

Resonant x-ray scattering study of NpRhGa₅ and NpCoGa₅B. Detlefs,^{1,2,*} S. B. Wilkins,^{1,2,†} R. Caciuffo,¹ J. A. Paixão,³ K. Kaneko,⁴ F. Honda,^{4,‡} N. Metoki,⁴ N. Bernhoeft,⁵ J. Rebizant,¹ and G. H. Lander¹¹European Commission, JRC, Institute for Transuranium Elements, Postfach 2340, Karlsruhe D-76125, Germany²European Synchrotron Radiation Facility, BP 220, F-38043 Grenoble, France³Departamento de Física, Universidade de Coimbra, P-3004 516 Coimbra, Portugal⁴Advanced Science Research Center, Japan Atomic Energy Agency, Tokai, Ibaraki 319-1195, Japan⁵CEA Grenoble, DRFMC/SPSMS, F-38054 Grenoble, France

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We report a resonant x-ray scattering study of the antiferromagnetic neptunium compounds NpCoGa₅ and NpRhGa₅ at the Np *M*₄ and Ga *K* edges. Large resonant signals of magnetic dipole character are observed below the Néel temperatures at both edges. The signals at the Np edges confirm the behavior determined previously from neutron diffraction, i.e., moments along the *c*-axis in NpCoGa₅ and in NpRhGa₅ a reorientation of the moments from the *c*-axis direction to the *ab* plane. In the latter material, on application of a magnetic field of 9 T along the [010] direction, we observe a change in the population of different [110]-type domains. We also observe a magnetic dipole signal at the Ga *K* edge, similarly to the reported UGa₃ case, that can be interpreted within a semilocalized model as an orbital polarization of the Ga 4*p* states induced via strong hybridization with the Np 5*f* valence band. Quantitative analysis of the signal shows that the Ga dipole on the two different Ga sites follows closely the Np magnetic moment reorientation in NpRhGa₅. The ratios of the signals on the two inequivalent Ga sites are not the same for the different compounds.

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I. INTRODUCTION

The recent discovery of unconventional superconductivity in PuCoGa₅ and PuRhGa₅ (Refs. 1 and 2) with relatively high superconducting temperatures $T_c \sim 18.5$ and 8 K, respectively, has resulted in considerable interest in the electronic properties of materials with 5*f* electrons. Both experimental^{1–3} and theoretical^{4–7} studies indicate that magnetic interactions might be important for understanding the pairing mechanism in these compounds. Therefore, investigation of the related U and Np-115 compounds is of interest with respect to the general properties of the actinide (An) and transition metal (*T*) isostructural An*T*Ga₅. U*T*Ga₅ systems exhibit a variety of properties, ranging from Pauli paramagnetism in UCoGa₅ (Refs. 8–10) to antiferromagnetism in UNiGa₅.¹¹ On the other hand, Np*T*Ga₅ compounds all show strong magnetic ordering.^{12–18}

NpCoGa₅ and NpRhGa₅ crystallize in the tetragonal HoCoGa₅-type structure which belongs to the space group *P*4/*mmm* (No. 123), similarly to other actinide-based 115 compounds, including PuCoGa₅ (see Fig. 1). In this structure, actinide atoms occupy the 1*a* positions, transition-metal ions are in the 1*b* positions (halfway between the actinide atoms along the *c* direction), and there are two crystallographic positions for Ga: one atom in the center of the basal planes [1*c*, addressed as Ga(1) in this paper] and four atoms in the 4*i* position, in the rectangular faces of the unit cell [Ga(2)] with the position (0 1/2 *z*). The Ga(1) site has four nearest Np neighbors, whereas the Ga(2) site has only two. For NpCoGa₅, with $z=0.3103$,¹² the nearest Ga neighbors of Np are at 2.964 Å [Np-Ga(2)] and 2.997 Å [Np-Ga(1)]. In NpRhGa₅, with $z=0.2987$,¹⁹ the Np-Ga interatomic distances are very close for Np-Ga(1) and Np-Ga(2), namely, 2.964 and 2.963 Å, respectively.

For a diffraction experiment, this crystal structure has an important feature. Taking into account the magnetic propagation vector $\mathbf{q}=[0\ 0\ 1/2]$, a general magnetic diffraction peak of the type (*H*,*K*,*L* ± 1/2) will always have a contribution from the Ga(1) position, but Ga(2) will contribute only to reflections with (*H*+*K*)=even, allowing the possibility to observe Ga(1) signal separately at (*H*+*K*)=odd.

Resonant x-ray scattering (RXS) is a technique complementary to neutron diffraction for determining the magnetic structure of materials. In the case of actinides, the use of RXS presents an advantage over neutrons as significantly smaller samples can be studied, minimizing the safety restrictions imposed by the radiotoxicity of actinide isotopes.

In the RXS process, a photon is virtually absorbed by a core level electron, which is promoted into an empty valence band state. The virtual excited state (core hole + photoelectron) then decays under emission of the scattered photon. The sensitivity of RXS to magnetism and orbital ordering arises from the periodic variation of the density of

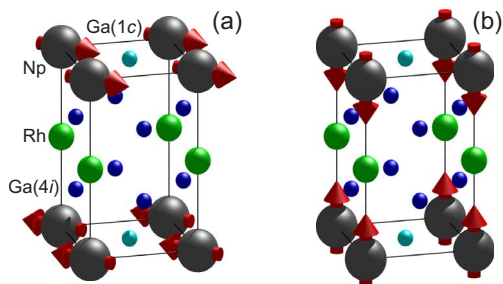


FIG. 1. (Color online) Crystal and magnetic structure of NpRhGa₅ at $T < T^*$ [panel (a)] and at $T^* < T < T_N$ [panel (b)] (Ref. 14). The magnetic structure of NpCoGa₅ is identical to the one of NpRhGa₅ at $T^* < T < T_N$ [panel (b)] (Ref. 13).

states near the Fermi level that are probed by the virtual photoelectron.^{20,21} The intensity of the superlattice reflections increases dramatically as the photon energy is tuned to the atomic absorption edge of the resonant ion. Information can be obtained by measuring the polarization-dependent scattering intensity at forbidden Bragg positions as a function of photon energy and azimuthal rotation angle (the angle describing the rotation of the crystal about the scattering vector). Direct information on the magnetic polarization of the Np $5f$ states is obtained at the Np M_4 and Np M_5 edges, as electric dipole transitions involve the promotion of a $3d$ core electron to an empty $5f$ state. Dipole transitions at the Ga K edge, on the other hand, involve the promotion of a $1s$ core electron of Ga to an empty $4p$ state.

