# Magnetic and dielectric properties in the langasite-type compounds: $A_3BFe_3D_2O_{14}$ (A=Ba, Sr, Ca; B=Ta, Nb, Sb; D=Ge, Si)

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The Fe-based langasites are the only reported compounds presenting a magnetic ordering in this rich family, besides being well known for piezoelectric properties and optical activity. The structural, magnetic, and dielectric properties of the Fe-langasite compounds, with various substitution of nonmagnetic cations, have been studied with x-ray and neutron-diffraction, magnetostatic measurements, Mössbauer spectroscopy, and dielectric measurements. The title compounds (trigonal space group P321) display a helical magnetic order with signatures of frustration below  $T_N \approx 24-35$  K, where an anomaly of the dielectric permittivity is observed. The influence of the cationic substitutions and the nature of the magnetoelectric coupling are hereafter addressed.

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#### I. INTRODUCTION

Multifunctional materials, in which coexist different physical properties (optical activity, laser properties, piezoelectricity, and/or ferroelectricity, ferroelasticity, magnetic ordering, etc.), are the subject of an intense research effort owing to their strong potential for various industrial applications. To date, the basic mechanisms at the origin of the coupling between these properties inside a single compound are still poorly understood. Experimental realizations of such materials are rare, and this is particularly the case in the field of multiferroics, i.e., compounds, which display both ferroelectric and magnetic ordering.<sup>1</sup> Proper multiferroics are defined as ferroelectric compounds, which undergo a magnetic ordering at lower temperature, as, for example, BiFeO<sub>3</sub>.<sup>2</sup> In these compounds, there is a large temperature gap between the ferroelectric and magnetic transition, and the coupling between the two properties is generally weak. For improper multiferroics [for example,  $TbMn_2O_5$ ,<sup>3</sup> the electric polarization is induced by the onset of a complex magnetic order within a paraelectric and generally centrosymmetric phase. Such materials therefore present a naturally strong coupling between magnetization and electric polarizations, thus, giving the opportunity to study the microscopic mechanisms driving such couplings.

The langasite family, the prototype of which is  $La_3Ga_5SiO_{14}$ , has been widely studied for the striking piezoelectric and nonlinear optical properties of its members,<sup>4–7</sup> related to the noncentrosymmetric nature of its  $Ca_3Ga_2Ge_4O_{14}$  structure type.<sup>8</sup> These compounds have generated a strong interest for applications in bulk acoustic waves and surface acoustic waves devices, as well as in nonlinear optics and electro-optics.<sup>4,9,10</sup>

The langasite structure belongs to the trigonal noncentrosymmetric P321 space group. The general formula is  $A_3BC_3D_2O_{14}$ , thus, containing four different cationic sites. The decahedral A site and the octahedral B site form a layer at z=0, while the two tetrahedral sites C and D are located on the plane z=1/2 (see Fig. 1).<sup>4,11</sup> Due to its atomic arrangement, this structure type is able to accommodate a large number of different cations with various sizes and valences, leading to a wide variety of isostructural compounds.<sup>4,12,13</sup> Among these, some contain magnetic cation sublattices. Therefore, this family might provide interesting examples of coexisting magnetic order and optical or electrical properties. Recently, we have undertaken the general investigation of the magnetic langasites.<sup>14</sup> In this paper, we present the study of the magnetic and dielectric properties of several Fe-containing langasite compounds with for-



FIG. 1. Polyhedral representation of the langasite structure with its four different cation sites on two layers.

TABLE I. Refined structural parameters obtained from x-ray powder diffraction on BNFS with a D8 Brucker diffractometer. a.d.p. is the atomic displacement parameter. The agreement factor of the fit is given by  $R_{\text{Bragg}}$ =3.2,  $R_{\text{wp}}$ =27.0, and  $\chi^2$ =1.5.

Atom	Wyckoff	x	у	z	a.d.p.
Ba	3 <i>e</i>	0.4339(2)	0	0	1.04(1)
Sb	1 <i>a</i>	0	0	0	0.9(1)
Fe	3 <i>f</i>	0.7513(6)	0	1/2	0.9(1)
Si	2d	1/3	2/3	0.459(3)	0.4(3)
01	2d	2/3	1/3	0.774(6)	1.4(3)
02	6 <i>g</i>	0.477(3)	0.300(2)	0.649(3)	1.4(3)
O3	6 <i>g</i>	0.209(2)	0.098(2)	0.236(3)	1.4(3)
	<i>a</i> =8.522 7(2) Å		c=5.235 3(1) Å		

mula  $A_3BFe_3D_2O_{14}$ , with A=Ba, Sr, Ca; B=Ta, Nb, Sb; and D=Ge, Si.

#### **II. EXPERIMENTAL**

## A. Synthesis and structural characterization

Powder samples were synthesized by solid-state reactions. The initial components of the powder mixtures were highpurity oxides or carbonates in stoichiometric quantity. The mixtures were ground, compacted, and heated up to 1150–1250 °C in Al<sub>2</sub>O<sub>3</sub> crucibles in air for 7 h. The pellets were heated at a rate ranging from 200 to 300 °C/h. The samples containing GeO<sub>2</sub> were kept at 1000 °C for 2 h before reaching the final temperature to prevent the loss of the relatively volatile germanium oxide. The synthesis conditions were chosen taking into account some properties of the initial and final compounds, such as the decomposition of the carbonates, the oxidation of Sb<sub>2</sub>O<sub>3</sub>, the fusion temperatures of GeO<sub>2</sub>, SrO, and of the final product. The products were analyzed with x-ray diffraction, using a D8 Brucker diffractometer in transmission geometry with the Cu  $K\alpha$ 1 radiation, to check the presence of possible impurities. As some of the products showed minor impurities (maximum 3%), they were ground, compacted again, and annealed for 10-50 h, up to three times in order to decrease the impurity content.

