



p-type Bi₂Se₃ for topological insulator and low-temperature thermoelectric applications

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The growth and elementary properties of *p*-type Bi₂Se₃ single crystals are reported. Based on a hypothesis about the defect chemistry of Bi₂Se₃, the *p*-type behavior has been induced through low-level substitutions (1% or less) of Ca for Bi. Scanning tunneling microscopy is employed to image the defects and establish their charge. Tunneling and angle-resolved photoemission spectra show that the Fermi level has been lowered into the valence band by about 400 meV in Bi_{1.98}Ca_{0.02}Se₃ relative to the *n*-type material. *p*-type single crystals with *ab*-plane Seebeck coefficients of +180 μV/K at room temperature are reported. These crystals show an anomalous peak in the Seebeck coefficient at low temperatures, reaching +120 μV K⁻¹ at 7 K, giving them a high thermoelectric power factor at low temperatures. In addition to its interesting thermoelectric properties, *p*-type Bi₂Se₃ is of substantial interest for studies of technologies and phenomena proposed for topological insulators.

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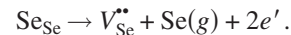
I. INTRODUCTION

Bi₂Se₃ is one of the binary end members of the (Bi,Sb)₂(Te,Se)₃ family of thermoelectric materials. Decades of work in the chemistry, physics, and processing of these materials have led to complex formulations of compounds and microstructures optimized for use as thermoelectrics under various conditions (see, e.g., Refs. 1 and 2). Due to the superiority of Bi₂Te₃-based materials for these applications, Bi₂Se₃, while well studied, has not been subjected to the same degree of intensive research as has its heavier-mass analog. One of the major issues for Bi₂Se₃-based thermoelectrics has been the difficulty in making the material *p* type. Unlike Bi₂Te₃, which can simply be made *n* or *p* type through variation in the Bi:Te ratio, the defect chemistry in Bi₂Se₃ is dominated by charged selenium vacancies, which act as electron donors,³ resulting in *n*-type behavior for virtually all of the reported transport studies (see, e.g., Refs. 3–11). *p*-type behavior for pure Bi₂Se₃ was reported in an early study⁹ but never since. Modern studies have shown that *p*-type behavior is possible when beginning with an *n*-type host material in the (Bi_{2-x}Sb_x)Se₃ solid solution with *x*=0.4 and then doping that composition with small amounts of Pb to create a quaternary *p*-type material.¹⁰

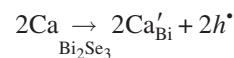
The present study is motivated by the desire to find a chemically less complex *p*-type Bi₂Se₃-based material to address the recent emergence of Bi₂Se₃ as one of the prime candidates for the study of topological surface states (see, e.g., Refs. 12–16) and for thermoelectric applications. The character and stability of the surface states in Bi₂Se₃ at room temperature has motivated the suggestion that they may be useful for quantum-computing applications if the Fermi level can be lowered to the Dirac point through *p*-type doping of the normally *n*-type compound.^{15,17,18} Therefore high-quality *p*-type crystals are important for both fundamental and applied research on Bi₂Se₃.

Unlike the case for Bi₂Te₃, where the chemical similarity of Bi and Te leads to antisite defects as the primary source of carrier doping in binary compounds, there is little tendency

for Bi/Se mixing in Bi₂Se₃ and the primary structural defect giving rise to electron doping is doubly charged selenium vacancies V_{Se}^{**} .³



Ordinarily, one compensates for the presence of donors in this chemical family through doping with Pb on the Bi site as Pb has one fewer electron than Bi. This substitution does not, however, lead to the formation of *p*-type material for Bi₂Se₃. We hypothesize that this is due to the fact that Pb in Bi₂Se₃ is ambipolar, much as is the case for Cu.¹¹ This indicates that a more ionic substitution on the Bi site may be required for hole doping of Bi₂Se₃, suggesting the use of Ca substitution, with the defect reaction,



with Ca substitution for Bi creating a negatively charged defect (Ca'_{Bi}) that in turn generates holes (h^*) to compensate the electrons created by the Se vacancies. Our results, described below, support this scenario as a good representation of the defect chemistry in this compound.

