



## Shallow impurity absorption spectroscopy in isotopically enriched silicon

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Inhomogeneous broadening due to isotopic randomness in natural Si has been shown to cause a broadening of many of the ground-state to excited-state infrared-absorption transitions of the shallow donor phosphorus and acceptor boron. Previously, it had been thought that the observed linewidths of shallow impurity transitions in silicon were at their fundamental lifetime limit. We report improved high-resolution infrared-absorption studies of these transitions in new samples of isotopically enriched <sup>28</sup>Si, <sup>29</sup>Si, and <sup>30</sup>Si. Some of the transitions in <sup>28</sup>Si show the narrowest linewidths ever reported for shallow donor and acceptor absorption transitions, and many higher excited states are now observed. The improved samples of <sup>29</sup>Si and <sup>30</sup>Si result in revised values for the dependence of shallow donor and acceptor binding energies on the average Si mass.

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### I. INTRODUCTION

Most of the works on the effects of the isotopic composition of the host material on the optical and electronic properties of semiconductors have focused on effects controlled by the average composition.<sup>1-3</sup> More recently, high-quality crystals of isotopically pure Si have become available,<sup>4,5</sup> which reveal effects that are controlled not by the average composition but rather by the randomness of the composition present in crystals having the natural isotopic abundance.<sup>6,7</sup>

Karaiskaj *et al.*<sup>7</sup> showed that the isotopic randomness present in natural Si (<sup>nat</sup>Si) causes a significant inhomogeneous broadening of many of the long-studied ground-state to excited-state infrared-absorption transitions of the shallow donor phosphorus and acceptor boron. This was surprising since it was thought that the observed linewidths of shallow impurities in silicon are at their fundamental lifetime limit.<sup>8-10</sup> Very recently, measurements of the excited-state lifetime for some of the absorption transitions in Si:P have been made which are in reasonable agreement with the reduced linewidths observed in <sup>28</sup>Si.<sup>11</sup>

Here we report on improved high-resolution infrared-absorption studies of the shallow impurities phosphorus and boron in new samples of isotopically enriched <sup>28</sup>Si, <sup>29</sup>Si, and <sup>30</sup>Si. These data improve on the linewidths of earlier spectra<sup>7,12</sup> particularly for the higher excited states due to reduced concentration broadening. Some of the transitions in <sup>28</sup>Si show the narrowest full width at half maximum (FWHM) ever reported for shallow donor and acceptor absorption transitions in semiconductors. In the case of boron the new samples also result in a significant increase in the number of observable absorption lines. With regard to the determination of the impurity-binding-energy shift with isotopic mass between <sup>28</sup>Si and <sup>30</sup>Si, the greatly improved spec-

tra of the new <sup>30</sup>Si sample provide more accurate results than in our preliminary study.<sup>12</sup> A similar effect has been observed<sup>13</sup> previously for the B acceptor in <sup>13</sup>C vs <sup>12</sup>C diamond, and later explained<sup>14</sup> in terms of changes in the ground-state and excited-state binding energies due to a small dependence of the hole effective mass on the host isotopic composition. The shift in transition energies for both B and P between <sup>30</sup>Si and <sup>28</sup>Si has been explained by the same mechanism, with the inclusion of the dependence of the dielectric constant on the host isotopic composition.<sup>12</sup>

### II. EXPERIMENTAL METHOD

The main improvement over our preliminary studies<sup>7,12,15</sup> was the improved quality of the samples used here, either in terms of the enrichment for <sup>28</sup>Si or in terms of the chemical purity and crystalline perfection for <sup>29</sup>Si and <sup>30</sup>Si. The <sup>28</sup>Si sample studied here was used before for photoluminescence excitation (PLE) experiments<sup>16</sup> and has an isotopic composition of 99.991% <sup>28</sup>Si+0.0075% <sup>29</sup>Si+0.0015% <sup>30</sup>Si. It also has an improved chemical purity and lighter doping levels with concentrations of [P]=2×10<sup>12</sup> cm<sup>-3</sup> and [B]=5×10<sup>13</sup> cm<sup>-3</sup>. For the boron spectra a sample with higher enrichment (99.995% <sup>28</sup>Si) was used, with a low phosphorus concentration of [P]=5×10<sup>11</sup> cm<sup>-3</sup> and boron concentration of [B]=4.5×10<sup>13</sup> cm<sup>-3</sup>.<sup>17</sup> The new <sup>29</sup>Si and <sup>30</sup>Si samples have a higher chemical purity but a lower isotopic enrichment, and the severe broadening and splitting<sup>18,19</sup> observed in the earlier samples are eliminated. The isotopic composition of the <sup>29</sup>Si sample is 4.32% <sup>28</sup>Si+91.37% <sup>29</sup>Si+4.30% <sup>30</sup>Si, with impurity concentrations of [P]=2×10<sup>13</sup> cm<sup>-3</sup> and [B]=5×10<sup>13</sup> cm<sup>-3</sup>, and for the <sup>30</sup>Si sample the enrichment

