# **First-principles simulations of copper diffusion in tantalum and tantalum nitride**

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To explore potential applications of tantalum and tantalum nitrides (TaN) as diffusion barrier materials in integrated circuits with Cu interconnects, we carry out detailed first-principles simulations of Cu/Ta and Cu/TaN systems. Various interfacial structures between Cu- and Ta-based compounds are examined by considering different surface orientations, in-plane arrangements, surface terminations, and chemical compositions. The coexistence of strong Cu-N ionic bonding and Ta-Cu covalent/metallic bonding dictates the stable interfacial structures. Using nudged elastic band method, we calculate the diffusion energy barriers of Cu to the pre-existing vacancies across Cu/Ta, Cu/TaN interfaces, and in bulk TaN compounds. As a comparison, Cu diffusion in Si is also studied. It was found that Cu can easily diffuse into Si either spontaneously or with small energy barriers. On the other hand, although the Cu/Ta interfacial diffusion barrier is low, the high vacancy formation energy in Ta renders Cu diffusion difficult. We find that fcc TaN is an excellent candidate for diffusion barrier material owing to its extremely high interfacial diffusion energy barrier. The bulk diffusion barrier of Cu in fcc TaN is also very high.

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### **I. INTRODUCTION**

Copper (Cu) has been widely accepted as an attractive material for interconnects in ultralarge-scale integrated (ULSI) circuits owing to its excellent electrical conductance and higher resistance to electromigration compared to Al and Al alloys. However, it is also well known that Cu atoms diffuse quickly into Si substrate and  $SiO<sub>2</sub>$  dielectric, which causes degradation of transistor reliability by forming impurity levels in the band structure, detrimental to the electrical properties of the transistor.<sup>1</sup> Therefore the integration of an effective diffusion barrier layer between Cu and Si substrates to prevent the interdiffusion and reaction becomes crucially important for the ULSI devices. $2-4$ 

Many materials have been considered as diffusion barriers in Cu metallization systems, including refractory metals and their nitrides. Among them, tantalum (Ta) and tantalum nitrides (TaN) have received the most attentions owing to their high thermal stability and resistance to form compounds with  $Cu<sup>3</sup>$  TaN system including Ta, Ta<sub>2</sub>N, and TaN have been selected as the diffusion barrier layers in experimental studies, and thus they are the focus of the present theoretical effort. On the experimental side, research is mostly concentrated on the growth of TaN thin films, the characterization of fabricated structures, and the annealing test of barrier effectiveness.<sup>5[–14](#page-8-5)</sup> It has been shown that the presence of N in TaN compounds enhances the resistivity to diffusions $6,7$  $6,7$  and the stacking of TaN compounds on Ta layers $11$  improves the performance of the barrier materials. However the relationship between the barrier efficiency and material structure has not been established. On the theoretical side, research has focused on bulk properties<sup>15</sup> and electronic structures of TaN compounds, $16-18$  the thermal stability of Cu/TaN/Si stacking structures, $19$  and statistical modeling of atomic diffusions.<sup>20</sup> However, the crucial issues such as why and how TaN compounds work as diffusion barrier materials are still not well understood. Here we present comprehensive first-principles study to understand the atomistic mechanism of Cu diffusion into TaN compounds and Si substrates.

In Sec. [II,](#page-0-0) we present the structural models and computational method for the relevant interfaces. The results are prePACS number(s): 68.35.Fx, 71.20.Be, 31.15.A-

sented and discussed in Sec. [III.](#page-2-0) The bulk properties of Ta and TaN compounds<sup>5-[7,](#page-8-7)[10](#page-8-14)-14</sup> are presented in Sec. [III A](#page-2-1) while the interfacial properties of Cu/TaN system are included in Sec. [III B.](#page-2-2) The interfacial and bulk diffusion barriers are calculated in Sec. [III C,](#page-4-0) followed by a summary in Sec. [IV.](#page-7-0)

# **II. CRYSTAL STRUCTURE AND COMPUTATIONAL METHOD**

<span id="page-0-0"></span>Four types of TaN crystalline structures are considered as candidates of diffusion barrier materials: bcc Ta,  $\delta$ -TaN with fcc structure, hexagonal  $\epsilon$ -TaN, and hexagonal Ta<sub>2</sub>N, shown in Fig. [1.](#page-0-1) Other relevant materials, such as  $\beta$ -Ta are not included in the present study because they are not thermodynamically stable. However, these materials may also be used as diffusion barriers under special conditions. $^{21}$  For each of them, Cu/barrier material interfaces are constructed by depositing Cu thin layers on top of the barrier substrates. The

<span id="page-0-1"></span>

FIG. 1. (Color online) Crystal structure of Ta, TaN compounds, and Cu: (a) bcc Ta, (b) fcc TaN, (c) hexagonal TaN, (d) hexagonal Ta<sub>2</sub>N, and (e) fcc Cu, and relevant orientations.  $\gamma$  is the angle between two horizontal axis.

detailed interfacial structures will be discussed in Sec. [III B.](#page-2-2)

