# **Water confined in nanopores: Spontaneous formation of microcavities**

John Russo, Simone Melchionna[,\\*](#page-6-0) and Francesco De Luca

*SOFT-INFM-CNR, Department of Physics, University of Rome La Sapienza, P.le A. Moro 2, 00185 Rome, Italy*

Cinzia Casieri

*SOFT-INFM-CNR, Department of Physics, University of L'Aquila, Via Vetoio, 67010 L'Aquila, Italy* (Received 16 January 2007; revised manuscript received 14 April 2007; published 6 November 2007)

Molecular dynamics simulations of water confined in nanometer sized, hydrophobic channels show that water forms localized cavities for pore diameter  $\geq 2.0$  nm. The cavities present nonspherical shape and lay preferentially adjacent to the confining wall inducing a peculiar form to the liquid exposed surface. The regime of localized cavitation appears to be correlated with the formation of a vapor layer, as predicted by the Lum-Chandler-Weeks theory [J. Phys. Chem. B 103, 4570 (1999)], implying partial filling of the pore.

DOI: [10.1103/PhysRevB.76.195403](http://dx.doi.org/10.1103/PhysRevB.76.195403)

PACS number(s): 64.70.Nd

# **I. INTRODUCTION**

Nanotubes<sup>1</sup> are important building blocks of nanocomposite materials and nanomachinery. When immersed in ionic solutions, nanometer-sized pores can be used for the detection and analysis of electrolytes and charged polymers, such as  $DNA<sub>1</sub><sup>2</sup>$  and to understand ion transport and selectivity in biological channels. $3$  A full understanding of the phase behavior of confined water is a prerequisite to interpret adsorption and conductivity data. In particular, experiments and simulations have shown that, for channels of subnanometer radius, water exhibits an intermittent filling and/or drying transition resulting from an underlying bistable free-energy landscape separated by a thermally activated barrier, a behavior specific to water and not observed in a monoatomic fluid.<sup>4[,5](#page-6-5)</sup> The switch between empty and filled states upon ion translocation has been advocated as a gating mechanism in passive biological channels.<sup>6,[7](#page-6-7)</sup>

Cavitation of water under confinement is related to the long-ranged attractive forces exerted by hydrophobic bodies. Two alternative mechanisms have been proposed for explaining the occurrence of these forces: on one hand, the presence of air-filled nanobubbles at the solid surface drives the attraction via a bubble-driven mechanism; on the other hand, longranged correlations in the critical region or near the spinodal line could induce an extended density depletion at the surfaces, which results in the attraction. $8-10$  $8-10$ 

The first line of reasoning relies on the preexistence of air-filled cavities at the solid surface.<sup>11</sup> However, the mechanism for their stabilization is not fully understood since the Laplace-Young equation prescribes an internal pressure of the order of  $10^2$  atm for nanometer-sized bubbles.<sup>12</sup> Two questions pertains how such large internal pressure can sustain stable or metastable cavities and if these are independently nucleated at the solid, corrugated surface. It has been suggested that line tension can act to stabilize such small cavities<sup>13</sup> by reducing the curvature of the bubble base on the solid surface. As a matter of fact, micron-sized air bubbles are commonly observed in proximity of hydrophobic corrugated surfaces and, in the recent literature, there is growing evidence for the presence of bubbles on corrugated surfaces at the nanoscale. In particular, recent atomic force microscopy experiments on silicon oxide wafer surfaces of controlled roughness reported on bubble formation at the solidwater interface, $14$  while synchrotron x-ray reflectivity measurements reported on a small depletion layer in lieu of localized cavitation.<sup>16</sup>

The second interpretation is based on the formation of a vapor layer in contact with the solid surface. Such depletion layer would involve a high entropic cost, growing with the extension of the exposed surface, but compensated by volume-dependent forces arising from molecular reorganization. The Lum-Chandler-Weeks (LCW) theory<sup>17</sup> formulates the hydrophobic effect in microscopic terms based on the competition between interfacial and bulk forces which therefore depend on the solute surface to volume ratio. The molecular mechanism underlying the force balance is commonly ascribed to the distortion of the hydrogen-bond network. In particular, for small spherical solutes, water arranges in a clathrate structure, while for larger size, the ensemble of hydrogen-bond vectors,  $O-H\cdots H$ , points preferentially toward the solute. Therefore, if the curvature of the embedded body is low, the distortion is large and entropic effects prevail over the enthalpic ones, and vice versa for small solutes.