II. EXPERIMENTAL

The single crystals of Bi_{2-x}Ca_xSe₃ were grown via a process of two-step melting, starting with mixtures of high-purity elements (Bi, 99.999%; Se, 99.9999%; Ca, 99.8%). First, stoichiometric mixtures of Bi and Se were melted in evacuated quartz ampoules at 800 °C for 16 h. The melts were then stirred before being allowed to solidify by air quenching to room temperature. Second, the stoichiometric amount of Ca was added in the form of pieces, using care to avoid direct contact of the added Ca with the quartz. The materials were then heated in evacuated quartz ampoules at 400 °C for 16 h followed by 800 °C for a day. The crystal growth process involved cooling from 800 to 550 °C over a period of 24 h and then annealing at 550 °C for 3 days. The

crystals were then furnace cooled to room temperature. They were cleaved very easily along the basal plane and were cut into approximately $1.0 \times 1.0 \times 6.0 \text{ mm}^3$ rectangular bar samples for the thermal- and electronic-transport measurements. Resistivity, Seebeck coefficient, and thermal-conductivity measurements were performed in a Quantum Design Physical Property Measurement System, using the standard four-probe technique, with silver paste cured at room temperature used for the contacts. Hall-effect measurements to determine carrier concentrations were performed at 1.5 K in a home-built apparatus. In all cases, the electric and thermal currents were applied in the basal plane (*ab* plane in the hexagonal setting of the rhombohedral cell) of the crystals. In order to probe the electronic states of native and Ca-related defects, Bi_2Se_3 and $\text{Bi}_{1.98}\text{Ca}_{0.02}\text{Se}_3$ samples were studied in a cryogenic scanning tunneling microscope (STM) at 4.2 K. The samples were cleaved *in situ* in ultrahigh vacuum to expose a pristine surface. The surfaces of the *p*-type crystals are fully stable in the STM experiments. High-resolution angle-resolved photoemission spectroscopy (ARPES) measurements were performed using 22–40 eV photons at beamline 12 of the Advanced Light Source (Berkeley Laboratory) and on beamline 5 at the Stanford Synchrotron Radiation Laboratory. The energy and momentum resolutions were 15 meV and 2% of the surface Brillouin zone, respectively, obtained using a Scienta analyzer. The samples were cleaved at 10 K under pressures of less than 5×10^{-11} torr, resulting in shiny flat surfaces. The spectra employed are those closest to the time of cleavage (about 10 min), which are the most representative of the bulk.

III. RESULTS

The rhombohedral crystal structure of Bi_2Se_3 consists of hexagonal planes of Bi and Se stacked on top of each other along the [001] crystallographic direction (hexagonal setting), with the atomic order Se(1)-Bi-Se(2)-Bi-Se(1), where (1) and (2) refer to different lattice positions.¹⁹ The unit cell consists of three of these units stacked on top of each other with weak van der Waals bonds between Se(1)-Se(1) layers, making the (001) plane the natural cleavage plane. Scanning tunneling spectroscopy (dI/dV) was performed to measure the density of states (DOS). The spectra of Bi_2Se_3 were *n* type, as expected, due to the presence of Se vacancies with the Fermi energy near the conduction band, consistent with previous STM results.²⁰ In contrast, a clear shift in the position of the Fermi level toward the valance band occurs in the $\text{Bi}_{1.98}\text{Ca}_{0.02}\text{Se}_3$ sample as shown in Fig. 1(a). The finite density of states inside the gap is due to surface states for which topological properties have been predicted.^{12–18}