Ultrathin Cu films deposited on bcc Ta (111) have been studied recently.<sup>22–[26](#page-8-17)</sup> It is generally believed that Cu grows on Ta (110) substrate in a layer-by-layer mode for a small number of monolayers and then switches to a threedimensional (3D) growth model. The relation between the number of stable Cu monolayers and the instability point is unclear. It is clear however from both experimental and theoretical results that Cu forms stable pseudomorphic films on top of Ta, i.e., films which have the same structure as the Ta substrate.<sup>21[,23](#page-8-18)</sup> Since 3D simulations of Cu islands or droplets on Ta based on first-principles are not feasible computationally, we focus on the pseudomorphic thin-film mode in this study. This is a reasonable approximation because the interfacial diffusions are highly localized, taking place near the interface. Monolayer of Cu is not a good choice for the diffusion barrier calculations because it introduces artificial Cu surface which is not present in reality. On the other hand, a pseudomorphic thin film with too many Cu monolayers is not realistic either because only a very small number of Cu layers are observed to be stable on Ta. Therefore, we decide to include three Cu  $(111)$  layers on top of Ta  $(110)$  substrate in the interfacial diffusion calculations. fcc TaN was reported to be a metastable structure<sup>16,[27](#page-8-19)</sup> but it is believed to be the most effective diffusion barrier material among all TaN compounds[.27](#page-8-19) The surface orientation of fcc TaN differs depending on the methods of fabrication; $^{28}$  it is reported however that the densely packed (111) orientation is considered the most effective orientation for barrier materials. The Cu/ fcc-TaN interface structures remain unclear experimentally except that Cu (111) has been reported as preferred orientation on fcc-TaN substrate. $8-14,27,28$  $8-14,27,28$  $8-14,27,28$  Therefore, we will study Cu (111)/fcc-TaN (111) interfaces by including three Cu (111) layers on top of TaN (111) substrate in the firstprinciples calculations[.29](#page-8-22)[–32](#page-8-23)

All calculations in this paper are carried out based on first-principles density-functional theory (DFT) with planewave basis and the projector augmented-wave method as implemented in the Vienna *Ab initio* Simulation Package. Nonrelativistic ultrasoft pseudopotential $^{33}$  and the generalized gradient approximation $34$  are used in the calculations. The energy cutoff of Ta, TaN compounds, Cu, and Si is 175, 348, 234, and 151 eV, respectively. The Fermi-Dirac smearing is used for all cases except for bulk calculations where the tetrahedron method is employed instead; the smearing energy is 0.2 eV throughout. For bulk calculations of bcc Ta, fcc TaN and Si, and hexagonal TaN and hexagonal Ta<sub>2</sub>N, the Monkhorst-Pack meshes of  $15 \times 15 \times 15$ ,  $11 \times 11 \times 15$ , and  $15 \times 15 \times 11$  are used, respectively.

The adhesive strength of the Cu/substrate interfaces are evaluated with the interfacial cohesive energy  $\gamma_c$  defined as the work per unit area that is required to separate the Cu/ substrate interfaces into isolated Cu layers and the substrate

$$
\gamma_c = \frac{E_{\text{int}} - E_{\infty}}{A}.\tag{1}
$$

Here  $E_{\text{int}}$  is the total energy of the Cu/substrate combined system, and  $E_{\infty}$  is the total energy when Cu and the substrate are separated to infinity. *A* is the area of the interface in the computational unit cell.

The *k*-point mesh of  $11 \times 11 \times 1$  is used for the interfacial calculations of Cu/fcc Ta, Cu/hexagonal Ta<sub>2</sub>N, and Cu/bcc Ta;  $8 \times 8 \times 1$  mesh is used for Cu/hexagonal TaN. The strain energy of Cu on the substrates is calculated separately by using a laterally strained unit cell.

The cohesive energy of the elemental bulk system is evaluated by subtracting the atomic energy from the total energy of the crystal. The atomic energy is calculated by using a large unit cell of 20 Å with spin-polarization corrections. The cohesive energy of TaN compounds is determined by subtracting the chemical potential of Ta and N atoms from the total energy. The chemical potential of Ta and N is determined with respect to bcc-Ta and free  $N_2$  molecules, respectively.

The vacancy formation energy  $(E_f)$  is calculated for various materials. For the elemental materials,  $E_f$  is defined as

$$
E_f = E_{n-1} - \frac{(n-1)}{n} E_n,
$$
 (2)

where  $E_n$  is the energy of the perfect bulk with *n* atoms in the unit cell, and  $E_{n-1}$  is the energy of this system with a vacancy. For binary compounds, the formation energy of Ta and N vacancies,  $E_f^{\text{Ta}}$  and  $E_f^{\text{N}}$ , can be calculated by

$$
\begin{cases}\nE_f^{\text{Ta}} = E_{n-1}^{\text{Ta-vac}} - E_n + \mu^{\text{Ta}}, \\
E_f^{\text{N}} = E_{n-1}^{\text{N-vac}} - E_n + \mu^{\text{N}},\n\end{cases} \tag{3}
$$

where  $\mu^{Ta}$  and  $\mu^{N}$  are chemical potentials of Ta and N in the TaN compound,  $E_n$  is the energy of perfect bulk system with *n* atoms, and  $E_{n-1}^{\text{Ta-vac}}$  and  $E_{n-1}^{\text{N-vac}}$  are the energy of the bulk system with a Ta or N vacancy, respectively. Unfortunately, the chemical potential of Ta or N atom is not well defined depending on the chemical environment of the atom. However, the chemical potentials should satisfy the following equation:

$$
x\mu^{\text{Ta}} + y\mu^{\text{N}} = E_n. \tag{4}
$$

*x* and *y* are the number of Ta and N atoms in the unit cell of the perfect bulk lattice with  $x+y=n$ . With this equation, we can estimate the range of the chemical potentials based on the fact that the chemical potential of each species should be lower than that of their corresponding elemental phase otherwise the elemental phase is preferred over the binary compound. Taking the chemical potential of Ta to that of bcc Ta and the chemical potential of N to that of free  $N_2$  molecule, we can estimate the range of *Ef*.

