMPARISON WITH OTHER S=3/2, S=1, AND $S=\frac{1}{2}$ SYSTEMS

This is the third part of a systematic study of the ground states of geometrically frustrated B-site ordered double perovskites. Beginning with the monoclinic phases, the S=3/2 compound, La₂LiRuO₆ shows antiferromagnetic long-range ordering,⁶ while the S=1 compound, La₂LiReO₆, finds a collective singlet ground state with a finite concentration of defects which can be polarized in applied fields, indicating a role for the reduced spin quantum number in ground-state determination.⁷ Remarkably, the $S=\frac{1}{2}$ analog, La₂LiMoO₆, is

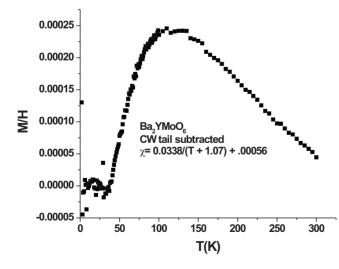


FIG. 17. The Curie-tail subtracted bulk susceptibility of Ba_2YMoO_6 .

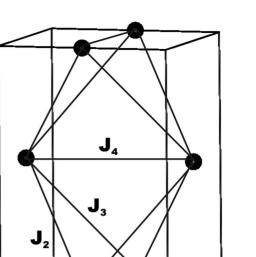


FIG. 18. $Mo^{5+}(Re^{6+})$ sites in La₂LiMoO₆ (Sr₂CaReO₆) showing two edge-sharing tetrahedra within the monoclinic unit cell. The four exchange pathways calculated in Table III are indicated.

nearly long-range ordered, showing at least short-range order in both the heat capacity and μ SR behavior. This is somewhat surprising as, normally, one expects unconventional behavior for $S=\frac{1}{2}$ due to the enhanced importance of quantum fluctuations. This observation is especially puzzling when compared to the isostructural, isospin material, Sr₂CaReO₆, which has a spin-frozen ground state.¹⁰

A possible explanation of this apparent paradox is provided by consideration of the role of the local environment of the $S=\frac{1}{2}$ magnetic ion in the two compounds. As already mentioned, the Mo-O coordination is octahedral with a weak tetragonal compression. In contrast the Re-O octahedron shows a weak tetragonal elongation.¹⁰ Thus, in La₂LiMoO₆ one expects an isolated d_{xy} ground state with nearly degenerate d_{xz} and d_{yz} at higher energies. Just the opposite level ordering will occur in Sr₂CaReO₆. This should give rise to a significant difference in the relative magnitudes of the various exchange pathways in the two materials. To test this hypothesis a spin dimer analysis was undertaken.^{26,27} There are four such exchange pathways J_1 to J_4 as shown in Fig. 18. Calculations were carried out assuming occupation of only the d_{xy} orbital for La₂LiMoO₆ and equal occupation of d_{xz} and d_{yz} for Sr₂CaReO₆ and the results are displayed in Table III. Note that for La₂LiMoO₆ the J_4 pathway exceeds the other three by at least an order of magnitude, while for

TABLE III. Comparison of relative exchange pathway (Fig. 18) strengths in La_2LiMoO_6 and Sr_2CaReO_6 .

Pathway	La ₂ LiMoO ₆ (d_{xy})	$Sr_2CaReO_6 (d_{xz}, d_{yz})$
J_1	0.14	1.0
J_2	0.014	0.16
J_3	4.3×10^{-4}	0.25
J_4	1.0	0.87

 Sr_2CaReO_6 there are three interactions of comparable magnitude, perhaps all four. Thus, these results suggest that a low-dimensional model is more appropriate for the Mo phase while a geometrically frustrated model is better for the Re material. This is consistent with the observations, as, for a low-dimensional magnet, strong, short-range spin-spin correlations can develop which will be detected by a local probe such as μ SR (Mo case), while geometric frustration is favored when the exchange pathways are of roughly equal strength (Re case).

Turning to the cubic materials, Ba₂YRuO₆ (S=3/2) shows a large frustration index, $f \sim 18$ but, in spite of detectable Y/Ru site mixing at the 1% level, is long-range AF ordered below 36 K.⁶ Cubic Ba₂YReO₆(S=1) is also highly frustrated, f > 12, with no detectable Y/Re site disorder, yet, it shows spin-freezing behavior with an ill defined freezing temperature. On the other hand, cubic Ba₂YMoO₆ ($S=\frac{1}{2}$) exhibits a most unusual heterogeneous ground state comprised, roughly equally, of gapped, collective spin singlet, and paramagnetic components. In spite of a $\sim 3\%$ Y/Mo site mixing there is no sign of spin freezing on any time scale investigated to 2 K. A singlet/triplet gap, $\Delta/k_B \sim 140$ K was inferred from NMR data. Neutron inelastic scattering experiments are currently underway to investigate further the nature of the gap. Among these three isostructural com-

pounds, the enhanced quantum fluctuations in the S=1 and $S=\frac{1}{2}$ materials appear to play an important role in suppression of long-range order.

Comparing Ba₂YMoO₆ to other $S = \frac{1}{2}$ cubic double perovskites, one notes immediately a sharp contrast with Ba₂LiOsO₆ and Ba₂NaOsO₆ (based on Os⁷⁺) which are antiferromagnetic and ferromagnetic, respectively, with minimal evidence for a role for geometric frustration.¹¹ This is a most puzzling situation as no clear pattern of behavior emerges for these isostructural/isospin materials which indicates that a detailed understanding of these remarkable differences will not be easily gained.

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MAGNETIC PROPERTIES OF THE GEOMETRICALLY...

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