Resonant inelastic soft x-ray scattering of CdS: A two-dimensional electronic structure map approach

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Resonant inelastic x-ray scattering (RIXS) with soft x rays is uniquely suited to study the electronic structure of a variety of materials, but is currently limited by low (fluorescence yield) count rates. This limitation is overcome with a high-transmission spectrometer that allows to measure soft x-ray RIXS "*maps*." The *S L*2,3 RIXS map of CdS is discussed and compared with density-functional calculations. The map allows the extraction of decay channel-specific "absorption spectra" giving detailed insight into the wave functions of occupied and unoccupied electronic states.

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I. INTRODUCTION

Since the first observation of resonant effects in soft x-ray fluorescence, $\frac{1}{1}$ resonant inelastic x-ray scattering [RIXS (Ref. $2)$ $2)$] with soft x rays has been successfully developed as a method to investigate the band structure of solids. $3-12$ $3-12$ Recently, RIXS was also used to study the electronic structure of liquids (e.g., water^{13[–15](#page-4-7)}). RIXS is a local technique: a wave function overlap between decaying valence electron and the spatially confined core hole is necessary, which gives information about the local distribution of the valence wave function with respect to the core hole wave function.

Due to the very small soft x-ray fluorescence yield and the small solid angle of high-resolution spectrometers, RIXS is a "low-count rate" technique. To date, this limits a RIXS series to a small number of spectra with selected excitation energies around the investigated absorption edge. We have recently developed a high-resolution, high-transmission soft x-ray spectrometer,¹⁶ which now allows recording complete RIXS "maps" in short time $(<1$ h). These "maps" display a two-dimensional intensity plot as a function of excitation *and* emission energy. They hence contain entire RIXS spectra for *each* data point in a conventional x-ray absorption spectroscopy (XAS) scan as well as decay channel-specific absorption spectra. We note that Agåker *et al.*[17](#page-4-9) presented soft x-ray emission data in a similar way, however, with a much wider step size and lower signal-to-noise ratio.

In this paper, we use the $SL_{2,3}$ emission of CdS to demonstrate the strengths of the RIXS map approach. CdS is one of the most important II-VI semiconductors and is used in various applications (e.g., thin-film solar cells, 18,19 18,19 18,19) nanoparticles, $20-22$ $20-22$ and light-emitting diodes²³). We show that the RIXS map approach substantially improves the extraction of band-structure information which is essential for an insight-based optimization of CdS-based devices in all of these applications. Especially if resonant effects are weak and nonresonant contributions dominate $\left[$ as is the case for CdS (Ref. [24](#page-4-15))] the dense two-dimensional plot makes it

much easier to identify dispersing features containing bandstructure information. Furthermore, the possibility to generate decay channel-specific XAS spectra opens a pathway to information about the local (spatial) distribution of the occupied and unoccupied states by comparing the map with density-functional theory calculations. Thus, we are able to separate L_2 and L_3 absorption spectra in spite of a spin-orbit splitting of only 1.2 eV.

II. EXPERIMENTAL AND THEORETICAL DETAILS

RIXS maps were recorded at Beamline 8.0.2 of the Advanced Light Source, Lawrence Berkeley National Laboratory, using a CdS(0001) single crystal (Mateck). The x-ray spectrometer is based on an entrance slitless design, a spherical collecting mirror, a variable line spacing grating, and a charge coupled device detector.¹⁶ The beam spot was \sim 20 μ m in the dispersive direction of the spectrometer resulting in a resolving power of >1000 . The beamline resolution was set to ≤ 150 meV at the *S L*₂₃ edge. With these settings, the transmission of our x-ray spectrometer is about 2 orders of magnitude higher than conventional x-ray spectrometers. This could be estimated based on a direct comparison (i.e., identical beamline parameters and flux) with the permanently installed SXF spectrometer at beamline 8.0.²⁵ The latter is a spherical grating spectrometer in Rowland geometry and is arguably one of the best soft x-ray spectrometers in the world. Emission and absorption energy scales were calibrated in accordance with our earlier measurements on CdS[.24](#page-4-15) The spectra within the map were normalized to the incoming photon flux which was measured with a gold mesh situated downstream of the last mirror of the beamline. An excitation energy step size of 0.1 eV was chosen. Theoretical RIXS maps were calculated based on the Kramers-Heisenberg formalism and density-functional theory using the local-density approximation (for more details see Ref. [24](#page-4-15)).