The interfacial diffusion barriers are calculated by displacing a Cu atom to a pre-existing vacancy across the interface. The minimum-energy path and the corresponding energy barrier are determined by using the nudged elastic band (NEB) method. The bulk diffusion barriers are also calculated similarly by moving a Cu atom to a pre-existing bulk vacancy along different directions.

In NEB calculations, the spring constant is 5  $eV/\text{\AA}^2$  and the images are optimized using the quasi-Newton method.  $4 \times 8 \times 1$  and  $6 \times 6 \times 1$  *k*-point meshes are used in the calculations of Cu/TaN and Cu/Si interfaces, respectively. The

TABLE I. Lattice constant  $(\overline{A})$  and cohesive energy  $E_c$  (eV/ atom) of various materials.

<span id="page-2-3"></span>

Structure	Lattice constant	$E_c$ (this work) $E_c$ (reference)	
fcc Cu	3.644	$-3.53$	$-3.49$ <sup>a</sup>
Diamond Si	5.458	$-4.64$	$-4.63$ <sup>a</sup>
bcc Ta	3.298	$-8.30$	$-8.10$ <sup>a</sup>
fcc TaN	4.406	$-1.00$	$-1.305^{\rm b}$
Hex TaN	$a=5.238$ $c=2.913$	$-0.82$	$-1.117^b$
Hex $Ta_2N$	$a=3.099$ $c=4.852$	$-0.88$	$-1.086b$

a From Ref. [35.](#page-8-26)

<sup>b</sup>From Ref. [16.](#page-8-10)

bulk diffusion calculations are carried out with  $4 \times 4 \times 4$  *k* mesh except for diffusion along [111] direction in fcc TaN in which a  $4 \times 6 \times 6$  mesh is used.

## **III. RESULT AND DISCUSSION**

<span id="page-2-0"></span>Four factors are taken into consideration for constructing Cu/substrate interface models: (a) crystalline structure of the substrates, (b) relative orientation of the substrates, (c) terminating layer of the substrates, and (d) in-plane arrangement at the interface. The optimal interfacial structure is determined by exploring the combination of the four factors with the lowest interfacial cohesive energy. Having obtained the optimal interfacial structures, we can carry out relevant diffusion barrier calculations.

#### **A. Bulk properties**

<span id="page-2-1"></span>In this paper, we focus on bcc Ta and three types of TaN compounds, including fcc  $\delta$ -TaN, hexagonal (hex-)  $\epsilon$ -TaN, and hexagonal (hex-) Ta<sub>2</sub>N; they have one Ta atom, one Ta and one N atom, three Ta and three N atoms, and two Ta and one N atoms per unit cell, respectively, shown in Fig. [1.](#page-0-1) The results of their bulk properties are summarized in Table [I,](#page-2-3) which also includes the bulk properties of Si and Cu.

The bulk properties of Cu, Si, and Ta agree well with the experimental data.<sup>35</sup> The difference in cohesive energy of TaN compounds compared to that of Stampfl and Freeman<sup>16</sup> may be due to the difference in chemical potential of N between our result and that of Stampfl (there is no report of N chemical potential in Ref.  $16$ ). If the chemical potential of N in our calculation is shifted by 0.6 eV, the cohesive energy of fcc TaN, hexagonal TaN, and hexagonal  $Ta_2N$  becomes −1.30, −1.13, and −1.08 eV, respectively, which agree well with Stampfl and Freeman.<sup>16</sup>

#### **B. Interfacial structures**

<span id="page-2-2"></span>In this work, we take the experimentally observed orientations of Cu/barrier interface: Cu (111) layers on top of (111) surface of fcc TaN,<sup>8-14</sup> (110) surface of bcc Ta,<sup>9[,10](#page-8-14)[,14](#page-8-5)</sup> (001) surface of hexagonal  $Ta_2N$ ,<sup>[5](#page-8-4)</sup> and (001) surface of hexagonal TaN. The interfacial cohesive energy is calculated as a function of terminating surface and in-plane arrangement for each of the substrates. First, we determine the lattice

<span id="page-2-4"></span>TABLE II. Lattice parameters and strain energy per atom *E* (eV) of the substrates. The strain is due to the mismatch between Cu  $(111)$  surface and the surface of the various substrates listed in the table.

