Hydrogen storage of calcium atoms adsorbed on graphene: First-principles plane wave calculations

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Based on first-principles plane wave calculations, we showed that Ca adsorbed on graphene can serve as a high-capacity hydrogen storage medium, which can be recycled by operations at room temperature. Ca is chemisorbed by donating part of its 4s charge to the empty π^* band of graphene. At the end the adsorbed Ca atom becomes positively charged and the semimetallic graphene changes into a metallic state. While each of the adsorbed Ca atoms forming the (4×4) pattern on the graphene can absorb up to five H₂ molecules, hydrogen storage capacity can be increased to 8.4 wt % by adsorbing Ca to both sides of graphene and by increasing the coverage to form the (2×2) pattern. Clustering of Ca atoms is hindered by the repulsive Coulomb interaction between charged Ca atoms.

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In order to develop an efficient medium of hydrogen storage, carbon-based nanostructures functionalized by transition-metal atoms have been a subject of active study.^{1–5} Recently, Yoon *et al.*⁶ demonstrated that covering the surface of C₆₀ with 32 Ca atoms can store 8.4 wt % hydrogen. Their result, which is crucial for safe and efficient hydrogen storage,⁷ inspired us to consider graphene as the substrate material for Ca atoms. Graphene is a precursor to C₆₀ and carbon nanotubes, but being a single atomic plane of graphite its both sides may be suitable for the adsorption of Ca atoms. Graphene by itself has been synthesized showing unusual electronic and magnetic properties.⁸

In this Rapid Communication, we showed that Ca atoms, in fact, can be bound on both sides of a graphene plane and each Ca atom absorbing four H₂ results in a medium of high-capacity hydrogen storage of 8.4 wt %. In the present case the binding energy of the fourth H₂ absorbed by Ca atoms is still significant and is ~ 300 meV. While each Ca atom donates part of its charge to the graphene layer, graphene, by itself, having a Fermi surface consisting of six points at the corners of the hexagonal Brillouin zone, is metallized. These results are obtained from our study based on first-principles calculations.⁹

We first consider the adsorption of a single Ca on the graphene as the substrate material. This is modeled by one Ca atom adsorbed on the hollow site (namely the H1 site above the center of the hexagon) for each (4×4) cell of graphene (namely, one Ca atom for every 32 carbon atoms). The Ca-Ca interaction is indeed negligible owing to the large distance of \sim 9.84 Å between them. A chemical bonding occurs between Ca and C atoms with a binding energy of 0.99 eV and Ca+graphene distance of 2.10 Å. Similar to the bonding mechanism of Ca on C₆₀, the Ca atom donates part of its charge from the 4s orbital to the π^* bands of graphene. Due to the formation of an electric field between Ca atom and the graphene layer, part of this charge is then back donated⁶ to the unoccupied 3d orbitals of Ca through their hybridization with π^* states. The resulting positive charge of the Ca atom is calculated to be ~ 0.96 electrons.¹⁰ The diffusion of the single Ca atom adsorbed on the graphene has to overcome relatively small energy barriers of Q=118 and 126 meV to diffuse to the top site (i.e., on top of the C atom) and bridge site (on top of the C-C bond), respectively. The Ca atom adsorbed on the top or bridge site becomes less positively charged (~0.89 and ~0.92 electrons, respectively).

A denser Ca coverage, which is energetically more favorable, is attained if one Ca is adsorbed on each (2×2) cell of graphene with a Ca-Ca distance of 4.92 Å. The Ca atom adsorbed on the top and bridge sites has a binding energy of 0.86 and 0.89 eV, respectively. However, energetically the



FIG. 1. (Color online) (a) Top-right panel: A (4×4) cell of graphene having four Ca atoms. As Ca at the initial position 0 is moved in the direction of the arrow, its z coordinate is optimized. The remaining three Ca atoms are fully relaxed. Beyond position 2 of the first Ca, the Coulomb repulsion pushes the second Ca atom in the same direction through positions 3', 4', and 5' to maintain a distance with the first Ca. Top-left panel: The variation of energy as the first Ca is moves through positions 1–5. (b) Bottom-right panel: Two Ca atoms adsorbed on each (4×4) cell of graphene with their initial positions 0 and 0'. As the first Ca moves from 0 to 1, the second one moves from 0' to 1' having the Ca-Ca distance of 3.74 Å, whereby the energy is lowered by ~ 0.176 meV. Two Ca atoms are prevented from being closer to each other and as the first Ca moves from 1 to 2-5 positions, the second one reverses its direction and moves through 2'-5' in the same direction as the first Ca atom. Bottom-left panel: The variation of the energy with the positions of Ca atoms.



