Transport properties of chemically synthesized polypyrrole thin films

C. C. Bof Bufon and T. Heinze[l*](#page-4-0)

Heinrich-Heine-Universität, Universitätsstrasse 1, 40225 Düsseldorf, Germany (Received 18 July 2007; published 19 December 2007)

The electronic transport in polypyrrole thin films chemically synthesized from the vapor phase is studied as a function of temperature as well as of electric and magnetic fields. We find distinct differences in comparison with the behavior of both polypyrrole films prepared by electrochemical growth as well as of the bulk films obtained from conventional chemical synthesis. For small electric fields *F*, a transition from Efros-Shklovskii variable range hopping to Arrhenius activated transport is observed at 30 K. High electric fields induce shortrange hopping. The characteristic hopping distance is found to be proportional to $1/\sqrt{F}$. The magnetoresistance $R(B)$ is independent of *F* below a critical magnetic field, above which *F* counteracts the magnetic-field-induced localization.

DOI: [10.1103/PhysRevB.76.245206](http://dx.doi.org/10.1103/PhysRevB.76.245206)

PACS number(s): 71.23.Cq, 72.20.Ee

I. INTRODUCTION

Polypyrrole (PPy) is a semiconducting polymer with some unusual properties compared to other organic semiconductors.¹ The material can be synthesized both chemically and electrochemically; the electrosynthesis² can be performed at low polymerization potentials, allowing the use of water as a solvent. $3-5$ $3-5$ Typically, such films have a rather large thickness above 1 μ m, and they are highly disordered as well as cross-linked; maximum conductivities of 1600 S/cm have been reported for stretched films.⁶ In addition, PPy can be doped electrochemically to a high level, which stabilizes the material properties under ambient conditions.^{7–[9](#page-4-7)} A wide range of applications has been demonstrated, such as gas sensors, $10-13$ $10-13$ biosensors, 14 or transistors. $15-17$ $15-17$

The transport properties of electrochemically synthesized PPy films have been studied extensively.^{1[,2](#page-4-2)} In the insulating state that is usually present, the samples typically follow the Efros-Shklovskii (ES)-variable range hopping model.^{18,[19](#page-4-14)} Such a system is assumed to be formed by metallic sites separated by tunnel barriers, $20,21$ $20,21$ which are generated by spatial variations in the charge density. The electric-field dependence of the conductivity was investigated by Ribo *et al.*[22](#page-4-17) More recently, Gomis *et al.*^{[23](#page-4-18)} reported an electric-fieldinduced transition from an insulating to a *metallic* state which is reached when the electric field is strong enough to delocalize a small fraction $(<0.01\%)$ of the charges.

Chemical synthesis, 24 on the other hand, allows film preparation on conductive as well as on insulating substrates, thereby complementing the range of applications. Chemically grown films have a pronounced egglike morphology, 2^5 markedly different than the characteristic fibers obtained by electrochemical synthesis. These films are, however, of notoriously poor quality in terms of roughness and conductivity. For example, their reported maximum room temperature conductivities are 40 S/cm^2 . This may be the reason why only a very limited number of works have addressed the transport properties of this kind of PPy films. The existing studies have demonstrated that in films with thicknesses larger than 60 μ m, the temperature dependence $\sigma(T)$ of the conductance is consistent with three-dimensional Mott vari-

able range hopping, i.e., $\ln(\sigma) \propto T^{-1/4}$.^{[24,](#page-4-10)[26](#page-4-20)} Up to now, chemical synthesis of PPy at reduced temperatures has not been reported, which is somewhat surprising considering the profound influence the growth temperature has on the conductivity of electrochemically synthesized films.²

Here, we present an investigation of the transport properties of PPy thin films with low roughness, prepared by a recently established scheme that allows the formation of thin films by chemical polymerization from the vapor phase.¹⁷ The differential conductance is studied as a function of electric and magnetic fields as well as of temperature. With small electric fields applied, we find that for low temperatures, the electronic transport can be described within the ES-variable range hopping model. Above a temperature of 30 K, Arrhenius-type activated transport is found. As the electric field is increased, a transition to short-range hopping is observed around a characteristic electric field of F_c = 2500 V/cm. This electric-field-induced reduction of the localization is also visible in magnetotransport measurements.