Resonant scattering intensities with magnetic dipole symmetry at the K edge of nominally nonmagnetic ions, such as Ga, have been reported previously for uranium compounds where the U sublattice is magnetically ordered.^{22–24} The effect is related to the large spatial extent of $4p$ states within a broad energy band around the Fermi level making them sensitive to the electronic structure at neighboring sites. Although the $4p$ states of Ga are not spin-polarized, orbital polarization can be induced by hybridization with the U $5f$ states.^{25,26} To our knowledge, no previous reports have been made of a similar phenomenon in a Np compound. Since, in general, increased localization is anticipated when the number of $5f$ electrons increases, this is not an obvious result.

The present RXS investigations have been undertaken to meet the following main objectives: (a) Just below T_N in both materials, the moments are along the tetragonal c axis, and this result is unambiguous from neutron scattering.^{13,14} However, the rotation of the Np moments at T_N^* to the $[110]$ direction in the case of NpRhGa₅ (see Fig. 1) is less obvious and should be confirmed by RXS. (b) To explore the hybridization between the Np $5f$ and Ga $4p$ states, since this has not been performed for Np systems. (c) To establish the directions of the “dipoles” from this hybridization at both Ga sites and to determine the ratio of their magnitudes at the individual Ga(1) and Ga(2) sites. The latter is an advance over what was studied recently for isostructural U compounds.²³

II. EXPERIMENTAL METHODS

Single crystals of NpRhGa₅ and NpCoGa₅ were grown by a Ga self-flux method at the Institute for Transuranium Elements, in Karlsruhe. Samples with (100) and (001) surfaces were cut for the experiments and encapsulated in a copper container with a Be window for x-ray optical access.

Experiments were carried out on the magnetic scattering beamline ID20 at the European Synchrotron Radiation Facility, Grenoble, France. By tuning the undulators to their first or third harmonic, both Np M_4 edge ($E=3.846$ keV) and Ga K edge ($E=10.364$ keV) were reached. A liquid nitrogen cooled Si(111) double monochromator and two vertically focusing Si mirrors provided a beam of 0.4×0.4 mm² at the sample position.²⁷

Two distinct scattering geometries and different sample environments were used: for measuring the azimuthal depen-

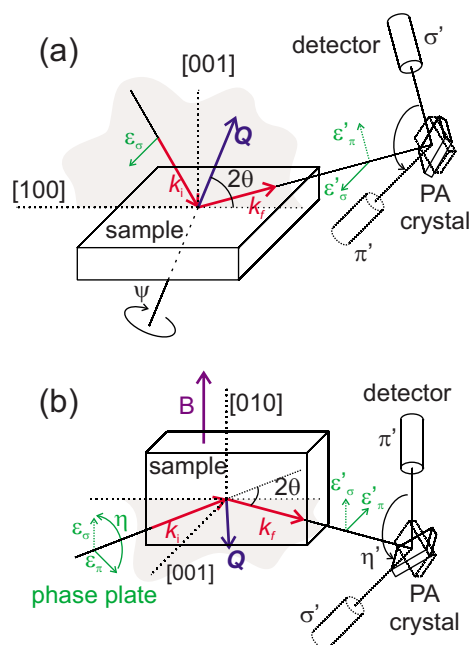


FIG. 2. (Color online) Coordinate system and polarization vectors relative to the incident and scattered beams.

dence of the superlattice peak intensity, the sample capsule was mounted in a ⁴He closed-cycle cryostat with base temperature of about 12 K. A vertical scattering geometry on a five-circle diffractometer with incident σ x-ray polarization was used [see Fig. 2(a)]. In an azimuthal scan, the sample rotates about the scattering vector, which implies a change of the angle between the incident electric field and the crystal axes. The resulting intensity oscillations give information on the symmetry and the orientation of the scattering tensor. In the vertical geometry, the instrumental setup does not support a heavy sample environment. The high magnetic field study on NpRhGa₅ was therefore performed in the second experimental hutch of ID20, using a horizontal geometry six-circle diffractometer equipped with a 10 T vertical split-pair superconducting magnet. In this geometry [Fig. 2(b)], the incident light polarization is π , i.e., with the electric field vector lying in the scattering plane. Due to the restrictions imposed by the 10 T cryomagnet, an azimuthal scan is not possible. A polarization scan, giving similar information as the azimuthal one, can be performed using a phase plate technique. Instead of rotating the sample, the incident light polarization η is turned from π to σ . A diamond phase plate of thickness of 100 μ m with a $[110]$ surface and the (111) Bragg reflection can be operated in the half-wave-plate mode so that the incident linear polarization can be rotated into an arbitrary plane by rotating the diamond crystal about the incident beam direction.^{28,29}

In all the scattering geometries, polarization analysis of the scattered beam was performed using the (111) reflection from a Au crystal for data at the Np M_4 edge and pyrolytic graphite (008) at the Ga K edge. These crystals, acting as polarization filters, were chosen because of their d spacings ($d_{(111)}^{\text{Au}}=2.3454$ Å, $d_{(008)}^{\text{PG}}=0.83860$ Å) that give Bragg diffraction close to the angle of 45° at the corresponding energies.

When the phase plate technique is used in the polarization scan, full polarization analysis of the scattered beam is necessary in order to determine the Stokes parameters P'_1 and P'_2 by fitting the measured intensity to the function

$$I' = \frac{I'_0}{2}[S + P'_1 \cos \eta' + P'_2 \sin \eta'], \quad (1)$$

where the angle η' describes the rotation of the polarization analyzer around the scattered beam and S is the leakage or component from the other polarized state. This arises due to the difference between the actual Bragg angle on the polarization analyzer and the ideal value of 45° .

From another point of view, P'_1 and P'_2 can be defined as

$$P'_1 = \frac{|E'_\pi|^2 - |E'_\sigma|^2}{|E'_\pi|^2 + |E'_\sigma|^2} \quad (2)$$

and

$$P'_2 = \frac{|E'_\pi + E'_\sigma|^2 - |E'_\pi - E'_\sigma|^2}{2(|E'_\pi|^2 + |E'_\sigma|^2)}, \quad (3)$$

where E'_σ and E'_π are the two components of the electric field vector of the scattered photons.³⁰ P'_2 is a measure of the phase relation between σ' and π' signals.

However, the polarization analysis is not complete as only the P'_1 and P'_2 components can be measured in this way, but a distinction between a depolarization and an occurrence of a circularly polarized component P'_3 can be made on the basis of experimental data and simulations because the degree of linear polarization $P'_{\text{lin}} = \sqrt{(P'_1)^2 + (P'_2)^2}$ is closely related to the total beam polarization $P' = \sqrt{(P'_1)^2 + (P'_2)^2 + (P'_3)^2}$. A real x-ray beam will have $P < 1$ (due to the finite efficiency of the phase plate) but it stays constant during a phase plate scan.