FIG. 2. (Color online) (a) The (2×2) cell of graphene lattice and the energy band structure of bare graphene folded to the (2×2) cell. (b) Single Ca atom is adsorbed on the H1 adsorption site of the (2×2) cell of graphene, energy band structure, and the corresponding total density of states (dotted dark/blue curve) and partial density of states projected to Ca 3*d* orbitals (green/gray curve). Isosurfaces of the difference charge density $\Delta \rho$ with pink (light) and blue (dark) isosurfaces indicating charge accumulation and charge depletion regions. Isosurface charge density is taken to be 0.0038 electrons/Å³. (c) Similar to (b) (excluding the partial and total densities of states), but Ca atoms are adsorbed on both sides of graphene at the H1 and H2 sites. (H1+H3 configuration is also shown.) (d) Partial densities of states on H *s* (dark/red curve) and Ca 3*d* (green/gray curve) orbitals for two, three, and four H₂ absorbed in H1 configuration, and also isosurface of difference charge densities corresponding to 4H₂+Ca+graphene configuration. The zero band energy is set to the Fermi energy E_F .

most favorable adsorption site is found to be the H1 site, which is 2.15 Å above the graphene with a binding energy of 1.14 eV. Here, the Ca-Ca coupling is subtracted from the calculated binding energy. In this dense (2×2) coverage, a stronger electric field is induced between Ca atoms and the graphene layer, which, in turn, leads to a larger back donation of charge from the graphene layer to 3*d* orbitals of the Ca atom. Hence, by increasing Ca coverage from (4×4) to (2×2) , adsorbed Ca atoms become less positively charged, but their binding energy increases. As demonstrated in Fig. 1, even if it is energetically more favorable, the clustering of adsorbed Ca atoms is hindered by the Coulomb repulsion.

We next consider the double-sided adsorption of Ca. The binding energy of the second Ca atom for the double-sided adsorption with H1+H2 and H1+H3 configurations indicated in Fig. 2(c) is 1.27 and 1.26 eV, respectively. Since the repulsive Coulomb interaction between Ca atoms on the upper and lower parts of the plane is screened by the negative charge around graphene, the binding energy of the Ca atom in the double-sided adsorption is larger than that in the single-sided adsorption. It is also found that 3d orbitals of both Ca atoms have higher occupancies as compared with Ca atom in the single-sided adsorption. It is noted, however, that the partial occupancy of 3d orbitals of Ca atoms does not cause any magnetic properties in the system. Our results indicate that a stable and uniform Ca coverage up to Θ =12.5% (Θ =25%) can be attained for single-sided (doublesided with H1+H2 or H1+H3) adsorption forming a (2 $\times 2$) pattern.

Finite-temperature *ab initio* molecular-dynamics (MD) simulations have also been carried out for Ca adsorbed on the (2×2) graphene unit cell for H1 geometry. Simulations are performed by normalizing the velocities of the ions and increasing the temperature of the system gradually from 0 to 900 K in 300 time steps. The duration of time steps is inten-

tionally taken as 3 fs, which is relatively longer for a MD calculation. If the system is unstable, the geometry of the structure can be destroyed much easier in long time steps. While the bonding between adsorbed Ca atoms and the graphene layer is sustained, the adsorbed (2×2) Ca layer begins to diffuse on the graphene layer as the temperature of the system rises over ~300 K. However, no structural deformation is observed indicating that the Ca+graphene system is found to be stable up to 900 K within 300 time steps.

Other alkaline-earth metals, such as beryllium and magnesium, do not form strong bonds with graphene. Since Be has an ionization potential of 9.32 eV,¹¹ which is much higher than that of a Ca atom (6.11 eV), the charge of its 2s orbital cannot be easily transferred to the graphene layer. A similar situation occurs also with Mg having an ionization potential of 7.64 eV. Besides, the hybridization of π^* orbitals of graphene with the *d* orbital of a Ca atom, which is absent in both Be and Mg, plays an essential role in strong binding of Ca to graphene. However, Ti and Co form strong bonds [with binding energies of 1.58 and 1.20 eV for the (2×2) adsorption pattern, respectively].¹² The binding energies of Fe, Cr, and Mo are rather weak.

