Low-moment antiferromagnetic ordering in triply charged cubic fullerides close to the metal-insulator transition

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We report on the ambient pressure ¹³C and ¹³³Cs NMR study of disorder-free A15-structured Cs₃C₆₀, which shows non-BCS superconductivity at 38 K under pressure. Temperature-independent ¹³C and ¹³³Cs spin-lattice relaxation rates prove an insulating ground state with a small effective magnetic moment 1.3–1.6 μ_B for *T* > 100 K. Below 46 K, A15 Cs₃C₆₀ orders into an antiferromagnetic structure best described by a magnetic wave vector, $\mathbf{q} = (\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$ with a staggered magnetic moment $\sim 0.9\mu_B$ per C₆₀. The large (*U/W*) ratio (~ 2.2), the opening of a gap in the electronic excitation spectrum and the small C³⁻₆₀ magnetic moment all underline the importance of electronic correlations in A15 Cs₃C₆₀.

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The interplay between strong electron correlations and high-temperature superconductivity has been widely recognized but simple model systems to test key aspects of theory are currently missing. The alkali fulleride, Cs₃C₆₀,¹ which is free of positional, chemical, and orientational disorder shows both a high T_c and a direct transition from an antiferromagnetic insulator (AFI) to a superconductor without any structural distortion.^{2,3} The superconducting state emerges in the body-centered-cubic (bcc) based A15 phase directly from the ambient pressure AFI state with the application of pressure above 3.6 kbar.^{2,3} T_c first increases with pressure but then exhibits a broad maximum at \sim 7 kbar where it reaches 38 K. The nonmonotonic dependence of T_c on pressure and the occurrence of superconductivity next to the AFI phase cannot be simply rationalized within the BCS formalism and highlight the importance of electronic correlations in A15 Cs₃C₆₀. This behavior is fundamentally different from that of the superconducting face-centered-cubic (fcc) A_3C_{60} phases, in which T_c increases monotonically with increasing interfulleride separation.⁴

The unconventional nature of the superconducting state emerging from the AFI state in A15 Cs₃C₆₀ raises important generic questions about the interplay between magnetism and superconductivity and, in particular, how the proximity to the metal to insulator transition (MIT) boundary together with the single molecule properties, such as the Jahn-Teller effect and Hund's rule coupling, determine the A15 Cs_3C_{60} ground state. Investigations of the magnetic properties hold the key to the understanding of the role of electronic correlations, electron-phonon coupling and crystal symmetry in determining the ambient pressure AFI and high-pressure superconducting states. Here we report temperature-dependent ¹³C and ¹³³Cs NMR measurements at ambient pressure on a powdered Cs₃C₆₀ sample. Our results confirm the insulating ground state in A15 Cs_3C_{60} (Ref. 3) where t_{1u} electrons become localized due to the large (U/W) ratio (~2.2). Antiferromagnetic (AFM) order with a small staggered moment of $\sim 0.9 \mu_B$ per C₆₀³⁻ unit is observed below $T_N = 46$ K. The small magnetic moment in A15 Cs₃C₆₀ arises either from the dynamic Jahn-Teller effect and/or because of the proximity to the MIT boundary. These findings are the hallmark of the importance of electronic correlations in expanded bccstructured fullerides and provide a link between the anomalous pressure dependence of T_c and the ambient pressure AFI state in Cs₃C₆₀.

Synchrotron x-ray diffraction (XRD) showed that the studied Cs₃C₆₀ batch contains predominantly A15 Cs₃C₆₀ [52.2(1)%] with minority fcc Cs₃C₆₀ [31.5(2)%] and body-centered orthorhombic (bco) Cs_{3+x}C₆₀ [16.3(2)%] phases. ¹³³Cs (*I*=7/2) and ¹³C (*I*=1/2) NMR experiments were performed in a 8.9 T magnetic field. Reference frequencies, ν (¹³C)=95.557 MHz and ν (¹³³Cs)=49.845 MHz were obtained from tetramethylsilane and CsNO₃ standards, respectively. In ¹³C NMR line-shape experiments, a Hahn echo pulse sequence with $\pi/2=6$ μ s was used. For ¹³³Cs NMR experiments we used a two-pulse (β) – τ –(β) – τ –echo sequence; the pulse length, $\tau_{\beta}=2$ μ s was optimized to amplify the A15 signal. A typical interpulse delay was τ =60 μ s. For spin-lattice relaxation time, *T*₁ measurements the saturation recovery technique was used. The repetition time was 0.2 s at ambient temperature.