Rietveld refinements with the program FULLPROF (Ref. 15) were carried out on the final products diffractograms. In all cases, the expected stoichiometry and the full occupation of all sites were found, without any sign of intersite substitution. As an example, the results for  $Ba_3NbFe_3Si_2O_{14}$  (hereafter referred to as BNFS) are reported in Table I. Table II summarizes the principal structural parameters for the investigated samples.

Single crystals of Ba<sub>3</sub>NbFe<sub>3</sub>Si<sub>2</sub>O<sub>14</sub> and Ba<sub>3</sub>TaFe<sub>3</sub>Si<sub>2</sub>O<sub>14</sub> (BTFS) were grown by the floating-zone method in a Cyberstar image furnace, under a 99% Ar+1% O<sub>2</sub> atmosphere, at a growth rate of 10 mm/h.<sup>16</sup> This technique has the advantage of being fast and free of contamination from a crucible. The single crystals were cut out of the grown ingot with a size roughly of 3 mm in diameter and 8 mm in length for the

TABLE II. Structural parameters and agreement factors of Fe langasites as refined from x-ray powder-diffraction data at room temperature with a D8 Brucker diffractometer.

Langasite	a (Å)	с (Å)	R <sub>Bragg</sub>	<i>R</i> <sub>wp</sub>	$\chi^2$
Ba <sub>3</sub> SbFe <sub>3</sub> Ge <sub>2</sub> O <sub>14</sub>	8.6174(1)	5.2708(1)	3.9	22.7	3.2
Ba <sub>3</sub> TaFe <sub>3</sub> Ge <sub>2</sub> O <sub>14</sub>	8.6166(1)	5.2618(1)	6.0	22.5	3.9
Ba <sub>3</sub> NbFe <sub>3</sub> Ge <sub>2</sub> O <sub>14</sub>	8.6073(2)	5.2686(2)	6.1	22.9	2.5
Ba <sub>3</sub> SbFe <sub>3</sub> Si <sub>2</sub> O <sub>14</sub>	8.5085(1)	5.25024(8)	3.1	20.2	2.8
Ba <sub>3</sub> TaFe <sub>3</sub> Si <sub>2</sub> O <sub>14</sub>	8.5231(2)	5.2354(2)	13.5	33.6	2.2
Ba <sub>3</sub> NbFe <sub>3</sub> Si <sub>2</sub> O <sub>14</sub>	8.5227(2)	5.2353(1)	3.2	27.0	1.5
Sr <sub>3</sub> SbFe <sub>3</sub> Si <sub>2</sub> O <sub>14</sub>	8.2888(2)	5.1445(2)	5.8	30.6	2.1
Sr <sub>3</sub> TaFe <sub>3</sub> Si <sub>2</sub> O <sub>14</sub>	8.2777(2)	5.1283(1)	4.3	27.0	2.0
Sr <sub>3</sub> NbFe <sub>3</sub> Si <sub>2</sub> O <sub>14</sub>	8.2563(2)	5.1306(1)	3.2	27.6	1.6
Ca <sub>3</sub> SbFe <sub>3</sub> Si <sub>2</sub> O <sub>14</sub>	8.1118(2)	5.0570(2)	5.7	26.0	2.0

neutron-diffraction measurements. The crystallographic quality was checked by Laue photographs. No impurity phase could be detected by x-ray powder diffraction of crushed crystal pieces. A small crystal piece of each compound was used for single-crystal x-ray diffraction analysis using a Kappa ApexII Bruker diffractometer equipped with graphite monochromatized Ag  $K\alpha$  radiation. This confirmed the crystal quality and the langasite-type structure and allowed to determine the handedness of each of these chiral crystals by the use of anomalous scattering sensitivity.

In all the compounds under study, the magnetic Fe<sup>3+</sup> cations form a peculiar array of triangles on a triangular lattice, in the plane at z=1/2 (Fig. 2). Two consecutive planes are separated from each others by a layer of  $A^{2+}$  and  $B^{5+}$  cations. The  $Fe^{3+}$  triangles are equilateral by symmetry. The distance between the Fe<sup>3+</sup> cations is 3.662(8) Å for BNFS. Two equivalent superexchange interactions J1 between two nearest-neighbor magnetic cations on one triangle are each mediated via an O3 anion. The Fe-O3-Fe angle 100.1(9)° and the Fe-O3 distances are 1.73(2) and 2.93(2) Å for BNFS. One Fe<sup>3+</sup> cation of a triangle interacts with four neighbors in the nearest triangles within the plane by the super-super-exchange paths J2 through two O2 anions, forming an edge of a DO4 tetrahedron (Figs. 1 and 2). The Fe-O2-O2 angles are  $144(1)^{\circ}$  and  $140(1)^{\circ}$ , and the Fe-O2 and O2-O2 distances are, respectively, 1.93(2) Å and 2.59(4) Å



FIG. 2. (Color online) Magnetic network of  $\text{Fe}^{3+}$  cations projected along the *c* axis (left), with the different intraplane (left) or interplane (right) exchange paths (dashed lines).



FIG. 3. (Color online) Magnetization measurements on a  $Ba_3NbFe_3Si_2O_{14}$  single crystal under a magnetic field applied parallel and perpendicular to the *c* axis. Top: magnetic isotherms at 2 and 275 K. Bottom: thermal variation of the *M*/*H* and its inverse under an applied magnetic field of 5 T. The continuous line represents the linear fit of *H*/*M* in a Curie-Weiss model.

in BNFS. The shortest distance between two Fe<sup>3+</sup> cations from neighboring planes is the *c* parameter [5.235 3(1) Å], with also two O2 oxygens in the exchange path forming an edge of the BO<sub>6</sub> octahedron. But one needs to distinguish three different interplane interactions, each one with multiple possible super-super-exchange paths. J4 is the interaction between a Fe<sup>3+</sup> cation and the cation just above or below in the adjacent plane, while J3 and J5 are the diagonal interactions between this Fe<sup>3+</sup> cation and the two other Fe<sup>3+</sup> cations of the neighboring triangle (Fig. 2). It is worth noticing that due to the structural chirality, J3 and J5 are obtained through different exchange paths and expected not to be equal.