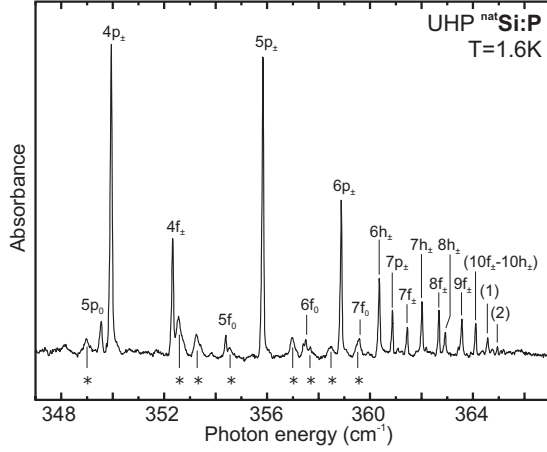


FIG. 1. High-energy end of the IR absorption spectrum of P-doped UHP <sup>nat</sup>Si at 1.6 K. Labels are assigned according to Pajot *et al.* (Ref. 24), no published data is available for lines (1) and (2). \* denotes absorption due to B.

is 2.50% <sup>28</sup>Si+7.70% <sup>29</sup>Si+89.80% <sup>30</sup>Si, with impurity concentrations of [P]=2 × 10<sup>13</sup> cm<sup>-3</sup> and [B]=9 × 10<sup>13</sup> cm<sup>-3</sup>. While the chemical purity of the enriched samples is improved, it still does not match that of ultrahigh-purity (UHP) natural silicon samples.

The samples were freely suspended in a sample chamber filled with superfluid He and sealed with polypropylene windows. The spectra were collected with a Bomem DA8.02 Fourier transform interferometer using either a silicon composite bolometer at 1.6 K or a Si:B photoconductive detector at 4.2 K, together with Mylar beamsplitters. For the high-resolution spectra a Global source was used. To improve the spectra an additional quartz halogen source was used to illuminate the sample in order to achieve photoneutralization. The instrumental resolution for the phosphorus spectra was 0.012 cm<sup>-1</sup>, and as low as 0.006 cm<sup>-1</sup> for boron spectra, as verified by the observed linewidths of residual gas absorption lines. Samples with different thicknesses were used to obtain spectra covering the stronger transitions as well as the very weak higher-lying ones.

III. RESULTS AND DISCUSSION

A. Natural silicon

For the donor phosphorus in <sup>nat</sup>Si (Fig. 1) we report narrower lines and higher excited states than shown previously.<sup>20-23</sup> The 2p<sub>0</sub> absorption line has a FWHM of 0.082 cm<sup>-1</sup> and the 7p<sub>±</sub> has a FWHM of only 0.057 cm<sup>-1</sup>. All energies and linewidths are listed in Table I. Our sample also reveals two absorption lines for which we could not

TABLE I. Observed energies and FWHM of phosphorus absorption transitions in silicon. All energies in cm<sup>-1</sup>.

|                                    | <sup>28</sup> Si |       | <sup>nat</sup> Si |       | <sup>29</sup> Si | <sup>30</sup> Si |
|------------------------------------|------------------|-------|-------------------|-------|------------------|------------------|
|                                    | Energy           | FWHM  | Energy            | FWHM  | Energy           | Energy           |
| 2p <sub>0</sub>                    | 275.090          | 0.033 | 275.108           | 0.082 | 275.128          | 275.147          |
| 2p <sub>±</sub>                    | 315.948          | 0.061 | 315.966           | 0.123 | 316.008          | 316.048          |
| 3p <sub>0</sub>                    | 323.436          | 0.135 | 323.460           | 0.166 | 323.499          | 323.541          |
| 4p <sub>0</sub>                    | 340.906          | 0.078 | 340.921           | 0.122 | 340.980          | 341.025          |
| 3p <sub>±</sub>                    | 342.429          | 0.051 | 342.449           | 0.105 | 342.492          | 342.540          |
| 5p <sub>0</sub>                    | 349.538          |       | 349.549           | 0.103 | 349.610          | 349.650          |
| 4p <sub>±</sub>                    | 349.924          | 0.029 | 349.952           | 0.089 | 349.990          | 350.037          |
| 4f <sub>±</sub>                    | 352.308          | 0.026 | 352.337           | 0.075 | 352.383          | 352.430          |
| 5f <sub>0</sub>                    |                  |       | 354.401           | 0.092 | 354.443          | 354.480          |
| 5p <sub>±</sub>                    | 355.814          | 0.022 | 355.841           | 0.072 | 355.879          | 355.931          |
| 6f <sub>0</sub>                    |                  |       |                   |       | 357.511          | 357.555          |
| 6p <sub>±</sub>                    | 358.857          | 0.023 | 358.888           | 0.071 | 358.935          | 358.983          |
| 7f <sub>0</sub>                    | 359.550          |       |                   |       |                  |                  |
| 6h <sub>±</sub>                    | 360.345          |       | 360.366           | 0.069 | 360.431          | 360.478          |
| 7p <sub>±</sub>                    | 360.844          |       | 360.876           | 0.057 | 360.915          | 360.958          |
| 7f <sub>±</sub>                    | 361.427          |       | 361.453           | 0.069 | 361.506          | 361.555          |
| 7h <sub>±</sub>                    | 361.995          |       | 362.029           | 0.063 | 362.082          | 362.125          |
| 8f <sub>±</sub>                    | 362.662          |       | 362.683           | 0.058 | 362.730          | 362.794          |
| 8h <sub>±</sub>                    | 362.897          |       | 362.929           | 0.068 | 362.990          |                  |
| 9f <sub>±</sub>                    | 363.546          |       | 363.575           | 0.078 | 363.635          |                  |
| 10f <sub>±</sub> -10h <sub>±</sub> |                  |       | 364.113           | 0.059 | 364.170          |                  |
| (a)                                |                  |       | 364.578           | 0.082 |                  |                  |
| (b)                                |                  |       | 364.957           | 0.057 |                  |                  |