Substrate	$\mathfrak a$ $\rm (\AA)$	$\mathcal C$ (Ă)	$\gamma$ (°)	$\Delta E$
Unstrained	2.58	6.31	60.0	
fcc TaN $(111)$	3.11	5.17	60.0	0.33
bcc Ta $(110)$	2.86	5.54	70.5	0.26
Hex TaN $(001)$	2.62	6.23	60.0	0.01
Hex Ta <sub>2</sub> N $(001)$	3.10	5.21	60.0	0.33
Si(100)	3.86	3.31	90.0	0.04
Si(111)	2.23	6.99	60.0	0.68

parameters and cohesive energy of strained Cu lattice and the results are summarized in Table [II.](#page-2-4)

The interfacial structure is constructed by placing a threelayer Cu slab on top of a six-layer of substrate slab, with a separation of 2 Å in between. A 30 Å vacuum is included to separate the periodic images along the surface-normal direction. To calculate  $E_{\text{int}}$ , the last two layers of the substrate are fixed while the rest of the system is allowed to relax until the energy difference between two consecutive configurations is less than  $10^{-4}$  eV.  $E_{\infty}$  is obtained by separating the Cu slab and the substrate of 15 Å, and then relaxing the structure. Convergence test including 12 layers of substrate yields an interfacial cohesive energy that is only  $0.05$  J/m<sup>2</sup> from the much smaller model. The good agreement between the two different choices of supercell suggests that interfacial cohesion is short ranged and primarily localized at the interface. The schematic diagrams of interfacial structure and the calculated cohesive energy are shown in Fig. [2.](#page-3-0)

## *1. Cu/fcc-TaN interface*

The pseudomorphic interface is constructed by straining the two-dimensional (2D) unit cell of Cu (111) surface to match the 2D unit cell of fcc-TaN (111) surface, with Cu  $\lceil 110 \rceil$  direction parallel to fcc-TaN  $\lceil 110 \rceil$  direction. Five inplane arrangements are examined, in which Cu atoms sit on various symmetric sites above the substrate:  $(1)$  top sites,  $(2)$ fcc sites,  $(3)$  hcp sites,  $(4)$  half way between the top and fcc sites, and  $(5)$  bridge sites, summarized in Fig.  $2(a)$  $2(a)$ . For each of the in-plane arrangement, two types of surface termination of TaN are considered: Ta and N termination. It is found that Cu atoms prefer to sit at the threefold fcc and hcp sites above Ta atoms and on top of N atoms (Fig. [2](#page-3-0)). The interfacial bond length of Ta-Cu and TaN is 2.72 and 1.93 Å, respectively. To understand the nature of interfacial cohesion, we plot the bonding charge density  $\rho_b(\mathbf{r})$ , defined as

$$
\rho_b(\mathbf{r}) = \rho_{\text{solid}}(\mathbf{r}) - \sum_{i} \rho_{\text{at}}(\mathbf{r} - \mathbf{R}_i),
$$
\n(5)

in Fig. [3.](#page-3-1) Here  $\rho_{\text{solid}}$  is the solid charge density of the system and  $\rho_{at}(\mathbf{r})$  is the atomic charge density centered at atom *i*, whose position is given by  $\mathbf{R}_i$ . The density of states (DOS) of interfacial atoms is shown in Fig. [3.](#page-3-1) For Ta-terminating sur-

<span id="page-3-0"></span>

FIG. 2. (Color online) Schematic of interfacial structure and the corresponding interfacial cohesive energy, from top to bottom: (a) Cu (111)/fcc TaN (111) with Ta termination, Cu (111)/fcc TaN (111) with N termination, (b) Cu  $(111)$ /bcc Ta  $(110)$ , (c) Cu  $(111)$ /hex  $Ta_2N$  (001) with Ta termination, Cu (111)/hex  $Ta_2N$  (001) with N termination, (d)Cu (111)/hex TaN (001) with TaN termination, Cu  $(111)$ /hex-TaN  $(001)$  with Ta termination,  $(e)$ Cu  $(100)$ /Si  $(100)$ , and (f) Cu (111)/Si (111). Only one layer of Cu atoms and two layers of the substrates are shown. The size of the spheres is scaled so that the larger the spheres, the closer the atoms to the interface (the largest spheres represent the atoms at the interface). The Cu spheres are scaled down to allow the substrate visible. The orientation of each interface is also shown in the figure. The interfacial cohesive energy  $(J/m^2)$  is labeled under each atomic configuration, with the lowest energy configuration for each substrate marked by an asterisk.

face, there is strong metallic bonding between a Cu atom and three neighboring Ta atoms. The metallic bonding across the interface, consisting of Cu 4*s* and Ta 6*s* states, is much stronger than the metallic bonding inside the Cu lattice. For N-terminating surface, strong ionic bonding is developed between Cu and N across the interface, with charge transferred from Cu to N. The ionic bonding between Cu and N is stronger than that between Ta and N. The bonding nature metallic vs ionic across the interface—dictates the stable interfacial structures.

<span id="page-3-1"></span>

FIG. 3. (Color online) Left, bonding charge density (in  $\AA^{-3}$ ) near the interface: from top to bottom, Cu/fcc TaN with Ta termination, Cu/fcc TaN with N termination, and Cu/bcc Ta. The atoms that are connected by a solid line are of interest, and their local DOS is shown on the right. The angular moment projected DOS is also shown.

