Polar catastrophe, electron leakage, and magnetic ordering at the LaMnO₃/SrMnO₃ interface

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Electronic reconstruction at the polar interface LaMnO₃/SrMnO₃ (LMO/SMO) (100) resulting from the polar catastrophe is studied from a model Hamiltonian that includes the double and superexchange interactions, the Madelung potential, and the Jahn-Teller coupling terms relevant for the manganites. We show that the polar catastrophe, originating from the alternately charged LMO layers and neutral SMO layers, is quenched by the accumulation of an extra half electron per cell in the interface region as in the case of the LaAlO₃/SrTiO₃ interface. In addition, the Mn e_g electrons leak out from the LMO side to the SMO side, the extent of the leakage being controlled by the interfacial potential barrier and the substrate induced epitaxial strain. The leaked electrons mediate a Zener double exchange, making the layers adjacent to the interface ferromagnetic, while the two bulk materials away from the interface retain their original type A or G antiferromagnetic structures. A half-metallic conduction band results at the interface, sandwiched by the two insulating bulks. We have also studied how the electron leakage and consequently the magnetic ordering are affected by the substrate-induced epitaxial strain. Comparisons are made with the results of the density-functional calculations for the (LMO)₆/(SMO)₄ superlattice.

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I. INTRODUCTION

Polar interfaces have commanded considerable interest recently because extra electrons may migrate to the interface to "heal" the polar catastrophe and these interfacial electrons may exhibit unusual two-dimensional properties. A polar interface of current interest is LaAlO₃/SrTiO₃ (LAO/STO),¹⁻⁶ which shows a variety of phenomena such as the Kondo resistance minimum, superconductivity, magnetism, and metallic or insulating behavior under varying circumstances.²

This paper is devoted to a theoretical study of the interface between LaMnO₃ and SrMnO₃, which is a polar interface (Fig. 1) with the extra twist that both constituent materials are also magnetic. Presence of the Mn-localized moments introduces a new interaction channel for the electron gas forming at the interface. In fact, in a similar system, viz., a single δ -doped LMO layer in a SMO matrix, where an extra electron per cell becomes introduced at the δ -doped layer, the formation of a spin-polarized two-dimensional electron gas was predicted due to the Zener double exchange between the itinerant electrons and the localized Mn moments.⁷ On the experimental front, it has been demonstrated that high-quality superlattices of the manganites can be grown by molecular-beam epitaxy and the magnetic properties can be controlled by the superlattice period as well as by substrate-induced strain.⁸⁻¹⁴ Various experimental and theoretical studies have found diverse magnetic phases for these superlattices.⁸⁻²¹

Both LMO and SMO are magnetic with LMO being a type A antiferromagnetic (AFM) insulator with the Mn $t_{2g}^3 e_g^1$ configuration and consisting of alternating positively charged LaO and negatively charged MnO layers along the (100) direction. On the other hand, SMO is a type G AFM insulator with Mn $t_{2g}^3 e_g^0$ configuration with neutral SrO and MnO₂ layers. As a result of the layer charge configuration, a polar catastrophe—the divergence of the Coulomb potential away from the interface—arises in this system (Fig. 1) as in the case of the LAO/STO interface. We note that unlike the latter

case, where different layer termination produces two different *n*- and *p*-type interfaces, for the LMO/SMO interface, the MnO_2 layers being common to both, we just have a single type of interface, which by simple electron counting, is expected to be *n* type, with extra electrons coming to the interface region as illustrated in Fig. 1. We study the issues of polar catastrophe, charge leakage, and magnetism at the interface by using a tight-binding model Hamiltonian that includes all the relevant interactions in the system, complementing the study with the *ab initio* density-functional calculations.

The main results that emerge from our work are the following. (i) Half an electron per unit cell accumulates at the interface to avoid the polar catastrophe much like the case of LAO/STO, although now the electrons are much more confined to the interface (Fig. 2). (ii) In addition, the $Mn(e_g)$ electrons leak from the LMO to the SMO side, spreading to several layers. (iii) While the LMO and the SMO layers away from the interface retain, respectively, the type A and



FIG. 1. Illustration of the polar catastrophe for the LMO/SMO (100) interface. The layers are neutral on the SMO side, but are charged ± 1 on the LMO side leading to the unrestricted growth of the Coulomb potential (dashed line) and the scenario where it is healed by accumulating 0.5 electrons per cell on the interfacial MnO₂ layer (solid line). The layer numbers indicated in this figure are used throughout the paper.