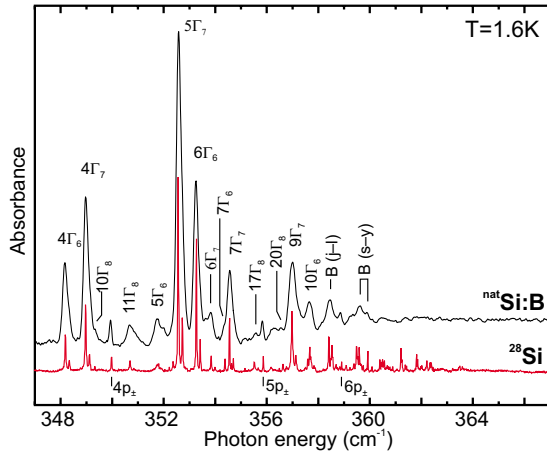


FIG. 2. (Color online) High-energy end of the IR absorption spectrum of B-doped  $^{nat}\text{Si}$  and of  $^{28}\text{Si}$  at 1.6 K. Labels are assigned according to Lewis *et al.* (Ref. 25). “a, b, ..., aa, and ab, ...” are used where no labels are available, and transitions due to P are labeled below the spectrum.

assign previously published final states and are therefore labeled (1) and (2). All other labels were assigned according to Pajot *et al.*<sup>24</sup>

We show a spectrum of the acceptor B in natural silicon in Fig. 2. Due to the high number of different labeling schemes we attempted to assign symmetry labels of theoretically calculated excited states wherever possible. These were given by Lewis *et al.*<sup>25</sup> where their energies are listed together with oscillator strength and compared to other labeling schemes.<sup>26,27</sup> Our spectrum clearly shows boron absorption lines up to the  $9\Gamma_7$  [labeled (11) by Fischer and Rome<sup>27</sup>] and  $10\Gamma_6$  transitions. Higher-energy lines that were verified to be B absorption transitions (by comparing to a  $^{28}\text{Si}$  sample, see Fig. 2) but for which no final-state label was available were labeled with letters “a, b, ..., aa, and ab, ...”

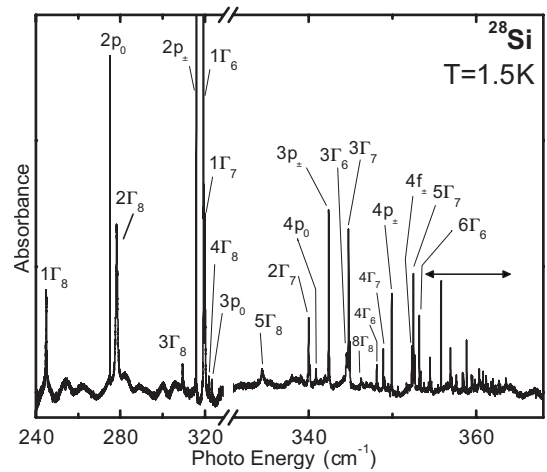


FIG. 3. Infrared-absorption spectrum of enriched, ultrapure  $^{28}\text{Si}$  at 1.5 K. All major B and P absorption lines are labeled. The arrow indicates the range shown on an expanded scale in Fig. 4. The instrumental resolution is  $0.02\text{ cm}^{-1}$ .

**B. Isotopically enriched  $^{28}\text{Si}$**

Figure 3 shows a complete spectrum of a  $^{28}\text{Si}$  sample containing both residual boron and phosphorus with all major lines labeled. The high-energy end of the spectrum is shown on an expanded scale in Fig. 4 due to the high density of transitions.