The cylindrical pore represents an opposite case to the spherical solute, where now the confining surface is concave. However, a similar enthalpic or entropic competition is expected and should depend on the pore diameter. Thus, a relevant information pertains if, for pore diameter larger than that characteristic of intermittent behavior, the liquid phase is completely stabilized or if some peculiar behavior still takes place. The occurrence of cavitation in water confined by cylindrical pores has been recently discussed in view of understanding the hysteresis involved in capillary evaporation.<sup>18</sup>

We report here the results of molecular dynamics (MD) simulations undertaken on cylindrical, hydrophobic pores of finite length. In Sec. II, the simulation setup and numerical details are described and in Sec. III, the molecular dynamics data are illustrated. In Sec. IV, the LCW theory is described and the numerical solutions are compared with the simulation results. The last section draws some conclusions and analyzes recent experimental observations.

<span id="page-1-0"></span>

FIG. 1. Schematic representation of a cut through the simulation cell. The dark area is the confining cylindrical wall and the shaded area is the region where water is maintained at mass density of 1 g/cm<sup>3</sup> (see text for details).

### **II. SIMULATION DETAILS**

The geometry of the simulation setup is depicted in Fig. [1.](#page-1-0) The two pore mouths are connected to the same, periodically folded, reservoir of quasibulk water. The pore diameter *d* and pore length *L* are varied to the following pairs of values  $(d, L) = (1.5, 4.0), (2.0, 4.0), (2.5, 4.0), (2.5, 8.0), (3.0, 4.0),$  and  $(3.5, 4.0)$  nm as used to label the runs. Simulations become rapidly costly with the pore size, and we did not attempt to extend our simulations to larger geometries. Besides the nominal values, the effective cylinder diameter and length were evaluated via the criterion that the repulsive walloxygen potential be less than  $k_B T$ , giving a reduction of the effective diameter and an increase of effective length by  $0.46$  nm.<sup>5</sup>

The simulation box is periodic in all three directions with dimensions depending on the pore geometry. The number of water molecules for all simulations ranges between 852 and 2464 units. Water is represented via the SPC/E computational model. $^{22}$  The confining wall-oxygen potential is modeled as a smooth surface generated by carbon atoms and distributed uniformly over the surface. The wall-water interaction acts between each water oxygen and a smooth Lennard-Jones potential integrated over the dark region of the wall, as shown in Fig. [1.](#page-1-0) Each carbon atom carries a Lennard-Jones potential with parameters  $\sigma = 0.345$  nm and  $\epsilon$ = 0.7294 kJ mol<sup>-15</sup>, and the standard Lorentz-Berthelot rules are used to construct wall-oxygen interactions. Electrostatic interactions between charged oxygen and hydrogen atoms are computed with the Ewald method via the smooth particle mesh Ewald implementation.<sup>19</sup> Moreover, the confining medium is taken as nonpolarizable.

The hydrophobic content of the wall has been characterized by simulating 862 water molecules in contact with a flat surface and by following the evolution of the equilibrated system for 100 ps in order to compute the contact angle. By smearing the number density of water oxygens over cubic cells of 0.3 nm edge, we have identified the external surface of the droplet by locating the isodensity surface with values comprised in the  $(1-2) \times 10^{-5}$  nm<sup>-3</sup> interval. The contact angle is found to be  $113^{\circ} \pm 5^{\circ}$ .

Special care is taken to keep the reservoir density under control, such that upon emptying or filling of the channel, the reservoir maintains a bulklike behavior with an average mass density of 1  $g/cm<sup>3</sup>$  away from the pore. This is obtained by varying over time the length of the reservoir, in the direction parallel to the pore axis, by a Berendsen type of piston, $20$ with a characteristic coupling time of 10 ps, during the equilibration and production runs. The feedback sets the average density in a stripe of thickness *t*= 10 nm placed at a distance  $l = 7$  nm away from the pore (see Fig. [1](#page-1-0)). The system temperature is controlled via a Nosè-Hoover thermostat<sup>21</sup> in order to avoid anomalous temperature drifts during both the equilibration process and the subsequent production runs. The system is simulated at 300 K, while some auxiliary simulations are made at 280 and 320 K. The evolution of the system is followed over times of 100 ps (equilibration) and, subsequently, of 1 ns (production). Within the simulation time window, stationarity is monitored by following the number of molecules populating the channel and the formation and size distribution of cavities. In order to monitor the effective stationarity of the equilibrated system, the run of the  $(2.5, 4.0)$  nm geometry has been further extended to 3 ns, without observing any departure from stationarity.