FIG. 2. Layer-projected Mn e_g occupancy across the interface, as obtained from the model Hamiltonian with dielectric constant ϵ = 10. About half an electron per Mn atom accumulate at the interface to remove the polar catastrophe and, furthermore, a small number of electrons leak from the LMO to the SMO side. Electrons at the interface form a spin-polarized 2D electron gas, sandwiched between the two insulating bulks.

type G AFM structures of the bulk, the interface becomes ferromagnetic (FM) due to the double exchange between the itinerant carriers and the Mn core spins. (iv) Finally, we show that the magnetic ordering at the interface is sensitive to the substrate-induced epitaxial strain. However, our results suggest the absence of any canted magnetic state at the interface.

II. MODEL HAMILTONIAN

Density-functional calculations on the manganites have provided important insights into the electronic structure.^{22,23} The important electrons near the Fermi energy are the itinerant $Mn(e_g)$ electrons, which interact with the localized $Mn(t_{2g})$ core spins via the double exchange.^{24,25} The other important terms to consider are the Jahn-Teller (JT) coupling of the e_g electrons with the octahedral vibrational modes and the Madelung potential of the constituent atoms that would lead to the polar catastrophe without the electronic reconstruction at the interface.

Incorporating these key interactions, we construct the model Hamiltonian

$$\mathcal{H} = \sum_{i\alpha} \left(\varepsilon_{i\alpha} + \frac{1}{\epsilon} \sum_{\nu} M_{i\nu} q_{\nu} \right) c^{\dagger}_{i\alpha} c_{i\alpha} + \sum_{\langle ij \rangle \alpha\beta} t_{i\alpha,j\beta} \cos(\theta_{ij}/2) \\ \times (c^{\dagger}_{i\alpha} c_{j\beta} + \text{H.c.}) + U \sum_{i} n_{i1} n_{i2} + \sum_{i} \mathcal{H}^{i}_{\text{JT}} + \frac{J}{2} \sum_{\langle ij \rangle} \hat{S}_{i} \cdot \hat{S}_{j},$$
(1)

which describes the motion of the $Mn(e_g)$ electrons in a matrix of Mn core spins. These electrons are effectively spinless as discussed later. The e_g electrons are restricted to the Mn sites, but all atoms in the structure (Mn, Sr, La, and O) contribute to the electrostatic potentials that these electrons see, so that the Madelung matrix M_{ij} goes over all atoms. In the Hamiltonian above, $c_{i\alpha}^{\dagger}$ creates an electron at the *i*th Mn site and α is the orbital index of the e_g electron (x^2-y^2 or z^2-1), $n_{i\alpha}$ is the corresponding number operator, $\langle ij \rangle$ denotes summation over nearest-neighbor pairs, and while the *i* summa-

tion runs over only the Mn sites, the ν summation runs over all atoms in the structure.

The first term in the Hamiltonian describes the onsite energy, where the energies $\varepsilon_{i\alpha}$ of the two e_g orbitals could be split due to strain (considered later in the paper). The Madelung energy is given by $E_{Mad} = \frac{1}{2\epsilon} \sum_{\nu\nu'} M_{\nu\nu'} q_{\nu} q_{\nu'}$, where q_{ν} denotes the total charge (ionic+electronic) of the ν th atom, ϵ is the dielectric constant, the diagonal terms of the Madelung matrix $M_{\nu\nu'}$ exclude the Coulomb contribution from the same site, and the factor of two comes from double counting. The Madelung potential seen by the e_g electron is given by $V_{Mad} = dE_{Mad}/dn_{i\alpha} = \frac{1}{\epsilon} \sum_{\nu} M_{i\nu} q_{\nu}$, which appears in the first term in the Hamiltonian. The Madelung matrix for the structure is obtained by using the standard Ewald summation method.