We were able to identify various defects and the sign of their charge state from the STM topographies of the filled states and unoccupied states. The STM topographies of the native Bi_2Se_3 (001) surface are dominated by one type of defect, which appears as a bright triangular protrusion in the topographies of the unoccupied states [Fig. 1(b)]. On average, these defects are about 40 Å across but vary in size between defects indicating that they are located in various layers beneath the surface. Given that no other defects were

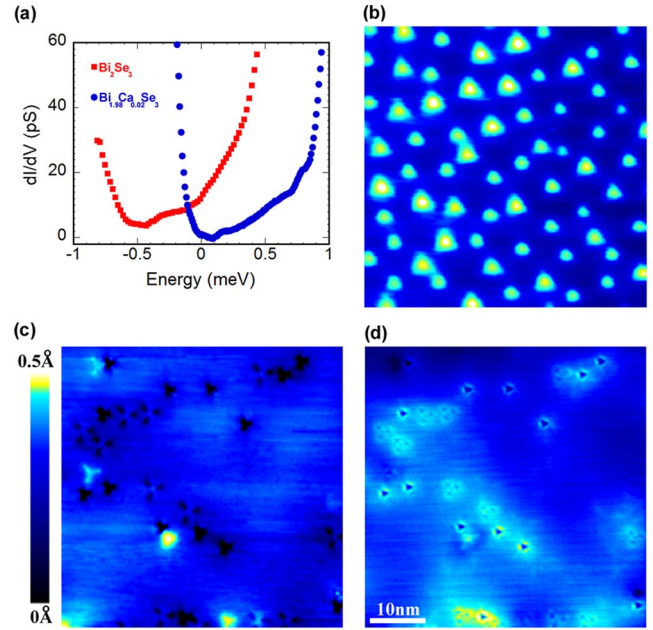


FIG. 1. (Color online) (a) Spatially averaged density of states (dI/dV) measurements showing the shift of E_F between *n*-type Bi_2Se_3 and *p*-type $\text{Bi}_{1.98}\text{Ca}_{0.02}\text{Se}_3$. (b) STM topography of the empty states of Bi_2Se_3 ($V_B = +1$ V, and $I = 10$ pA) showing triangular-shaped defects observed at various intensities, indicating they are located in different layers beneath the surface. (c) Topography of the empty states of $\text{Bi}_{1.98}\text{Ca}_{0.02}\text{Se}_3$ ($V_B = +2.0$ V and $I = 10$ pA) showing clover-leaf-looking defects and a substantial reduction in the density of the triangular defects, which dominated the undoped samples. (d) Topography of the filled states over the same area as in (c) ($V_B = -1.0$ V and $I = 10$ pA). The area around the triangular defect near center shows a depression around it in the filled states, demonstrating it is positively charged. In contrast, the Ca-related defects exhibit an area of enhancement around them, indicating they are negatively charged. All STM topographies are $500 \times 500 \text{ \AA}^2$.

observed, we attribute these triangular defects to Se vacancies. Figures 1(c) and 1(d) show the topography of the unoccupied and occupied states of the Ca-doped Bi_2Se_3 , respectively. Comparison between Figs. 1(b) and 1(c) makes it clear that the density of triangular defects has been reduced significantly in the Ca-doped samples. In addition, the STM topography of the $\text{Bi}_{1.98}\text{Ca}_{0.02}\text{Se}_3$ (001) surface shows distinct defects that were not present in Bi_2Se_3 samples. In topographic images of the empty states, the shape of these threefold symmetric defects resembles a clover leaf [Fig. 1(c)]. Based on their two distinct spatial extents, we conclude that they are located at two different crystallographic positions; most likely the smaller one is located in a layer nearer the surface and the other one in a layer deeper beneath the surface. Because these defects occur only in Ca-doped samples, we identify them as Ca-related defects.