FIG. 1. (Color online) Experimental RIXS map of CdS. The emission intensity is color/grayscale-coded (see color scale/ grayscale in Fig. [2](#page-1-1)) and given as a function of emission energy and excitation energy. The upper panel shows a nonresonant x-ray emission spectrum (excitation energy: 175.3 eV). The right panel shows an absorption spectrum with fluorescence yield detection, i.e., the $SL_{2,3}$ emission intensity (integrated between emission energies of 133 and 159 eV) as a function of excitation energy.

III. RESULTS AND DISCUSSION

To demonstrate the strength of the RIXS map approach, CdS is a particularly suitable example since its $SL_{2,3}$ spectrum consists of several well-separated features that can be attributed to different decay channels[.24](#page-4-15)[,26](#page-4-17) As reported previously, band-structure information is difficult to obtain from "conventional" CdS RIXS, since the spectra are dominated by incoherent contributions, giving rise to only small resonant effects in the spectra.²⁴ The *S* $L_{2,3}$ map of CdS, recorded in 33 min, is shown in Fig. [1.](#page-1-0) Above the map, the nonresonant x-ray emission spectrum (excited at 175.3 eV) is plotted. The $SL_{2,3}$ emission spectrum consists of transitions from the S 3s-derived band (in the following "3s emission") around 148 eV, from Cd 4d-derived bands ("Cd 4d emission") at 150.7 and 151.9 eV, and from the upper valence band ("UVB emission," $154-160$ eV), into $2p$ core holes. $26-28$ Each of these transitions forms a doublet because of the spin-orbit splitting $[1.2 \text{ eV (Ref. 28)}]$ $[1.2 \text{ eV (Ref. 28)}]$ $[1.2 \text{ eV (Ref. 28)}]$ of the S $2p$ core hole, which is clearly visible in the sharp Cd 4*d* emission lines. In addition, we find a strong elastically scattered Rayleigh line at the position of the excitation energy (175.3 eV) and a broad feature around 191 eV that can be related to the emission of visible light. This visible light is emitted from the excitation spot on the sample and is (indirectly) reflected onto the detector (note that the energetic position of this feature is not correlated with the real energy of these photons).

On the right-hand side of the map in Fig. [1,](#page-1-0) the integrated intensity of the emission spectra (between 133 and 159 eV, i.e., excluding Rayleigh line and visible light) is plotted as function of excitation energy. This spectrum represents the

FIG. 2. (Color online) Top: calculated RIXS map of CdS. Bottom: contour lines of the calculated map and the corresponding experimental RIXS map of CdS.

(remarkably smooth) partial fluorescence yield XAS spec-trum which agrees well with previously published data.^{24[,26](#page-4-17)} The Rayleigh line is found as a diagonal line in the middle of the map representing the energy of the exciting photons. On the low-energy side of this feature, the $SL_{2,3}$ emission spectrum of CdS is found, while the high-energy side is dominated by the visible light signal. (A very weak feature associated with the Cd $M_{4.5}$ emission, excited and detected in higher orders, is also present at about 170 eV.)

In Fig. [2](#page-1-1) (top) the calculated RIXS map of CdS is shown on an expanded photon energy scale. The calculation includes experimental (Gaussian) broadening, but no further broadening due to lifetime effects. We find that the S 3*s* and Cd 4d emissions (left) exhibit no shift in energy since the dispersion of the corresponding bands is weak. In contrast, directly above the absorption edge the UVB emission (right) shifts to lower emission energies with increasing excitation energy. This shift, which reappears at the L_2 edge, can be explained by the downward dispersion of the uppermost valence band and the excitation energy-dependent shift of the excitation/emission process away from the Γ point.²⁴