The second term in the Hamiltonian is the electronic hopping energy. We have taken the Hund's energy J_H to be ∞ , so that the coupling between the core and the itinerant spins $\mathcal{H}_{Hund} = -J_H \Sigma_{i\alpha} \tilde{S}_i \cdot \tilde{s}_{i\alpha}$ makes the electron state inaccessible, where the electron spin is antialigned with the local t_{2g} core spin. Thus the itinerant electrons are effectively spinless and the electron hopping is diminished by the Anderson-Hasegawa $\cos(\theta_{ij}/2)$ factor,²⁵ where θ_{ij} is the angle between the (classical) core spins at the two sites. The nearest-neighbor hopping integral t depends on the relative positions of the two Mn sites in the lattice. For nearest-neighbor hopping in the xy plane or along the z axis, we have

$$t_{\alpha\beta}^{xy} = \frac{V_{\sigma}}{4} \begin{pmatrix} 1 & \mp \sqrt{3} \\ \mp \sqrt{3} & 3 \end{pmatrix}, \quad t_{\alpha\beta}^{z} = V_{\sigma} \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix}, \tag{2}$$

where V_{σ} is the $dd\sigma$ matrix element, the \mp sign corresponds to hopping along x (- sign) or y (+ sign) directions, and the much smaller $dd\delta$ interaction has been neglected. The third term in the Hamiltonian is the Coulomb repulsion between the two e_g orbitals on the same site.

The $J\bar{T}$ coupling term on each site is given by^{26,27}

$$\mathcal{H}_{\rm JT} = \frac{1}{2} K(Q_2^2 + Q_3^2) - g(Q_3 \tau_z + Q_2 \tau_x), \tag{3}$$

where $\vec{\tau}$ is the pseudospin describing the two e_g orbitals, viz., $|\uparrow\rangle = |z^2 - 1\rangle$ and $|\downarrow\rangle = |x^2 - y^2\rangle$. With the corresponding creation operators being c_{i1}^{\dagger} and c_{i2}^{\dagger} , respectively, we have: $\vec{\tau} = \sum_{\alpha\beta} c_{i\alpha}^{\dagger} \vec{\tau}_{\alpha\beta} c_{i\beta}$, where the greek indices denote the orbitals and *i* is the site index. The quantities Q_2 and Q_3 are, respectively, the basal plane distortion mode and the octahedral stretching mode at the *i*th site, *K* is the elastic stiffness constant, and *g* is the JT coupling strength. The final term in the Hamiltonian describes the AFM superexchange interaction between the Mn t_{2g} core spins.

The typical values of the Hamiltonian parameters used in our calculations are: $K=9 \text{ eV}/\text{Å}^2$ following from the optical studies on $\text{La}_{0.85}\text{Sr}_{0.15}\text{MnO}_3$,²⁸ g=2.0 eV/Å, and $V_{\sigma}=-0.5 \text{ eV}$ following earlier density-functional results,²⁷ J = 26 meV, estimated from the Neél temperature of CaMnO₃,^{29,30} a compound similar to SrTiO₃, and finally, U = 3 eV, which is a reasonable for the Mn(e_g) electrons. The values for the JT distortions in the LMO bulk are:³¹ Q_2^0 = 0.28 Å and Q_3^0 =-0.10 Å. These distortions are bulklike

on the LMO side and go to zero on the SMO side, where there are no e_g electrons. There is a transition region in between, where, for simplicity, we have taken the distortion strengths to be linearly dependent on the site electron occupancy of the e_g orbitals, which would be the result for the isolated octahedron. This is easily seen from an examination of the single-site JT Hamiltonian (3). If the electron occupancy *n* is taken to be a continuous variable as appropriate for a mean-field model, it immediately follows from the diagonalization of Hamiltonian (3) that the optimized magnitude of the distortion is given by: $(Q_2^2 + Q_3^2)^{1/2} = gn/K$. Following this argument, we use the distortion magnitudes at each Mn site as: $Q_2 = n \times Q_2^0$, where Q_2^0 is the magnitude for bulk LMO and similarly for Q_3 .

There is one more point to be made regarding the model. The measured value of the dielectric constant for LMO is 16–18 while for SMO, it is roughly 35.^{32,33} From work on the LAO/STO interface, it has been argued that the dielectric constant for STO is drastically reduced³⁴ in the presence of an electric field, which exists at the interface. We, however, use a uniform dielectric constant in our model calculations following earlier authors,³⁵ which is reasonable within the spirit of our model. We find that the electron-density profile near the interface region obtained from our model using $\epsilon \approx 8-10$ fits well with the *ab initio* density-functional results. Unless otherwise stated, we have taken $\epsilon = 10$ in our model calculations.