II. SAMPLE PREPARATION AND CHARACTERIZATION

PPy films were synthesized via chemical polymerization from pyrrole vapor in solutions of $HC1:H_2O_2$. The preparation scheme follows that one described in detail in a previous publication,¹⁷ except that our solvent was cooled, with a minimum growth temperature of $T_g = 277.5$ K. At lower temperatures, the polymerization kinetics became unacceptably slow. A thin PPy film was formed on a doped and oxidized Si substrate containing four Pt electrodes. The film thickness is proportional to the exposure time to the vapor and can be tuned between a few nanometers and $\approx 0.5 \mu$ m. In the present study, we focus on films of thickness 70 ± 10 nm. We observe that besides growth at T_g > 282 K, also water created by the decomposition of H_2O_2 , an aging process in the solution, increases the contact resistance. Therefore, fresh solution has been used for each sample.

Films have been grown at temperatures between 277.5 and 300 K in solutions with volume fractions varying between $HC1:H_2O_2=1:1000$ and 5:1000. Cyclic voltammetry measurements⁹ allow us to estimate the doping density of all

TABLE I. Summary of the sample growth conditions and transport parameters. T_g denotes the growth temperature, ξ the localization length, and r the ES-variable range hopping distance.

Sample	$\frac{1}{g}$ (K)	Volume fraction	σ (300K) (S/cm)	(nm)	r(2.1K) (nm)	r(30K) (nm)
А	282.0	1:1000	10	1.5	30	8
B	277.5	1:1000	12	3.4	44	12
C	277.5	4:1000	20	8.8	72	19

samples to $p \approx 10^{21}$ cm⁻³. This and the fact that the doping density depends neither on the growth temperature nor on the volume fraction of the solution indicate that the films are in the fully charged state, corresponding to 0.25 and 0.33 holes per pyrrole ring.^{28,[29](#page-5-1)} The electronic transport has been studied in 11 samples, all showing qualitatively identical behavior. Typical room temperature conductivities of 10 S/cm $<\sigma$ (300 K) < 20 S/cm are found, with no apparent systematic dependence on T_{g} or on the volume fraction of the solution. At temperatures below \approx 30 K, however, samples grown at T_g > 282 K show substantially lower conductivities than samples grown below this temperature. In the following, we focus on three samples, the parameters of which are summarized in Table [I.](#page-1-0)

Figure [1](#page-1-1) shows an atomic force microscope image of the surface of sample A and the corresponding four-electrode device as seen in an optical microscope (inset), where the gap between the electrodes is 2 μ m. The PPy film covers the four Pt electrodes (c1 to c4). The roughness (single standard deviation) decreases with decreasing growth temperature, varying from 25% of the film thickness for the samples grown at 300 K to 6% for the samples grown at 277.5 K. The film morphology shows egglike structures well known for chemically synthesized $PPy₁²⁵$ with an average diameter of \approx 50 nm.

Transport measurements have been carried out in a ⁴He gas flow cryostat with a temperature range between 2.1 and 300 K. The cryostat is equipped with a superconducting magnet (maximum magnetic field of 8 T). Our setup has a dc resolution of \approx 10 pA. By comparing two-probe with four-

FIG. 1. (Color online) Morphology of sample A, as measured with an atomic force microscope. The inset shows a top view of the PPy film on top of the four Pt electrodes.

probe measurements, we found negligible contact resistances for all experimental conditions investigated. Samples that were measured at temperatures above 30 K with applied electric fields $F > 1500$ V/cm got permanently damaged, while below 30 K, up to 9500 V/cm could be applied.