This shift can also easily be identified in the (magnified) experimental map (Fig. [2,](#page-1-1) bottom) most obviously as a shift of the high-energy edge of the valence-band emission. Note that the experimental spectra are a sum of resonant (coherent) and nonresonant (incoherent) contributions and are dominated by the latter. In fact, in an earlier work by Zhou *et al.*, [26](#page-4-17) no resonant changes in the *L*2,3 emission spectra of CdS could be identified at all. This leads to the observation that in the experimental data the Cd 4*d* emission and the low-energy part of the UVB emission already appear at lower excitation energies than in the calculation which only represents the resonant (coherent) emission. This can also be clearly seen by the higher intensity near the onset of the experimental absorption scans compared to the calculated ones as will be discussed below. The unambiguous presence of dispersing features in the present experimental data demonstrates the power of the map approach to identify weak resonant features. By generating a contour plot of the calculated map and plotting it on top of the experimental map (see Fig. [2](#page-1-1)), we can now directly compare theory and experiment. We find a very good agreement of positions and intensity variations of the various features over the entire excitation energy range, validating the calculated band structure. In fact, this approach can be used to optimize the calculated band structure for less known materials to a degree that was previously impossible. Note that the theoretical map does not include the lifetime broadening that is present in the experiment (and that depends on the emission energy, i.e., that varies throughout the emission spectrum). Thus, the spectral features are more clearly seen in the calculated map as compared to the experimental.

The RIXS map approach also allows to studying the excitation energy-dependent intensity of selected decay channels. To date, partial fluorescence yield spectra are recorded with the total count rate from a selected energy window of an x-ray spectrometer. The RIXS map in Fig. [1](#page-1-0) represents an absorption scan (with an XAS-typical excitation energy step size) in which a high-resolution x-ray emission spectrum with good statistics is recorded at *each* excitation energy. This allows to deliberately choose specific spectral features to obtain an "absorption" scan for a particular decay channel (e.g., emission from a specific valence orbital/band). In the following, we will call such extracted spectra "absorption spectra" although such spectra are usually taken in an integrating mode.

In the present case, we can easily separate S 3*s* emission, Cd 4*d* emission, and emission from the UVB. Furthermore, with the exception of the UVB emission, we can distinguish between L_2 and L_3 emission, enabling us to plot a separate *S L*₂ and *S L*₃ absorption spectrum over the whole energy range, despite a spin-orbit splitting of only 1.2 eV. The separation of the different features (S 3s and Cd 4d emission peaks and their spin-orbit splitting) was performed as follows. Below the L_2 edge, it is easy to separate S 3s and Cd 4*d* emission, because the L_2 core hole is not yet "turned" on" and the separation between the L_3 -derived S 3s and Cd 4*d* emission is sufficiently large and can be fitted as shown in Fig. [3.](#page-2-0) For a more detailed decomposition of the *L*³

FIG. 3. Fit of the experimental data with four spectral components exemplarily shown at two excitation energies. Below each spectrum, the corresponding residuum is given.

emission see Ref. [17.](#page-4-9) Assuming that the peak shapes of the L_2 emission are very similar to those of the L_3 emission (which is supported by our calculations), we have shifted the two L_3 components (i.e., the S 3s and Cd 4d features, respectively) by the spin-orbit splitting of 1.2 eV to describe the L_2 emission. Each spectrum was then fitted with these four (2) \times 2) components using only the intensities as fit parameters. The resulting spectral decomposition is exemplarily shown for two different excitation energies in Fig. [3.](#page-2-0) The derived peak areas are used in the following to compile the decay channel-specific absorption spectra called "S 3*s*" and "Cd 4d" in the following). For the UVB emission, no separation into L_2 and L_3 is possible due to the presence of the dispersive features. Therefore, the (overall) fluorescence yield of the UVB emission was determined by integrating between emission energies of 154 and 161 eV (called "UVB" in the following).

The experimental L_3 and L_2 absorption spectra are shown in Fig. [4](#page-3-0)(a). The dashed line (labeled L_2^*) represents the L_2 spectrum shifted by 1.2 eV (i.e., the spin-orbit splitting) to lower excitation energies and multiplied by a factor of 2 (to account for the multiplicity of L_2 and L_3). One would expect the absorption spectra of both edges to be equal (if the multiplicities are taken into account). Indeed, the direct comparison between L_2^* and L_3 *qualitatively* shows the same features in both spectra. However, there are significant *quantitative* differences. For example, the absorption edge (labeled A) is weaker for L_2^* and is slightly shifted to higher energies. To understand the quantitative differences, the "competition" between L_2 and L_3 absorption has to be taken into account. Wherever strong L_3 absorption occurs, less photons are available for the L_2 absorption and vice versa. Since the L_3 absorption is about twice as strong, its impact on the L_2 absorption is stronger than the impact of L_2 on L_3 . A close look at the spectra shows that feature A for L_3 has its maximum at the absorption onset of L_2 , explaining the weaker and delayed absorption onset in the $L₂$ absorption. Similarly, feature B appears weaker and with a maximum at lower energies for \hat{L}_2^* than for L_3 , because feature C for L_3 appears at the high-energy side of feature B of L_2 , reducing its intensity and shifting the maximum to lower energies. This also leads to the fact that feature B of L_2^* is narrower than feature B of