Figure 1 shows the ¹³C NMR powder spectra of Cs_3C_{60} for selected temperatures. The presence of different phases in the investigated sample is reflected in the multicomponent spectrum measured at 300 K [Fig. 1(a)]: a main sharp line (signal A) at 199 ppm, a broad background extending between 100(10) and 340(20) ppm (signal B) and a weak line centered at 180 ppm (signal C). The main signal A (relative intensity ~50%) is attributed to the dominant A15 polymorph following the assignment of Ref. 2 based on magic angle spinning ¹³C NMR. Signals B and C are then due to the coexisting fcc and bco minority phases.

The above line-shape assignment allows us to follow the temperature dependence of the A15 ¹³C NMR shift, ¹³ δ_{iso} , between 400 and 300 K. In this temperature range, ¹³ δ_{iso} increases from 196 to 199 ppm with decreasing temperature [inset Fig. 2(a)]. In fullerides, ¹³ δ_{iso} has two main contributions: the temperature-independent C_{60}^{3-} chemical shift, σ_{iso}



FIG. 1. (Color online) (a) ¹³C NMR spectrum at 300 K. Signal A is due to the majority A15 Cs₃C₆₀ phase while components B and C are due to the coexisting fcc Cs₃C₆₀ and bco Cs_{3+x}C₆₀ phases. (b) Temperature evolution of the ¹³C NMR spectra below 80 K. Note the sudden line shape change and broadening below 46 K. (c) ¹³C NMR spectrum at 20 K. The thin solid red line is the calculated ¹³C NMR line shape for the AFM2 structure, $\mathbf{q} = (\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$ and $\mu_S = 0.9\mu_B$. The narrow part of the spectrum not described by the fit is due to the coexisting fcc phase.

=150 ppm (Ref. 5) and the Fermi contact shift, ${}^{13}\delta_S$. ${}^{13}\delta_S$ is expressed with the hyperfine coupling constant, ${}^{13}A$, and the uniform spin susceptibility, χ_S , as

$$^{13}\delta_{S} = \left(\frac{^{13}A}{\gamma_{e}\gamma_{C}\hbar}\right)\chi_{S},\tag{1}$$

where γ_e and γ_C are the electron, and ¹³C nuclear gyromagnetic ratios. Taking ¹³ δ_S =49 ppm and a typical C_{60}^{3-} value, ¹³ $A/2\pi$ =0.69 MHz,⁶ we calculate the room-temperature spin susceptibility as χ_S =8.3×10⁻⁴ emu/(mol C₆₀) from Eq. (1). Interpreting the increase in ¹³ δ_{iso} with decreasing temperature as the signature of a Curie-Weiss behavior of χ_S with a Weiss constant, θ =-68 K,³ we can extract an effective moment, μ_{eff} ~1.6 μ_B . This is comparable to μ_{eff} =1.32(1) μ_B extracted directly from the magnetic susceptibility data of an A15 sample with bco and fcc impurities.³ It is also very close to μ_{eff} =1.73 μ_B expected for the localized *S*=1/2 spin state.

The *bco* $Cs_{3+x}C_{60}$ ¹³C NMR signal can be easily separated from the other two spectral components below 300 K since it has much longer T_1 . Therefore, spectra obtained in measurements with short repetition times are dominated by the rapidly relaxing A15 phase [Figs. 1(b) and 1(c)]. This allows us to accurately determine the temperature dependence of ¹³C $1/T_1$ for cubic A15 (Ref. 3) and compare it with that of the orthorhombic antiferromagnetic insulators, $(ND_3)K_3C_{60}$ (Refs. 7 and 8) and (CD₃ND₂)K₃C₆₀, which differ in symmetry and unit-cell volume per C_{60}^{3-} (Fig. 3). For all three phases, $1/T_1$ is nearly temperature independent at high temperatures [a sudden decrease in $1/T_1$ in $(CD_3ND_2)K_3C_{60}$ is due to the structural phase transition at 220 K (Refs. 9 and 10)]. These results contradict the Korringa relation, T_1T $(\Delta K)^2$ = const which is followed in metallic fcc A_3C_{60} .¹¹ The deviation from the Korringa relation and the similarity in $1/T_1$ with insulating (ND₃)K₃C₆₀ and (CD₃ND₂)K₃C₆₀