# **B.** Magnetization measurements

The magnetostatic properties of BNFS and BTFS single crystals and of all the powder title compounds were investigated under magnetic fields up to 5 T in the temperature range from 2 to 300 K with a commercial Quantum Design MPMS superconducting quantum interference device magnetometer, and up to 10 T from 1.6 to 300 K with a purposebuilt magnetometer using the anti-Helmholtz two-coil axial extraction method. Figure 3 illustrates for BNFS the thermal evolution of the magnetization divided by the magnetic field (i.e., equal to the linear susceptibility  $\chi$  for temperatures greater than  $\approx 26$  K), and of its inverse, measured under a



FIG. 4. Thermal variation of the M/H of a powder sample of Ba<sub>3</sub>SbFe<sub>3</sub>Si<sub>2</sub>O<sub>14</sub> under an applied magnetic field of 0.1 T.

magnetic field of 5 T applied both perpendicular to the c axis and parallel to it. A cusp in the M/H measurements suggested the onset of a magnetic transition at 26 K, further corroborated by a sharp peak in the specific heat.<sup>17</sup> Above this temperature, no significant anisotropy is observed within the accuracy of the measurements, which is expected for Fe<sup>3+</sup> ions without orbital contribution. Below the magnetic transition, whereas M/H is almost constant for H parallel to the c axis, the in-plane susceptibility drops, although not to zero as would be the case for a canonical antiferromagnetic transition. This implies a more complex magnetic arrangement. This is also illustrated on the magnetization curves M(H) shown on Fig. 3. At high temperature (275 K), the magnetization is the same for the two orientations of the applied field. On the contrary, at low temperature (2 K), an anisotropy of the magnetostatic properties comes out: the magnetization measured with an applied field parallel to the c axis is no longer linear and shows a slight curvature at small fields. This curvature would indicate the rise of a small component along the c axis. At high temperatures (150–300 K), a linear fit of the inverse of M/H yields, in a Curie-Weiss model  $\chi = C/(T - \theta)$ , an effective moment  $\mu_{\rm eff} = g\sqrt{S(S+1)} = 5.95 \mu_B$ , compatible with the value of the Fe<sup>3+</sup> free ion (3 $d^5$ , J=5/2,  $\mu_{eff}$ =5.92 $\mu_B$ ,  $M_{sat}$ =5 $\mu_B$ ), and a negative Curie-Weiss temperature of -171 K, characteristic of antiferromagnetic interactions.

The magnetic behavior of a BTFS crystal was found essentially similar to that of BNFS, and this was also the case for all the investigated compounds prepared as powders: all of them undergo an antiferromagnetic ordering transition in the 24–35 K range. As an example, the magnetic susceptibility for the Ba<sub>3</sub>SbFe<sub>3</sub>Si<sub>2</sub>O<sub>14</sub> powder compound is shown in Fig. 4, where the magnetic transition is clearly visible at  $T_N=35$  K. The values of  $T_N$ ,  $\theta$ , and Fe<sup>3+</sup> magnetic effective moments obtained in a Curie-Weiss fit of the inverse magnetic susceptibilities are summarized in Table III. All compounds, whatever the cations on sites A, B, and D, present a Néel temperature around 25 K, except those containing Sb<sup>5+</sup> cations on site B. These latter displays a magnetic transition around 35 K and at the same time a noticeably smaller absolute value of the Curie-Weiss temperature. In order to understand the microscopic origin of this difference, and more generally to further our understanding of the magnetic order

TABLE III. Magnetic parameters obtained from magnetization measurements of Fe langasites: Néel temperatures and Curie-Weiss temperatures.

Langasite	<i>T<sub>N</sub></i> (K)	<i>θ</i> (К)
Ba <sub>3</sub> NbFe <sub>3</sub> Si <sub>2</sub> O <sub>14</sub>	26	-173
Ba <sub>3</sub> NbFe <sub>3</sub> Ge <sub>2</sub> O <sub>14</sub>	24	-177
Ba <sub>3</sub> TaFe <sub>3</sub> Si <sub>2</sub> O <sub>14</sub>	28	-160
Ba <sub>3</sub> TaFe <sub>3</sub> Ge <sub>2</sub> O <sub>14</sub>	24	-165
Ba <sub>3</sub> SbFe <sub>3</sub> Si <sub>2</sub> O <sub>14</sub>	35	-114
Ba <sub>3</sub> SbFe <sub>3</sub> Ge <sub>2</sub> O <sub>14</sub>	34	-111
Sr <sub>3</sub> NbFe <sub>3</sub> Si <sub>2</sub> O <sub>14</sub>	26	-242
Sr <sub>3</sub> SbFe <sub>3</sub> Si <sub>2</sub> O <sub>14</sub>	36	-128

in these compounds, microscopic probes, such as neutronscattering and Mössbauer spectroscopies, were used.