In previous publications<sup>7</sup> on isotopically enriched  $^{28}\text{Si}$  only the low-energy absorption lines of the donor phosphorus were found to be sharper than in  $^{nat}\text{Si}$  due to concentration broadening of higher-excited states. With the new higher-quality  $^{28}\text{Si}$  material we can report narrower P and B absorption linewidths for many of the high-energy transitions as well. The phosphorus  $5p_{\pm}$  line has a FWHM of  $0.022\text{ cm}^{-1}$  ( $0.019\text{ cm}^{-1}$  correcting for the instrumental res-

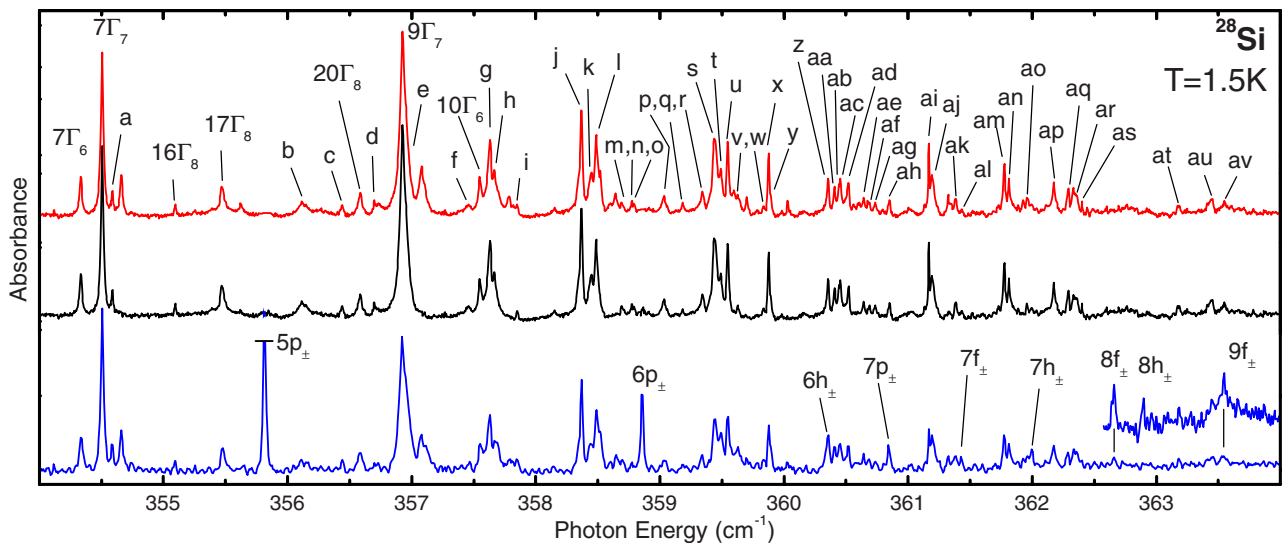


FIG. 4. (Color online) Infrared-absorption spectrum of enriched, ultrapure  $^{28}\text{Si}$  at 1.5 K (high-energy end). The top two spectra are from a sample with low-P concentration. All identified  $^{10}\text{B}$ - $^{11}\text{B}$  pairs are labeled. The middle spectrum has all  $^{10}\text{B}$  absorption lines removed synthetically. The instrumental resolution is  $0.006\text{ cm}^{-1}$ . The bottom spectrum and inset show phosphorus absorption lines taken from two samples with higher residual P concentration, both at a resolution of  $0.02\text{ cm}^{-1}$ .

olution of  $0.012 \text{ cm}^{-1}$ ), five times narrower than that reported by Andreev *et al.*<sup>23</sup> and only two times wider than the narrowest absorption line reported for the deep center Se.<sup>28</sup> The use of samples with different residual P levels made it possible to identify weak high-energy P absorption lines up to the  $9f_{\pm}$  transition, as shown at the bottom of Fig. 4. Table I shows the measured position and FWHM of phosphorus absorption lines in  $^{28}\text{Si}$ ,  $^{\text{nat}}\text{Si}$ ,  $^{29}\text{Si}$ , and  $^{30}\text{Si}$ .

Thanks to the reduction in concentration broadening we have observed narrower absorption lines for the acceptor boron as well. Most of the boron transitions reveal a  $\sim 0.154 \pm 0.002 \text{ cm}^{-1}$  splitting in  $^{28}\text{Si}$  which was attributed to the difference in binding energy between  $^{10}\text{B}$  and  $^{11}\text{B}$  acceptors.<sup>7</sup> The doublet intensity ratio reflects the  $^{11}\text{B}/^{10}\text{B}$  natural abundance ratio of  $\sim 80/20$ . This characteristic doublet can be used to identify many high-energy B absorption transitions that have not been reported previously. For easier reference we attached new alphabetic labels “a, b, ..., aa, and ab, ...” to these lines. The observed linewidths for these higher-energy B transitions are even narrower than those of P.

