Dominance of magnetoelastic coupling in multiferroic hexagonal YMnO₃

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Hexagonal YMnO₃ with space group $P6_3cm$ is one of the rare examples of multiferroic materials that exhibit codependence of a robust ferroelectric phase along with antiferromagnetic ordering. This is primarily ascribed to tilting of the MnO₅ polyhedra driven by magnetoelectric coupling. We report on the effect of magnetic field at the atomic level in YMnO₃ by utilizing magnetic field and temperature-dependent neutron-diffraction measurements. We show that near the Néel temperature the lattice parameters, effective magnetic moment per site, Mn-O bond lengths, and O-Mn-O bond angles show large variations and these are further modified in the presence of magnetic field. We observe distinct changes with the application of magnetic field in the paramagnetic state both in atomic positions and in the bulk dielectric constant. Our results provide unambiguous confirmation of the role played by exchange striction over and above the much studied magnetoelectric coupling in this frustrated antiferromagnet.

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I. INTRODUCTION

Several recent discoveries involving magnetism driven ferroelectricity and new insight into the intertwined states of electric, magnetic, and elastic order parameters have redefined the broad scope of research in multiferroic materials. 1-7 Such multifunctional materials are of great technological significance; potentially it could lead to eight-state memory devices, gate ferroelectrics based field-effect transistors, and electric field controlled magnetic resonance devices. 10-14 Furthermore, because of the associated rich magneticelectric-elastic phase diagram, new functionalities and their theoretical foundation are under intense investigation.^{4,15,16} In this context, the rare-earth manganites (RMnO₃) have attracted considerable attention. Both orthorhombic (for large ionic radius R=La, Pr, Nd, Sm, Eu, Gd, Dy, and Tb; space group *Pbnm*), ^{17,18} as well as hexagonal (for smaller ionic radius R=Ho, Er, Tm, Yb, Lu, Sc, and Y; space group P63cm) (Ref. 19) phases of RMnO3 exhibit multiferrocity but the microscopic origins are different. In orthorhombic case, the magnetic frustration leads to spin-lattice coupling which is induced by inverse Dzyaloshinski-Moriya interaction,⁵ whereas in the hexagonal case, tilting of MnO₅ bipyramids and buckling of rare-earth layers are responsible for multiferroicity.²⁰ In particular, the hexagonal phase of YMnO₃ has been treated as the prototype for a microscopic understanding of the magnetoelectric effect. ^{21–25} It shows antiferromagnetic (AF) ordering below $T_N \sim 65$ K with moments aligned in the ab plane and a ferroelectric transition at $T_{\rm C} \sim 900$ K.^{26,27} Detailed zero-field neutron scattering suggests that all structural parameters change at $T_{\rm N}$ implying strong spin-lattice coupling and consequent magnetoelectric coupling. 21,25 It was shown that electric polarization across the antiferromagnetic transition showed the same temperature dependence as the effective ordered moment μ assigned to Mn³⁺ state. But very recent studies have indicated giant magnetoelastic coupling in YMnO3, almost two orders of magnitude larger than any other magnetic material and thus leading to large scale displacement of all the atoms in the unit cell.²⁵ This sets a question as to whether the magnetic field dependence of dielectric constant in YMnO₃ is caused by magnetoelectric coupling, that necessarily requires an ordered magnetic state, or due to exchange-striction driven magnetoelastic coupling. Using magnetic field dependent neutron scattering we show that it is magnetoelasticity that dominates over very weak magnetoelectric coupling in hexagonal YMnO₃.