#### C. Neutron-diffraction study

Neutron powder-diffraction (NPD) measurements were performed at the Institut Laüe Langevin on samples of the compounds Ba<sub>3</sub>NbFe<sub>3</sub>Si<sub>2</sub>O<sub>14</sub> (BNFS), Ba<sub>3</sub>SbFe<sub>3</sub>Si<sub>2</sub>O<sub>14</sub> (BSFS), Sr<sub>3</sub>NbFe<sub>3</sub>Si<sub>2</sub>O<sub>14</sub> (SNFS), and Sr<sub>3</sub>SbFe<sub>3</sub>Si<sub>2</sub>O<sub>14</sub> (SSFS) using the D1B instrument ( $\lambda$ =2.52 Å). These four compounds were chosen in order to track, via the structural and magnetic arrangements determination, the influence of large cell parameter variation (Sr versus Ba) and the microscopic origin of the different transition temperatures (Nb versus Sb). A BNFS single crystal was also studied on the D15 diffractometer of the Institut Laüe Langevin ( $\lambda$ =1.1743 Å). The thermal evolution of the diffraction patterns were measured on D1B using an orange cryostat by increasing the temperature at a rate of 0.42 K/min with 75 scans of 10 min each. In order to obtain sufficient statistics at 30 K (above the magnetic transition), 20 K (below the magnetic transition), 1.8 K (for BSFS, SNFS and SSFS), and 1.5 K (the lowest reachable temperature, for BNFS), 6 scans of 20 min were summed at each temperature. The magnetic structure was solved from refinement of the D15 and D1B diffractograms measured on BNFS (Fig. 5).<sup>17,18</sup> The magnetic structures of the three other compounds were refined using the same ordering scheme (see Fig. 6). The magnetic peaks could be indexed using an incommensurate propagation vector  $(0,0,\tau)$ , with  $\tau$  ranging from 0.14 for SNFS to 0.19 for BSFS, and the magnetic structure was found to be a helical spin arrangement propagating along the c axis from equal moments lying in the (a,b) plane at 120° from each other within each triangle (see Fig. 5). This 120° arrangement results from the usual compromise of frustrated Heisenberg spins on a triangle-based lattice. All spins rotate around c by  $\pm 2\pi\tau$  between two consecutive Fe<sup>3+</sup> layers. It is worth noting that a helical magnetic order often results either from the presence of frustration of interactions in the helix direction<sup>19</sup> or from Dzyaloshinskii-Moriya interactions in a ferromagnetic structure.<sup>20</sup> In the present case, it was shown that the helical structure is generated by the twist in the magnetic



FIG. 5. (Color online) Magnetic structure of the Fe langasites: within each triangle of the (a,b) plane, the Fe<sup>3+</sup> magnetic moments are rotated by  $2\pi/3$  from each other. The global phase factor, which cannot be determined by neutron diffraction, was arbitrary chosen equal to zero in this representation (one moment pointing toward the center of the triangles). Along the *c* axis, the helix propagates with a period of  $1/\tau$  in cell unit.

super-super-exchange paths from plane to plane. Furthermore, the in-plane 120° magnetic arrangement and the helical propagation both possess a definite sense of rotation defined as chirality, which is related to the structural chirality. A thorough investigation of this interesting aspect has been previously reported in Ref. 18 and will not be discussed further here.

The main results of the NPD refinements carried out for the four samples at 1.8 K are summarized in Table IV. The magnetic-moment values are close to  $4\mu_B$  and they are smaller for Nb compounds than for Sb ones. This is markedly smaller than the expected value for a saturated  $Fe^{3+}$ magnetic moment  $(5\mu_B)$ . An explanation for this behavior could be the strongly covalent nature of the Fe-O bonds for  $Fe^{3+}$  cations in tetrahedral coordination, which is known<sup>21</sup> to favor spin transfer toward the oxygen orbitals and therefore decrease the apparent magnetic moment on the  $Fe^{3+}$  cations. Indeed, in order to obtain accurate refinements of the NPD data, we had to introduce an ad hoc "magnetic Debye-Waller factor," similar to an overall isotropic atomic displacement term. The refined values of the corresponding  $B_{mag}$  parameters are given in Table IV. The effect of this term can be viewed qualitatively as a modification of the magnetic form factor with increased spin density at larger distances from the center of the electron cloud, as would be expected in the presence of spin transfer to the oxygen orbitals. Another qualitative information is given by the diffractograms measured at temperatures up to 20 K above the magnetic transition, where some diffuse scattering centered on the first nuclear peak is visible. This signal is characteristic of the onset of short-range magnetic correlations in the (a,b)planes. The width of the signal decreases, i.e., the correlation length of this short-range order increases, down to the magnetic transition where it disappears at the expense of the magnetic Bragg peaks characteristic of the three-dimensional long-range order (see Fig. 7).

As seen in Table IV, the  $\tau$  values of the antimony compounds are higher (between 0.177 and 0.196) than those of



FIG. 6. (Color online) Rietveld plot for  $Ba_3NbFe_3Si_2O_{14}$  (top left),  $Ba_3SbFe_3Si_2O_{14}$  (top right),  $Sr_3NbFe_3Si_2O_{14}$  (bottom left), and  $Sr_3SbFe_3Si_2O_{14}$  (bottom right) neutron powder data at 1.8 K (1.5 K for BNFS) from D1B, including nuclear and magnetic phases.

the niobium compounds (around 0.14). The  $\tau$  values appear also slightly larger for the barium compounds than for the strontium ones, especially in the Sb compounds. However, the  $\tau$  values are much less sensitive to the Sr/Ba substitution than to the Sb/Nb one, although the former has a much larger effect on the lattice parameter due to the big difference of

TABLE IV. Refined lattice parameters, magnetic-moment value, overall isotropic atomic displacement parameter, z component of the propagation vector, lengths and angle involved in the main interplane super-super-exchange path, and goodness of the fit parameters obtained from neutron powder-diffraction data of Fe langasites at 1.8 K (1.5 K for BNFS) on D1B.

