

Superconducting fluctuations in the reversible magnetization of the iron-pnictide $\text{Ba}_{1-x}\text{K}_x\text{Fe}_2\text{As}_2$ S. Salem-Sugui, Jr.,¹ L. Ghivelder,¹ A. D. Alvarenga,² J. L. Pimentel, Jr.,³ Huiqian Luo,⁴ Zhaosheng Wang,⁴ and Hai-Hu Wen⁴¹*Instituto de Física, Universidade Federal do Rio de Janeiro, 21941-972 Rio de Janeiro, RJ, Brazil*²*Instituto Nacional de Metrologia Normalização e Qualidade Industrial, 25250-020 Duque de Caxias, RJ, Brazil*³*Instituto de Física, Universidade Federal do Rio Grande do Sul, 91501-970 Porto Alegre, RS, Brazil*⁴*National Laboratory for Superconductivity, Institute of Physics and National Laboratory for Condensed Matter Physics, P.O. Box 603, Beijing 100190, People's Republic of China*

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We report on isofield magnetization curves obtained as a function of temperature in two single crystals of $\text{Ba}_{1-x}\text{K}_x\text{Fe}_2\text{As}_2$ with superconducting transition temperature $T_c=28$ and 32.7 K. Results obtained for fields above 20 kOe show a well-defined rounding effect on the reversible region extending 1–3 K above $T_c(H)$ masking the transition. This rounding appears to be due to three-dimensional critical fluctuations, as the higher field curves obey a well known scaling law for this type of critical fluctuations. We also analyzed the asymptotic behavior of \sqrt{M} vs T curves in the reversible region which probes the shape of the gap near $T_c(H)$. Results of the analysis suggests that phase fluctuations are important in $\text{Ba}_{1-x}\text{K}_x\text{Fe}_2\text{As}_2$ which is consistent with nodes in the gap.

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I. INTRODUCTION

Among the iron-pnictide systems found until now,^{1,2} $\text{Ba}_{1-x}\text{K}_x\text{Fe}_2\text{As}_2$ is one of the most studied. Experiments on this system includes, local magnetization,³ resistivity and bulk magnetization,^{4,5} specific heat,^{6,7} magnetoresistance,⁸ NMR,⁹ thermal conductivity,¹⁰ ARPES,^{11,12} electronic relaxation,¹³ vortex dynamics,¹⁴ combined muon-spin rotation, neutron scattering, and magnetic force spectroscopy¹⁵ among others, but fluctuations studies are still lacking, which motivated this investigation.

Superconducting fluctuations are important in the vicinity of the transition temperature T_c and have been extensively studied in all kinds of superconductors.^{16–18} In the case of layered systems, fluctuation superconductivity is enhanced, and there are robust theories predicting the behavior of many measurable quantities with temperature and magnetic field, in or out of the critical region.^{16,19–25} Comparison of experimental results with these theories helps to understand the nature of the fluctuations, its dimensionality^{17,22,26–28} and give additional insight about the pairing mechanism symmetry of the studied system.^{23,29}

In this work we study the effect of superconducting fluctuations in the region of reversible magnetization of the new iron-pnictide system $\text{Ba}_{1-x}\text{K}_x\text{Fe}_2\text{As}_2$,^{30,31} which is a fully gaped layered superconductor.⁶ This system is a hole doped oxygen-free iron-pnictide superconductor with T_c ranging from 24 to 38 K depending on doping.^{30,31} Similar to the high- T_c cuprates the $\text{Ba}_{1-x}\text{K}_x\text{Fe}_2\text{As}_2$ system presents a “bell-shaped” phase diagram of T_c against doping,^{32,33} but the system has a low anisotropy with an anisotropy factor γ between 2 and 3^{4,8} and a s -wave multiband pairing symmetry.^{3,11} A nodeless s -wave gap is claimed in Ref. 11, but Ref. 10 show evidence for nodes in the gap, and a recent theoretical work shows that a multiband- s -wave gap can have nodes.³⁴ The multiband s -wave pairing mechanism in iron-pnictides is still on debate, whether it is a conventional