III. RESONANCE EFFECTS

For better understanding of the magnetism in these compounds, searches for RXS signals were performed at the Np $M_{4,5}$ and Ga K edges in both NpCoGa₅ and NpRhGa₅. Resonant signals were found at positions in the reciprocal space corresponding to the magnetic propagation vector $\mathbf{q} = [0 \ 0 \ 1/2]$, i.e., ordering wave vectors previously found by neutron diffraction.^{13,14} In both compounds, all resonant signals were $\sigma\pi'$ polarized, indicating that they arise from magnetic dipole order.

In NpCoGa₅, resonances were found both at Np M_4 and Np M_5 edges, with the former much stronger and with a maximum at 3.846 keV. Further data on the Np sublattice were recorded at this energy. Superlattice diffraction peaks corresponding to the propagation $\mathbf{q} = [0 \ 0 \ 1/2]$ were also found at the Co K edge (7.709 keV) but the energy dependence of the signal suggests that it is nonresonant in character.

The Np M_4 resonant spectra from both NpCoGa₅ and NpRhGa₅ are shown in the top panel of Fig. 3. The slightly different widths of the two curves are due to the different modes of data collection. The spectral shape of the curve for the Np M edges appears much as found in previous studies, a

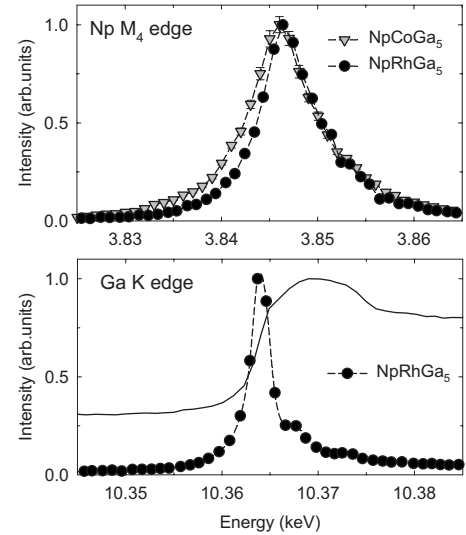


FIG. 3. Energy dependence of the resonant x-ray scattering signal in NpCoGa₅ and NpRhGa₅. Upper frame: Np M_4 data collected at $\mathbf{Q} = (0 \ 0 \ 2.5)$ (for NpCoGa₅) and $\mathbf{Q} = (0 \ 0 \ 3.5)$ (for NpRhGa₅). In the case of NpCoGa₅, the intensity corresponds to integration over θ scans; in the case of NpRhGa₅, only energy scans with fixed \mathbf{Q} were performed. Lower frame: Ga K -edge data recorded at $\mathbf{Q} = (0 \ 0 \ 6.5)$ for NpRhGa₅. All data were collected at base temperature ($T = 11.7$ K). The solid line in the lower panel represents the fluorescence spectrum at the Ga K edge in NpRhGa₅.

single Lorentzian signal with a full width at half maximum (FWHM) of ~ 8 eV (Ref. 31) showing that the resonances are, as expected, $E1-F^{[1]}$ in nature.³²

The Ga K -edge resonance is also similar to those found for uranium compounds,^{22,23} centered close to the absorption edge but with perhaps a small “bump” on the high-energy side. The energy width of the resonance in the Co compound was larger than in the Rh one by about 50%. This is a similar situation to that reported in UNiGa₅ and UPdGa₅,²³ where the $3d$ compound (UNiGa₅) has a larger width at the Ga K edge than the compound with the $4d$ transition-metal ion (UPdGa₅). As the magnetic structures of the two UTGa₅ compounds differ, the effects are more difficult to compare. However, taken together with the present data, they provide rare direct evidence for the influence of the transition metal on the valence bands and the magnetic exchange coupling.

IV. EXPERIMENTS USING THE RESONANCES

The large resonant enhancement at the Ga K edge observed in UTGa₅ compounds²³ is also present in the NpTGa₅ system, giving us the possibility to study, indirectly, the hybridization between the Np and Ga sublattices. Furthermore, the crystal structure of these compounds allows us to separate signals originating from two crystallographically inequivalent Ga positions in the lattice by examining different reflections with $(H+K)$ even and odd, which was not done in the case of the UTGa₅ systems.

A. NpCoGa₅

Figure 4 shows a comparison of the temperature dependence of Np M_4 and Ga K -edge signals in NpCoGa₅ in the

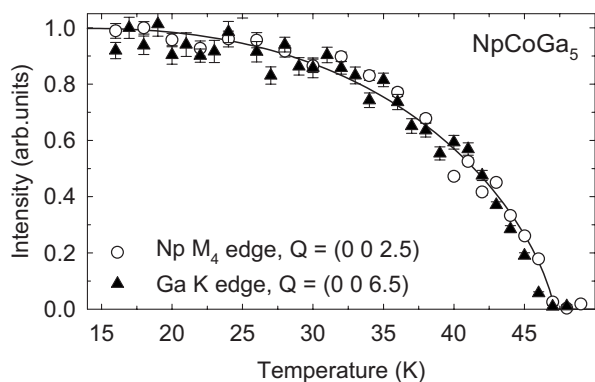


FIG. 4. Temperature dependence of the RXS signal in NpCoGa_5 at $Q=(0\ 0\ 2.5)$ at $\text{Np } M_4$ edge (open symbols) and at $Q=(0\ 0\ 6.5)$ at $\text{Ga } K$ edge (filled symbols). The solid line serves as a guide for the eye.

rotated polarization channel $\sigma\pi'$. In both cases, a specular magnetic Bragg reflection $(0\ 0\ L+1/2)$ is shown. For the $\text{Ga } K$ edge, this type of reflection includes contribution from the two crystallographically inequivalent Ga positions. The match in the temperature dependence of the two resonant signals indicates a common origin of the scattering process associated with the antiferromagnetic state. The Néel temperature T_N of $46.9(2)$ K deduced from our measurements is in good agreement with the previous bulk measurements¹² and neutron diffraction data.¹³ The $\text{Ga } K$ -edge data were collected with the primary beam attenuated by an $\sim 300\ \mu\text{m}$ aluminum foil corresponding to transmission of about 15%. Such an attenuation was found necessary to avoid local beam heating of the sample at the $\text{Ga } K$ edge.

The temperature dependence of the $\text{Np } M_4$ -edge signal in NpCoGa_5 was measured in more detail at $Q=(0\ 0\ 2.5)$ (see Fig. 5). Figure 5(a) shows the temperature dependence of the integrated intensity. From a parametric fit of the scaling law for magnetization, $I \propto M^2 \propto (-t)^{2\beta}$, where $t=(T-T_N)/T_N$, we deduce a value of $\beta=0.39(1)$, which is in good agreement with the value of $0.37(1)$ obtained from neutron scattering.¹³ Figure 5(b) shows the variation of the FWHM, which gives the critical exponent $\nu=0.66(8)$ relating the thermal variation of the correlation lengths in the paramagnetic state. Theoretical values for β and ν are 0.37 and 0.71 for the three-dimensional (3D) Heisenberg antiferromagnet, and 0.33 and 0.63 for a 3D Ising system.³³ Although our data on ν are not of sufficient accuracy to make a definitive statement, our experiments give little evidence for any special magnetic anisotropy (as would be the case for a 3D Ising system) in these materials.