Langasite	a, c (Å)	$m(\mu_B)\ B_{mag}\  au$	Fe-O3, <i>O3-O3</i> (Å) Fe-O3-O3 (°)	$R_{ m Bragg} \ R_{mag} \ \chi^2$
	8.5026(6)	4.04(5)	1,87(1)	0.7
BNFS	5.2136(7)	3.9(9)	2,69(2)	5.8
		0.1429(2)	168.7(7)	28.0
	8.297(1)	3.87(9)	1.84(8)	0.9
SNFS	5.155(1)	5(2)	2.68(6)	9.2
		0.1398(3)	159(2)	35.5
	8.5048(5)	4.26(3)	1.854(9)	1.2
BSFS	5.2449(4)	2.1(4)	2.77(1)	4.8
		0.1957(1)	166.5(5)	44.3
	8.2896(9)	4.31(5)	1.84(1)	1.8
SSFS	5.140(1)	4.6(7)	2.71(2)	14.2
		0.1769(2)	162.2(8)	20.3

their ionic radius (1.56 Å for Ba versus 1.4 Å for Sr). After examination of the refined structures of the four compounds, and especially focusing on the lengths and bonds angle of the magnetic exchange paths, no systematic trends could be extracted from the data that would explain the peculiarity of the Sb-based compounds magnetic properties on pure structural grounds (see, for example, the lengths and angle involved in the main interplane super-super-exchange path in Table IV). The influence of the Sb cation in the Fe langasites is therefore more probably ascribable to the ion electronic state than to induce structural distortion. We will come back to this aspect in the discussion.



FIG. 7. (Color online) Powder neutron-diffraction patterns of the compound  $Ba_3NbFe_3Si_2O_{14}$ , below the magnetic transition, at 1.5 K, and above the magnetic transition, at 30 K.



FIG. 8. (Color online)  ${}^{57}$ Fe Mössbauer absorption spectra in Ba<sub>3</sub>NbFe<sub>3</sub>Si<sub>2</sub>O<sub>14</sub> at selected temperatures. The spectra at 4.2, 23, and 26 K (circles) are fitted (black lines) to the helical magnetic structure model determined by neutron scattering. At 26 K, a quadrupolar subspectrum contribution (represented in red), overlapping the magnetic signal, suggests that the magnetic transition is first order.

#### D. Mössbauer measurements

Mössbauer absorption spectra on the isotope <sup>57</sup>Fe ( $E_0$ =14.4 keV) were recorded for the BNFS compound at room temperature and in the temperature range 4.2–30 K, in zero external magnetic field (see Fig. 8). At 27 K and above, the spectrum consists of a quadrupolar hyperfine doublet characteristic of the paramagnetic phase. At 27 K, the isomer shift with respect to the  $\alpha$ -Fe reference is  $\delta = 0.35(1)$  mm/s (1 mm/s corresponds to 11 MHz) and the quadrupolar hyperfine splitting is  $\Delta E_{O} = |eQV_{ZZ}|/2$ =1.29(1) mm/s, where Q is the quadrupole moment of the nuclear excited state and  $V_{ZZ}$  is the principal component of the electric field gradient (EFG) tensor at the <sup>57</sup>Fe nucleus site. These values are typical of a Fe<sup>3+</sup> ion, although the  $\Delta E_O$ value is somewhat larger than generally found in ferric insulators, indicating a strongly distorted Fe site, compared to a perfect tetrahedral environment, in agreement with crystal analysis. The point symmetry at the Fe site is low (a twofold axis along the crystal a axis) and, thus, the directions of the EFG tensor axes cannot be determined from symmetry considerations alone.

Below 27 K, a magnetic hyperfine structure appears, with six-line characteristic spectra showing the presence of a magnetic hyperfine field acting on the nuclear moment. This is the fingerprint of a long-range magnetic order. The 4.2 K spectrum (see Fig. 8) corresponds to a single saturated hyperfine field  $H_{hf}$ =440(2) kOe; considering the hyperfine proportionality constant typical for Fe<sup>3+</sup> insulators of 110 kOe/ $\mu_B$ , this yields a unique Fe<sup>3+</sup> magnetic-moment value of  $4\mu_B$ , in agreement with the neutron-derived value. Close inspection of the 4.2 K spectrum reveals slight inhomogeneous line broadenings, most clearly seen when com-

paring the widths of the two central lines (labeled 3 and 4 in Fig. 8) and of the two intermediate lines (2 and 5). This spectral effect is due to a distribution of one or more hyperfine parameters. The magnetic structure determined by neutron diffraction being an incommensurate transverse spiral with propagation vector along c, then the angle between the hyperfine field, proportional to the Fe<sup>3+</sup> moment, and the principal-axis OZ of the EFG tensor, linked to the crystal axes, shows a distribution. The second-order shifts of the hyperfine energies due to the quadrupolar coupling then lead to a broadening which is different for each line.<sup>22</sup> The line fits in the magnetic phase in Fig. 8 were performed using this model; the key parameter determining the size of the broadenings being the angle  $\Theta$  between OZ and the propagation vector, which is found to be  $\Theta \simeq 36^{\circ}$ . On heating, the lines become broader and the overall magnetic splitting decreases, indicating that the mean hyperfine field decreases and that a distribution in hyperfine field values appears. The broadenings are significant near  $T_N$  (see the spectra at 23 and 26 K in Fig. 8). At 26 K, a small intensity paramagnetic doublet (13% relative weight) is present together with the magnetic order spectrum. At 27 K, the sample as a whole is paramagnetic. The coexistence of paramagnetic and magnetically ordered regions near  $T_N$  is usually associated with a first-order magnetic transition. However, in the other measurements reported here, the temperature evolutions of magnetic and electric properties across the transition do not display a clear first-order character.