The structure of hexagonal YMnO₃, as depicted in Fig. 1, consists of close-packed layers of bipyramidal MnO₅ where each Mn ion is surrounded by three equatorial (in plane) and two apical ${\rm O^{2-}}$ ions. Since ${\rm Y^{3+}}$ ($4p^6$) is nonmagnetic, the magnetic property in YMnO₃ is controlled by the Mn³⁺ ($3d^4$) with spin S=2. The MnO₅ bipyramids are corner linked to form a triangular lattice in the ab plane and are separated

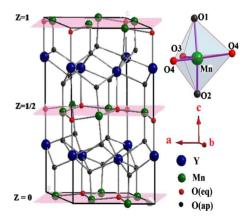


FIG. 1. (Color online) (a) Schematic representation of the crystal structure of hexagonal YMnO $_3$. Here apical oxygen (O_{ap}) and equatorial oxygen (O_{eq}) atoms are represented with different symbols. Mn atoms are situated at z=0, z=1/2, and z=1 plane and each Mn is surrounded by five oxygen atoms forming MnO $_5$ trigonal bipyramidal structure. O1, O2 represent apical oxygen (O_{ap}) atoms and O3, O4 represent equatorial oxygen (O_{eq}) atoms.

from one another along c axis by rare-earth layers and hence theories relating to two-dimensional (2D) magnetism have been invoked. ^{28,29} Due to antiferromagnetic interaction between the spins of the close-packed Mn³⁺ ions, located in the z=0 and z=1/2 planes, the moments get aligned into a 120° structure in the ab plane. ^{24,30} Consequent upon the 2D magnetism and triangular lattice, the magnetic structure in YMnO₃ is frustrated. The ferroelectric polarization on the other hand appears along the c axis perpendicular to the Mn-O plane ³¹ and it is understood that tilting of MnO₅ trigonal bipyramids and buckling of Y layers are the source of spontaneous electric polarization in the absence of external electric field. ^{20–26}

II. EXPERIMENTS

The polycrystalline samples investigated were prepared by conventional solid-state sintering process at ambient pressure. High purity powders of cation oxides Y₂O₃ (99.99%) and MnO₂ (99.99%) were thoroughly mixed in a ratio of 1:2 to achieve the stoichiometry of YMnO₃. Then it was compacted and calcinated at 1100 °C for 13 h. To ensure homogeneity and density of pellets, the sintered pellets were ground, compacted, and reheated twice at 1300 °C for 12 h. Room-temperature powder x-ray diffraction (XRD) studies of the samples were performed using a Bruker D8 x-ray diffractometer with Cu $K\alpha$ radiation ($\lambda = 1.5406$ Å). The neutron-diffraction (ND) measurements were carried out on powder samples using the multi-position sensitive detector based focusing crystal diffractometer set up by UGC-DAE Consortium for Scientific Research Mumbai Centre at the National Facility for Neutron Beam Research (NFNBR), Dhruva reactor, Mumbai (India) at a wavelength of 1.48 Å. ND patterns were recorded at 10, 30, 60, 100, and 300 K. ND patterns were also recorded at 30, 60, and 100 K in an external magnetic field of 5 T. The samples were placed in vanadium cans that were directly exposed to neutron beam for 300 K data. For low temperature and in-field neutron data, vanadium cans filled with the powder samples were loaded in a cryogen-free magnet system. The data were analyzed using Rietveld method and the refinement of both crystal and magnetic structures was carried out using the FULL-PROF program.³² Temperature- and frequency-dependent dielectric measurements on the pellets were performed using a QUADTECH 1920 precision LCR meter.³³ Resistivity of the insulating samples was measured using a constant voltage source in a two-probe configuration. Magnetization and specific heat data were recorded in Quantum Design MPMS, superconducting quantum interference device (SQUID), and PPMS, respectively.