# *2. Cu/bcc-Ta interface*

The 2D unit cell of Cu (111) surface is strained and placed on top of bcc-Ta (110) surface with Cu [112<sup>*j*</sup> direction parallel to Ta  $\lceil 1\overline{1}0 \rceil$  direction.<sup>23</sup> Because  $\lceil 001 \rceil$  and  $\lceil 1\overline{1}1 \rceil$  directions are no longer equivalent, one more type of bridge site has to be considered for the (110) surface of bcc Ta. There are five in-plane arrangements to be explored:  $(1)$  top sites, (2) threefold sites where Cu atoms sit at one third of the long diagonal of Ta  $(110)$  unit cell,  $(3)$  half way between  $(1)$  and  $(2)$ ,  $(4)$  bridge sites along  $[001]$  direction, and  $(5)$  bridge sites along  $[1\overline{1}1]$  direction [Fig. [2](#page-3-0)(b)]. We find that Cu atoms prefer the bridge sites above Ta atoms along  $[001]$  direction and the interfacial Ta-Cu bond length is 2.66 Å. This result agrees with that of Hashibon *et al.*[23](#page-8-18) The bonding charge density and density of states of the interface are presented in Fig. [3:](#page-3-1) the interfacial cohesion is primarily due to a mixture of covalent/metallic bonding between Cu 4*s* and Ta 6*s* states. These states are delocalized around the interface.

# *3. Cu/hex-***Ta2N** *interface*

The Cu (111) 2D unit cell is strained to fit the hexagonal Ta<sub>2</sub>N (001) 2D unit cell, with Cu [1<sup> $\overline{10}$ </sup>] direction parallel to

 $Ta_2N$  [100] direction.  $Ta_2N$  (001) surface is similar to fcc-TaN (111) surface—both of them have hexagonal unit cells with either Ta or N termination. The in-plane arrangements of the two interfaces are also similar as shown in Fig.  $2(c)$  $2(c)$ . It is found that Cu atoms prefer the top sites on N atoms and fcc sites above Ta. The Cu-Ta and Cu-N bond lengths are 2.65 and 1.94 Å, respectively.

### *4. Cu/hex-TaN interface*

The hexagonal TaN has a much larger unit cell so that 2  $\times$  2 Cu (111) 2D unit cell can be placed on top of each TaN  $(001)$  2D unit cell, with Cu  $\left[1\overline{1}0\right]$  direction parallel to TaN [100] direction. There are two types of termination of TaN (001) surface: TaN and Ta. Three in-plane arrangements are considered, in which Cu atoms sit on, referring to the TaN surface:  $(1)$  top sites,  $(2)$  threefold (including both fcc and hcp) sites, and (3) bridge sites, shown in Fig.  $2(d)$  $2(d)$ . We find that for TaN termination which has a 1:3 Ta to N ratio, Cu atoms prefer to sit on top of *both* Ta and N atoms (see Fig. [2](#page-3-0)). The interfacial Cu layer develops a zigzag structure due to the different bond length of Cu-Ta  $(2.35 \text{ Å})$  and Cu-N  $(1.98 \text{ Å})$ . For Ta termination, 3/4 of the interfacial Cu atoms sit on the bridge sites and 1/4 of the Cu atoms sit on top of exposed Ta atoms at the subsurface. The Cu-Ta bond length is 2.73 and 2.65 Å, respectively.

Based on above discussions, the in-plane arrangements of the Cu/TaN interfacial structures could be summarized as follows: for N-terminated surface, Cu atoms prefer to sit directly on top of N atoms to form strong ionic bonds; for Ta-terminated surface, Cu atoms take either the fcc or bridge sites to form a mixture of covalent and metallic bonds. In this case, the interfacial Cu layer maintains the lattice structure of the substrate—as an extension of the substrate. For the mixed surface termination, the in-plane arrangements follow the same rules with respect to the majority species of the surface atoms.

#### *5. Cu/Si interface*

It is known that Cu reacts with Si to form  $Cu<sub>3</sub>Si$  interme-tallic compound<sup>2[,36](#page-8-28)</sup> at the interface, rendering a complicated Cu/Si interfacial structure unattainable by first-principles calculations. Here, we focus on unreconstructed Cu/Si interfaces instead with two orientations: Cu (111)/Si (111) (Refs. [37](#page-8-29) and [38](#page-8-30)) and Cu (100)/Si (100) (Ref. [39](#page-8-31)); both of them have been examined experimentally. Our modest goal here is to determine the simplistic "perfect" interface for which Cu diffusion barriers can be extracted and compared to Cu/TaN system. Similar to the procedures outlined for TaN compounds, various in-plane arrangements are considered. The results show that the (111) interface has a much lower cohesive energy than the (100) interface, thus energetically more stable. Cu atoms prefer the bridge sites on Si (100) surface and a mixture of top, fcc, and hcp sites on Si (111) surface [Figs.  $2(e)$  $2(e)$  and  $2(f)$ ].

Because fcc-TaN and bcc-Ta substrates provide stronger adhesive power to Cu than other materials, they are potentially better candidates for diffusion barrier materials. In addition, much more experimental work on the two materials

<span id="page-4-1"></span>TABLE III. Vacancy formation energy  $E_f$  (eV) in bulk Cu, bulk diamond-Si, bcc-Ta, and fcc-TaN. For fcc-TaN, the range of  $E_f$  is presented, corresponding to N-rich and Ta-rich conditions. The number of atoms in the computational unit cell is also listed.