In order to detect the cavities, we have used a coarsegraining procedure by tessellating the space with cubic cells of 0.02 nm edge. An empty cell is defined by having the distance from any oxygen atom greater than 0.3 nm. The wall position is defined by the largest radial distance of an oxygen atom from the pore axis and adding an offset of 0.1 nm. A cavity is defined as the cluster of contiguous empty cells which do not belong to the wall region. The distinction among clusters is made via a graph algorithm and sorted according to size. In this way, the identity of cavities is clearly established.

## **III. MOLECULAR DYNAMICS RESULTS**

The simulation data present two distinct behaviors: for the geometries  $(1.5, 4.0)$  nm at  $T = 300$  K and  $(2.5, 4.0)$  nm at *T*= 280 K, we observe emptying of the pore, with a large vapor region extending between the two pore mouths; on the other hand, for the geometries  $(2.0, 4.0), (2.5, 4.0), (2.5, 8.0),$  $(3.0, 4.0)$ , and  $(3.5, 4.0)$  nm at  $T=300$  K and  $(2.5, 4.0)$  nm at *T*= 320 K, water persists inside the pore at density close to liquid state, with formation of nanobubbles in proximity of the confining wall.

At first, we report on the process of emptying of the channel for the  $(1.5, 4.0)$  nm geometry at  $T=300$  K, as depicted in Fig. [2.](#page-2-0) Given an initial, apparently stable liquid inside the channel, a number of distinct lateral cavities are formed in proximity of the cylinder wall. Subsequently, one of such bubbles grows in size, rapidly extending over the whole pore volume. The final state appears to be stable over the 1 ns time scale. The homogeneous growth of the vapor region is consistent with the recently proposed model of capillary evaporation in hydrophobic pores.<sup>18</sup>

Intermittent emptying or filling of the channel has been previously reported at  $T=300 \text{ K}$  for  $d \le 1.5 \text{ nm}$  and L  $\leq 1.0$  nm (and eventually for larger diameters at lower temperatures) by using MD simulations with the same computational model as used here.<sup>5</sup> In the previous work, it was

<span id="page-2-0"></span>

FIG. 2. Snapshots of the  $(1.5, 4.0)$  nm channel at  $T=300$  K at instants 100 ps (panel a), 110 ps (panel b), 120 ps (panel c), and 130 ps (panel d) of the production run, showing the process of pore emptying. The pictures are produced with the surface generation algorithm of the VMD software (Ref. [27](#page-6-21)) by taking into account the oxygen atoms only.

found that the time scale of emptying or filling oscillations is of the order of  $\sim$ 100 ps. In the current case, the direct observation of intermittency is prohibited in terms of CPU time. In fact, given the larger pore diameters, intermittency could take place over time scales longer by 1 order of magnitude or more.<sup>7</sup> Therefore, we preferred to focus on the interfacial structuring of the liquid in the filled state.

It is interesting to note that the geometry  $(2.5, 4.0)$  nm exhibits pore emptying for  $T = 280$  K (see Fig. [3](#page-2-1)) and pore filling for  $T=300$  and 320 K. The fact that emptying or filling of the pore is sensitive to differences in temperature as small as 20 K is an indication that the underlying bulk phase diagram, with the rather narrow region of bulk liquid water and the close-by liquid-vapor coexistence, is an important driving factor for the confined fluid. Moreover, the number of water molecules populating the channel at 320 K is substantially larger by about 27% than that at 300 K. This behavior is not surprising since the energetics of water, mostly contributed by its hydrogen-bond network, is highly perturbed by confinement. Thus, the prevalence of entropic forces, as compared to bulk conditions, tends to populate the channel more as temperature increases.