III. RESULTS AND DISCUSSION

All the peaks in room-temperature XRD pattern for YMnO₃ were satisfactorily indexed in hexagonal crystal structure with space group $P6_3cm$. Energy-dispersive x-ray spectroscopy measurement confirmed the stoichiometry and within the experimental error, the molar ratio of Y:Mn:O was found to be 1:1:3. Figure 2 shows the reciprocal magnetic

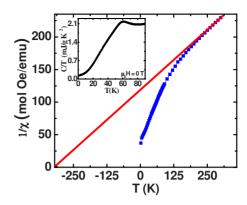


FIG. 2. (Color online) Temperature variation in the inverse magnetic susceptibility measured in zero-field-cooled conditions under $\mu_0 H$ =0.5 T. Inset shows the zero-field specific heat. Anomaly in both χ vs T as well as specific heat at \sim 62 K is a signature of antiferromagnetic ordering.

susceptibility $(1/\chi)$ as a function of temperature for YMnO₃ which indicates $T_{\rm N} \sim 62$ K. The extrapolated Curie-Weiss temperature $(\Theta_{\rm CW})$ is found to be \sim -330 K and the ratio of $\Theta_{\rm CW}$ and $T_{\rm N}$, that relates to the degree of frustration, is estimated \sim 5.3. The zero-field specific-heat data plotted in the inset of Fig. 2, shows sharp deviation at $T_{\rm N}$. After subtracting the phonon contribution, the zero-field magnetic entropy is estimated to be \sim 11.45 J/mol K up to 90 K.²⁹

Figure 3(a) shows Rietveld refinement of roomtemperature ND data that confirm the hexagonal structure of YMnO₃ in space group $P6_3cm$. Lattice parameters a=6.149 Å and c = 11.363 Å are in excellent agreement with published data.^{24–26} ND pattern does not show the presence of any secondary phase thus confirming the phase purity. Structural parameters after the Rietveld refinement of neutron-diffraction data for YMnO3 at room temperature are shown in the Table I. In the table, Biso is the isotropic Debye-Waller factor (one of the refinement parameters). Zero-field ND data were taken at 10, 30, 60, 100, and 300 K and there is no evidence of structural change from hexagonal structure. We observe that both the lattice constants a and cshow significant changes near Néel temperature. Lattice constant a and the unit-cell volume show positive thermal expansion whereas lattice constant c shows negative thermal expansion. Previous studies have reported this anomalous behavior of negative thermal expansion of c axis to persist above the ferroelectric transition.²⁶

Magnetic field dependent ND has been carried out at 30 K corresponding to a bulk antiferromagnetic state, at 60 K to a crossover state, and at 100 K to a paramagnetic state. In Fig. 3(b) we show the refined ND pattern at 60 K for at 0 and 5 T magnetic field. ND data were taken in the warming cycle. After collecting the data at the particular temperature, field was reduced to zero and sample temperature was raised well beyond the Néel temperature to erase the possibility of field-induced spin arrest. We observe a clear signature of enhancement in (002) Bragg peak in ND data at 60 K (not observed at lower temperatures) in the presence of 5 T magnetic field. The (002) peak is nuclear in nature and does not carry any magnetic contribution in the AF-ordered structure of YMnO₃. Hence, the origin of this enhancement is attributed

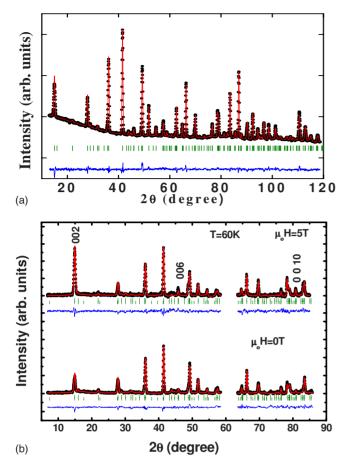


FIG. 3. (Color online) (a) Neutron-diffraction data (symbols) taken at 300 K for YMnO₃. The solid line represents the calculated pattern with hexagonal ($P6_3cm$) symmetry. (b) Neutron powder-diffraction patterns of YMnO₃ at 60 K (near $T_{\rm N}$) recorded at μ_0H =0 and 5 T. The lines below the bars in the figure indicate the difference between the observed and calculated diffraction patterns. The bars indicate the positions of the nuclear Bragg peaks in (a), and at 60 K (b), the upper and lower sets of bars correspond to nuclear and magnetic phases, respectively. R factors for fitting at 60 K are $\chi^2(0 \text{ T})=2.23$, $R_{\rm p}(0 \text{ T})=2.3\%$, $R_{\rm wp}(0 \text{ T})=3.12\%$, and $R_{\rm exp}=2.09\%$ and $\chi^2(5 \text{ T})=4.25$, $R_{\rm p}(5 \text{ T})=3.32\%$, $R_{\rm wp}(5 \text{ T})=4.29\%$, and $R_{\rm exp}=2.08\%$.