The final frame [Fig. 5(c)] shows the change in the position of the magnetic diffraction peak. The small offset from 2.500 below T_N arises from a systematic error in the determination of the lattice parameter. As verified by measuring the charge $(0\ 0\ 2)$ reflection, this systematic error stays constant with temperature, so that the variation of the position between T_N and 48.5 K must be considered real even if it is only 2 parts in 10^3 . This shift of the peak in the paramagnetic state is not connected with the development of incommensurate fluctuations; otherwise, there would be a matching peak

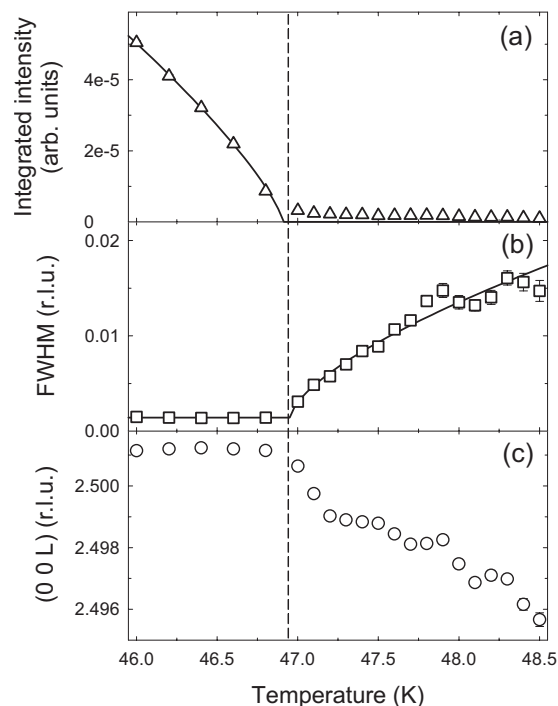


FIG. 5. Details of the temperature dependence of the RXS signal at the $\text{Np } M_4$ edge in NpCoGa_5 : (a) integrated intensity, (b) full width at half maximum, and (c) reciprocal space position of the $Q=(0\ 0\ 2.5)$ magnetic Bragg peak. The solid lines are fit to the data giving the β (upper panel) and ν (middle panel) critical parameters. T_N is marked as a dashed vertical line.

from the $(0\ 0\ 3)$ charge peak seen just *above* $(0\ 0\ 2.5)$. Instead, this is another observation of the so-called q shift.³⁴ Given the extremely good resolution of synchrotron x rays, especially at energies as low as the $\text{Np } M$ edges, this is relatively easy to observe with good crystals but is not yet understood.

Turning to the Ga resonance, the focus is on the direction of the apparent dipoles at the Ga sites and their relative magnitudes. Since in NpCoGa_5 , the Np moments are along the high symmetry direction of the structure, the c axis, at all temperatures, it is expected that any effective Ga dipole will be along this direction, as has been inferred by nuclear magnetic resonance–nuclear quadrupole resonance (NMR-NQR) experiments at the Ga sites.^{35,36}

For the direction of the dipoles, the most informative measurements in RXS experiments are those tracing the azimuthal dependence of the intensity in both $\sigma\sigma'$ and $\sigma\pi'$ polarization channels.^{32,37,38}

The $\text{Ga } K$ -edge resonant signal was present only in the $\sigma\pi'$ scattering channel, suggesting a magnetic-dipole-like origin of the scattering, as found previously for signals at the $\text{Ga } K$ edge.^{22,23} Collecting azimuthal scans in order to determine the direction of the dipoles on either of the Ga sites turned out to be experimentally difficult due to multiple scattering effects interfering with the signal. Such effects manifest themselves as spikes of high intensity in the data for certain values of azimuth and are more serious for larger energies (shorter wavelengths), which is the case at the $\text{Ga } K$ edge.

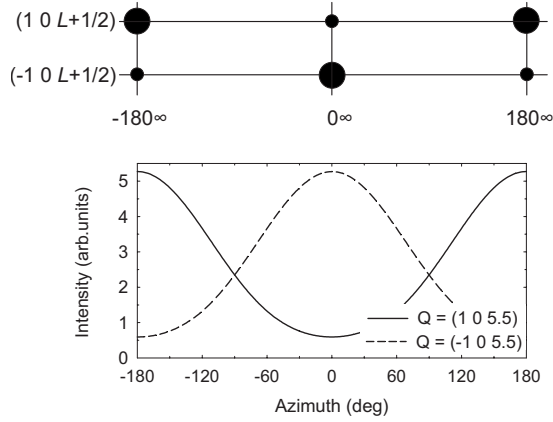


FIG. 6. Schematic representation of the intensity of azimuthal scans at reflections $\mathbf{Q}=(\pm 1 0 L+1/2)$ for NpCoGa₅ taken at the Ga *K* edge. Only Ga(1) contributes at this scattering vector. The large symbols in the top panel correspond to high measured intensity; the small circles correspond to low intensity. Lower panel: A simulated azimuthal scan for $\mathbf{Q}=(1 0 5.5)$ and $\mathbf{Q}=(-1 0 5.5)$ with effective Ga dipole moment parallel to [001].

Despite these experimental artifacts, a consistent picture may be given in which a schematic representation of the data, together with a simulated azimuthal dependence, is shown in Fig. 6. The observed intensities are represented in the top frame by large (small) points for high (low) intensity for the azimuthal angles shown. This pattern of intensities was found for a series of reflections with different *L* values. The lower frame of Fig. 6 shows the intensity of the $\mathbf{Q}=(\pm 1 0 5.5)$ reflections, calculated for an effective dipole moment along [001], as an example. In general, for a chosen $\mathbf{Q}=(H 0 L)$ reflection and the actual scattering geometry [see Fig. 2(a)], the azimuthal dependence for a signal originating from magnetic dipoles oriented along the [001] direction can be analytically written as

$$I_{\sigma\pi'} \propto |f_{\sigma\pi'}|^2 \propto \left| \frac{\sin \theta_{(H0L)} + \delta \cos \theta_{(H0L)} \sin \psi}{\sqrt{1 + \delta^2}} \right|^2, \quad (4)$$

where $\theta_{(H0L)}$ is the Bragg angle for the $\mathbf{Q}=(H 0 L)$, ψ is the azimuthal value, and δ is a parameter characterizing the off-specular nature of the chosen reflection, $\delta = \frac{Ha^*}{Lc^*}$. This means that, when going to higher values of *L* at fixed *H*, the difference between the 0° and ±180° changes less dramatically on approaching the [001] direction, parallel to the direction of the effective Ga magnetic dipoles.