 s -wave^{35,36} or unconventional with nodes.^{34,37}

We demonstrate in the present study that, contrary to what was expected,⁷ isofield reversible magnetization curves obtained in $\text{Ba}_{1-x}\text{K}_x\text{Fe}_2\text{As}_2$ for magnetic fields, H , in the range of 20–50 kOe show a considerably large amplitude fluctuations in the vicinity of $T_c(H)$ with a well-defined rounding effect which masks the transition. This rounding effect is reminiscent of magnetization curves obtained in high- T_c superconductors.^{20–22,38,39} In the case of cuprate superconductors, superconducting activity above T_c appears to be related with the so-called pseudogap^{40,41} which is not considered in the theories for layered systems.⁴² Despite some similarities between iron pnictides and cuprates in what concerns for instance the existence of magnetic fluctuations and magnetic order (AF anomaly) in the nonsuperconductor precursors,³³ most likely there is no such pseudogap phase in iron pnictides.⁴³ Furthermore the study of fluctuations effects in this iron-pnictide system is of particular interest, allowing further comparison with newly developed theories.

We also address the existence of phase fluctuations in $\text{Ba}_{1-x}\text{K}_x\text{Fe}_2\text{As}_2$ by analyzing the asymptotic behavior of \sqrt{M} vs T curves in the reversible region. The existence of nodes in the gap may enhance phase fluctuations effects in the vicinity of T_c (Ref. 23) changing the shape (the asymptotic behavior) of the gap in this region. The quantity \sqrt{M} near T_c is directly proportional to the amplitude of the order parameter⁴⁴ and \sqrt{M} vs T curves can probe the shape of the gap near $T_c(H)$.^{23,29} Our analysis suggests that phase fluctuations are important near T_c in $\text{Ba}_{1-x}\text{K}_x\text{Fe}_2\text{As}_2$.

II. EXPERIMENTAL

Two high quality single crystals of $\text{Ba}_{1-x}\text{K}_x\text{Fe}_2\text{As}_2$ were investigated, with $T_c=32.7$ and 28 K, corresponding to a potassium content of $x=0.28$ and 0.25, respectively, and with masses of approximately 0.05 and 0.3 mg. Both show a fully developed superconducting transition with width ΔT_c

≈ 1 K for sample with $T_c = 32.7$ K and width $\Delta T_c \approx 2$ K for sample with $T_c = 28$ K. The crystals were grown by a flux-method described elsewhere.³¹ Similar samples made by the same group were used in various previous investigations.^{3,4,7,14} Since anisotropy is low in this system,^{4,8} the measurements were carried out only for the direction $H \parallel c$ axis. Magnetization data were obtained with a commercial magnetometer based on a superconducting quantum interference device (SQUID). The data were obtained after cooling the sample from temperatures well above T_c in zero applied magnetic field (zfc) to a desired temperature below T_c ($T_{min} \approx 10$ K). Magnetic fields up to 50 kOe were applied, reaching the desired value without overshoot. The data were obtained by continuously heating the sample, and collecting magnetization results within fixed increments of temperature, $\delta T \approx 0.1$ K, up to $T_{max} \approx 80$ K. We also obtained field-cooled (fc) curves, which provide the reversible (equilibrium) magnetization. The background magnetization due to the normal state contribution was determined and removed for each data set by fitting to the form $M_b = b(H)/T + a(H)$ in a temperature window well above T_c .

III. RESULTS AND DISCUSSION

Figures 1(a) and 2(a) show zfc magnetization curves as obtained for each sample after background removal. Insets of Figs. 1(a) and 2(a) show details of selected field-cooled and zero-field-cooled magnetization curves as obtained in a wider temperature range, and illustrate the background removal procedure used in all curves. We observe that the background removal for sample with $T_c = 32$ K is paramagnetic from 100 Oe up to 10 kOe. The paramagnetic signal increases with field up to 1 kOe. Above 1 kOe a field increasing diamagnetic signal suppresses the paramagnetic one, which results in an overall diamagnetic signal for fields higher than 17 kOe. The origin of this effect is unknown. The trend observed for this sample (for the magnetization of the normal state) for fields higher than 10 kOe is similar to the trend observed in YBaCuO and other cuprates. On the other hand, the sample with $T_c = 28$ K has a paramagnetic background signal which increases with field, as in Pauli paramagnetism. The hump appearing in the field-cooled curves just below the irreversible temperature, T_{irr} , of each curve in the insets of Figs. 1(a) and 2(a) was observed for all curves, even for low values of the applied magnetic field.