The above arguments related with the binding of Ca to graphene are confirmed by examining the band structure and the charge difference isosurfaces presented in Fig. 2. Both H1+H2 and H1+H3 adsorption configurations are included in our calculations because there is a small energy difference (H1+H2 structure is 26 meV more energetic.) between them. Hence, both adsorption configurations should be observable at room-temperature conditions. Charge difference isosurfaces are obtained by subtracting charge densities of Ca and bare graphene from that of Ca+graphene, namely, $\Delta \rho = \rho_{Ca+gr} - \rho_{Ca} - \rho_{gr}$. It is seen that there is a significant charge accumulation between the adsorbed Ca atom and graphene, which forms the ligand field. Partial occupation of 3*d* orbit-



FIG. 3. (Color online) Sites and energetics of Ca adsorbed on graphene with the (2×2) coverage and absorption of H₂ molecules by Ca atoms. d_c is the average C-C distance in the graphene layer. E_L is the binding energy of Ca atom adsorbed on H1 site, which is a minimum energy site. For H1+H2 or H1+H3 configuration, corresponding to double-sided adsorption, E_L is the binding energy of the second Ca atom and \overline{E}_L is the average binding energy. For H1, H1+H2, and H1+H3 configurations, E_1 is the binding energy of the first H₂ absorbed by each Ca atom; E_n (n=2-5) is the binding energy of the last *n*th H₂ molecule absorbed by each Ca atom; \overline{E}_n is the average binding energy of nH₂ molecules absorbed by a Ca atom. The last row indicates the sites and energetics of one Ca atom adsorbed on each (4×4) cell of graphene and absorption of H₂ molecules by each Ca atom. Only the (4×4) coverage can absorb five H₂ molecules. The shaded panel indicates energetically the most favorable H₂ absorption configuration.

als of Ca can be most clearly demonstrated by the projected density of states in Fig. 2(b). The empty π^* bands become occupied through charge transfer from 4s orbitals of adsorbed Ca and eventually get distorted due to $3d - \pi^*$ hybridization between 3d orbitals of Ca and the states of π^* bands as a result of the charge back donation process. Occupation of distorted graphene π^* bands gives rise to the metallization of semimetallic graphene sheets for all adsorption sites. It is also seen that charge density around graphene layer increased significantly as a result of double-sided adsorption of Ca. The increase in charge back donation to 3d orbitals becomes clear by the increased 3d-projected density of states below the Fermi level. Changing the adsorption configuration from H1+H2 to H1+H3 does not make any essential changes in the electronic structure. One notes that the position of Fermi energy and hence electron density can be monitored by the controlled doping of Ca atoms. The metallization process is also important for graphene nanoribbons, which form conductive interconnects and spintronic devices in the same nanostructure.^{12,13} It might be an interesting study to investigate the magnetic and electronic properties of Ca adsorption on graphene nanoribbons due to its different bonding mechanism.

We next study the absorption of hydrogen molecules by Ca atoms. A summary of energetics and geometry related with the absorption of molecular H_2 for H1, H1+H2, and H1+H3 sites for the (2×2) and H1 site for the (4×4) coverage is given in Fig. 3. The binding mechanism of H_2 invokes not only the adsorbed Ca atom but also the graphene

layer. In the case of single and double H₂ absorption, the absorbed molecules are parallel to graphene and all hydrogen atoms are equidistant from Ca atoms. As a result, both hydrogen atoms of each absorbed H₂ have the same excess charge of ~ 0.08 electrons. Once the number of H₂ absorbed by each Ca atom exceeded two, absorbed H₂ molecules tend to tilt toward Ca atoms because of increased positive charge of Ca atoms and the symmetry of the bonding configuration of H₂ molecules. The charges of Ca, H atoms closer to Ca, H atom farther from Ca, and graphene are calculated for the 8H₂+2Ca+graphene system corresponding to H1+H2 configuration in Fig. 3 to be \sim +1.29, \sim -0.06, \sim -0.11, and \sim -1.23 electrons. One hydrogen atom of tilted H₂, which is closer to Ca, has more excess charge than the other one. It is important to note that charges transferred to absorbed H₂ are not only from Ca atoms. Graphene atoms at close proximity also supply charge through the back donation process. At the end, ionic bonding through attractive Coulomb interaction between positively charged Ca and negatively charged H and weak van der Waals interaction are responsible for the formation of mixed bonding between H₂ molecules and Ca adsorbed on graphene. The above discussion is substantiated by the partial density of states in Fig. 2(d). The excess charge on H s and Ca 3d orbitals and their contribution to the states below the Fermi level increase with increasing number of H₂ molecules. Broadening of the molecular level of H₂ at \sim -9 eV indicates significant H₂-H₂ interaction that in turn increases the binding energy. In fact, the binding energy of the first H₂ molecule to the Ca atom which prefers to be parallel to the graphene layer is generally small. The average binding energy for two H₂ molecules which are again located parallel to the graphene layer and for three or more H₂ molecules which are tilted around Ca atoms is larger. We note that the adsorption of Ca atoms and also H₂ molecules slightly affect the underlying graphene lattice and C-C distance. The average C-C distance of bare graphene is increased from 1.41 Å upon adsorption of Ca and absorption of H₂ to d_c values indicated in all (2×2) structures in Fig. 3. Since Ca-Ca interaction is negligible in (4×4) structures, there is no variation in average C-C distance.