III. RESULTS AND INTERPRETATION

In Fig. [2,](#page-1-2) the temperature dependence of the conductance $G(T)$ for the three samples under small electric fields (F) $= 10$ V/cm) is shown. Below 30 K, $G(T)$ behaves in accordance with the standard ES-variable range hopping relation, $18,19$ $18,19$ given by

$$
G(T) \propto \exp\bigg[-\bigg(\frac{T_0}{T}\bigg)^{1/2}\bigg],\tag{1}
$$

with

$$
T_0 = \frac{2.8e^2}{4\pi\epsilon_0 \epsilon_r k_B \xi}.\tag{2}
$$

Here, ξ denotes the localization length and $\varepsilon_r = 13.6$ is the dielectric constant of PPy.^{30,[31](#page-5-3)} Below 4.6 K, the current vanishes in our noise floor. We have fitted $G(T)$ to Eq. ([1](#page-1-3)) for temperatures below 30 K. For sample A, T_0 = 2340 K is obtained, corresponding to $\xi = 1.5$ nm (see Table [I](#page-1-0) for the cor-

FIG. 2. Conductance as a function of $T^{-1/2}$ for samples A, B, and C, normalized to the values measured at T_c = 30 K. The full lines are fits to ES-variable range hopping at temperatures below T_c , while the dashed line represents the fit to the Arrhenius law for $T>T_c$.

responding results obtained for samples B and C). The characteristic hopping distance *r* within the ES-variable range hopping model is given by

$$
r = \left(\frac{e^2 \xi}{4\pi\epsilon_0 \epsilon_r k_B T}\right)^{1/2}.
$$
 (3)

The values of *r* at 2.1 and 30 K are displayed in Table [I.](#page-1-0) At the critical temperature $T_c = 30 \text{ K}$, $G(T)$ shows a crossover from ES-variable range hopping to Arrhenius behavior, which is characterized by

$$
G(T) \propto \exp(-U/k_B T). \tag{4}
$$

Such a crossover is expected at a temperature where nearest neighbor hopping begins to dominate over variable range hopping.³² It has been observed in several other systems, for example, in gold nanoparticle multilayers³³ or in ZnO nanocrystal assemblies.³⁴

For nearest neighbor hopping, the activation energy *U* is given $by³⁵$

$$
U = \frac{\xi}{8d} k_B T_0,\tag{5}
$$

where *d* denotes the nearest neighbor distance. From fits of Eq. (4) (4) (4) to the data, the activation energy is found to be U $= 16 \pm 1$ meV for all samples. Via Eq. ([5](#page-2-1)), this corresponds to $d = 2 \pm 0.5$ nm.

We proceed by discussing the effect of high electric fields. Figure $3(a)$ $3(a)$ shows the *IV* traces as a function of the temperature for sample A. All samples exhibit nonlinear *IV* characteristics below 90 K. In Fig. $3(b)$ $3(b)$, the differential conductance $G(T)$ is shown for sample A for various electric fields *F*. Clearly, the electric field has a profound effect on the conductance; it can induce changes of *G* over more than 4 orders of magnitude at low temperatures over the accessible electric field range, and strong deviations from Eq. (1) (1) (1) occur: the shape of $G(T)$ becomes strongly dependent on F , while the temperature dependence of *G* decreases with increasing electric field. Our data can be interpreted within the extension of the ES-variable range hopping model to significant electric fields: it has been argued that for samples in the ES-variable range hopping regime, the electric field reduces the Coulomb energy over a characteristic hopping distance *r* by *eFr*, [36](#page-5-8) which for intermediate electric fields results in a modified conductivity given by

$$
G(F,T) \propto \exp\left(-2\frac{r}{\xi} - \frac{\xi}{2.8r}\frac{T_0}{T} + \frac{eFr}{k_B T}\right). \tag{6}
$$

This intermediate regime is defined by $F_0 = k_B T/eL \leq F$ $\leq 2k_B T/(e \xi) = F_1$, where F_0 and F_1 denote a lower and an upper critical electric field, respectively. *L* is a length parameter of the order of the maximum hopping length, the exact numerical value of which is under a controversial discussion.^{37-[39](#page-5-10)} In this intermediate regime, one should expect that *r* depends on both temperature and electric field. In our samples, we find that in this intermediate regime, namely, for $F \ge 2500 \text{ V/cm} \approx F_1(5 \text{ K}) = F_c$ and for temperatures below 5 K, $ln(G)$ shows a $1/T$ dependence to high accuracy, see Fig. $4(a)$ $4(a)$. Here, F_c denotes a characteristic