The reversible magnetization in each curve of Figs. 1(a) and 2(a) corresponds to a region where M approaches zero with a low slope (see arrows marking the position of T_{irr} for $H = 50$ kOe). This fact is better exemplified in Figs. 1(b) and 2(b) where selected curves obtained for fields higher than 40 kOe show a rather large reversible region with a well-defined rounding effect as M approaches zero. In contrast to that, the insets of Figs. 1(b) and 2(b) and Figs. 3(a) and 3(b) show curves obtained with lower fields ($H < 20$ kOe), where the reversible region approaches zero linearly, as expected in a second-order phase transition. It is possible to see on the low field curves presented in Figs. 3(a) and 3(b) that the linear reversible region clearly defines $T_c(H)$. Insets of Figs. 3(a) and 3(b) show details of the zfc low field curves. The results

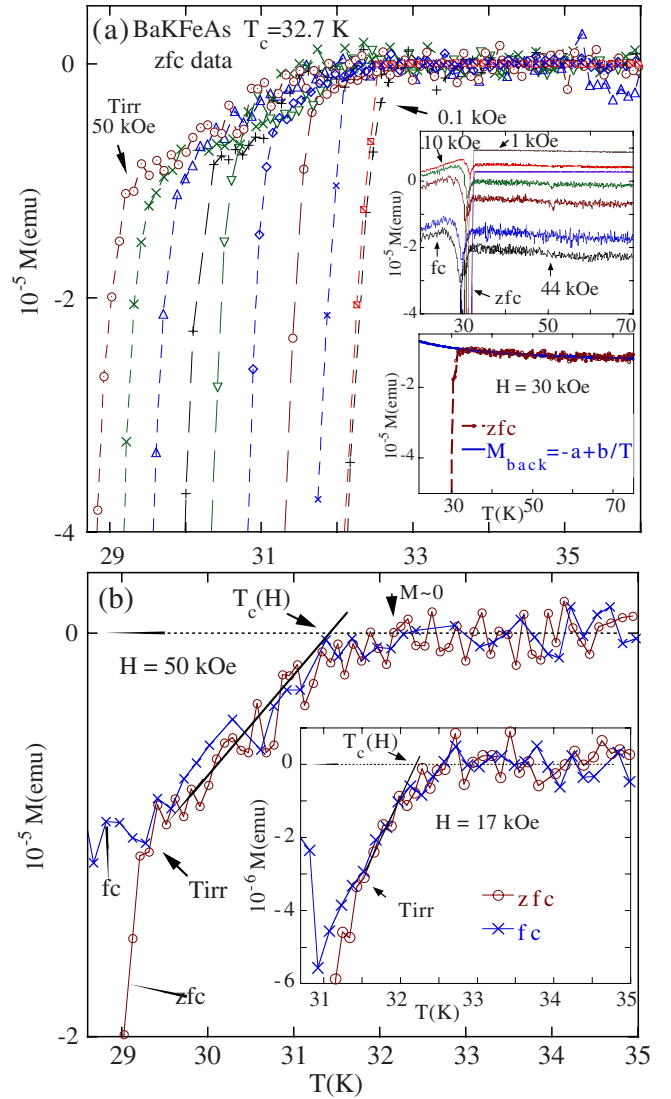


FIG. 1. (Color online) Isofield M vs T curves for sample with $T_c = 32.7$ K. (a) zfc curves for $H = 0.1, 0.5, 5, 10, 17, 24, 30, 37, 44,$ and 50 kOe. Top inset show zfc-fc curves for (top to bottom) $1, 10, 0.1, 17, 24, 37,$ and 44 kOe; low inset show detail of the background removal. (b) Detail of reversible region for $H = 50$ kOe. Inset: detail of reversible region for $H = 17$ kOe.

of Figs. 1(b) and 2(b) and the respective insets also exemplify the linear extrapolation of the reversible magnetization⁴⁴ used to estimate the mean-field value of $T_c(H)$ in each curve. It is possible to visualize on the curves of Figs. 1(b) and 2(b) (marked by arrows) that the magnetization reaches zero for temperatures ~ 1 and ~ 3 K above $T_c(H)$, respectively. This rounding effect masking the second-order phase transition was observed in all curves obtained for fields above 20 kOe, and it is more pronounced in the sample with $T_c = 28$ K. This rounding is reminiscent of high-field diamagnetic fluctuations observed in high- T_c superconductors which have been extensively studied.^{20–22,38,39} It should be mentioned that a similar but less pronounced rounding effect have also been observed in Nb with $\kappa = 4$,²⁶ which is a well known BCS superconductor. It is important to mention that, since the rounding effect in the higher field