The *p*-type character of the  $^{28}\text{Si}$  sample makes it necessary to use photoneutralization in order to see the donor transitions. The photoneutralization also reduces electric fields due to ionized impurities, and thus reduces the inhomogeneous Stark broadening of both boron and phosphorus absorption lines. For a number of B lines we measure a FWHM in the range of  $0.010\text{--}0.013 \text{ cm}^{-1}$  ( $0.008\text{--}0.012 \text{ cm}^{-1}$  corrected for the instrumental resolution). This is more than 20 times narrower than B transitions reported by Lewis *et al.*<sup>25</sup> for B in  $^{\text{nat}}\text{Si}$ , and only about 1.5 times wider than the narrowest absorption line reported for the deep center Se.<sup>28</sup> The measured position and FWHM of B absorption lines in  $^{28}\text{Si}$ ,  $^{\text{nat}}\text{Si}$ ,  $^{29}\text{Si}$ , and  $^{30}\text{Si}$  are shown in Tables II and III. Figure 4 shows a spectrum of the high-energy end of boron absorption lines. We have also generated a spectrum that eliminates the  $^{10}\text{B}$  components through a shift-and-subtract procedure to simplify the identification of many boron-related absorption features.

**I. Isotope broadening**

The broadening seen in  $^{\text{nat}}\text{Si}$  or any sample of mixed isotopic composition is dominated by an effect<sup>7</sup> that is independent of the small shifts in binding energy between pure  $^{28}\text{Si}$ ,  $^{29}\text{Si}$ , and  $^{30}\text{Si}$  which will be discussed later. The wave function of the ground state is relatively compact; so in samples with mixed isotopes, individual impurities can have significantly different local isotopic compositions. These fluctuations induce shifts (and splittings for acceptors<sup>29</sup>) of the ground states, which can be related to the known shifts of valence-band and conduction-band energies with average isotopic composition. The excited-state wave functions are much more extended and therefore sample an isotopic composition closer to the average. The difference in isotopic composition sampled by excited-state and ground-state results in inhomogeneous broadening. The valence-band shifts more than the conduction band with the isotopic composition<sup>7</sup> causing a stronger broadening for the acceptor B than for the donor P.

TABLE II. Observed energies and FWHM of lower energy boron absorption transitions in silicon. For  $^{28}\text{Si}$  the energies of the  $^{11}\text{B}$  components are given, the transition energy of  $^{10}\text{B}$  is  $0.154 \text{ cm}^{-1}$  higher. All energies in  $\text{cm}^{-1}$ . (Continued in Table III.)

| Symmetry<br>(Ref. 25)/label | $^{28}\text{Si}$ ( $^{11}\text{B}$ ) |       | $^{\text{nat}}\text{Si}$ | $^{29}\text{Si}$ | $^{30}\text{Si}$ |
|-----------------------------|--------------------------------------|-------|--------------------------|------------------|------------------|
|                             | Energy                               | FWHM  | Energy                   | Energy           | Energy           |
| $1\Gamma_8$                 | 244.929                              | 0.423 | 244.946                  | 245.089          | 245.193          |
| $2\Gamma_8$                 | 278.260                              | 0.839 | 278.295                  | 278.443          | 278.571          |
| $3\Gamma_8$                 | 309.503                              | 0.458 | 309.531                  | 309.704          | 309.827          |
| $1\Gamma_6$                 | 319.335                              | 0.094 | 319.374                  | 319.535          | 319.687          |
| $1\Gamma_7$                 | 320.013                              | 0.386 | 320.032                  | 320.199          | 320.347          |
| $4\Gamma_8$                 | 321.887                              | 0.339 | 321.910                  | 322.106          | 322.254          |
| $5\Gamma_8$                 | 334.490                              | 0.395 | 334.517                  | 334.688          | 334.846          |
| $2\Gamma_6$                 | 338.032                              | 0.419 | 338.042                  |                  |                  |
| $6\Gamma_8$                 | 339.080                              | 0.130 | 339.151                  | 339.336          |                  |
| $2\Gamma_7$                 | 340.025                              | 0.064 | 340.045                  | 340.264          | 340.407          |
| $7\Gamma_8$                 | 342.021                              | 0.083 |                          |                  |                  |
| $3\Gamma_6$                 | 344.539                              | 0.140 | 344.544                  | 344.754          | 344.883          |
| $3\Gamma_7$                 | 344.783                              | 0.041 | 344.834                  | 345.012          | 345.164          |
| $8\Gamma_8$                 | 346.268                              | 0.120 | 346.303                  | 346.499          |                  |
| $4\Gamma_6$                 | 348.132                              | 0.043 | 348.171                  | 348.355          | 348.510          |
| $4\Gamma_7$                 | 348.918                              | 0.042 | 348.982                  | 349.162          | 349.330          |
| $10\Gamma_8$                | 349.277                              | 0.026 |                          |                  |                  |
| $11\Gamma_8$                | 350.640                              | 0.055 | 350.689                  |                  |                  |
| $5\Gamma_6$                 | 351.703                              | 0.120 | 351.751                  |                  |                  |
| $5\Gamma_7$                 | 352.517                              | 0.029 | 352.593                  | 352.760          | 352.924          |
| $6\Gamma_6$                 | 353.221                              | 0.024 | 353.259                  | 353.448          | 353.605          |
| $6\Gamma_7$                 | 353.796                              | 0.036 | 353.847                  |                  | 354.170          |
| $7\Gamma_6$                 | 354.332                              | 0.028 |                          |                  |                  |
| $7\Gamma_7$                 | 354.507                              | 0.025 | 354.574                  | 354.748          |                  |
| (a)                         | 354.589                              | 0.012 |                          |                  |                  |
| $16\Gamma_8$                | 355.095                              | 0.018 |                          |                  |                  |
| $17\Gamma_8$                | 355.473                              | 0.033 | 355.584                  |                  |                  |
| (b)                         | 356.110                              |       |                          |                  |                  |
| (c)                         | 356.439                              |       |                          |                  |                  |
| (d)                         | 356.699                              |       |                          |                  |                  |
| $20\Gamma_8$                | 356.585                              | 0.049 |                          |                  |                  |
| $9\Gamma_7$                 | 356.925                              | 0.044 | 357.005                  | 357.178          |                  |
| (e)                         | 356.961                              | 0.049 |                          |                  |                  |
| (f)                         | 357.458                              |       |                          |                  |                  |
| $10\Gamma_6$                | 357.549                              | 0.036 | 357.662                  |                  |                  |
| (g)                         | 357.628                              | 0.042 |                          |                  |                  |
| (h)                         | 357.668                              | 0.019 |                          |                  |                  |
| (i)                         | 357.850                              | 0.018 |                          |                  |                  |
| (j)                         | 358.367                              | 0.024 | 358.470                  |                  |                  |