Material	Atoms per cell		$E_f$	$E_f$ in Refs.
fcc Cu	108	1.04		1.28 <sup>a</sup>
Diamond Si	64	3.66		$3.53^{b}$
bcc Ta	128	2.96		2.95 <sup>c</sup>
N vacancy in fcc TaN	64	0.84	$-1.15$	
Ta vacancy in fcc TaN	64	$-3.09$	$-1.10$	

<sup>a</sup> From Refs. [40](#page-8-33) and [41.](#page-8-34)

<sup>b</sup>From Ref. [42.](#page-8-35)

c From Refs. [41](#page-8-34) and [43.](#page-8-36)

have been reported, we therefore focus on fcc TaN and bcc Ta for diffusion barrier calculations in the next section.

#### **C. Cu diffusion barriers**

# *1. Vacancy formation energy*

<span id="page-4-0"></span>Due to the large size of Cu atoms, interfacial and bulk diffusions of Cu will normally involve vacancies—diffusion via interstitials is energetically highly unfavorable. We start by calculating vacancy formation energy for various materials and the results are summarized in Table [III.](#page-4-1) It is found that the vacancy formation energy of Si and Ta is very large—much larger than that in Cu, suggesting the necessity of pre-existing vacancies for diffusion in Si and Ta. As alluded before, the vacancy formation energy of TaN compounds depends on the chemical potential of each species. We estimate the range of the vacancy formation energy of the compounds by imposing the constraint<sup>44</sup> that the chemical potential of Ta and N in a TaN compound should not be greater than that in bcc-Ta and free  $N_2$  molecules. The extreme case of equality of the chemical potential in the elemental and the binary phase for one species indicates the rich condition of this element. Interestingly, the Ta-vacancy formation energy of in fcc TaN is always negative, ranging from  $-3.09$  (N rich) to  $-1.10$  eV (Ta rich), and N-vacancy formation energy in fcc TaN ranges from 0.84 (N rich) to −1.15 eV (Ta rich). The results suggest that vacancies are actually favored in fcc TaN, especially with Ta vacancy. The results agree with the finding of Stampfl and Freeman<sup>16</sup> that  $Ta_4N_5$ , which is an fcc structure with ordered Ta vacancies, is more stable than fcc TaN.

In the NEB calculations, the initial state is the interfacial structures determined in the previous section, with a vacancy introduced in the substrate across the interface. The final state involves the same interfacial structure but with the nearest-neighbor Cu atom displaced to the vacancy in the substrate, leaving behind a vacancy in Cu. Before proceeding to NEB calculations, both the initial and final states are relaxed by the conjugate-gradient method until the energy is converged to  $10^{-3}$  eV. The Cu top layer and the last two layers of the substrate are held fixed in the relaxation and NEB calculations. The bulk diffusion barriers are also calcu-

<span id="page-5-0"></span>

FIG. 4. (Color online) Cu/Si interfacial diffusions: (a) Cu  $(111)/Si$   $(111)$  interfacial structure with a diffusing Cu atom and a Si vacancy at the interface. The Cu atom diffuses into the Si vacancy spontaneously during the relaxation. (b) Cu (100)/Si (100) interfacial structure with a diffusing Cu atom and a Si vacancy at the interface. The Cu atom diffuses into the vacancy with 0.07 eV energy barrier. The energy profile for the diffusion is shown in (c). (d) Cu (100)/Si (100) interfacial structure with a diffusing Cu atom and a Si vacancy at one layer below the interface. The Cu atom diffuses into the vacancy with 0.73 eV energy barrier. The energy profile of the diffusion is shown in (e).

lated for Ta and TaN compounds in the similar manner: two or more adjacent vacancies are introduced in the bulk, and a Cu atom is placed at one of the vacancies as the initial state and at the adjacent vacancy as the final state.

## *2. Cu/Si interfacial diffusion*

For Cu (111)/Si (111) interface, periodic boundary conditions are applied along Si  $\lceil 110 \rceil$  and  $\lceil 112 \rceil$  directions. The supercell contains three Cu and eight Si layers in which there are 31 Si and 36 Cu atoms; a vacuum slab of 15 Å is included. A Si vacancy is introduced right below a Cu atom [see Fig.  $4(a)$  $4(a)$ ]. We find that, after the relaxation of the initial state, the Cu atom moves to the Si vacancy *spontaneously* with no energy barrier for diffusion. This result is consistent with the fact that Cu and Si react easily at the interface.<sup>2</sup>

For Cu (100)/Si (100) interface, the interface plane has a  $2 \times 2$  unit cell along Si  $\lceil 0\bar{1}1 \rceil$  and  $\lceil 011 \rceil$  directions, for which the periodic boundary conditions are applied. The supercell consists of three Cu and eight Si layers, with 31 Si and 24 Cu atoms. Two types of Si vacancy are considered: a fourfold

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FIG. 5. (Color online) Cu/bcc-Ta interfacial diffusions: (a) interfacial structure with a diffusing Cu atom and a Ta vacancy at the interface. The Cu atom diffuses into the vacancy with 0.07 eV energy barrier. The energy profile for the diffusion is shown in (b). (c) Interfacial structure with a diffusing Cu atom and a Ta vacancy at one layer below the interface. The Cu atom diffuses into the vacancy with 0.29 eV energy barrier. The energy profile of the diffusion is shown in (d).

site below Cu atoms and a site directly below a Cu atom in the second Si layer [see Fig.  $4(b)$  $4(b)$ ]. It is found that there is a small energy barrier (0.07 eV) for the Cu atom diffusing into the first vacancy, and 0.73 eV barrier into the second vacancy.