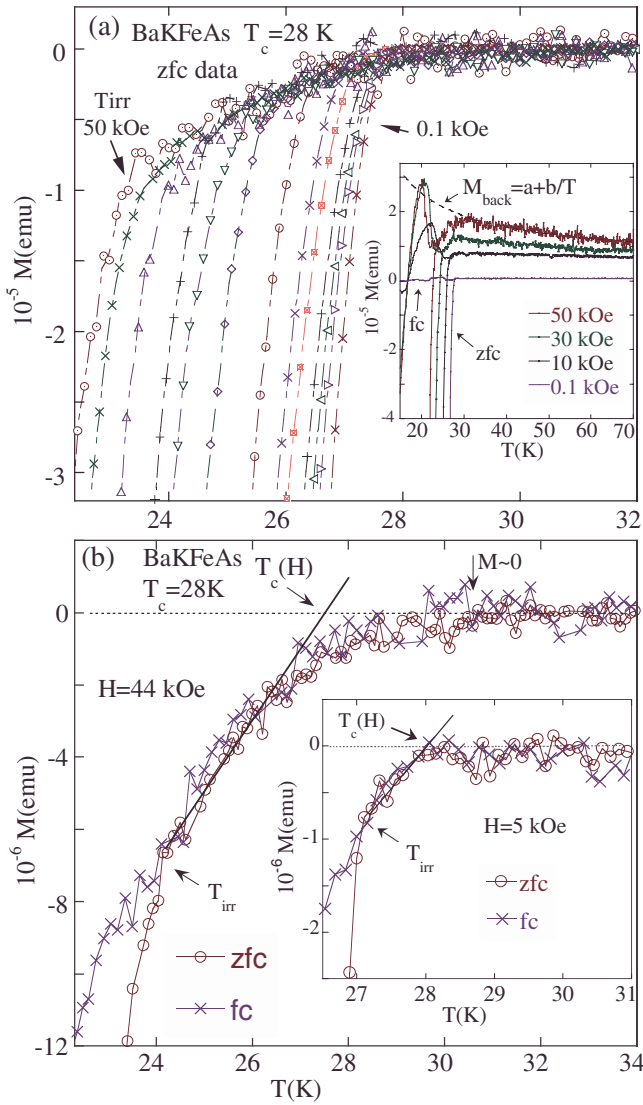


FIG. 2. (Color online) Isofield M vs T curves for sample with $T_c = 28$ K. (a) zfc curves for $H = 0.1, 0.3, 0.5, 1, 3, 5, 10, 17, 24, 30, 37, 44,$ and 50 kOe. Insets: zfc-fc curves and background removal. (b) Detail of reversible region for $H = 50$ kOe. Inset: detail of reversible region for $H = 5$ kOe.

curves extends above T_c which is defined here at the onset of diamagnetic signal, we discard the possibility of the rounding effect to be influenced by sample inhomogeneity. Also, the existence of any sample inhomogeneity is expected to produce a clear rounding in the reversible magnetization curves near the transition of low field curves, which is not observed in the reversible magnetization of the low field curves presented in Figs. 3(a) and 3(b).

In the present investigation, we perform a scaling analysis of the magnetization curves using the results obtained in Ref. 22 for a layered material which consider fluctuations-fluctuations interactions within the Ginzburg-Landau formalism. These authors²² obtained expressions for two-dimensional (2D) and three-dimensional (3D) critical fluctuations with the approximation that the magnetic field is high enough for all carriers to lie in the lowest Landau level (LLL). To perform the scaling we replace the temperature x