## E. High-resolution x-ray diffraction

The remarkable magnetic properties of the Fe langasites underlined in the previous sections may also have consequences on their dielectric behavior. Indeed, the noncentrosymetric P321 space-group symmetry of the langasites does not allow the existence of an electric polarization. However, we have established that the Fe-langasite compounds undergo a transition toward a magnetic helical order, whose symmetries are compatible with ferroelectricity: preservation of the threefold axis and loss of the twofold axes. It is therefore interesting to determine whether a structural phase transition and a lowering of symmetry authorizing a ferroelectric order appear in the temperature region of the magnetic transition. The D1B data have not revealed any such modification in the four samples studied. However, the limited Qrange and spatial resolution make this instrument moderately suitable for the detection of subtle structural anomalies. In order to follow the structure as function of temperature with a much higher sensitivity, we have used high-resolution synchrotron powder diffraction at the ID31 beam line of the ESRF, equipped with a Ge(111) multianalyzer stage. This experiment was performed on the Ba3SbFe3Si2O14 compound. The sample contained in a 1-mm-diameter quartz capillary was placed inside a helium flow horizontal cryostat allowing sample rotation. Data collections were carried out in the range  $2\theta = 5^{\circ}$  to  $35^{\circ}$  at 26 temperatures between 250 and 10 K at an incident energy of 30 keV  $[\lambda = 0.398 \ 16(2) \ \text{Å}]$ . The diffractograms were analyzed by Rietveld refinement using the FULLPROF program. The back-



FIG. 9. (Color online) Rietveld plot for Ba<sub>3</sub>SbFe<sub>3</sub>Si<sub>2</sub>O<sub>14</sub> x-ray powder data at 250 K from ID31;  $R_{\text{Bragg}}$ =2.58,  $R_{\text{wp}}$ =23.4, and  $\chi^2$ =3.6.

ground was interpolated and the Bragg reflection shapes were described using a Thomson-Cox-Hastings profile function and a uniaxial description of anisotropic peak broadening about the [001] direction. All positional parameters in the P321 space-group description were refined, and all atoms were given isotropic atomic displacement parameters (a.d.p.), those of all oxygen atoms being constrained to be equal. The Rietveld plot for the 250 K data refinement is shown in Fig. 9.

The refined parameters at 250 K and 10 K are given in Table V and do not exhibit any anomalous difference, the only marked variations being the expected cell contraction and the decrease in the a.d.p.'s with temperature. Figures 10(a)-10(d) display the temperature evolution of the cell parameters, quadratic term U of the Gaussian peak width function, and a.d.p.'s of the cations. An obvious anomaly is detected in the a-parameter variation below 35 K (i.e., the magnetic ordering transition temperature for this compound). However, the amplitude of the anomaly is quite small since the cell parameter change between 40 and 10 K is only about 0.001 5 Å. One also observes anomalies below 35 K on the *c*-parameter evolution, but their amplitudes are even much smaller. Therefore, we cannot claim that they provide an evidence for a structural change. The U parameter depends on the instrumental resolution (which does not vary with temperature) and the presence of strain in the sample. This parameter, related to Gaussian strain, increases in cooling and then starts decreasing below about 40 K. This could be related to the building up of strain in the compound followed by a relaxation at lower temperature due to a structural reorganization associated to a phase transition. In this context, the increase in the cation isotropic a.d.p.'s could be due to the accommodation of atomic displacements associated to this structural transition.

If a structural phase transition coupled to the onset of magnetic order was present, then the symmetry of the low-temperature phase should keep the threefold axis and loose the twofold axis. The expected symmetry would then be *P*3, which allows an electric polarization. In this space group, the silicon and each of the oxygen sites are split into two positions. Refinements of the 10 K synchrotron data with the *P*3 symmetry were attempted but did not lead to conclusive re-

TABLE V. Refined structural parameters obtained from highresolution x-ray powder diffraction on BSFS on ID31, at 250 K ( $R_{\text{Bragg}}$ =2.58;  $R_{\text{wp}}$ =23.4;  $\chi^2$ =3.6) and 10 K ( $R_{\text{Bragg}}$ =2.35;  $R_{\text{wp}}$ =22.0;  $\chi^2$ =0.95). a.d.p. and U are, respectively, the atomic displacement parameter and the quadratic term of the Gaussian peak width.

Structural parameters refined at250, 10 (K)					
Atom	Wyckoff	x	у	z	a.d.p.
Ba	3 <i>e</i>	0.43747(7) 0.43686(6)	0	0	1.29(1) 1.000(8)
Sb	1 <i>a</i>	0	0	0	1.07(2) 0.92(2)
Fe	3 <i>f</i>	0.7527(2) 0.7523(1)	0	1/2	1.27(3) 1.11(2)
Si	2d	1/3	2/3	0.481(1) 0.479(1)	1.22(7) 1.00(7)
01	2d	2/3	1/3	0.790(2) 0.783(2)	1.39(8) 1.02(6)
02	6 <i>g</i>	0.4739(9) 0.4742(9)	0.2966(8) 0.2956(7)	0.649(1) 0.647(1)	1.39(8) 1.02(6)
O3	6 <i>g</i>	0.2174(7) 0.2161(7)	0.1001(6) 0.0986(6)	0.219(1) 0.223(1)	1.39(8) 1.02(6)
a (Å)		<i>c</i> (Å)		U	
8.51009(1) 8.50665(1)		5.251660(7) 5.247587(8)		0.0071(3) 0.0122(4)	

sults. However, the departure from the *P*321 symmetry may be very small leading to hardly detectable atomic displacements. As a conclusion, the results of this temperaturedependent high-resolution structural study might indicate the presence of a structural phase transition coupled to the onset of magnetic order. Single-crystal x-ray diffraction experiments might help determine the nature of the lowtemperature phase.