For a fixed azimuthal angle, in this case $\psi=0$, we have made a study of the intensities at the Ga *K* edge for a series of reflections, both along the specular (0 0 *L*) and off-specular (1 0 *L*) directions. A comparison of these intensities allows a determination of the dipole signals associated with the Ga(1) and Ga(2) sites to be made. Recall that, because of the symmetry, Ga(1) contributes to *all* reflections and Ga(2) only to those with *H*+*K*=even.

Table I shows the comparison between the calculated and observed intensities of the resonant scattering signal in NpCoGa₅ at *T*=12 K at the Ga *K* edge. The calculated structure factors for both Ga positions are given ($f_{\text{Ga}(1)}$ and $f_{\text{Ga}(2)}$) as well as the resonant geometric factor $t_{\sigma\pi'}$.³² The calculated RXS intensity is corrected for the Lorentz factor $L=(\sin 2\theta)^{-1}$ and for an angular factor *A* that accounts for the fraction of the incident beam intercepted by the sample,

$$A = \frac{\sin(\theta + \alpha)\sin(\theta - \alpha)}{2 \sin \theta \cos \alpha}. \quad (5)$$

Here, α is an “asymmetry” angle, i.e., the angle between the specular direction and the scattering vector.³⁹

Given the often greater than 10% uncertainty in the observed intensities, the agreement between the observed and calculated intensities is reasonable, although there does appear to be a different scale factor needed between the specular and off-specular reflections. This is almost certainly due to absorption effects not properly accounted for, especially as the surface of the crystal was not polished (i.e., flat), even

TABLE I. Comparison of the calculated and observed intensities in NpCoGa₅. For details, see the text. The experimental uncertainties in parentheses refer to the last significant digit. $I_{\sigma\pi'}$ is the calculated intensity I_{calc} .

\mathbf{Q}	Calculations						Expt.	
	<i>L</i>	<i>A</i>	$f_{\text{Ga}(1)}$	$f_{\text{Ga}(2)}$	$t_{\sigma\pi'}$	$I_{\sigma\pi'}$	I_{expt}	$I_{\text{calc}}/I_{\text{expt}}$
(1 0 5.5)	1.145	0.2243	−2	0	0.4847	0.2419	2.4(3)	0.10(1)
(1 0 6.5)	1.050	0.2786	−2	0	0.5728	0.3839	3.2(4)	0.12(2)
(1 0 7.5)	1.004	0.3279	−2	0	0.6610	0.5752	5.0(5)	0.11(1)
(1 0 8.5)	1.013	0.3748	−2	0	0.7491	0.8525	6.0(5)	0.14(1)
(0 0 5.5)	1.179	0.2424	2	−2.152	0.4847	0.1933	1.3(3)	0.14(3)
(0 0 6.5)	1.065	0.2864	2	7.955	0.5728	0.9753	6.2(5)	0.15(1)
(0 0 7.5)	1.008	0.3305	2	−3.732	0.6610	0.3161	1.8(5)	0.17(5)
(0 0 8.5)	1.008	0.3745	2	−5.194	0.7491	0.3403	2.3(3)	0.14(2)

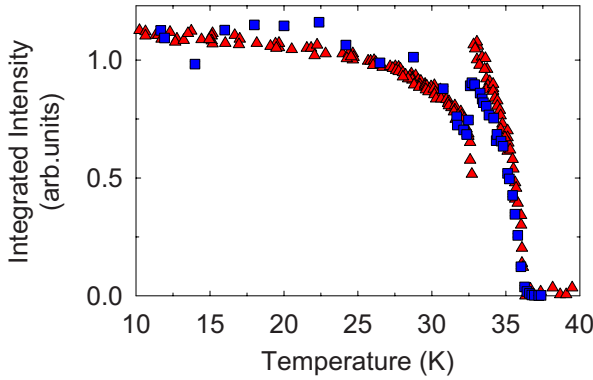


FIG. 7. (Color online) Comparison of the temperature dependence of the RXS with neutron-derived intensities (after Ref. 14) in NpRhGa₅. The RXS data (blue squares) from the (0 0 3.5) reflection taken at the Np M_4 edge are shown unaltered; the neutron magnetic moment is squared to be comparable with the intensities and multiplied by the geometrical factors involved in the RXS experiment (red triangles).

though the crystal quality was good. The best agreement, as shown in the final column of the table, for the (1 0 $L+1/2$) and (0 0 $L+1/2$) series of scattering vectors is for a ratio between Ga(1) and Ga(2) dipoles of

$$m[\text{Ga}(2)] = 0.14(2) \cdot m[\text{Ga}(1)]. \quad (6)$$

B. NpRhGa₅

The magnetic structure of NpRhGa₅ below $T_N = 37$ K is more complex than the one of NpCoGa₅ due to the magnetic phase transition occurring at $T^* = 32$ K where the Np magnetic moments reorient from the c -axis direction to lie in the basal ab plane (see Fig. 1), with their moments along $[110]$ and $[\bar{1}\bar{1}0]$ directions according to neutron scattering.¹⁴ This magnetic phase transition is accompanied by a discontinuous change in the magnetic moment amplitude, suggesting a change of the $5f$ electronic states.¹⁴

In our RXS experiment, we are able to test the conclusions of the neutron experiments in three different ways: first by examining the temperature dependencies of the intensities; second, by performing azimuthal scans; and third, by examining the polarization of the scattered photons to determine the domain population.

Figure 7 shows the temperature dependence of the RXS signal in NpRhGa₅ at the Np M_4 edge for $\mathbf{Q} = (0\ 0\ 3.5)$. The RXS signal is compared with the temperature dependence of the Np moment as deduced from neutron scattering by multiplying the moment (squared) by the relevant geometric scattering factors. Two effects are present in this simulation. The first is the growth of the moment as a function of temperature. This is taken from Fig. 5 of Ref. 14 and includes a discontinuity at T^* . The second is the reorientation of the moments at T^* that has a drastic effect on both the neutron and x-ray intensities. The good agreement between the neutron-derived and RXS intensity is the first indication that the envisaged model for the two magnetically ordered phases is correct.