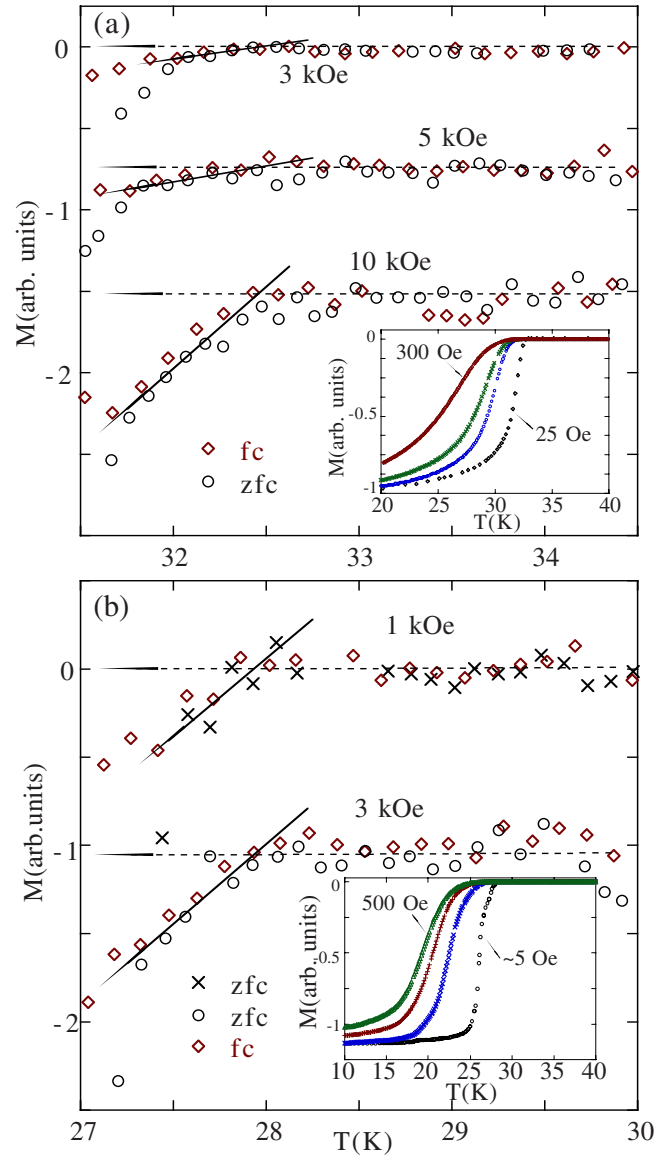


FIG. 3. (Color online) Selected low field M vs T curves showing detail of the reversible region. (a) zfc-fc curves for sample with $T_c = 32.7$ K. (b) zfc-fc curves for sample with $T_c = 28$ K. The curves were shifted vertically for clarity. Insets: zfc curves for lower fields. The lowest field curve in the inset of Fig. 3(b) was obtained with an ac field of 1 Oe at 1 kHz in the presence of a ~ 5 Oe remnant field of the magnet.

axis and magnetization y axis of each curve to the respective scaling forms $[T - T_c(H)] / (TH)^{(D-1)/D}$ and $M / (TH)^{(D-1)/D}$ where D is the dimensionality, and plot together all scaled curves. The only free parameter in the scaling procedure is the mean-field temperature $T_c(H)$ which is adjusted for each curve so that all results fall in a single universal curve.

Based on the low anisotropy of the BaKFeAs system we expect that fluctuations are of three-dimensional nature. However, since spin density waves, and superconductivity may coexist in this system for certain values of doping^{13,15,32} and two-dimensional magnetic fluctuations have been recently observed above T_c (Ref. 9) we also performed a two-dimensional scaling analysis. Figures 4(a) and 4(b) show the