The charge state of the defects can be inferred by observing the bending of the host bands caused by the Coulomb field surrounding a charged defect. A positively charged defect lowers the electronic energy level in its neighboring region, leading to a depression area in the STM topography of the filled states and an enhancement in the topography of the

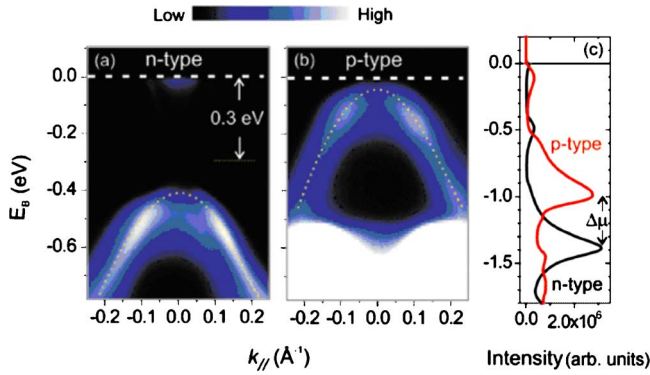


FIG. 2. (Color online) (a) The valence-band structure of *n*-type Bi₂Se₃ measured by ARPES near the Fermi energy and the Γ point of the Brillouin zone. The chemical potential (the Fermi level) is about 0.4 eV above the top of the valence band, about 0.3 eV above the surface Dirac point (Ref. 15). (b) The band structure of a Ca-doped Bi₂Se₃ crystal (Bi_{1.98}Ca_{0.02}Se₃) measured under similar conditions. The chemical potential is within 30 meV of the valence band. For (a) and (b), the Γ point is 0.0 on the horizontal axes and the band dispersions are shown in the $\pm M$ directions. (c) The momentum-selective DOS near the Γ point, compared for the *n*- and *p*-type crystals, covering a large binding energy range. A large shift of the chemical potential with Ca doping can be traced by considering the shift of DOS peaks in the valence band. The drop of the chemical potential by about 380 meV confirms the hole-doped nature of the Ca-doped samples.

unoccupied states. We expect this to be observed in imaging the ionized donors and the opposite effect for imaging negatively charged defects, such as acceptors. The clover-leaf-shape defects are surrounded by a region of enhancement in the topography of the filled states [Fig. 1(d)] implying that they are negatively charged, consistent with a Ca acceptor. A comparison between the triangular defect close to the center of the image in Figs. 1(c) and 1(d) shows a region of depression in the topography of the filled states [Fig. 1(c)], and hence implies the presence of a positively charged defect. This observation is expected for Se vacancies, which are known to be electron donors and in their ionized state be positively charged. Thus the STM data support the defect-chemistry model described above for Ca-doped Bi₂Se₃, with the added observation that the concentration of defects in general is lower in the Ca-doped samples than for native Bi₂Se₃.

The ARPES data showing valence-band energy-dispersion curves in the vicinity of the Γ point of the Brillouin zone for *n*- and *p*-type Bi₂Se₃ are presented in Figs. 2(a) and 2(b). For the *n*-type crystal, the valence band is clearly observed below E_F , as is a small pocket of the conduction band near the Γ point. For the *p*-type crystal, only the valence band is observed. This chemical-potential shift indicates that the Ca-doped crystal is hole doped relative to the *n*-type Bi₂Se₃ crystal. In the *p*-type doped samples, the surface-state bands are not observed, indicating that the Fermi level is below the energy of the Dirac point. Judging from the position of the strongest valence bands, the energy dispersion curves through the Γ point show that the chemical potential in *p*-type Bi_{1.98}Ca_{0.02}Se₃ is shifted by approximately 400 meV