Lifetime broadening as a limiting factor for the width of absorption lines dominates for some transitions, hence their FWHM does not decrease significantly in isotopically enriched  $^{28}\text{Si}$ . An example would be the  $1\Gamma_7$  transition shown in Fig. 5 or  $1\Gamma_8$  in Fig. 7. This lifetime broadening effect was explained by Kane<sup>8</sup> and confirmed by Barrie and



TABLE III. Observed energies and FWHM of high energy  $^{11}\text{B}$  absorption transitions in  $^{28}\text{Si}$ . All energies in  $\text{cm}^{-1}$ .

| Label | Energy  | FWHM  | Label | Energy  | FWHM  |
|-------|---------|-------|-------|---------|-------|
| (k)   | 358.446 | 0.040 | (ad)  | 360.520 | 0.015 |
| (l)   | 358.487 | 0.027 | (ae)  | 360.641 | 0.025 |
| (m)   | 358.694 | 0.020 | (af)  | 360.689 | 0.012 |
| (n)   | 358.773 | 0.013 | (ag)  | 360.735 | 0.029 |
| (o)   | 358.792 | 0.015 | (ah)  | 360.848 | 0.022 |
| (p)   | 359.032 | 0.035 | (ai)  | 361.167 | 0.010 |
| (q)   | 359.184 | 0.019 | (aj)  | 361.195 | 0.036 |
| (r)   | 359.341 | 0.030 | (ak)  | 361.382 | 0.023 |
| (w)   | 359.442 | 0.043 | (al)  | 361.434 |       |
| (t)   | 359.492 | 0.032 | (am)  | 361.773 | 0.019 |
| (u)   | 359.547 | 0.018 | (an)  | 361.812 | 0.015 |
| (v)   | 359.625 |       | (ao)  | 361.957 | 0.012 |
| (w)   | 359.835 | 0.017 | (ap)  | 362.173 | 0.028 |
| (x)   | 359.876 | 0.013 | (aq)  | 362.289 | 0.020 |
| (y)   | 359.895 | 0.014 | (ar)  | 362.356 |       |
| (z)   | 360.356 | 0.013 | (as)  | 362.401 | 0.007 |
| (aa)  | 360.407 | 0.019 | (at)  | 363.180 |       |
| (ab)  | 360.440 | 0.017 | (au)  | 363.446 |       |
| (ac)  | 360.455 | 0.017 | (av)  | 363.553 |       |

Nishikawa<sup>9,10</sup> as a result of transitions to other nearby excited states involving acoustic phonons.

We had earlier developed a model that explains both the magnitude and the distribution of the acceptor ground-state splitting caused by the isotopic disorder present in  $^{\text{nat}}\text{Si}$ ,<sup>29</sup> in