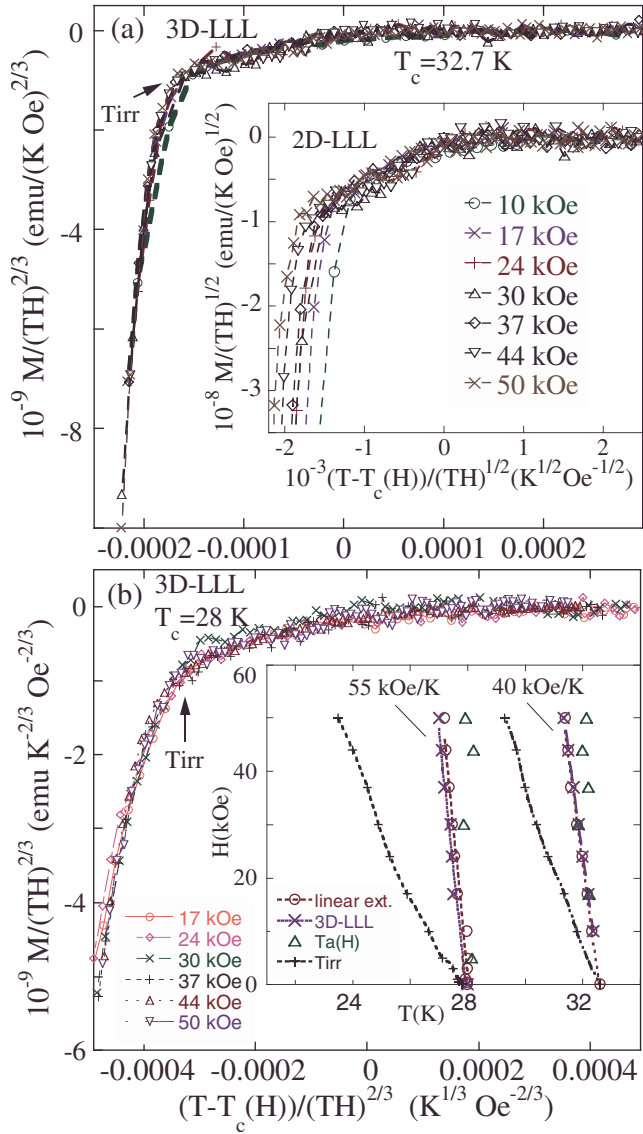


FIG. 4. (Color online) Collapse of magnetization curves presented in Figs. 1(a) and 2(a) for $H > 10$ kOe after the 3D-LLL scaling. (a) Sample with $T_c = 32.7$ K. Inset: 2D-LLL scaling of the same data. (b) Sample with $T_c = 28$ K. Inset: phase diagram of the studied samples.

results of the scaling for $D=3$ for both samples. Results for fields lower than 17 kOe fail to collapse in the single curve. The values of $T_c(H)$ obtained from the scaling analysis are in strictly good agreement with values obtained from the linear extrapolation of the reversible magnetization (see Fig. 3). It should be observed that not only the reversible magnetization follows the scaling and collapses into a single curve but also a portion of the irreversible region lying below the arrow marking the position of T_{irr} . The inset of Fig. 4(a) shows the results of the two-dimensional scaling using values of $T_c(H)$ obtained from the linear extrapolation procedure. A similar result, not shown, was obtained for the other sample. Even a simple visual comparison between Fig. 4(a) and its inset unambiguously confirms that the fluctuations are of three-dimensional nature. Although it is possible to obtain a good collapsing curve with the two-dimensional scaling, the

resulting $T_c(H)$ values are more than 1 K lower than the values obtained from the linear extrapolation which is physically meaningless.

To better quantify the dimensionality of the BaKFeAs system, we estimate the value of the parameter¹⁹ $r = 8(m/M)[\varsigma_{GL}(0)/(\pi s)]^2$ for our samples, where m and M are the effective mass of the quasiparticles along the layers plane and perpendicular to the layers respectively, $\varsigma_{GL}(0)^2 = \phi_0/(2\pi T_c |dH_{c2}/dT|)$ is the Ginzburg-Landau coherence length at $T=0$, ϕ_0 is the quantum flux, and $s \sim 13$ Å (Refs. 30 and 31) is the c -axis lattice constant of the system. The parameter r , first defined in Ref. 16, carries important information about the dimensionality of the system. It is worth mentioning that the above expression for r defined in Ref. 19 was obtained for a layered system with the magnetic field applied perpendicular to the layers, and coincides with the expression for r defined by Klemm *et al.*¹⁶ for systems in the dirty limit when calculated at $T=T_c$. The calculated values are: $r=0.11$ for the crystal with $T_c=28$ K where we used $|dH_{c2}/dT|=55$ kOe/K, $\sqrt{M/m}=3$ and $\varsigma_{GL}(0)=14.6$ Å, and $r=0.13$ for the crystal with $T_c=32$ K where we used $|dH_{c2}/dT|=40$ kOe/K, $\sqrt{M/m}=\gamma=3$, and $\varsigma_{GL}(0)=15.9$ Å. A plot of the reduced field $H/H_{c2}(0)$ vs r is presented in Fig. 9 of Ref. 16, which helps to identify the dimensionality behavior of fluctuations in a given system when the value of r is known, and also predicts if this system can exhibit a field-induced-dimensionality crossover (3D toward 2D) in the vicinity of T_c . For our samples with $r \sim 0.1$, a $D=3$ is expected, which agrees with the 3D-LLL scaling analysis results, but a dimensionality crossover (3D to 2D) is predicted to occur for fields higher than $0.5H_{c2}(0)$. Since the system has an anisotropy parameter lying between 2 and 3, we also calculate the value of r for $\sqrt{M/m}=2$, which produced $r \sim 0.3$ for both samples, corresponding to a dimensionality $D=3$ with no predicted dimensionality crossover induced by field. Values of $T_c(H)$ obtained for both samples from the linear extrapolation of the reversible magnetization and from the 3D-LLL scaling are plotted with values of T_{irr} and shown in the inset of Fig. 4(b). The resulting values of dH_{c2}/dT for each sample are shown in this figure and are in reasonable agreement with values presented in the literature.^{7,31}