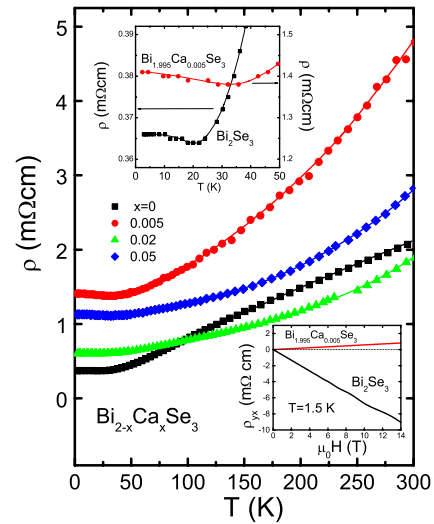


FIG. 3. (Color online) Temperature-dependent resistivity between 2 and 300 K in the *ab* plane of single crystals of Bi₂Se₃ and Ca-doped variants. The stoichiometric material is *n* type and the Ca-doped materials are all *p* type. The upper inset shows the resistivities in the low temperature regime. The lower inset shows the Hall-effect data employed to determine the carrier concentrations for undoped Bi₂Se₃ and one Ca-doped crystal.

relative to the *n*-type crystal [Fig. 2(c)]. Lower hole-doping levels, which would be obtained by tuning the Ca concentration, are expected to lead to materials whose chemical potential is very close to the Dirac point and, therefore, is of interest in fundamental and applied studies of the topological surface states.¹⁵

The 2–300 K resistivities in the *ab* plane for undoped Bi₂Se₃ and Bi_{2-x}Ca_xSe₃ crystals for $x=0.005$, 0.02, and 0.05 are shown in Fig. 3. All show the weakly metallic resistivities commonly seen in high carrier-concentration small band-gap semiconductors, with resistivities in the 0.3–1.5 mΩ cm range at temperatures near 10 K. The lightly doped $x=0.005$ material is *p* type with a carrier concentration at room temperature determined by Hall-effect measurements (lower inset, Fig. 3) to be approximately $1 \times 10^{19} \text{ cm}^{-3}$. This crystal has a resistivity ratio $\rho_{300}/\rho_{4.2}$ of about 3, as does the undoped *n*-type crystal. The upper inset shows the low temperature resistivity region in more detail for *n*- and *p*-type crystals. The decreasing resistivity seen on cooling is arrested at these low temperatures and rises slightly below 20–30 K. The Hall resistivity does not change appreciably below 20 K, suggesting that the carrier concentration is essentially constant in this temperature regime. Quantum oscillations have been observed in the resistivity for both crystals. The period of the oscillations allows k_F (the Fermi wave vector) to be determined and combined with the measured resistivity, the metallicity parameters at 4 K can be estimated as $k_FL=13$ and 113 for the *p*-type and *n*-type crystals, respectively. This yields mean-free paths L of 18 and 370 nm, respectively, well within the metallic regime. Thus the origin of the resistivity upturns cannot yet be determined.

The corresponding *ab*-plane Seebeck coefficients are shown in Fig. 4. The room temperature Seebeck coefficient for the *n*-type undoped Bi₂Se₃ crystal $-190 \mu\text{V K}^{-1}$ is large

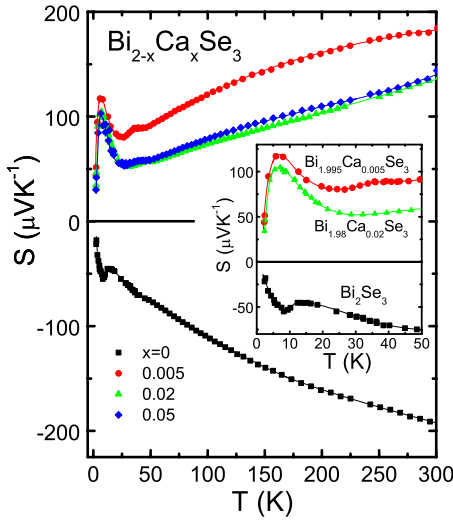


FIG. 4. (Color online) Temperature-dependent Seebeck coefficients between 2 and 300 K in the *ab* plane of single crystals of Bi_2Se_3 and Ca-doped variants. The inset shows the low temperature region for both pure and lightly Ca-doped Bi_2Se_3 . The undoped Bi_2Se_3 is *n* type, with a carrier concentration of $8 \times 10^{17} \text{ cm}^{-3}$ and the Ca-doped material with $x=0.005$ is *p* type with a carrier concentration of $1 \times 10^{19} \text{ cm}^{-3}$.