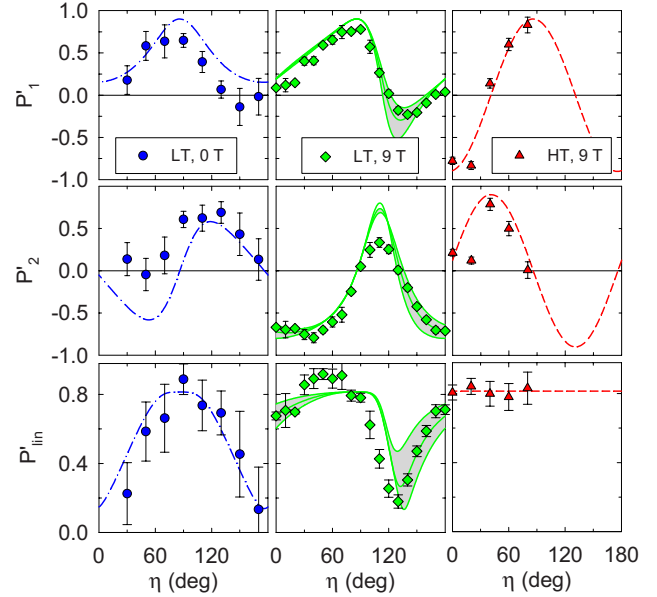


FIG. 8. (Color online) P'_1 , P'_2 , and P'_{lin} in the pseudoazimuthal dependence (a phase plate scan) of the Np M_4 -edge signal in NpRhGa₅ at $\mathbf{Q} = (0\ 0\ 2.5)$ at $T = 20$ K (denoted as LT) and 33 K (HT) with magnetic field $B = 9$ T $\parallel b$ axis. In the scan, the incident light polarization η is being rotated from the σ state ($\eta = 0^\circ$) through the π state ($\eta = 90^\circ$) back to the σ state ($\eta = 180^\circ$). All the zero-field data are recorded in the ZFC state. The dash-dot and solid lines correspond to the most probable model for the Np magnetic moments: equal population of the $[110]$ and $[\bar{1}\bar{1}0]$ domains for ZFC data at $T = 20$ K and an approximately 9:1 ratio for domain population at $B = 9$ T; the shaded area in the central panels are delimited by simulation curves for domain populations of 95:5 and 85:15, see text. In the HT phase, on the right-hand panels, the moments are along the $[001]$ axis.

The agreement shown in Fig. 7 is probably as good as can be expected between the two techniques and shows that the reorientation of the Np moments at T^* away from the $[001]$ axis certainly occurs. Small differences between the neutron and RXS results around T^* may arise from the lack of temperature stability in the RXS case or, more interestingly, because the scale factor relating the moment to the RXS signal *changes* at T^* . This might suggest a transition between two subtly different electronic states, as already suggested by Jonen *et al.*¹⁴ from their neutron experiments.

Although the moment direction in the high-temperature state, $T^* < T < T_N$, is clearly established as $[001]$, the situation below T^* is more complex as the moments can have any direction in the basal ab plane. The neutron experiments are interpreted with the moments along $[110]$ and $[\bar{1}\bar{1}0]$ directions, forming two domains. We therefore set out to confirm this using the new 10 T magnet facility available at ID20. Unfortunately, use of the heavy sample environment, such as the 10 T cryomagnet, makes azimuthal scans impossible so that phase plate scans, described in Sec. II, were necessary.

Figure 8 shows P'_1 , P'_2 , and P'_{lin} values measured at the Np M_4 edge in NpRhGa₅ as a function of polarization direction η of the incident light. The data were recorded at $\mathbf{Q} = (0\ 0\ 2.5)$ at $T = 20$ K [i.e., at $T < T^*$, denoted as low tem-

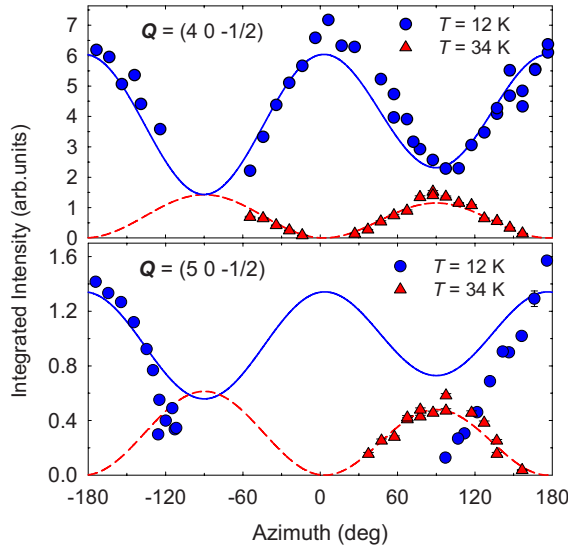


FIG. 9. (Color online) Azimuthal dependence of the Ga K -edge resonant signal ($\sigma\pi'$ channel) at two scattering vectors $\mathbf{Q}=(4\ 0\ -1/2)$ and $\mathbf{Q}=(5\ 0\ -1/2)$ at $T=12$ and 34 K. Lines correspond to the model described in the text.

perature (LT)] and 33 K [i.e., at $T^* < T < T_N$, denoted as high temperature (HT)] in both zero-field state and with magnetic field $B=9$ T applied along the b axis. Although the zero-field data were not measured with high statistics (the error bars correspond not only to the errors coming from the integration of the analyzer rocking curves but also from the fit to the Stokes function [Eq. (1)]), they agree with the model shown in blue solid line—equal population of domains with Np magnetic moments along $[110]$ and $[1\bar{1}0]$ directions. Comparison of the zero-field data and the 9 T data in the $T < T^*$ (LT) phase (blue circles and green diamonds) shows the magnetic field effect: the domain population for the 9 T LT phase changes to 90% $[110]$ domains vs 10% $[1\bar{1}0]$ domains, indicating that the applied magnetic field of 9 T is insufficient to induce a single domain, although it goes a long way to establish such a monodomain state. The choice of $[110]$ over $[1\bar{1}0]$ is a result of the field not being exactly along the $[010]$ direction, i.e., a small misorientation of the crystal.

The difference between the lower panels for the LT state shows that we are particularly sensitive to the direction and the domain population with this technique. The difference in the values of P'_{lin} and the measured value $P=0.81(2)$ is the result of *depolarization* of the scattered photon beam, which can only occur if domains with different scattered beam polarizations contribute to the total signal. For a single domain state (e.g., the HT state), there is no depolarization, and the linear scattered component is the same as the incident component, i.e., $P'_{\text{lin}}=P$. It is thus interesting to observe the minima in P'_{lin} . For an equal domain state, the minima occur at the symmetric positions $\eta=0^\circ, 180^\circ$, whereas as the domain population changes, the minima in P'_{lin} also change. The shaded simulations are for models with domain populations of 95:5 and 85:15. The most probable domain population appears to be 90:10 at $B=9$ T. The HT phase (represented by red triangles in Fig. 8) data can be fitted to the Np