FIG. 3. (a) Measured *IV* characteristics of sample A at different temperatures. (b) The temperature dependence of $G(T) = dI/dV(T)$, for various electric fields F . The straight line is the fit of $G(T)$ at $F = 10$ V/cm for sufficiently large temperatures, i.e., for conductances above the noise floor, to the Efros-Shklovskii model, see Fig. [2.](#page-1-2)

electric field. According to Eq. (6) (6) (6) , this would be expected for a temperature-independent hopping distance. This observation implies that in this regime, *r* is mostly determined by the electric field in our samples $[r = r(F)]$ and depends only weakly on temperature. We have therefore fitted $G(T)$ for different electric fields in this regime under the assumption of a temperature-independent hopping distance, using $r(F)$ as a fit parameter.

In Fig. $4(b)$ $4(b)$, these values are shown as a function of $F^{-1/2}$. It is observed that for electric fields above \approx 2500 V/cm, $r(F)$ becomes proportional to $F^{-1/2}$, with a slope of $dr/d(F^{-1/2}) = 6.13 \times 10^{-6}$ (V m)^{1/2}. For lower fields, *r*(*F*) deviates from this relation and the fits become worse, probably because in this range, *r* develops a significant temperature dependence. Dvurechenskii *et al.*[36](#page-5-8) have argued that in strong electric fields, i.e., for $F > k_bT/(e \xi)$, the energy gained by the electric field overcomes the activation energy such that the transport becomes activationless, which means that the last two terms in the exponent of Eq. (6) (6) (6) cancel each other, and a temperature-independent conductivity evolves with an electric-field dependence given by

FIG. 4. (a) Differential conductance of sample A (symbols) and the corresponding fits to Eq. ([6](#page-2-3)) in the range $eF\xi \ge k_B T$. (b) The electric-field dependence of the fitted values for *r* follow a $1\sqrt{F}$ dependence (full line) above the critical field F_c = 2500 V/cm (dashed line).

$$
G(F) \propto \exp\bigg[-\frac{2r(F)}{\xi}\bigg],\tag{7}
$$

with

$$
r(F) = \sqrt{\frac{e}{4\pi\epsilon\epsilon_0}} \frac{1}{\sqrt{F}}.\tag{8}
$$

Our data show the same functional dependence of *G* on *F*, even though activation still plays a significant role for the transport. Further theoretical work is necessary to understand this regime in more detail. This model predicts a slope of $dr/d(F^{-1/2}) = 1.03 \times 10^{-5}$ (V m)^{1/2}, in rough agreement with (i.e., 70% larger than) our value determined from the experiment. We speculate that either the dielectric constant increases in high electric fields or the electric fields accessible in our experiment are not high enough for Eq. (7) (7) (7) to hold, even though the same functional dependence is found. We note that similar discrepancies have been reported in the literature for other systems.³⁵

FIG. 5. Effect of a magnetic field on the *F* dependence of the differential conductance as measured on sample A. Inset: the magnetoresistance as measured on this sample at *F*= 2500 V/cm and 9500 V/cm. The data are normalized to their value at $B=0$.

The behavior of $G(T)$ in large electric fields could be also attributed to Joule heating, which would be most prominent at low temperatures under high electric fields and cause a saturation of *G* as the temperature decreases. From the heat generated at *F*= 9500 V/cm and the thermal conductivity of the oxide layer underneath the PPy film, we estimate the maximum increase of the sample temperature by Joule heating to $\Delta T \sim 0.5$ K. Therefore, the Joule heating effect can be neglected in our experiments.