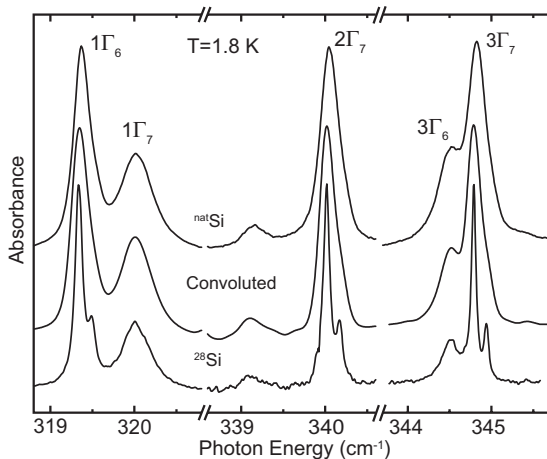


FIG. 5. Absorption lines  $1\Gamma_6$ ,  $1\Gamma_7$ ,  $2\Gamma_7$ ,  $3\Gamma_6$ , and  $3\Gamma_7$  of the B acceptor are compared between  $^{\text{nat}}\text{Si}$  (top) and  $^{28}\text{Si}$  (bottom). Lines  $1\Gamma_6$ ,  $2\Gamma_7$ , and  $3\Gamma_7$  are significantly narrower in  $^{28}\text{Si}$ , revealing an identical doublet structure with a splitting of  $0.154 \text{ cm}^{-1}$  due to the difference in binding energy between  $^{10}\text{B}$  and  $^{11}\text{B}$ . The  $1\Gamma_7$  transition is broad in both spectra, indicating the dominance of excited-state lifetime broadening for this state even in  $^{\text{nat}}\text{Si}$ . The middle spectrum shows an excellent agreement between the  $^{\text{nat}}\text{Si}$  spectrum and the  $^{28}\text{Si}$  spectrum convoluted with the previously calculated isotopic broadening of the B ground state in  $^{\text{nat}}\text{Si}$  (Ref. 29).

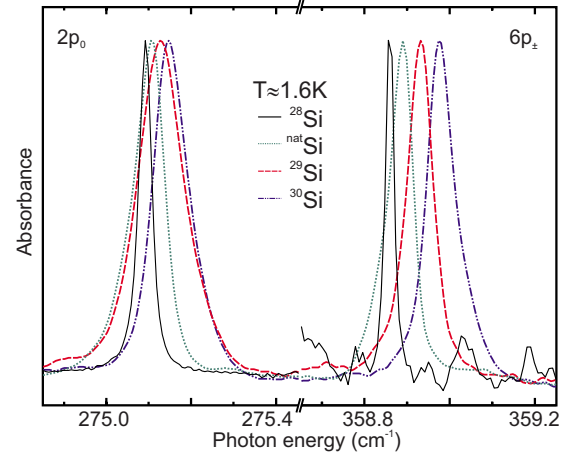


FIG. 6. (Color online) Shifts for two representative P transitions ( $2p_0$  and  $6p_{\pm}$ ) in  $^{28}\text{Si}$ ,  $^{\text{nat}}\text{Si}$ ,  $^{29}\text{Si}$ , and  $^{30}\text{Si}$ .

order to explain an acceptor ground-state splitting which can be observed in acceptor-bound exciton spectra in  $^{\text{nat}}\text{Si}$ . We computed the eigenvalues of the ground state for B, for different configurations of random distributions of isotopes around the lattice site, with an average composition corresponding to  $^{\text{nat}}\text{Si}$ . The perturbation induced by the isotopes splits the fourfold degenerate eigenvalues of the acceptor ground state into Kramers doublets and shifts them randomly, leading to a broad distribution. This distribution of the B ground-state eigenvalues has been convoluted with the lines  $1\Gamma_6$ ,  $1\Gamma_7$ ,  $2\Gamma_7$ ,  $3\Gamma_6$ , and  $3\Gamma_7$  obtained from a  $^{28}\text{Si}$  sample and is shown in Fig. 5 together with transitions in natural Si and isotopically pure  $^{28}\text{Si}$ . The result is seen to be in excellent agreement with the spectrum observed in  $^{\text{nat}}\text{Si}$ , showing that the inhomogeneous isotopic broadening of the infrared-absorption transitions can be accounted for with no adjustable parameters.

## 2. Line shapes

The phosphorus absorption lines exhibit tails in  $^{\text{nat}}\text{Si}$  and  $^{30}\text{Si}$ . In natural silicon the tail is toward the lower-energy end, in  $^{30}\text{Si}$  it is on the high-energy side of the peak. The  $^{28}\text{Si}$  lines do not show this asymmetry while the  $^{29}\text{Si}$  absorption lines show broadening on both sides. Figure 6 clearly shows the effect, especially for the  $2p_0$  line.

## C. Binding-energy shifts

Figures 6 and 7 show the energies for two representative P and B transitions in  $^{28}\text{Si}$ ,  $^{\text{nat}}\text{Si}$ ,  $^{29}\text{Si}$ , and  $^{30}\text{Si}$ , respectively. The dependence of  $\epsilon_0$  and  $m^*$  on the isotopic mass scales the ground-state and excited-state binding energies by an identical factor,<sup>12</sup> and thus the largest shifts are observed for transitions to the highest-excited states. To obtain the actual isotope shift between  $^{28}\text{Si}$  and  $^{30}\text{Si}$  it was necessary to scale the energy of the  $^{30}\text{Si}$  transition since the  $^{30}\text{Si}$  sample has an enrichment of only 89.8%  $^{30}\text{Si}$ . To obtain an appropriate scaling factor for the shift of the binding energy  $\Delta E_B = E_B(^{28}\text{Si}) - E_B(^{30}\text{Si})$ , we simply assume that the binding energy depends linearly on the average Si mass.