compared to those usually reported for this material, which are typically in the -50 to $-100 \mu\text{V K}^{-1}$ range.^{3–11} The carrier concentration for this *n*-type Bi_2Se_3 is $8 \times 10^{17} \text{ cm}^{-3}$ (lower inset, Fig. 3). The magnitude of the Seebeck coefficient decreases smoothly with temperature until around 15 K (inset, Fig. 4), where it becomes distinctly more negative in a small peak with an onset temperature roughly corresponding to that of the upturn in the resistivity. A similar peak in Seebeck coefficient has been observed previously in this temperature range in *n*-type Bi_2Se_3 .³ The *p*-type materials show similar but more unusual behavior. The room temperature Seebeck coefficient for the lightly doped *p*-type material is again very high, reaching approximately $+180 \mu\text{V K}^{-1}$. This value is larger than what is observed in the quaternary *p*-type $(\text{Bi}, \text{Sb}, \text{Pb})_2\text{Se}_3$ materials¹⁰ and remains large and *p* type over the full temperature range of measurement. Crystals with Ca-doping levels as low as $\text{Bi}_{1.9975}\text{Ca}_{0.0025}\text{Se}_3$ are *p* type. A dramatic low temperature peak in the Seebeck coefficient (inset, Fig. 3) is seen for all *p*-type compositions studied. The low temperature Seebeck coefficient peaks of -60 and $+120 \mu\text{V K}^{-1}$ for pure and doped Bi_2Se_3 at 7 K represent very high values when compared to other small band-gap semiconductors at this low temperature. Similarly anomalous low temperature peaks have been observed in $\text{Bi}_{1-x}\text{Sb}_x$ alloys near $x=0.07$,²¹ another material in the vicinity of a Dirac point.^{12–14} The narrow low temperature peak in S in Bi_2Se_3 is similar to that seen in elemental Bi, where it has been attributed to phonon drag.²²

The total thermal conductivities (κ) in the *ab* plane are shown in Fig. 5. They display the behavior typical of high-quality crystals, increasing with decreasing temperature as the phonon contribution to κ grows, until low temperatures, where the phonon mean-free path becomes comparable to intradefect distances. The low temperature regime for *n*- and

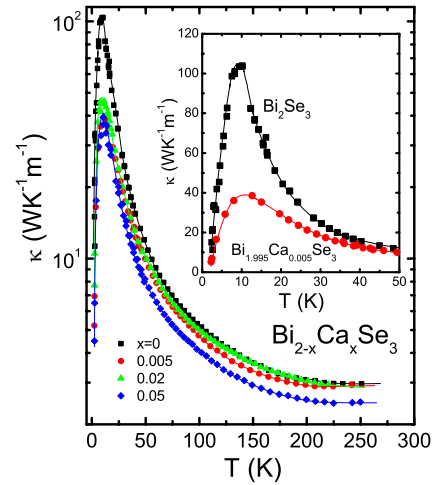


FIG. 5. (Color online) Temperature-dependent total thermal conductivities between 2 and 300 K in the *ab* plane of single crystals of Bi_2Se_3 and Ca-doped variants. The inset shows the low temperature region for both pure and lightly Ca-doped Bi_2Se_3 .

p-type crystals is shown in the inset. The thermal conductivity for the *n*-type crystal reaches the relatively high value of about $100 \text{ W K}^{-1} \text{ m}^{-1}$ at 10 K and all the Ca-doped materials show a somewhat lower maximum thermal conductivity in the $40\text{--}50 \text{ W K}^{-1} \text{ m}^{-1}$ range.