#### *3. Diffusion barriers in bcc Ta*

The Cu  $(111)/Ta$   $(110)$  interface has a  $2 \times 2$  unit cell in Ta  $\lceil 110 \rceil$  and  $\lceil 001 \rceil$  directions, of which the periodic boundary conditions are applied. The supercell includes three Cu and four Ta layers with 31 Ta and 24 Cu atoms.

First, in the initial state, a vacancy is introduced at the top Ta layer; in the final state, a Cu atom is moved to the Ta vacancy. A small energy barrier of 0.07 eV is found for this diffusion process, accompanied by an energy drop of 0.63 eV in the final state, shown in Fig.  $5(a)$  $5(a)$ . Based on the final state, another vacancy is introduced at the second Ta layer and the Cu atom is displaced from the first vacancy to the second one. It is found that there is a barrier of 0.29 eV with an energy drop of  $0.54$  $0.54$  $0.54$  eV, shown in Fig.  $5(b)$ .

The above results indicate that, as Cu atom diffuses further into Ta, the energy barrier increases and the final state becomes less favorable. Therefore it would be interesting to examine the "asymptotic" interfacial diffusion behavior: Cu diffusion in bulk Ta. The diffusion energy barriers are evaluated by moving a Cu atom between two adjacent vacancies along different directions in bulk Ta. The cubic supercell consisting of 54 Ta atoms is used in the calculation. The

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FIG. 6. (Color online) Bulk diffusion barriers of Cu in bcc Ta. The energy barriers along different directions are shown. The arrow points from the diffusing Cu atom to the vacancy for each direction of interest.

results of bulk diffusion barrier are shown in Fig. [6.](#page-6-0) The lowest bulk diffusion barrier is  $0.65$  eV and is along [111] direction. Therefore, we conclude that Cu diffusion in Ta becomes increasingly more difficult going from interface to bulk. Furthermore, owing to the large vacancy formation energy, the probability of existing vacancies in Ta is low, which limits the rate of Cu diffusion in Ta. In other words, bcc Ta could be a good candidate for diffusion barrier material.

# *4. Diffusion in fcc TaN*

To model interfacial diffusion in fcc TaN, a  $2 \times 2$  supercell in  $\lceil 112 \rceil$  and  $\lceil 110 \rceil$  directions is used, including three Cu layers and six TaN layers. The supercell contains 24 Ta s, 24 N, and 24 Cu atoms before a vacancy is introduced. Four diffusion processes are considered with the vacancy placed at either the top or the second layer of the substrate with both Ta and N terminations.

The results are rather dramatic: upon relaxation of the final states, the Cu atom originally occupying the Ta or N vacancy is repelled back, indicating that the vacancy sites are not energetically stable for Cu occupation. Thus no diffusion barrier can be extracted. The only exception is the N vacancy at the second layer of Ta-terminated substrate. In this case, although a final state can be located (i.e., Cu is stable in the N vacancy), its energy is 4.6 eV higher than the initial state. Moreover, the diffusion energy barrier from the initial to final state is a staggering  $5.4$  eV (Fig. [7](#page-6-1)). The results strongly suggest that the interfacial diffusion of Cu into fcc TaN is highly improbable: Cu is either not stable in a vacancy site or its diffusion barrier is way too high.

To be complete, we have calculated bulk diffusion barriers in fcc TaN following the same procedure outlined for bcc Ta. The supercell consists of 48 Ta and 48 N atoms, 36 Ta and 36 N atoms, and 24 Ta and 24 N atoms for diffusion along  $[100]$ ,  $[110]$ , and  $[111]$  directions, respectively. The results are summarized in Fig. [8.](#page-7-1) The lowest bulk diffusion barrier is 1.2 eV and the corresponding diffusion paths are along  $[110]$  direction via Ta vacancies or along  $[100]$  direction via adjacent TaN-Ta vacancies. The bulk diffusion barrier in fcc TaN almost doubles that in bcc Ta, indicating that Cu atoms will be practically immobile even if they manage to diffuse into fcc TaN across the interface.

Next we discuss briefly the strain effect on the diffusion energy barriers. In all our calculations so far, Cu layers were stretched to fit the substrate lattice, e.g., 11% tensile strain on bcc Ta and 21% tensile strain on fcc TaN, respectively, and the substrate is strain-free. However, as Cu layers grow thicker, a compression strain could develop in Cu, which reduces the tensile strain of Cu layers at the interface and introduces a compression in the substrate. To model this strain effect on diffusion, we apply uniform compression strains upon the previous pseudomorphic models. Once

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FIG. 7. (Color online) Cu/fcc-TaN interfacial diffusions. No stable lattice site in the substrate can be found for Cu occupation (a) with a Ta vacancy at the interface, (b) with a Ta vacancy at one layer below the interface, or (c) with a N vacancy at the interface. For all three cases here, the Cu atom was initially placed at the vacancy (Initial site); after the relaxation, the Cu atom was "repelled" back and its final position is represented by the green sphere. The only exception is shown in (d) where the final stable site is a N vacancy at one layer below the interface, represented by the green sphere. The energy profile for the diffusion is shown in (e) with a huge barrier of 5.4 eV.