The maximum number of absorbed H₂ per adsorbed Ca atom is four for the (2×2) coverage yielding a H₂ storage capacity of 8.4 wt % and five for the (4×4) coverage of graphene. The reason why we include the (4×4) coverage even if the resulting gravimetric density is very low $(\sim 2.3 \text{ wt }\%)$ is to mimic the Ca-H₂ interaction in the absence of H_2 - H_2 interaction occurring in the (2 × 2) coverage. The fifth H₂ molecule can be bound to the top of the Ca atom in the (4×4) coverage with a significantly high binding energy. The other four H₂ molecules remain in quadrilateral positions around Ca. When we compare graphene with C_{60} ,⁶ we can conclude that C₆₀ with a single Ca adsorbed on the surface yields similar results with the (4×4) coverage on graphene. However, increasing adsorbed Ca coverage results in lower binding energies of absorbed H₂ molecules in the present case. Unfortunately, we cannot comment on the case of high Ca coverage of C₆₀ since Yoon et al.⁶ did not give details on the energetics of H₂ molecules in denser Ca adsorption. They have just emphasized that adsorption of 32 Ca results in full coverage of the C₆₀ surface and this structure can absorb up to 92 H₂ molecules with a binding energy of ~ 0.4 eV. Under these circumstances, a single Ca atom can hold only three H_2 molecules. In graphene structures, while the charge on (i.e., charge depletion or positive charge) Ca increases with increased number of the absorbed H_2 molecules, the electric field around Ca increases. This, in turn, results in a decrement in the distance between adsorbed Ca and polarized H_2 molecules. The charge on graphene decreases as well.

In conclusion, this Rapid Communication deals with two different subjects which are of current interest, namely, graphene and hydrogen storage. First, we showed that recently synthesized graphene with carriers behaving as massless Dirac fermions can be metallized as a result of the adsorption of Ca atoms. Electrons donated by Ca are accommodated by the π^* bands of graphene, which is partly back donated to calcium's 3d orbitals. Ca atoms can be bound to both sides of graphene and can attain 25% coverage without clustering. Second, we found that each adsorbed Ca can absorb up to four hydrogen molecules. At full coverage this yields a storage capacity of ~ 8.4 wt %, which is higher than the value set for feasible gravimetric density of hydrogen storage. The calculated bonding energies of hydrogen molecules are suitable for room-temperature storage, while above room temperature hydrogen molecules are released and Ca atoms remain adsorbed on graphene for further recycling. Even though storage capacities higher than the present case are achieved⁵ in different nanostructures, our results may be important for efficient hydrogen storage since graphene flakes are now easily available.

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and LDA result in very close atom configurations. Numerical results are acquired by using VASP [G. Kresse and J. Hafner, *ibid.* **47**, 558(R) (1993)]. A plane wave basis set with kinetic energy cutoff $\hbar^2 |\mathbf{k}+\mathbf{G}|^2/2m=900$ eV has been used. The Brillouin zone has been sampled by $(19 \times 19 \times 1)$ and $(9 \times 9 \times 1)$ special mesh points in **k** space for (2×2) and (4×4) graphene cells, respectively. In the course of structure optimizations, the convergence for energy is chosen as 10^{-6} eV between consecutive steps, and the maximum force allowed on each atom is less than 10^{-2} eV/Å. The pressure on the system is kept smaller than ~0.1 kbar per unit cell.

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