to preferred orientation of grains possibly brought about by the presence of weak field-induced ferromagnetic correlations. Peaks like (006) and (00 10) also show increase in intensity. We invoked the preferred orientation parameter in the Reitveld refinement, which resulted in an excellent fit to the data [Fig. 3(b)]. The gap at around 60° is due to interference peaks from the magnet shroud.

The temperature and field variation in all the parameters studied are summarized in Fig. 4. It is known that the refinement of magnetic structures in powder samples is quite complicated in the ordered state owing to the fact that the magnetic grains may have different magnetic structures depending on the field orientation with respect to the grains. Hence, in the absence of any previous data in presence of external magnetic field either in powder or single crystal, the present results on polycrystalline samples in the ordered state (<60 K) represent an average picture of the spin structure.

TABLE I. Structural parameters after the Rietveld refinement of neutron-diffraction pattern of YMnO₃ at room temperature. Atomic positions of Y1 and O3 at 2a (0,0,z); Y2 and O4 at 4b (1/3,2/3,z); and Mn, O1, and O2 at 6c (x,0,z) (for Mn, z=0).

Parameters		
a (Å)		6.1490
c (Å)		11.3627
V (Å ³)		372.073
Y1	Z	0.27206
	Biso	0.422
Y2	Z	0.22900
	Biso	0.422
Mn	X	0.32472
	Biso	0.498
O1	x	0.30952
	Biso	0.450
	Z	0.15127
	Biso	0.450
O2	X	0.64491
	Biso	0.445
	Z	0.32599
	Biso	0.445
O3	Z	0.47814
	Biso	0.795
O4	Z	0.01227
	Biso	0.795
	Discrepancy factors	
χ^2		3.93
$R_{\rm p} \ (\%)$		2.17
R _{wp} (%)		2.89
$R_{\rm exp}$ (%)		1.23

ND patterns taken at 10 and 30 K show the expected magnetic intensities, in particular, the peak (101) which is forbidden by the space group $P6_3cm$. Appearance of this peak is a signature of the antiferromagnetic ordering below $T_{\rm N}$ characterized by the propagation vector k=0. For the magnetic refinement of the ND data, the structure described by the basis vectors of the irreducible representation Γ_1 was used. Since no new peaks were observed in the presence of external magnetic field, it is deduced that the basic magnetic structure is not changed and hence, the same irreducible representation was used to fit the in-field ND data.

We observe that at 30 K, for 5 T magnetic field, lattice constant c decreases compared to zero-field value. This value suppression becomes larger at 100 K [Fig. 4(b)]. On the other hand, the lattice parameter a decreases with respect to zero-field value at 30 K but near $T_{\rm N}$ the value increases significantly [Fig. 4(a)]. Thus in the presence of magnetic field at temperature above and below $T_{\rm N}$, both the lattice parameters get altered as compared to zero-field value. We note that there is no orbital degree of freedom as the 4d electrons of Mn³⁺ occupy the low-energy doublets (xz, yz and xy, x^2