We solve the model Hamiltonian within the Hartree approximation, where we replace the Coulomb interaction term in Eq. (1) by its mean-field approximated value: $Un_1n_2 \approx U(n_1\langle n_2 \rangle + \langle n_1 \rangle n_2 - \langle n_1 \rangle \langle n_2 \rangle)$. Tests show that the exchange term in the Hartree-Fock approximation, which is neglected here, contributes very little to the total energy. A supercell geometry is adopted for the convenience of calculation; we find that the (LMO)₁₀/(SMO)₁₀ cell is large enough for our purposes. For a fixed core spin configuration, beginning with an initial set of Mn site occupancies, the band structure was computed in the Brillouin zone by diagonalizing the Hamiltonian, from which new site occupancies were determined, and the process was repeated until self-consistency was reached to the desired accuracy.

To compare with the results of our model calculations, we have also performed an *ab initio* density-functional calculation using the linear muffin-tin orbitals method (LMTO) with the generalized gradient approximation to the exchange-correlation functional with the Coulomb correction (GGA+U) using a somewhat smaller supercell, viz., (LMO)₆/(SMO)₄, and a value of U=3 eV, which is reasonable for the Mn(e_g) electrons. In both the model as well as the first-principles calculations, the unit cell is always doubled in the planar direction so as to treat both the FM and the AFM cases on equal footing and also to reveal any possible charge ordering.

We note that the Coulomb interaction U is not too critical for the two constituent bulks, LMO and SMO, because of a strong JT interaction and/or a crystal-field splitting. Because of this, small increase in the U value is not expected to produce significant changes in the physics discussed here. On the LMO side, only one of the two $e_g\uparrow$ states is filled with the Hubbard gap $\Delta \approx 2g(Q_2^2+Q_3^2)^{1/2}+U$, where the first TABLE I. Relative energies (per Mn interface atom) for different magnetic configurations. The intralayer magnetic couplings are denoted by the symbols F or A (FM or AFM ordering within the plane), while bracketed symbols (F) or (A) denote the coupling between the adjacent interface layers. (F, A) means that half the interlayer bonds are FM and the other half are AFM. The lowest energy structure, corresponding to the first line of the table, is shown in Fig. 3.

Magnetic order at the interface					Energy	
Intralayer layer#–1	Interlayer	Intralayer layer#0	Interlayer	Intralayer layer#1	DFT (eV)	Model (eV)
F	(F)	F	(F)	F	0	0
F	(F)	F	(F, A)	А	0.162	0.406
F	(A)	F	(F)	F	0.101	0.175
F	(A)	F	(F, A)	А	0.295	0.684
F	(F, A)	А	(A)	А	0.957	1.026

term is the single-particle JT splitting as obtained from the diagonalization of Eq. (3), so that the states are already strongly split by the JT interaction. Thus although the gap value would increase with U, the essential nature of the insulating state is well described without the Coulomb term, a result established early on from density-functional studies of the bulk LMO, where it was found that an insulating state results within the local-density approximation provided the correct crystal structure with the JT distortions is taken into account.^{22,23} Soon after, Benedetti and Zeyher³⁶ showed that in the limit that the Coulomb interaction is much larger than the JT coupling, both effects can be lumped together into a single effective coupling constant. The finite-temperature phase boundaries between orbitally ordered states are remarkably the same, even at a quantitative level, whether one includes the Coulomb interaction or not, provided one increases the strength of the JT interaction to compensate for the lack of a Coulomb term. At the same time, in the bulk SMO, the e_g states are empty and the crystal-field splitting between t_{2g} and e_g produces the gap there. In the interface region, there are extra electrons occupying the Mn e_g states, which can charge order, if the Coulomb interaction, especially the nearest-neighbor U, is large. In our calculations, we found no significant charge order, which is impeded by the fact that the electrons can spread into several layers around the interface region, resulting in a low-filling factor of the interface bands.