Finally, we perform an analysis of the asymptotic behavior of the order parameter amplitude near the onset of superconductivity. The approach used is based on the conventional theory of the upper critical field H_{c2} ,⁴⁴ where the magnetic induction B obtained from the Ginzburg-Landau equation can be expressed as⁴⁵

$$B = H - \frac{4\pi e\hbar}{mc} |\psi|^2, \quad (1)$$

where ψ is the superconducting order parameter. The magnetization $M = (B-H)/4\pi$ is then given by

$$M = -\frac{e\hbar}{mc} |\psi|^2. \quad (2)$$

Within the Abrikosov approximation,⁴⁴ it follows that \sqrt{M} is directly proportional to the average amplitude of the order

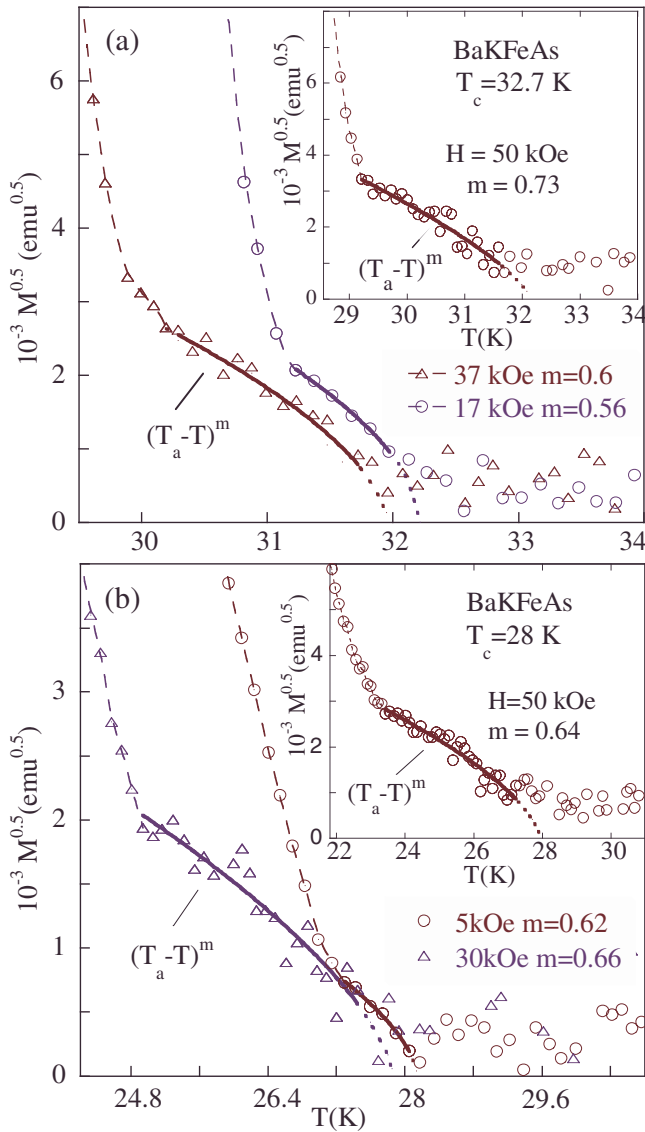


FIG. 5. (Color online) Selected isofield curves of \sqrt{M} vs T where M is the reversible magnetization. (a) Sample with $T_c = 32.7$ K. Inset: curve for $H = 50$ kOe. (b) sample with $T_c = 28$ K. Inset: curve for $H = 50$ kOe.