The efficiency of a material for thermoelectric cooling or power generation at temperature T is described by the thermoelectric figure of merit ZT .²³ The materials parameter is $Z=(S^2/\rho)(1/\kappa)$, where the power factor, defined as the square of the Seebeck coefficient S divided by the electrical resistivity, has been separated from the total thermal conductivity κ . Due to the very high thermal conductivities of the single crystals, the Bi_2Se_3 -based *n*- and *p*-type materials are of limited use as practical thermoelectric materials in single-crystal form, especially at low temperatures. The resulting low values of the thermoelectric figure of merit are shown in the inset to Fig. 6. The Seebeck coefficients and electrical resistivities do, however, suggest that these materials may have potential for use as thermoelectrics in the very low temperature regime. To illustrate this fact we have plotted the temperature dependences of the power factors in the main panel of Fig. 6. The anomalous low temperature peaks in all the materials, especially for the *p*-type material, where the power factor at 7 K is higher than it is at 300 K and comparable to that of the *n*-type material at 300 K, are particularly intriguing. The underlying origin of these peaks, and also the more subtle anomalies seen in the transport properties in the 30–40 K range in all materials, is not presently understood.

IV. CONCLUSIONS

Through consideration of the defect chemistry of Bi_2Se_3 , we have identified Ca as a dopant that when present in sub-percent quantities results in the formation of a *p*-type material. This result is of particular interest when compared to the fact that doping Bi_2Se_3 with Mn and Fe, also expected to be divalent, results in *n*-type material.^{24,25} The use of *p*-type

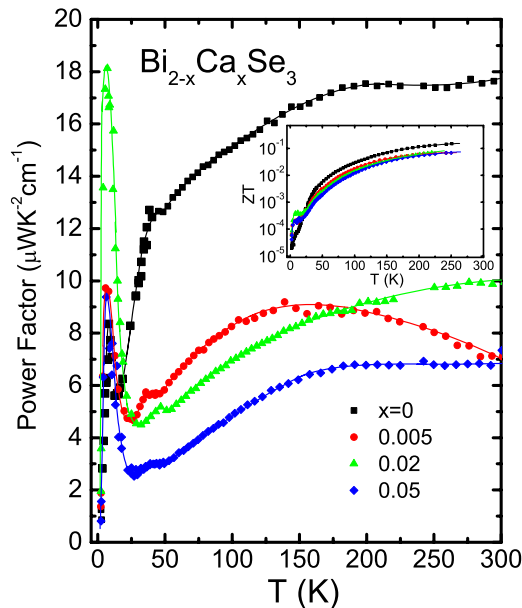


FIG. 6. (Color online) Temperature-dependent thermoelectric power factor between 2 and 300 K in the *ab* plane of single crystals of Bi₂Se₃ and Ca-doped variants. All materials show a peak at low temperatures but the peak in the *p*-type variant with 1% Ca-doping (Bi_{2-x}Ca_xSe₃ with *x*=0.02) is particularly dramatic. The inset shows the thermoelectric figure of merit in the same temperature range.

Bi₂Se₃ for the fundamental study of topological surface states and for devices based on these states for quantum computing will be of considerable future interest. The dramatic low temperature peaks found in the Seebeck coefficients in Bi_{1-x}Sb_x and Bi₂Se₃, materials that have strong spin-orbit coupling and nearby Dirac points,^{12–16,19} suggests that these characteristics may be related. In addition, processing of the microstructure of *n*- and *p*-type Bi₂Se₃ to reduce the thermal conductivity to the <1 W K⁻¹ m⁻¹ range typically observed for polycrystalline materials in this family, if it can be performed while maintaining the power factors observed in the current work, promises the possibility of low temperature thermoelectric applications. For the case of elemental Bi, where the low temperature peak in *S* has been attributed to phonon drag, it has been argued that the thermal conductivity cannot be degraded without concurrently degrading the Seebeck coefficient,²⁶ which may or may not be the case for Bi₂Se₃. Finally, the development of more sophisticated crystal-growth methods for lightly doped *p*-type Bi_{2-x}Ca_xSe₃ crystals will be of interest for the study of topological surface states.

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