FIG. 2. (Color online) (a) Temperature dependence of the square root of the ¹³C NMR second moment. Inset: A15 ¹³C NMR shift (left scale) and the calculated χ_S (right scale) at high temperature. (b) Temperature dependence of the A15 ¹³³Cs NMR shift (solid circles). Inset: temperature dependence of the bulk χ_S (open circles) reproduced from Ref. 3. Vertical dashed lines mark T_N =46 K.

clearly rule out a metallic ground state for A15 Cs_3C_{60} and are fully consistent with the nuclear relaxation in exchange coupled antiferromagnetic insulators, where $1/T_1$ is in the high-temperature limit given by¹²

$$\frac{1}{T_1} = \sqrt{2\pi} \frac{{}^{13}A^2 + \frac{1}{2}A_{dip}^2}{3g^2\mu_B^2} \frac{\mu_{eff}^2}{\omega_{ex}}.$$
 (2)

Here the dipolar hyperfine coupling constant is $A_{dip}/2\pi$ =3.38 MHz (Ref. 6) and the exchange frequency ω_{ex}^2 = $2zk_B^2 J^2 S(S+1)/3\hbar^2$ is determined by the interfulleride exchange interactions, *J*, and the number of near neighbors in the bcc lattice, *z*=8, yielding J/k_B =30 K for A15 Cs₃C₆₀. Assuming antiferromagnetic exchange interactions, *J* can be expressed as $J=4t^2/U$, where *t* is the interfullerene transfer integral. For bcc lattice, $t \sim W/16$ and by taking a typical value for the on-site Coulomb repulsion, $U \sim 1$ eV,^{13,14} we estimate W=0.43 eV. The extracted bandwidth is essentially identical with that calculated, W=0.49 eV (Ref. 15) and implies that nonfrustrated A15 Cs₃C₆₀ is insulating because of the large (U/W)=2.2 ratio. We now turn to ¹³³Cs NMR, which is an established probe

We now turn to ¹³³Cs NMR, which is an established probe of local structural details through the quadrupolar interaction and of magnetic properties via electron-nuclear dipolar interactions. In the presence of quadrupole effects, the position of the central $\frac{1}{2} \leftrightarrow -\frac{1}{2}$ transition is unaffected to first order by



FIG. 3. (Color online) (a) Temperature dependence of the ¹³C spin-lattice relaxation rate, $1/{}^{13}T_1$, in A15 Cs₃C₆₀ (open circles), orthorhombic (ND₃)K₃C₆₀ (magenta upper triangle) and (CD₃ND₂)K₃C₆₀ (blue down triangles) phases. The A15 ¹³³Cs spin-lattice relaxation rate, $1/{}^{133}T_1$ is shown as black solid circles. Dotted lines are guides to the eye. (b) Temperature dependence of the ¹³C and ¹³³Cs spin-lattice relaxation rates ratio, ${}^{133}T_1/{}^{13}T_1$.

the electric field gradient (EFG, $V_{ij} = \frac{\partial^2 V}{\partial x_i \partial x_j}$), while the shift of the satellite lines is proportional to a quadrupole frequency, $\nu_Q = \frac{3eQV_{zz}}{2I(2I-1)h}$, which is related to the strength of the EFG V_{zz} and the ¹³³Cs quadrupole moment, Q. Moreover, the structure of the EFG tensor is extremely sensitive to the local symmetry of the Cs site. For A15 Cs₃C₆₀, the site symmetry of the single Cs site (-4m.2) is compatible with uniaxial ($\eta = \frac{V_{xx} - V_{yy}}{V_{zz}} = 0$) quadrupolar interaction. We optimized our pulsed echo sequence in order to obtain nearly pure A15 ¹³³Cs NMR spectra³ with a typical I=7/2 quadrupole powder line shape [Fig. 4(a)]. A satisfactory agreement with the measured spectrum at 100 K can be achieved with $\nu_Q = 39(1)$ kHz and $\eta=0$ [Fig. 4(a)].

In the line-shape analysis, we introduced a temperaturedependent ¹³³Cs NMR shift, ¹³³ δ_{iso} which first increases with decreasing temperature as expected for a paramagnetic insulator. The temperature-dependent part of the ¹³³Cs shift can be expressed as ¹³³ $\delta_S = (\frac{13}{2\sqrt{\gamma_c t}})\chi_S$, where γ_{Cs} is the ¹³³Cs gyromagnetic ratio and ¹³³A is the corresponding hyperfine coupling constant. A linear relationship between ¹³³ δ_S and χ_S is obeyed between room temperature and ~120 K, yielding ¹³³A/2 π =0.35(3) MHz. However, below ~120 K, ¹³³ δ_{iso} suddenly begins to shift to lower frequencies [Fig. 2(b)]. On the other hand, magnetic-susceptibility measurements³ reveal no anomalous response and the bulk χ_S increases monotonically in this temperature range [inset to Fig. 2(b)]. Although the measured χ_S includes contributions from the coexisting fcc and bco phases, it appears unlikely that the anomalous temperature dependence of ¹³³ δ_S below ~120 K can be ex-