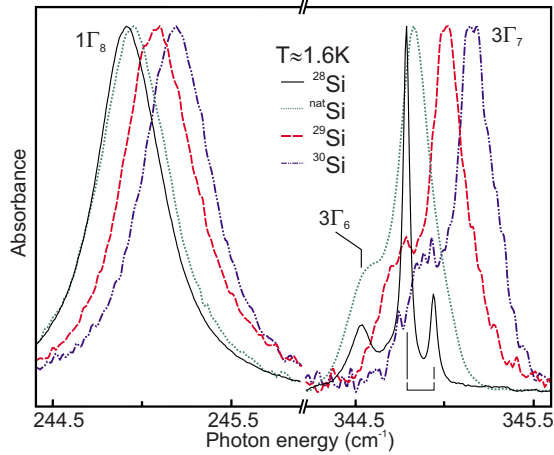


FIG. 7. (Color online) Shifts for two representative B transitions ( $1\Gamma_8$  and  $3\Gamma_7$ ) in  $^{28}\text{Si}$ ,  $^{\text{nat}}\text{Si}$ ,  $^{29}\text{Si}$ , and  $^{30}\text{Si}$ . While the  $1\Gamma_8$  absorption line is dominated by lifetime broadening in all samples, the  $3\Gamma_7$  transition reveals the  $^{11}\text{B}/^{10}\text{B}$  splitting in  $^{28}\text{Si}$ .

At the high-energy end of the spectrum the changes in the energy shift between  $^{28}\text{Si}$  and  $^{30}\text{Si}$  from line to line are very small, since the excited-state binding energies and their shifts with the average Si mass become small. This allows us to choose a high-lying absorption line with strong intensity, which shows essentially the full binding-energy shift of the ground state between pure  $^{28}\text{Si}$  and pure  $^{30}\text{Si}$ . For phosphorus we selected one of the sharpest features, the  $6p_{\pm}$  transition. Scaling the measured shift we obtain the P ground-state binding-energy shift between pure  $^{28}\text{Si}$  and pure  $^{30}\text{Si}$ ,  $\Delta E_B = (-0.14 \pm 0.01) \text{ cm}^{-1}$ . The  $6p_{\pm}$  transition has a binding energy of only 1.08 meV versus 45.6 meV of the phosphorus ground state. In the case of boron we chose the highest-isolated line in the spectrum, the  $3\Gamma_7$  transition. For  $^{28}\text{Si}$  we use the energy of the  $^{11}\text{B}$  component due to its high abundance. The resulting B ground-state binding-energy shift between pure  $^{28}\text{Si}$  and pure  $^{30}\text{Si}$  is then  $\Delta E_B = (-0.41 \pm 0.02) \text{ cm}^{-1}$ .  $3\Gamma_7$  has an  $E_B$  of 2.41 meV versus 45.6 meV of the boron ground state. Hence the transition energies of both  $6p_{\pm}$  and  $3\Gamma_7$  can be considered close to the ionization energy. Table IV lists the experimentally deter-

TABLE IV. Experimentally determined energy shifts for select transitions between  $^{28}\text{Si}$  and  $^{30}\text{Si}$  and the calculated shift of the binding energy  $\Delta E_B = E_B(^{28}\text{Si}) - E_B(^{30}\text{Si})$  for P and B between pure  $^{28}\text{Si}$  and pure  $^{30}\text{Si}$  (in  $\text{cm}^{-1}$ ).  $\Delta E_B$  has an error of  $\pm 0.01$  for P and  $\pm 0.02$  for B.

|            | P          |            |            |              | B           |             |             | $\Delta E_B$ |
|------------|------------|------------|------------|--------------|-------------|-------------|-------------|--------------|
|            | $2p_{\pm}$ | $3p_{\pm}$ | $6p_{\pm}$ | $\Delta E_B$ | $1\Gamma_8$ | $1\Gamma_6$ | $3\Gamma_7$ |              |
| $\Delta E$ | -0.10      | -0.12      | -0.13      | -0.14        | -0.26       | -0.35       | -0.38       | -0.41        |

mined energy shift for select transitions together with  $\Delta E_B$  for P and B.

#### IV. CONCLUSION

We have shown improved spectra of the shallow impurities phosphorus and boron in natural silicon,  $^{28}\text{Si}$ ,  $^{29}\text{Si}$ , and  $^{30}\text{Si}$ . For phosphorus in  $^{\text{nat}}\text{Si}$  we observe higher-excited states than reported previously. In  $^{28}\text{Si}$  we show high-energy absorption transitions of phosphorus up to the  $9f_{\pm}$  line. The observed FWHM is significantly narrower than in natural silicon. In the case of boron, we find strong evidence of the existence of many more highly-excited states than previously reported. We developed a way of identifying those transitions with the help of their boron isotope components. Many of these transitions are extremely sharp. They are the sharpest reported for shallow impurity absorption transitions in silicon. We also measure the binding-energy shift in samples with different host isotopic compositions for B and P and find that the ground-state binding-energy shift  $\Delta E_B$  between pure  $^{28}\text{Si}$  and pure  $^{30}\text{Si}$  is smaller than previously estimated. These significant improvements were made possible by the use of greatly improved isotopically enriched silicon samples.

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