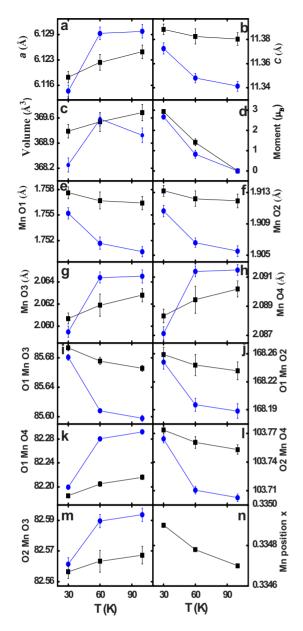


FIG. 4. (Color online) Temperature and field dependence of (a) lattice constant a, (b) lattice constant c, (c) unit-cell volume, (d) ordered magnetic moment per Mn atom, [(e)-(h)] Mn-O bond lengths, and [(i)-(m)] O-Mn-O bond angles. The O-Mn-O bond angles are measured in degrees. (n) x position of Mn atom as a function of temperature. Values are obtained from refinement of neutron powder-diffraction data at 30, 60, and 100 K in zero field (\blacksquare) and 5 T (\blacksquare) magnetic field. O1, O2 represent apical oxygen atoms and O3, O4 represent equatorial oxygen atoms.

 $-y^2$) and hence the changes in lattice parameters are not due to Jahn-Teller distortion.³⁴ These large changes in the paramagnetic state with the application of field that can only be attributed to strong magnetoelastic coupling. We also note that the zero-field effective moment obtained from ND data at 30 K is estimated to be $2.9\mu_{\rm B}$, much smaller than ionic value of $4\mu_{\rm B}$. This reduction in Mn magnetic moment is because of 2D geometrical frustration in the Mn lattice. The Mn magnetic moment reduces as temperature is raised from 10 to 60 K and as shown in Fig. 4(d), in the presence of 5 T

magnetic field, effective Mn moment decreases further. The ordered Mn moment decreases by $\sim\!40\%$ near Néel temperature as compared to zero-field value. This indicates increased frustration among Mn spins with the application of magnetic field.

The field-dependent variation in lattice parameters as a function of temperature gives indication that the tilting of MnO_5 polyhedra can be tuned by a relatively small field of 5 T. To investigate this possibility, we discuss next how the magnetic field affects the Mn-O bond distances and O-Mn-O bond angles both in the antiferromagnetic and paramagnetic states and correlate this to the magnetic field dependent dielectric constant.

In the paramagnetic state, the Mn atom is located at x $\approx 1/3$ in the geometry of a two-dimensional triangular lattice. With the onset of ordering at T_N , it is reported that the position of Mn atom shifts by 3.3% from $x \approx 1/3$ value.^{21–23} Similar trend is observed in our analysis on ND data in absence of magnetic field. The variation in the Mn atomic position is \sim 3% from 300 to 10 K. We further observe that in zero field, all Mn-O bond distances show significant variation at T_N . As the temperature decreases below Néel temperature, the Mn and apical oxygen (Oap) bond lengths increase whereas Mn and equatorial oxygen (O_{eq}) bond lengths decrease.^{25,27} With the application of 5 T magnetic field, all the Mn-O bond lengths get further modified. The magnetic field affects all the Mn-O bonds whether it is $O_{eq}\left[O(3)\right.$ and O(4)] or $O_{ap}[O(1)]$ and O(2)]. These changes seen in all four Mn-O bond distances as a function of temperature and magnetic field are shown in Figs. 4(e)-4(h). Clearly at 30 K, magnetic field decreases the Mn- O_{ap} bond length and this change is more pronounced above $T_{\rm N}$. On the other hand, at 30 K, the magnetic field decreases the Mn-O_{eq} bond length but near T_N , it increases considerably as compared to zerofield value. These variations are also seen when O-Mn-O bond angles are calculated from Rietveld refinement of powder ND data [shown in Figs. 4(i)-4(m)]. We conclude that application of magnetic field both in the paramagnetic and antiferromagnetic states lead to decrease in distance between Mn and $O_{ap}[O(1)]$ and O(2) whereas $O_{eq}[O(3)]$ and O(4) go farther from Mn. This leads to reduction in the tilting of MnO₅ polyhedra. Consequently, it is expected that polarization in presence of magnetic field will decrease as compared to zero-field value both below and above T_N . Refined x positions of Mn atom as a function of temperature in zero magnetic field is shown in Fig. 4(n). The position of Mn does not vary significantly in the neutron data recorded in the presence of magnetic field.