FIG. 4. (Color online) (a) Temperature dependence of the ¹³³Cs NMR powder spectra for A15 Cs₃C₆₀. For comparison we include the high-temperature fit of the quadrupolar powder spectrum with ν_Q =39 kHz and η =0 (bottom) and the low-temperature fit for the AFM2 structure with \mathbf{q}_2 = $(\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$ (top). (b) Comparison between the experimental ¹³³Cs NMR spectrum at 14 K (thick blue line) and the calculated spectra for the AFM2 (solid red line) and AFM1 [\mathbf{q}_1 =(1,1,1), dashed black line] structures. In both simulations, μ_S =0.9 μ_B .

plained in terms of a sudden change in $\chi_S(T)$ and we therefore attribute it to a change in ¹³³A. As ¹³³A is given by the Fermi contact interaction due to the nonzero Cs 6*s* orbital admixture in the t_{1u} orbital and the core-polarization hyperfine coupling resulting from the exchange polarization of the Cs core electrons by unpaired C_{60}^{3-} electrons, a plausible explanation for the observed temperature dependence of ¹³³ δ_{iso} is that the Fermi contact interaction begins to change around 120 K. This change in the Fermi contact interaction may be associated with the onset of dynamic Jahn-Teller distortion at the C_{60}^{3-} anions on the time scale of our NMR experiments.

Interestingly, ¹³C $1/T_1$ also becomes gradually suppressed below ~120 K [Fig. 3(a)].³ We stress that in this temperature range the C_{60}^{3-} units are already static on the ¹³C NMR time scale and there is no structural phase transition that could account for the $1/T_1$ reduction. Therefore the observed temperature dependence of $1/T_1$ should reflect a change in the C_{60}^{3-} spin dynamics, described by the imaginary part of the spin susceptibility, $\chi''(\vec{q}, \omega)$. Then the ¹³C 1/T₁ suppression is consistent with the opening of a small gap in the spin excitation spectrum at discrete points in \vec{q} space so that $\chi''(\vec{q},\omega) \propto e^{-\Delta_q/T}$. We estimate that the wave-vectordependent spin gap, Δ_q is on the order of 0.1 eV, which is a typical energy scale for the excitations induced by the dynamic Jahn-Teller effect.¹⁶ At the same time, the temperature dependence of ¹³³Cs $1/T_1$ is nearly identical to that of ¹³C $1/T_1$ [Fig. 3(a)]. Noting that ¹³³Cs $1/T_1$ (T) is determined in part by the temperature dependence of 133 A and in part by that of $\chi''(\vec{q}, \omega)$, we conclude that the temperature-invariant $^{133}T_1/^{13}T_1$ ratio [Fig. 3(b)] reflects the dominant effect of $\chi''(\vec{q},\omega)$ on ¹³³Cs $1/T_1$. Therefore, the gap in the excitation spectrum detected in ¹³C $1/T_1$ is additionally supported by the ¹³³Cs $1/T_1$ data and may be linked with the anomalous temperature dependence of ¹³³ δ_{iso} . Since such a gap is not present in the low-symmetry large unit-cell volume $(ND_3)K_3C_{60}$ and $(CD_3ND_2)K_3C_{60}$ systems, we attribute it to a specific property of the insulating A15 state close to the MIT boundary.

At temperatures below 46 K, the ¹³C NMR signal suddenly becomes very symmetric and broadens with decreasing temperature [Figs. 1(b) and 1(c)] leading to a dramatic increase in M_2 [Fig. 2(a)]. At the same time, the ¹³³Cs NMR line shape also dramatically broadens,³ becomes more symmetric and the details of the quadrupole line-shape structure are lost [Fig. 4(b)]. The ¹³³Cs NMR spectra continuously broaden on cooling below 46 K and the ¹³³Cs NMR second moment follows the magnetic order parameter, unambiguously confirming the AFM ordering of the A15 phase.³