III. RESULTS AND DISCUSSIONS

We examined the computed total energy for different configurations of the core Mn spins and found that the minimum-energy structure is one where away from the interface, the G- and the A-type antiferromagnetism of the bulks are recovered, while the interface region becomes ferromagnetic. The magnetic configurations at the interface are characterized by magnetic ordering within each plane, indicated by unbracketed symbols in Table I, and between the adjacent planes, which are indicated by bracketed symbols. Deeper in



FIG. 3. (Color online) Minimum-energy magnetic configuration at the LMO/SMO interface for typical parameters and unstrained condition as obtained from both the density-functional and model calculations. The first MnO_2 layer on the SMO side can be tuned FM or AFM by changing the strain condition as discussed in the text.

the bulks, both LMO and SMO are AFM-type A and G, respectively. The computed energies for different magnetic configurations are listed in Table I and the configuration with the lowest energy is illustrated in Fig. 3. The results presented in the following sections correspond to the lowest-energy configuration, unless otherwise stated, and we note that quantities such as charge reconstruction and Madelung potentials are rather insensitive to the magnetic configuration.

A. Polar catastrophe and interfacial charge reconstruction

As widely discussed in the context of the LAO/STO interface, alternately stacked positive and negative layers—in the present case LaO and MnO₂ layers respectively—lead to a divergent Coulomb potential, the so-called polar catastrophe. In Fig. 4, we have plotted the initial Madelung potential of the charged layers (taking the nominal charged states for all atoms) and the final potential after charge reconstruction has occurred and self-consistency has been achieved.

Charge reconstruction at the interface occurs in two ways as may be seen from Fig. 5. First, a monopole charge, half electron per cell, or $3.4 \times 10^{14} e/cm^2$ accumulates at the interface region to cancel the original electric field discontinuity at the interface. A significant portion of these electrons resides on the interfacial MnO₂ layer as seen from the figure. The interface region demands this monopole charge in order to quench the polar catastrophe. In our supercell geometry, which has two identical interfaces per supercell and also an extra electron per cell after satisfying the nominal ionic charges of all atoms, this electron was quite conveniently shared between the two interfaces. Thus we have half an electron per cell available at each interface, exactly the amount needed to quench the polar catastrophe. In the experimental situation, this monopole charge must come from the surfaces and/or bulk defect states as necessary, so that the demand for the monopole charge at the interface can be met. A second aspect of the charge reconstruction is that the $Mn(e_{o})$ electrons leak from the LMO side into the SMO side, creating a dipole moment at the interface, which results in a potential discontinuity of about 2 eV as seen from the bottom



FIG. 4. Madelung potential seen by the Mn ions in various layers without and with the charge reconstruction as obtained from the self-consistent calculation using the model Hamiltonian [Eq. (1)]. Without the charge reconstruction, the potential grows unrestricted away from the interface (polar catastrophe), which is healed by accumulation of half an electron per cell at the interface. The reconstructed charge at the interface has a dipole moment that leads to a potential step (bottom figure).

part of Fig. 4. The magnitude of this surface dipole-moment density is estimated to be $p \approx 0.11 e/\text{\AA}$.

The interfacial electronic reconstruction is consistent with the layer-projected densities of states (DOSs) shown in Fig. 6. Here we see that at the interfacial MnO₂ layer, approximately one fourth of the e_g states are occupied indicating a net occupancy of about half an electron per Mn atom. The DOS for the layers away from the interface resemble the bulk electronic configuration of the respective materials. Layers close to the interface have either a small number of electrons in the e_g bands (SMO side) or a small number of electrons missing (LMO side), consistent with the electron distribution of Fig. 5.



FIG. 5. (Color online) Mn e_g occupancy across the LMO/SMO interface for different values of the dielectric constant ϵ (symbols connected by lines) compared with the density-functional results for the (LMO)₆/(SMO)₄ superlattice (filled squares). An increased ϵ results in a diminished Madelung potential and, consequently, electrons leak deeper into the bulk.



FIG. 6. (Color online) Layer-projected Mn e_g densities of states obtained from the model Hamiltonian indicating extra electrons or holes accumulated at the interfacial layers, while away from the interface, the e_g states are either half filled (LMO) or unoccupied (SMO). The electrons are effectively spinless with only the spin state aligned parallel to the Mn core spin at a particular Mn site allowed to be occupied ($J_H = \infty$), so that we have a single spin channel in this figure. Within this single spin e_g bands, the interfacial Mn atoms, on layer #0, are roughly quarter-filled, so that there are approximately $0.5e^-$ per Mn atom.