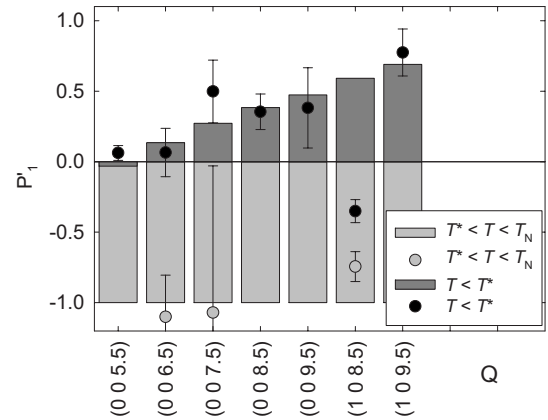


FIG. 10. Stokes parameter analysis for NpRhGa₅ at the Ga K edge. In the high-temperature phase, $P'_1=-1$ for all reflections; the measured values are indicated with open points. In the low-temperature phase ($T < T^*$), the calculated values are given by the height of the bar graphs, with the measured values as closed circles. The measurements are for $B=0$ T, so an equal domain population model is assumed.

magnetic moments pointing along the $[001]$ direction even when magnetic field of 9 T is applied along the b axis, which is consistent with the known phase diagram in a magnetic field.⁴⁰

The sensitivity of the polarization of the scattered particle to the moment direction and domain population is also exploited in spherical neutron polarimetry (SNP).⁴¹ In both cases, the information may be obtained from a *single* reflection rather than the standard technique of comparing intensities of a number of different reflections.⁴² However, the x-ray technique may be used in a magnetic field, whereas the nature of the neutron interaction with a magnetic field restricts the SNP technique to zero applied field. Clearly, this is a considerable advantage when the domain population, as well as possibly the moment directions, can be changed by the application of a magnetic field.

Turning now to the Ga K -edge spectra, in Fig. 9, we show the results for two reflections in zero applied field but at different temperatures, above (triangles) and below (circles) the reorientation transition at T^* . Only Ga(1) contributes to the signal at $\mathbf{Q}=(5\ 0\ -1/2)$ but contributions from both Ga sites are present at $\mathbf{Q}=(4\ 0\ -1/2)$. In the HT state ($T=34$ K), the Ga dipoles are assumed to point along the $[001]$ axis and the agreement for both reflections with the model is acceptable.

The intensities at the Ga K edge clearly scale approximately as the moment on the Np site, which changes considerably below T^* , mostly because of the thermal effects as $T_N \sim 36$ K, but there is also a discontinuity in the moment itself.¹⁴ In the LT state, there are some discrepancies with the model, but they are attributed to difficulties in measuring the intensity as a function of azimuthal angle over such a large azimuthal range. The domain population has been assumed as 50:50, corresponding to the zero-field cooled (ZFC) state discussed in connection with Fig. 8.

The method of determining the Stokes parameters as used in Fig. 8 for the Np M_4 resonance was used also for the Ga K

TABLE II. Comparison of the calculated and observed intensities in NpRhGa₅ in the LT phase. For details, see the text and Table I for notation. The experimental uncertainties in parentheses refer to the last significant digit.

Q	Calculations							Expt. I_{expt}	$I_{\text{calc}}/I_{\text{expt}}$
	L	A	$f_{\text{Ga}(1)}$	$f_{\text{Ga}(2)}$	$t_{\pi\sigma'}(110)$	$t_{\pi\sigma'}(1\bar{1}0)$	$I_{\pi\sigma'}$		
(0 0 6.5)	1.065	0.2864	2	7.467	-0.618	-0.538	2.782	54(1)	19.4(4)
(1 0 7.5)	1.004	0.3279	-2	0	-0.448	-0.376	0.225	4.1(2)	18(1)
(1 0 9.5)	1.113	0.4200	-2	0	-0.296	-0.245	0.138	3.0(2)	22(1)

edge and can confirm the reorientation of the Ga dipoles as suggested by the results and modeling in Fig. 9. In the case of the Ga K -edge resonance, there is difficulty in making the integration of the analyzer crystal because strong inelastic scattering, associated with the $K\alpha_1$ and $K\alpha_2$ emission lines at about 1000 eV below resonance, can affect the measurement of the integrated intensities, and thus P'_1 and P'_2 . We show the results for P'_1 in the two states for a number of different reflections in Fig. 10.

In the HT state, $I_{\pi\pi'}=0$ exactly for the specular reflections and it is almost zero for off-specular ones due to the azimuth value given by the direction of magnetic field with respect to the sample. From this and from the definition of P'_1 [Eq. (2)], it follows that $P'_1=-1$ for all specular reflections and it is very close to -1 for off-specular ones. Although the P'_1 was not measured at all reflections shown in Fig. 10, subsequent temperature dependence curves on these reflections confirmed the absence of the $\pi\pi'$ channel signal.

At the moment reorientation temperature T^* , some of the intensity is transferred into the $\pi\pi'$ channel so that in the LT state, the sign of P'_1 changes and approaches $+1$ as the ratio $I_{\pi\pi'}/I_{\pi\sigma'}$ increases with increasing scattering angle $\theta_{(H0L)}$ and decreasing off-specularity δ . The agreement between the experimental and calculated P'_1 values indicate that the direction of the moments on both Ga(1) and Ga(2) follows that of the Np magnetic moment. Recall that both Ga sites contribute to the reflections with $(H+K)=\text{even}$, but only the Ga(1) contributes to reflections with $(H+K)=\text{odd}$.

Similarly to the case of NpCoGa₅, intensities of several reflections must be compared in order to estimate the ratio between amplitudes of the Ga(1) to Ga(2) dipoles. Table II shows this comparison in the LT phase, i.e., when model with dipoles pointing along the $[110]$ directions and an equal domain population is considered. The calculated structure factors for both Ga positions are given ($f_{\text{Ga}(1)}$ and $f_{\text{Ga}(2)}$) as well as the resonant geometric factor $t_{\sigma\pi'}$, calculated for the azimuthal angle $\psi=-86.06^\circ$ with respect to the $[010]$ azimuthal reference. The best agreement, as shown in the final column of the table, gives

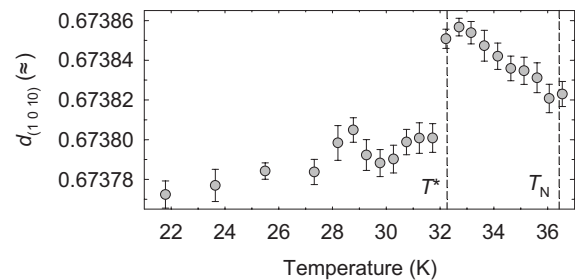
$$m[\text{Ga}(2)] = 0.43(4) \cdot m[\text{Ga}(1)]. \quad (7)$$

A similar analysis in the HT phase was not performed because of difficulties due to the limited stability temperature range of this phase.