parameter. For the magnetization data, the above equation is valid for the entire reversible region, where we applied the linear extrapolation method to estimate $T_c(H)$. Near the superconducting transition the temperature dependence of the magnetization can be expressed as $\sqrt{M} \propto [T_c(H) - T]^m$, in terms of the mean-field transition temperature $T_c(H)$. The mean-field exponent is given by $m = 1/2$ for a s -wave BCS superconductor.⁴⁵ This analysis can infer the existence of phase fluctuations in the order parameter.^{23,29}

Figure 5(a) and 5(b) and their insets show selected curves of \sqrt{M} vs T where it is possible to see that the asymptotic behavior of the reversible region is quite distinct, showing the shape of the gap (opening) in the vicinity of $T_c(H)$. This clearly indicates the region (temperature window) where the analysis should be performed. The solid lines represent the fitting of the selected data to a form $\sqrt{M} \propto [T_a(H) - T]^m$, where $T_a(H)$ denotes the apparent transition temperature, and

m is the fitting exponent. Resulting values of $T_a(H)$ are plotted in the inset of Fig. 4(b). It should be mentioned that the values of $T_a(H)$ do not follow the trend suggested in the main figures, with $dT_a(H)/dH < 0$ as followed by $T_c(H)$. The latter is exemplified by the curves shown in each inset, where the value of $T_a(H)$ for a higher field curve is little higher than the value for a lower field. This prevented all analyzed data to be shown in one figure, since the curves intercept each other. Results of these analysis show that values of $T_a(H)$ (dotted lines show extrapolation of the fittings to $T_a(H)$) are slightly larger than values of $T_c(H)$ as well values of the exponent m are larger than the expected value $1/2$. These deviations might be associated to the spread of the data, but we also note that values of m are consistently larger than $1/2$ and increases with field for both samples, which might be not casual but an effect of phase fluctuations. This can be due to the existence of nodes in the order parameter of this system. It is shown in Ref. 23 that phase fluctuations play an important role when the order parameter has a node, with an overall effect that reduces the density of states changing the shape of the gap in the vicinity of T_c . As a result, the value of the exponent m increases above the expected value $1/2$ (Ref. 29) as observed here. Within this scenario, $T_a(H)$ represents the onset of phase coherence, which occurs a little above the mean field temperatures $T_c(H)$. Since magnetic field enhances fluctuations effects in layered systems²⁰ the exponent m is expected to increase with field, as observed. It should be mentioned that the existence of nodes in the order parameter would produce an angular anisotropy in Arpes measurements which was not observed in Refs. 11 and 12. On the other hand the authors of Ref. 37 developed an extended s -wave fully gaped theory for iron pnictides with unconventional pairing which shows that the above mentioned angular anisotropy of the gap due to nodes would not be observed in the case that the gap change sign between the different Fermi surfaces. More recently a theoretical work also developed assuming unconventional pairing for these systems explains why nodes appears in some experiments and do not in others.⁴⁶

As a final remark it is important to notice that all curves of Figs. 5(a) and 5(b) clearly show a gap closing at $T_a(H) \approx T_c(H)$ which suggests that our results follow the behavior expected for a conventional multiband s -wave symmetry superconductor.^{35,36,47} On the other hand, since we observe a value of the exponent m larger than $1/2$ which might be related to the existence of nodes in the gap, the possibility that the pairing is unconventional as proposed in Refs. 37 and 34 cannot be discarded.

In conclusion, we observe three-dimensional fluctuations magnetization of the lowest-Landau-level type in $Ba_{1-x}K_xFe_2As_2$ in a temperature window exceeding 3 K above $T_c(H)$. Analysis of the reversible magnetization allowed a study of the asymptotic behavior of the gap near $T_c(H)$. Results of the analysis produced values for the exponent m larger than $1/2$ suggesting that phase fluctuations are important near T_c in $Ba_{1-x}K_xFe_2As_2$ which is consistent with nodes in the gap.

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