B. Density-functional results and half-metallic behavior

In this section, we report the results of our densityfunctional-theory (DFT) calculations, which validate the results of our model and also address the issue of half metallicity of the conduction bands at the interface. Half-metallic behavior, where one spin band is metallic, while the other is insulating, was already predicted for the delta-doped LMO/ SMO structure, where a single LMO layer is doped in a matrix of SMO.⁷ There, the extra electrons coming from the LMO layer became confined in the electrostatic potential well of the LMO layer producing a ferromagnetic alignment of the core Mn spins at the interface and, in turn, became spin polarized owing to the Zeeman field of the Mn moments. Our DFT studies show that we have a similar situa-



FIG. 7. Variation in the energy of the lowest Mn e_g state of each MnO₂ layer, obtained using DFT-LMTO from the layer-projected wave-function characters for the (LMO)₆/(SMO)₄ superlattice. This variation in energy is indicative of the potential experienced by the Mn e_g electrons across the interface.

tion for the LMO/SMO interface with the difference that now the interfacial electrons originate from the polar catastrophe rather than from the La dopants in the delta-doped structure.

The DFT calculations were performed for the $(LMO)_6/(SMO)_4$ superlattice using the LMTO method with the gradient approximation³⁷ for the exchange correlation functional and including the on-site Coulomb term (GGA + *U*) with *U*=3 eV. We used the rotationally invariant formulation of the GGA+*U* method and used the "around-mean-field" correction to the double counting of the Coulomb energy included in the density-functional theory.^{38,39}

Both the in-plane and the out-of-plane lattice parameters were taken to be the average lattice parameters of LMO and SMO. The experimentally observed basal-plane Jahn-Teller distortions were included in the LMO part of the structure, while for the interface MnO₂ layer, the distortions were taken as half of the bulk value, in view of the fact that the e_{a} electron occupancy is about half for this layer and following our earlier argument that the magnitude of the Jahn-Teller distortion is proportional to the local e_g electron occupancy, as was argued from Eq. (3). Beyond this, other lattice relaxation effects such as the screening of the interface electrons due to lattice polarization were not included. This relaxation is expected to cause the interface electrons to spread somewhat further into the bulk away from the interface but to otherwise not change the essential physics of the problem. Effect of lattice relaxation for a similar system, viz., deltadoped SrTiO₃/(LaTiO₃)₁/SrTiO₃ was discussed in our earlier work using detailed density-functional calculations.⁴⁰ We did not find any significant charge ordering on the interfacial MnO₂ layer, which has approximately 0.5 electrons per Mn atom in the e_{a} bands, because neither the intersite Coulomb interactions nor the Jahn-Teller coupling is strong enough to produce the charge ordering.

In Fig. 7, we have shown the relative potential seen by the Mn e_g electrons at each MnO₂ layer as obtained from the DFT calculations. The variation in the potential across the interface is obtained by calculating the energy of the lowest Mn e_g band state in each MnO₂ layer, which can be obtained from the layer-projected wave-function characters. From the figure, we see that the magnitude of the potential discontinu-



FIG. 8. Density-functional results for majority and minority spin Mn *d* densities of states for SMO and LMO layers away from the interface indicating the bulklike insulating behavior. Results are for the innermost MnO_2 layers in the (LMO)₆/(SMO)₄ superlattice.

ity at the interface (about 2 eV) is similar to the one obtained from the model calculation (Fig. 4).

The layer-projected densities of states for the $(LMO)_6/(SMO)_4$ superlattice, as obtained from the DFT calculations, are shown in Figs. 8 and 9. From the figures, we see that the DOS for the innermost MnO₂ layers shows bulk-like behavior, while the occupation of the Mn e_g states for



FIG. 9. Same as Fig. 8 for interfacial layers, indicating the presence of carriers at the interface, which are also spin polarized. Spinminority states are unoccupied indicating half metallicity.



FIG. 10. Energy splitting of the Mn e_g orbitals due to in-plane compressive and tensile strain conditions used in our model Hamiltonian.

the interfacial layers are very similar to the results obtained from our model calculation (Fig. 6).

A notable feature of the density-functional results is that, for each layer the minority-spin states are completely unoccupied at the Fermi level, leading to the half-metallic behavior. In other words the two-dimensional electron gas formed at the interface is completely spin polarized. We note that this behavior is obviously absent in the widely studied LAO/ STO interface, which lacks any magnetic atoms.