Figure [5](#page-3-2) shows the differential conductance at 2.1 K as a function of *F* for various magnetic fields, taking sample A as an example. For all electric fields, the magnetic field tends to localize the charges, thus counteracting the electric-fieldinduced delocalization. In the inset of Fig. [5,](#page-3-2) the magnetoconductance is shown for different electric fields. For $B \leq 4$ T, $R(B)$ is independent of *F* within experimental accuracy. At $B \approx 4$ T, the curvature of $R(B)$ switches from positive to negative, while for larger magnetic fields, the normalized resistance change induced by *B* becomes weaker as *F* increases.

To the best of our knowledge, the magnetoresistance of a disordered medium in the variable range hopping regime under high electric fields has not been studied up to now. The theory of magnetotransport in such systems under negligible electric fields, however, is well established, $18,40$ $18,40$ and in the following, we use it to interpret our measurements. This seems well justified for the low magnetic-field regime where only a very small influence of the electric field on $R(B)$ is observed. According to Shklovskii and Efros,¹⁸ the magnetic confinement reduces the wave function overlap between sites. Within a percolation model, this causes the resistance to increase exponentially as *B* increases according to

$$
R(B) \propto \exp[A(T)B^2],\tag{9}
$$

where

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$$
A(T) = 0.036 \left(\frac{e\xi^2}{\hbar}\right)^2 \left(\frac{T_0}{T}\right)^{3/2}.
$$
 (10)

Below 4 T, Eq. ([9](#page-3-3)) fits our data well, with the fit parameters $A(2.1 \text{ K}) = 0.017 \text{ T}^{-2}$ and 0.014 T⁻² for the measurements at $F=2500$ V/cm and $F=9500$ V/cm, respectively. From Eq. ([10](#page-4-22)), we expect *A*(2.1 K) \approx 0.015 T⁻² for sample A in good agreement with the fit parameters. For $B \gtrsim 4$ T, deviations from Eq. (9) (9) (9) are observed. Theory^{18[,40](#page-5-11)} predicts that for negligible electric fields and $B \gg B_c = n^{1/3} \hbar / e \xi$ (*n* denotes the density of impurities), the magnetoresistance has the form

$$
R(B) \propto \exp[\sqrt{B/B_c}], \qquad (11)
$$

which has been observed in several experiments.^{2[,41](#page-5-12)} Our data are fitted well by Eq. (11) (11) (11) for $B > 4$ T. The measurements indicate a value of $B_c \approx 4$ T. This would correspond to an impurity density of $n=7\times10^{14}$ cm⁻³, i.e., an average distance between impurity sites of 110 nm, much larger than the characteristic hopping distance, a result which cannot be interpreted in a straightforward way. We note that even though our data can be described qualitatively by Eq. ([11](#page-4-23)), its application is questionable considering the significant effect *F* has on $R(B)$ in this regime and the fact that B is not large compared to B_c . Also, a behavior according to Eq. ([11](#page-4-23)) for *B* $\approx B_c$, i.e., outside the range of validity of Eq. ([11](#page-4-23)), has been observed in other experiments, see, e.g., Ref. [41.](#page-5-12) Additional theoretical studies are required to understand this regime in more detail.

IV. SUMMARY AND CONCLUSIONS

The electronic transport properties of thin, chemically grown polypyrrole films have been investigated. In contrast to previous experiments performed on much thicker films, we find that the Efros-Shklovskii variable range hopping dominates at temperatures below 30 K, and the Arrhenius activated transport is observed at higher temperatures. Nonlinearities in the current-voltage characteristics are found, which can be interpreted within an extension of the Efros-Shklovskii model to high electric fields. In agreement with this model, we observe that the hopping distance is proportional to $1/\sqrt{F}$ above a characteristic field of \approx 2500 V/cm in our system, which marks a transition to short range hopping. Moreover, for small magnetic fields, the measured magnetoresistance is in quantitative agreement with the Shklovskii-Efros description of magnetic-field-induced localization in disordered media. At large magnetic fields, we observe an electric-field-induced reduction of the localization which requires further theoretical study.

ACKNOWLEDGMENTS

Financial support by the *Heinrich-Heine-Universität Düsseldorf* is gratefully acknowledged. The authors acknowledge fruitful discussions with D. Basko.

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