#### F. Dielectric measurements

In order to test the possible influence of the magnetic ordering on the dielectric properties of Fe langasites, dielectric measurements were performed at the Néel Institute by measuring the complex impedance of our samples using a commercial HP 4284A LCR-meter. The purpose-built experimental setup consists of a sample holder protected by a Dewar for a direct immersion in liquid helium of an helium container. Four coaxial cables linked to the electronic devices allow the complex impedance measurement. A model of capacitor and resistance in parallel was selected to extract the dielectric permittivity constant proportional to the capacitance of the sample, designed to approach the ideal geometry of a parallel-plate capacitor. The metallic electrodes are realized by sputtering with a silver target. Systematic check of the amplitude and frequency dependence were undertaken to



FIG. 10. (Color online) Thermal variation in some refined parameters from ID31 x-ray powder-diffraction data on Ba<sub>3</sub>SbFe<sub>3</sub>Si<sub>2</sub>O<sub>14</sub>: (a) cell parameter *a* (Å); (b) cell parameter *c* (Å); (c) quadratic term *U* of the Gaussian peak width function; (d) a.d.p.'s of Ba<sup>2+</sup>, Sb<sup>5+</sup>, and Fe<sup>3+</sup> cations.

establish the better conditions of measurements ruling out extrinsic effects. The chosen conditions were finally an amplitude voltage of 1 V and a frequency within the range of 10–100 kHz. The measurements under magnetic field were performed at the CRISMAT laboratory, with a similar experimental setup designed to work in a commercial Quantum Design PPMS and allowing to reach magnetic fields of 9 T.

The powder samples of BNFS, BTFS, and BSFS were prepared by pressing thin pellets, which were annealed at 1100 °C for 78 h. Single-crystal samples of BNFS and BTFS were oriented and cut within the rods obtained in the image furnace in order to have two different orientations for the applied electric field: along the c axis and along the  $a^*$ axis.

The thermal variation in the dielectric permittivity constant of all the powder samples shows a small cusp near the temperature associated with the magnetic transition: 24 K for BNFS and BTFS, 30 K for BSFS (the small difference with the magnetic  $T_N$  is not surprising for a first-order transition). This cusp is a contribution from the dielectric permittivity within the (a,b) plane. It is indeed clearly visible in the single-crystal samples with the electric field applied along the  $a^*$  axis (also reported in Ref. 23), while it is absent for the other orientation perpendicular to the (a,b) plane, which only shows a broad variation at higher temperature without any slope discontinuity (see Fig. 11 for BNFS). For a powder sample (see BSFS measurement on Fig. 12), the observed cusp is obviously smaller than for a single crystal, as crystallites of every orientation, even those not presenting this effect, contribute to the signal.

The variation in the relative increase in the dielectric permittivity as a function of the magnetic field applied in the direction of the electric field (perpendicular to the c axis) is illustrated for different temperatures by the Fig. 13. It shows mainly a quadratic dependence with the field. As the dielectric permittivity is the second partial derivative of the free energy with respect to the electric field, the magnetoelectric coupling terms measured here correspond to the terms of second order in electric field within the free-energy development

$$-\frac{1}{2}\epsilon_0\epsilon_{ij}E_iE_j-\frac{1}{2}\gamma_{ijk}E_iE_jH_k-\frac{1}{2}\eta_{ijkl}E_iE_jH_kH_l-\cdots.$$

The results obtained for the Fe langasite means that only  $\eta_{ijkl}$  contributes to the measured magnetoelectric effect. It is worth noting that this coupling term is always present in the free-energy development, as it is of second order in both electric and magnetic field, so no particular symmetry con-



FIG. 11. Thermal variation in the electric capacity (proportional to the dielectric permittivity) of BNFS single crystal for an electric field applied perpendicular to the c axis (left) and parallel to it (right).



FIG. 12. (Color online) Thermal variation in the electric capacity (proportional to the dielectric permittivity) of a pellet of BSFS powder. The red line is a linear extrapolation of the data above 30 K shown to emphasize the cusp.

ditions determine its existence, unlike for  $\gamma_{ijk}$ . This quadratic coefficient however varies with the temperature, being maximum close to the Néel temperature. This variation reflects the critical behavior of the magnetoelectric effect describable in the frame of the fluctuation-dissipation theory.<sup>24</sup> Other magnetoelectric coupling terms are accessible when measuring the magnetic dependence of the electric polarization (which is the first partial derivative of the free energy with respect to the electric field).

# **III. DISCUSSION**

#### A. Magnetic properties

Our investigations of the Fe-langasites magnetic properties have revealed an original magnetic order at low temperature associated to the triangular array of triangles of magnetic Fe<sup>3+</sup>. The magnetic moments are orientated at  $120^{\circ}$ from each other within the triangles and propagate helically perpendicular to the triangular planes. There are at least two



FIG. 13. (Color online) Magnetic dependence of the relative variation in the dielectric permittivity of a BNFS single crystal for several temperatures. Both magnetic and electric fields are applied perpendicular to the c axis. The lines are parabolic fits. The inset shows the quadratic coefficient of these fits versus temperature.

energy scales in this system since the intratriangle superexchange is expected to be much stronger than the in-plane and out-of-plane intertriangle interactions, which are mediated by two oxygens. The Curie-Weiss temperature mainly reflects this intratriangle interaction, which also gives rise to magnetic fluctuations above the ordering temperature (see Fig. 7). The Curie-Weiss temperature is larger than the Néel temperature by almost an order of magnitude. The threedimensional ordering sets in when the temperature becomes of the order of the super-super-exchange paths within the planes and between them. We have previously shown<sup>18</sup> that this helical arrangement results from a twist of the interplane interaction: the strongest interaction among the three that link one Fe<sup>3+</sup> of a triangle to the three Fe<sup>3+</sup> of the triangle of the next plane is diagonal (J3 or J5). If, moreover, the two other interactions are zero, it is easily shown that the z component of the propagation vector would be exactly  $\tau = 1/6 = 0.167$ , i.e., a rotation of the moments of 60° from plane to plane.<sup>18</sup> The departure of the propagation vector from 1/6 arises when the two other interplane interactions are no more negligible.