We now proceed to address the low-temperature magnetic structure of the A15 phase by simulating the ¹³³Cs NMR spectra using the formalism developed earlier for ammoniated and methylaminated alkali fullerides^{8,10} and A_1C_{60} .¹⁷ The orientation of a staggered magnetic moment, μ_{s} , placed at the center of the C60 molecule, was calculated in the spinflop phase (the spin-flop field is usually on the order of only 100 mT in fullerides⁹). For simplicity only collinear magnetic structures are considered. Two possible magnetic structures, which are compatible with the bcc symmetry¹⁸ are described by ordering vectors $\mathbf{q}_1 = (1, 1, 1)$ (AFM1) and \mathbf{q}_2 $=(\frac{1}{2},\frac{1}{2},\frac{1}{2})$ (AFM2). Which of the two magnetic structures will prevail depends on the relative strength of the firstnearest-neighbor (J_1) and second-nearest-neighbor interactions (J_2) . There is a quantum phase transition from AFM1 to AFM2 at $J_2/J_1=0.705$.¹⁸ Best agreement between experimental and simulated spectra [solid line in Fig. 4(b)] was obtained for the AFM2 structure [inset Fig. 4(b)] with μ_s =0.9 μ_B . As a consistency check, we also calculated the ¹³C NMR line shape [Fig. 1(c)] and found an acceptable agreement. The simple AFM1 structure with the same μ_{S} results in a ¹³³Cs NMR line, that is, broader than the experimental spectrum [dashed line in Fig. 4(b)]. In order to match the experimental spectrum, a reduced $\mu_s = 0.6 \mu_B$ has to be used. Although our results cannot unambiguously distinguish between the two magnetic structures, they point to a small staggered moment of less than $1\mu_B$ per C³⁻₆₀. The alternative disordered magnetic moment ground state is in disagreement with both the observation here that M_2 increases sharply at the ordering temperature and with ZF- μ SR measurements³ which find a long-range magnetically ordered ground state.

Our ¹³C and ¹³³Cs NMR results provide additional evidence for the ambient-pressure AFI ground state of A15 Cs_3C_{60} .³ An important finding of the present work is the reduced magnitude of the magnetic moment: in the paramagnetic phase, μ_{eff} =1.3–1.6 μ_B , while in the AFM phase, μ_S =0.6-0.9 μ_B . For a system, that is, deep in the Mott insulating state, the t_{1u} electrons are localized on each C₆₀ unit and result in either a high-spin (HS) S=3/2 or a low-spin (LS) $S=\frac{1}{2}$ state. The measured μ_{eff} is significantly smaller than the HS value and much closer to that of the LS state. This implies that in A15 Cs₃C₆₀ the LS state, stabilized by the Jahn-Teller effect, narrowly prevails over the HS state favored by the interorbital Hund's rule exchange and the observed gap is due to the energy difference between these two states. However, the Jahn-Teller effect has to be dynamic since our XRD studies show that cubic symmetry is maintained down to 4 K.³ The diamagnetic shift of ${}^{133}\delta_{iso}$ is then presumably related to the broken orbital rotational symmetry on the NMR time scale. The long-range orbital-ordering temperature with static Jahn-Teller molecular distortions should be very low. For instance, in monoclinic TDAE-C₆₀, Jahn-Teller dynamics freeze below 9 K.¹⁹⁻²² This scenario is in agreement with recent theoretical investigations underlying the importance of electronic correlations and the dominance of the dynamic Jahn-Teller effect in cubic fullerides close to the MIT boundary.²³ An alternative explanation for the reduced magnetic moment could be based purely on the proximity of A15 Cs₃C₆₀ to the MIT border. In this context, the magnetic susceptibility of narrow-band electron systems is expected to obey the Curie-Weiss law for a wide range of U(Ref. 24) but local excitations can dramatically renormalize the values of μ_{eff} and μ_S when the system with large U/W is in the vicinity of the MIT boundary. Further theoretical and experimental investigations are needed to distinguish between these two models.

In conclusion, the NMR results are consistent with an ambient pressure insulating ground state for A15 Cs₃C₆₀, which orders antiferromagnetically below T_N =46 K with a reduced staggered magnetic moment of ~0.6–0.9 μ_B per C³⁻₆₀. The most likely magnetic structure is described by the magnetic wave vector $\mathbf{q} = (\frac{1}{2}, \frac{1}{2}, \frac{1}{2})$ and suggests the importance of interfulleride exchange coupling not only between first but also between second nearest C³⁻₆₀ neighbors. The small C³⁻₆₀ magnetic moments, the large (U/W)=2.2 ratio, and the small gap in the electronic excitation spectrum reflect the importance of the electronic correlations in alkali-doped fullerides with expanded unit cells.

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