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FIG. 8. (Color online) Bulk diffusion barriers of Cu in fcc TaN are shown in different directions. The arrow points from the diffusing Cu atom to the vacancy in each direction of interest.

again, pseudomorphic models capture the essential physics taking place at the interface and at the same time render the computation feasible. We found that although the diffusion energy barrier changes as a function of applied strain, the general conclusions remain the same. For example, with a 5% compression, no stable final configuration was found for Cu occupying TaN interfacial vacancies—the diffusing Cu atom was pushed back at the Cu/fcc-TaN interface. As a result, no diffusion barrier can be obtained. For Cu/bcc Ta, we found that Cu diffusion to bcc Ta has a relatively lower energy barrier (comparing to fcc TaN) of 0.3 eV with 0.4 eV energy drop between the initial and final states. These results are consistent with the general conclusion that Cu diffusion into bcc Ta is energetically preferred with relatively lower energy barriers while the interfacial diffusion into fcc TaN is energetically strongly unfavorable.

One can understand the reason why the interfacial diffusion barrier of fcc TaN is much higher than that of bcc Ta by considering the bulk vacancy formation energy. The vacancy formation energy in Cu is much lower than that in bcc Ta; therefore it is energetically favorable for a Cu atom to occupy a vacancy in bcc Ta, leaving behind a Cu vacancy. However, the situation is opposite in fcc TaN: the vacancy formation energy is negative, i.e., Ta vacancies are energetically preferred in fcc TaN; therefore it is unfavorable for Cu to occupy a Ta vacancy. Since the formation energy of N vacancy in fcc TaN is either negative (for Ta rich) or positive but smaller (for N rich) than that of Cu, it is also energetically unfavorable for Cu to occupy the N vacancy in fcc TaN. This result should be contrasted to that in Cu/Si interfacial diffusion. Although the vacancy formation in Si is similar to that in bcc Ta, the physics of Cu/Si and Cu/Ta interfacial diffusions is very different. Since Cu chemically reacts with Si, Cu diffusion into Si is primarily driven by the chemical reactions, not controlled by vacancy formation in Si. The fact that Cu can spontaneously diffuse into Si vacancy suggests that Cu atoms indeed prefer to intermix with Si atoms. On the contrary, Cu is not believed to react with bcc Ta and no stable Cu-Ta compound has ever been observed. Therefore the intermixing of Cu and Ta is entirely accomplished by interfacial diffusion. The large Cu diffusion barriers observed in bulk Ta reflects the immiscibility of Cu and Ta. The high value of vacancy formation energy in Ta is the limiting factor for the Cu diffusion.

One can also make sense of the diffusion barriers from the atomic structure point of view. It is found that the diffusion barrier along different direction is correlated with the corresponding Cu-Ta bond length at their saddle points. Highenergy barriers at the saddle point result from large compressions of the bonds. For example, in bcc Ta, the Cu-Ta bond lengths at the saddle points for  $[111]$ ,  $[100]$ , and  $[110]$  diffusions are 2.7, 2.5, and 2.3 Å, respectively, and they correspond to an energy barrier of 0.65, 2.7, and 5.8 eV, respec-tively, shown in Fig. [8.](#page-7-1) The bonding environment in fcc TaN is more complicated but the general trend applies as well. The Cu-Ta bond lengths at the saddle points for diffusion along  $[100]$ ,  $[110]$  N-vacancy, and  $[111]$  directions are 2.4, 2.3, and 2.1 Å, respectively, corresponding to an energy barrier of 1.2, 2.5, and 3.0 eV.

### **IV. CONCLUSION**

<span id="page-7-0"></span>We perform DFT calculations for various interfacial structures, including Cu/bcc Ta, Cu/fcc TaN, Cu/hex Ta<sub>2</sub>N, Cu/ hex TaN, and Cu/Si. Different surface orientations, in-plane arrangements, and surface terminations are examined in detail. It is found that Cu/bcc-Ta and Cu/fcc-TaN interfaces are most stable from the cohesive energy point of view. The preferred interfacial structures are dictated by the coexistence of strong Cu-N ionic bonding and Cu-Ta covalent/ metallic bonding.

Based on the results of interfacial structure, we carry out DFT-NEB calculations for diffusion energy barriers across the interfaces, and in bulk of bcc Ta and fcc TaN. As a comparison, the diffusion energy barriers are also determined for Cu/Si interfaces. We find that Cu atom can diffuse spontaneously into a Si vacancy across Cu (111)/Si (111) interface. There is a smaller energy barrier of 0.08 eV for Cu to cross Cu (100)/Si (100) interface. Although the diffusion barrier of Cu into a Ta vacancy across Cu (111)/bcc-Ta (110) interface is only 0.07 eV, the vacancy formation energy of Ta is very high, limiting the rate of interfacial diffusion. Because vacancy formation is energetically preferred in fcc TaN, Cu diffusion into fcc-TaN vacancy is nearly impossible, with either no stable lattice sites for Cu occupation or with extremely high diffusion energy barrier (5.4 eV). Although both bcc Ta and fcc TaN can serve as diffusion barrier materials, their working mechanisms are different: Cu diffusion into bcc Ta is suppressed due to the high formation energy of Ta vacancy; Cu diffusion into fcc TaN is prohibited because of the extremely high interfacial diffusion energy barrier. Overall, fcc TaN is a better material for diffusion barrier. In this work, we have not considered the diffusions along grain boundaries or dislocations, which could be important. However, such calculations are beyond the scope of firstprinciples simulations and thus should be left for future studies, possibly by multiscale modeling.

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