C. Effect of strain on electron leakage and magnetic ordering

In this section, we study the effect of strain on the electron leakage across the interface, which, in turn, affects the magnetism. Density-functional calculations have shown that strain alters the relative energy between the two e_g orbitals, causing a change in the orbital ordering.¹⁴ A change in the symmetry of the occupied state from x^2-y^2 to z^2-1 would increase electron hopping across the interface leading to an increase in electron leakage. Strain is taken into account in our model Hamiltonian (1) via the on-site energy

$$\varepsilon_{i\alpha} = \begin{cases} 0 & (\alpha = x^2 - y^2) \\ \Delta & (\alpha = z^2 - 1), \end{cases}$$
(4)

where a positive Δ corresponds to an in-plane tensile strain (see Fig. 10).

The computed layer occupancy of the electrons is plotted in Fig. 11, where we have shown the electron leakage to various Mn layers in the SMO side. As expected, the layer



FIG. 11. Electron leakage to the individual MnO_2 layers on the SMO side as a function of strain.



FIG. 12. The total energy as a function of the canting angle θ and strain Δ . The parameter θ is the angle between the neighboring Mn core spins in the first MnO₂ layer on the SMO side. The figure shows that the considered MnO₂ plane either stabilizes with FM order or AFM order depending on the strain condition. No canted magnetism is found.

occupancy diminishes with increasing Δ , a result of the lower on-site energy for the x^2-y^2 orbital, which leads to a larger x^2-y^2 character of the occupied e_g electrons and consequently to diminished electronic hopping across the interface. The layer occupancy of the interface layer #0 remains close to $0.5e^-$, the density needed to quench the polar catastrophe.

The magnetism in the manganites is determined by a competition between the superexchange between the core t_{2g} spins and the double exchange between the core spins and the itinerant e_g carriers. The strength of the latter clearly depends on the concentration of the itinerant carriers. In SMO bulk, the AFM superexchange is the only term, since there are no e_g electrons, which leads to a Néel-type G order. As the concentration of the superexchange and the double exchange could lead to a canted magnetic state, eventually resulting in a ferromagnetic state if the double exchange dominates.²⁵

To study if strain can affect the magnetic behavior by modifying the electron leakage, we have solved the Hamiltonian with different orientation of the Mn core spins in order to obtain the ground-state magnetic configuration. Canted states were also considered in addition to FM and AFM states. Within the range of strain studied, the strain being parametrized by the energy-splitting parameter Δ , we find that the magnetic ground state does not change from the one shown in Fig. 3, except for the magnetic configuration of the layer #1, which can be altered between FM and AFM depending on the strain condition. In particular, the electron leakage to this layer can be large enough to produce a net ferromagnetic interaction.



FIG. 13. Magnetic phase diagram for the first MnO_2 layer on the SMO side as a function of the dielectric constant ϵ and strain Δ . Rest of the layers maintain the magnetic behavior of the corresponding bulk materials, either AFM or FM within each layer, throughout the range of parameters considered.

Figure 12 shows the total energy as a function of the canting angle θ between neighboring core spins in the MnO₂ layer #1. There is a transition between FM and AFM states, but we do not find the occurrence of a canted state within our model. Since the electron leakage beyond this layer is small, we see the bulk magnetic ordering beyond the first layer. Figure 13 shows the magnetic phase diagram for the same MnO₂ layer as a function of strain and the dielectric constant.

IV. SUMMARY

In summary, by solving a model Hamiltonian in the meanfield theory, we studied the charge reconstruction at the polar interface of LMO/SMO. The results were complemented by ab initio density-functional calculations of the $(LMO)_6/(SMO)_4$ superlattice. Two types of electronic reconstructions were found at the interface. First, there is an accumulation of an extra half electron per cell in the interface region as in the case of the LAO/STO interface in order to quench the polar catastrophe. Second, the Mn e_g electrons leak out from the LMO side to the SMO side and alter the magnetism at the interface, while away from the interface, the magnetism of the respective bulk materials is preserved. Our calculations suggest the presence of a half-metallic twodimensional electron gas in the interfacial region under certain strain conditions. Indeed, experimental evidence for half metallicity for this interface was recently obtained from magneto-optical Kerr effect.⁴¹ We note that the LMO/SMO interface is a magnetic counterpart of the much studied polar interface between LAO and STO and as such presents an extra degree of freedom for the study of the two-dimensional electron physics.

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