In the present study, we have focused on the effect on the magnetic properties of different nonmagnetic cations on sites A, B, and D. The most striking result is that all the magnetic characteristics are roughly identical for all compounds even when the substitution produces a large variation in the cell parameters, except for those containing Sb (in place of Nb or Ta). The presence of this cation systematically increases the Néel temperature, decreases the Curie-Weiss one, increases the value of the ordered magnetic moment, and increases the  $\tau$  value (i.e., shortens the helical modulation period). The origin of this effect could be structural, the Sb<sup>5+</sup> radius being slightly smaller than the Ta<sup>5+</sup> or Nb<sup>5+</sup> ones. However, no systematic trend on exchange path geometry was revealed by the structural investigation performed with powder neutron scattering on chosen compounds. The microscopic mechanism at play should therefore be of electronic origin. It could be related to the larger Pauling electronegativity of Sb<sup>5+</sup> (2.05) with respect to Nb<sup>5+</sup> (1.6) and Ta<sup>5+</sup> (1.5).<sup>25</sup> The departure of this value from the oxygen electronegativity (3.44) gives the degree of ionicity/covalency and polarization of the cation-oxygen bond involved in the magnetic exchange paths. This should therefore give a more covalent character to the Sb-O bond. The electronic structure of the Sb<sup>5+</sup> cation is also different from the Nb<sup>5+</sup>/Ta<sup>5+</sup> ones (different column of the periodic table) with, in particular, a full outermost 4dshell.

Remembering that two consecutive  $Fe^{3+}$  triangles along the *c* axis are coupled via oxygen anions forming the octahedral coordination of the *D* site cation (see Fig. 2), it is not surprising that a change in the electronic affinities of this cation has consequences onto the magnetic coupling within and between the planes. For instance, the increased covalence of the Sb-O bond seems in turn to decrease the strength of the J1 Fe-O-Fe bond involving the same oxygen ions. The consequence of this is the observed lowering of the Curie-Weiss temperature and smaller spin transfer from the Fe<sup>3+</sup> to the oxygen (hence, a larger ordered moment).

The influence of the electronic properties of Sb on the Néel temperature and on the helix propagation vector is more

difficult to track since it implies more complicated exchange paths between two planes. It is however interesting to note that the angle of rotation of the spin is larger than  $60^{\circ}$  for Sb compounds and smaller than  $60^{\circ}$  for the Nb/Ta ones. This implies a contribution of the two weaker interplane interactions, whose ratio would be inverted between Sb compounds and Nb/Ta ones.

## **B.** Dielectric properties

It is of course of interest to address the question of the influence of this increased Sb-O bond covalence on the dielectric properties of the Fe langasites. The dielectric measurements on all powder samples have not shown significant difference though, with a similar cusp of the dielectric permittivity close to  $T_N$ , suggesting the same kind of magnetoelectric coupling for the different compounds. This comparative study could be deepened by electric polarization measurements.

The dielectric properties reported here for the Fe langasites are strikingly similar to those of YMnO<sub>3</sub>. The magnetic structure of this compound presents some resemblance with the Fe-langasite one: a triangular array of in-plane magnetic moments oriented at 120° from each other in the ordered phase. The dielectric measurements performed on this multiferroic compound show a comparable anomaly in the thermal variation in the (a, b) in-plane dielectric permittivity while nothing is visible for the dielectric permittivity measured along the c axis, and a quadratic dependence of the dielectric permittivity close to this anomaly with the magnetic field (note, however that, in the YMnO<sub>3</sub> study, the magnetic field was oriented perpendicular to the electric one). This anisotropic dielectric behavior of YMnO<sub>3</sub> has been described in a phenomenological Landau description of ferroelectric antiferromagnets including a fluctuative part.<sup>24</sup> Unlike the langasites, YMnO3 is already ferroelectric at temperatures well above the magnetic transition (proper multiferroic). Anyway, the magnetic ordering still induces an additional contribution to the overall electric polarization. The rise of electric polarization at the Néel temperature has also been claimed very recently in the Fe langasite by Zhou et  $al.^{23}$  from polarization measurements performed along the *c* axis. This would imply that, at variance with YMnO<sub>3</sub>, these langasite compounds should be classified as improper multi-ferroics, the magnetic transition driving a paraelectric-ferroelectric transition. Such behavior has already been reported in another compound containing an Fe triangular lattice, where the electric polarization is induced at the Néel transition in the *c* direction along the axis of the helix and perpendicular to the plane of the moments oriented at 120° from each other.<sup>26</sup>

## **IV. CONCLUSION**

The Fe Langasites are the only compounds of this family to evidence a magnetic ordering whose peculiar arrangement reflects magnetic frustration and the chirality of the structure. This rich family offers several Fe-based compounds with different cationic substitutions among which we have highlighted the singular role of the Sb cation on the magnetic properties. The langasite structure is noncentrosymmetric and a further loss of symmetry elements is achieved in the magnetic structure that leave an overall polar structure authorizing the appearance of a spontaneous electric polarization. This would then be associated to a structural phase transition as suggested by high-resolution x-ray diffraction. Dielectric measurements reveal the presence of magnetoelectric coupling through an anomaly at the Néel temperature in the thermal variation in the dielectric permittivity and its quadratic dependence with the magnetic field. The Fe langasite could then be an example enlarging the class of magnetoelectric/multiferroic triangle-based antiferromagnets.

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