Figure 5 shows the temperature-dependent dielectric constant (ϵ) of a sintered pellet of YMnO₃ across the antiferromagnetic transition at a frequency of 1 kHz and at μ_0H =0, 3, and 5 T. To rule out the possibility of leakage current dominating the measurement, in the top inset we show the resistivity as a function of temperature both at zero field and at μ_0H =4 T. There is no trace of magnetoresistance, so one can safely assign the changes in the dielectric constant with the magnetic field to be of capacitive origin. With zero external field, a broad shoulder appears in the vicinity of \sim 62 K which is a signature of a weak first-order phase transition (antiferromagnetic ordering). With the application

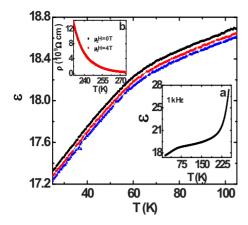


FIG. 5. (Color online) Temperature dependence of dielectric constant measured at different magnetic field $\mu_0H=0$ T (\blacksquare), 3 T (*), and 5 T (\blacktriangle) taken at 1 kHz frequency in the temperature range 25–105 K. Inset (a) shows temperature-dependent dielectric constant in the temperature range 10–265 K. Change in slope at $T\sim$ 62 K reflects the antiferromagnetic ordering. Inset (b) shows temperature dependence of resistivity (ρ) at $\mu_0H=0$ T (\blacksquare) and 4 T (\blacksquare).

of 3 T magnetic field, the dielectric constant decreases and this is more when 5 T magnetic field is applied. The estimated magnetocapacitance $\left[\varepsilon(T,H) - \varepsilon(T,0)/\varepsilon(T,0) \times 100\right]$ at T=65 K are 0.33 and 0.5 for magnetic fields of 3 T and 5 T, respectively. Clearly, the magnetic field suppresses the tilting of MnO₅ polyhedra in the antiferromagnetic state as indicated in our field-dependent neutron-scattering data. Further, the observed magnetocapacitance for 5 T magnetic field at 30, 60, and 90 K are of comparable magnitude, 0.552, 0.528, and 0.424, respectively. For pure magnetoelectric coupling (change in polarization due to change in magnetic state of Mn³⁺), induced polarization P goes as $\sim \mu_{\rm eff}^2$, where $\mu_{\rm eff}$ is the magnetic moment.^{21,25} Since effective moment decreased by 40% at 5 T near T_N , the corresponding extrapolated ΔP would be substantially larger than what is observed experimentally near T_N . Most importantly, we observe that the magnitude of dielectric constant decreases in the paramagnetic state where there is no ordered magnetic state and the magnetocapacitance values are similar both below and above $T_{\rm N}$. It again reinforces the interpretation that dominant changes in the presence of magnetic field, both in the antiferromagnetic and in the paramagnetic states, have the origin in magnetoelasticity. In essence, the spin exchange interactions in YMnO₃ are frustrated and the spins in the system can undergo a transition into an ordered AF state by releasing frustration through the lattice displacements. This provides a suitable mechanism for the magnetodielectric effect in a frustrated spin system. We note that the multiferrocity reported in the incommensurate spin frustrated system such as orthorhombic TbMnO₃ and YMnO₃ are in conformity with this picture.

IV. CONCLUSIONS

In conclusion, high-quality polycrystalline samples of hexagonal YMnO₃ have been extensively characterized using magnetization, specific heat, dielectric constant, and magnetic field dependent neutron diffraction. At the microscopic level, the changes in lattice constant, Mn moment, Mn-O bond length, and O-Mn-O bond angle are quantitatively estimated both above and below the Néel temperature. A relatively small field of 5 T is found sufficient to usher in significant changes in atomic positions and in dielectric constant both in the antiferromagnetic as well as the paramagnetic state. This is reflective of the dominant role played by magnetoelastic coupling vis á vis weak magnetoelectric coupling in this extensively studied multiferroic compound.

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