FIG. 4. (a) Separated experimental L_3 and L_2 absorption spectra extracted from RIXS maps of CdS (solid lines). For comparison, the dashed line shows the magnified $(\times 2)$ L_2 spectrum after a 1.2 eV shift (L_2^*) . (b) Separated experimental absorption spectra of different decay channels ("UVB" corresponds to the upper valence-band emission intensity). (c) Calculated absorption spectra for the different decay channels. (d) Amplified difference spectra of the experimental spectra in (b) (shown as solid lines) and of the calculated spectra in (c) (dashed lines). (e) Energy dependence of the intensity of the emitted visible light. For comparison, the inverted $L_{2,3}$ emission intensity is shown as a dashed line (on an arbitrary intensity scale).

*L*3. All other differences between the two absorption spectra can be explained in a similar way.

In Fig. $4(b)$ $4(b)$, the $L_{2,3}$ absorption spectra of the different decay channels ("S 3s," "Cd 4d," and "UVB") are plotted versus excitation energy (after edge-jump normalization). We find very similar spectra for the three decay channels, except for a significant difference close to the absorption onset, which is observed and explained in the following. The RIXS intensity (described by the Kramers-Heisenberg formalism) depends on matrix elements containing the ground state, the intermediate state (i.e., a core hole and an electron in the conduction band), and the final state (i.e., a valence hole and an electron in the conduction band). Since the initial state and the ensemble of intermediate states are the same for all decay channels, the observed differences give insight into the transition matrix elements between intermediate and final states and thus into the wave functions of the unoccupied and occupied states (taking the operator describing the emitted photon into account). Indeed, our calculations in Fig. [4](#page-3-0)(c) similarly show a strong emission from the upper valence band and a weak Cd 4*d* emission near the absorption onset. Note that the calculated spectra have a smaller intensity close to the absorption edge due to the presence of a core exciton in the experiment, 24.29 which is not included in the calculation. For a direct comparison between theory and experiment, we have removed the spectral impact of the core exciton, by calculating difference spectra in which the absorption spectrum for the S 3*s* decay channel was subtracted from those of the UVB and Cd 4*d* emission, respectively (note that this approach assumes that the spectral contribution of the core exciton is independent of the decay channel in which it is observed). The good agreement of the experimental (solid) and theoretical (dashed) difference spectra near the absorption onset [Fig. $4(d)$ $4(d)$] validates the calculated wave functions and thus gives detailed local (spatial) information about the wave functions of the occupied valence *and* unoccupied conduction band states.

The visible light emission caused by the x-ray excitation of the sample also shows an interesting behavior. As apparent from Fig. $4(e)$ $4(e)$, it is proportional to the inverse $S L_{2,3}$ absorption. This is explained as follows: below the $SL₂$ absorption edge, the exciting x rays penetrate deep into the bulk, creating only Cd 4*s*, Cd 4*p*, and valence holes. Decay cascades of these holes, as well as decay and reabsorption processes of the photoexcited electrons, lead to fluorescence in the visible range. Once the excitation energy is high enough to excite S 2*p* electrons, the attenuation length of the x rays is strongly reduced [from 0.4 to 0.1 μ m (Ref. [30](#page-4-20))]. This reduces the probability of the mentioned decay processes because a larger fraction of the photoexcited electrons is produced closer to the surface. Effectively, the creation of valence holes is reduced, and hence the intensity of the visible fluorescence, which, in consequence, shows a minimum at all photon energies at which the $SL_{2,3}$ absorption shows a maximum.

IV. SUMMARY

We have presented a full resonant inelastic soft x-ray scattering map of CdS. We have demonstrated the advantage of the map approach when identifying even weak bandstructure-related features in very good agreement with our theoretical maps. For CdS, the RIXS maps also allow (a) the separation of the SL_2 and L_3 absorption spectra and (b) the extraction of decay channel-specific absorption spectra. These give insight into the wave functions of unoccupied states with respect to the decaying valence states. The RIXS map concept thus gives valuable detailed insight into the electronic structure of a variety of material systems that is not attainable with any other technique.

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