Finally, we also address the question of a possible lattice distortion in NpRhGa₅. Onishi and Hotta⁴³ examined the role of orbital degrees of freedom in determining the magnetic

behavior of NpTGa₅ compounds, based on a j - j coupling scheme previously used to address the properties of UTGa₅ and PuTGa₅ compounds.⁴⁴ A theory based on the doublet-singlet crystal field model⁴⁵ predicts a ferroquadrupolar order (FQO) in this compound. A homogeneous quadrupolar moment $\langle O_{xy} \rangle$ should be accompanied by an orthorhombic lattice distortion below T^* . The only possible allowed subgroup consistent with this FQO is $Cmmm$ (No. 65), corresponding to a distortion of the tetragonal ab plane along the $[110]$ and $[1\bar{1}0]$ axes. Concomitantly, the primitive tetragonal lattice is converted into an orthorhombic C -face centered lattice where the orthorhombic a and b axes are the $[110]$ and $[1\bar{1}0]$ diagonals of the tetragonal unit cell, and the tetragonal and orthorhombic c axes coincide. The orthorhombic distortion should split reflections of the (HKL) type with $H, K \neq 0$. Since the magnetism of this material requires that the $[001]$ axis be in the scattering plane, because reflections have $(HKL \pm 1/2)$ indices, we have not performed experiments in the $(HK0)$ plane, so a definitive answer as to whether this distortion appears at T^* cannot be given.

Using a Ge(111) analyzer to improve the resolution of the spectrometer, we have examined reflections of the $(H0L)$ form and in Fig. 11, we show the change of the lattice d spacing as a function of temperature for the (1010) reflection. A θ - 2θ scan through the (1010) reflection was done at each temperature and the θ value at the maximum intensity converted to equivalent d spacing. These experiments were done in the configuration with $B=9$ T in an attempt to have a majority domain population, which can often lead to a clearer understanding of any possible lattice distortion associated with the magnetic ordering. The d spacing of the studied reflection is principally sensitive to the c -axis length. There is no apparent change at T_N as expected for a second-order phase transition,⁴⁶ but a small change corresponding to


 FIG. 11. Temperature dependence of the d spacing $d_{(1010)}$ for the $Q=(1010)$ reflection in NpRhGa₅ at $B=9$ T \parallel b axis.

$\Delta c/c \sim 1.3 \times 10^{-4}$ occurs at T^* . This is probably a magnetostrictive effect when the moments move away from the [001] axis, but a more complete study with different orientations of the crystals is necessary to draw firm conclusions. There was no sign of any “two-peak structure” in the scans at low temperature.

V. DISCUSSION AND CONCLUSIONS

Our main objective in these studies of NpCoGa₅ and NpRhGa₅ has been to confirm the results of the neutron experiments on the same materials and to see to what extent the RXS technique can bring additional information on the hybridization between the Np 5*f* and other electron states. From the shape of the Np resonances and their azimuthal dependencies, there is no sign of any quadrupole contribution, as was found, for example, in NpO₂ (Ref. 37) and UO₂.³⁸ Quadrupole ordering may, of course, occur at a different wave vector as compared to the magnetic scattering, but the shape of the resonances (Fig. 3) argues that the moments are strictly dipole in nature. Ferroquadrupolar ordering, as predicted by Kiss and Kuramoto⁴⁵ for low-temperature phase of NpRhGa₅, occurs at the position of the charge reflections, and is thus difficult to observe. However, via coupling to the lattice, it should give rise to a lattice distortion, which we have not observed.

With respect to the resonances at the Ga *K* edge, we have shown that the phenomenon of a strong resonance exists in Np as well as U compounds. As far as our experiments can determine, the effects are wholly induced by the polarization of the Np moments. For both the temperature dependence (Figs. 4 and 7) and the direction, the apparent Ga dipoles (Figs. 6, 9, and 10) follow that of the Np moments.

By analyzing the polarization of the scattered photon beam and determining the Stokes parameters (Figs. 8 and 10), we show that the technique is extremely sensitive to the direction of the moments as well as the domain population. As shown in Fig. 8, this information may be deduced from a single reflection even when a magnetic field is applied. In the case of a similar technique in neutron scattering,^{41,42} the same information may be deduced, but the technique is restricted to zero applied field.

We have examined, briefly, the possibility of a lattice distortion at T^* in NpRhGa₅. An effect is observed but this is probably a magnetostrictive change in the *c* lattice parameter. No effect, at least in the *c* axis, is observed at T_N . Our experience has been that when a lattice distortion occurs, at least *two* peaks are seen with the high resolution available with synchrotron *x* rays, and this is not the case. The FWHM of the lattice peak changes by only a small amount between the LT and HT states, suggesting strain effects rather than a lattice distortion.

Finally, with respect to hybridization, we have deduced the ratios of the dipoles at the Ga(1) site as compared to those at the Ga(2) site (see Fig. 1 for the structure). In the case of NpCoGa₅, the ratio of the signals Ga(1)/Ga(2) ~ 7 ,

whereas in NpRhGa₅, it appears closer to about a third of this value, i.e., ~ 2.5 . Given that the nearest neighbor configuration of the Ga(1) has four equidistant Np atoms in a ferromagnetic configuration, compared to two Np neighbors for the Ga(2) site, we would already expect a factor of 2 in the relative transferred field. In the case of the Co compound, the distances for the Ga(1)-Np and Ga(2)-Np are 2.96 and 3.00 Å, respectively. These same distances are equal at 2.96 Å in the Rh compound. To a first approximation, we may discount these small differences in distance and would expect the hybridization to be similar in the Co and Rh compounds, whereas it is not experimentally.

Comparisons may be also made with the hyperfine coupling constants as deduced in the experiments with NMR-NQR. The directions of the Ga dipoles can be obtained from this technique, as shown by Ohama *et al.*⁴⁷ For NpCoGa₅, Sakai *et al.*³⁶ gave an isotropic hyperfine coupling constant of 46 kOe/ μ_B for Ga(1) and 36 kOe/ μ_B for Ga(2). However, since the hybridization in the RXS case involves the polarization of the Ga 4*p* orbitals, which are anisotropic, it may be more appropriate⁴⁸ to compare the *anisotropic* part of the hyperfine coupling constant, and in this case, the values are 13 kOe/ μ_B for Ga(1) and 4 kOe/ μ_B for Ga(2). This ratio is in rough accord with our measurements, since the RXS result should be divided by 2 to normalize for the number of Np nearest neighbors. No NMR-NQR experiments have yet been reported on NpRhGa₅. So far, no calculations have been performed of the possible signals at the Ga *K* edges in these 115 materials, but there seems sufficient information at this stage, together with the previous work on U-115 compounds,²³ to encourage such theoretical efforts. Both the shapes of the resonances, which are different between NpCoGa₅ and NpRhGa₅ (see discussion connected to Fig. 3), and the differing ratios of the Ga(1)/Ga(2) dipole strengths suggest that the transition-metal *d* states play a significant role in the physics of these compounds and do not simply act as “spacers.”

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