For the filled channel, the liquid interface displays the patterns, as shown in Figs. [4](#page-2-2) and [5.](#page-3-0) The interface is rather corrugated by the presence of cavities appearing in proximity of the confining wall (lateral cavities) and is rarely observed as spherical shape located around the cylinder axis. The cavi-

<span id="page-2-1"></span>

FIG. 3. Snapshot of the configuration of the  $(2.5, 4.0)$  nm channel at *T*= 280 K taken at instant 500 ps of the production run. Picture generated as in Fig. [2.](#page-2-0)

ties resemble spherical caps or rounded cones, with volumes much larger than the molecular size  $(v_w \approx 0.027 \text{ nm}^3)$ . The average volumes range between  $\langle v \rangle / v_w = 5.7$  for the  $(d, L)$  $=(2.0, 4.0)$  nm geometry and  $\langle v \rangle/v_w = 21.0$  for  $(d, L)$  $=(3.5, 4.0)$  nm. The peculiar pattern of the liquid exposed surface is rather representative of the highly cohesive char-

<span id="page-2-2"></span>

FIG. 4. Snapshot of the configuration of the  $(2.5, 4.0)$  nm channel at *T*= 300 K taken at instant 500 ps. Picture generated as in Fig. [2.](#page-2-0)

<span id="page-3-0"></span>

FIG. 5. Evolution of cavities (shaded regions) formed in the  $(2.5, 4.0)$  nm pore at  $T=300$  K and analyzed on a slab thickness of 0.1 nm placed at the midpoint of the pore axis. The four snapshots (a-d) correspond to successive configurations separated by 1 ps. The white region corresponds to the wall region, gray to water filled regions, and black to the empty regions (see text for details).

acter of water. It should be noticed that the shape of the vapor cavities along the transversal section does not appear to be flattened against the wall, while in the longitudinal direction, visual analysis does not allow to draw a clear conclusion. We infer that line tension effects can be important only along the longitudinal direction but not on the transverse direction. In terms of dynamics, the cavities present high mobility with fast reshaping on the 1 ps time scale, as obtained by following the ten largest cavities during the simulations and by computing the average lifetime. The lifetime was found to be insensitive to the length and size of the pore.

The distribution of cavity size is illustrated in the normalized histograms of Fig. [6.](#page-3-1) A systematic increase of cavities of larger volume with the pore diameter is visible, accompanied by a depletion of smaller, molecular-sized ones. The distribution becomes more shifted to the right as the diameter of the cylinder grows. In contrast, water in proximity of a planar hydrophobic surface exhibits cavities with reduced volumes, basically indistinguishable from fluctuations of size of the molecular volume  $v_w$ .

In Fig. [7](#page-3-2) we report the same histograms but we filter out the contributions arising from cavities of volume  $v \lt v_w$ . By rescaling the abscissa of the cylinder surface area, the histograms become peaked around the same value  $v/(v_w 2\pi Ld)$  $\approx 0.02$  nm<sup>-2</sup>, and width increasing with the pore diameter. However, the integrated cavity volume per unit surface is mostly contributed by the large-volume tail of the distributions, which appear to be equal for the  $(2.5, 4.0)$  and  $(3.5, 4.0)$ 4.0) geometries but significantly shifted to the left for the  $(1.5, 4.0)$  case. Therefore, cavitation does not seem to grow further as the diameter is larger than 2.5 nm. On the other hand, raising temperature to *T*= 320 K reduces the size of the voids, i.e., by stabilizing the liquid state, in agreement with

<span id="page-3-1"></span>

FIG. 6. Frequency of occurrence of cavities with volume *v* as a function of volume normalized by the value per water molecule  $(v_w=0.027 \text{ nm}^3)$  for  $(d,L)$  equal to  $(2.0, 4.0)$  nm (solid line),  $(2.5, 4.0)$  nm (dashed line),  $(2.5, 8.0)$  nm (long dashed line),  $(3.5, 4.0)$  nm (dot-dashed line), and for water close to an infinite plane (dotted line). All data are taken at  $T=300$  K. To highlight the dependence on the pore geometry, the normalized frequency of occurrence  $P(v)$  is multiplied by the volume. The inset displays the unscaled frequency (same symbols of the main plot).

the larger number of water molecules populating the channel.

The longer channel does not appear to affect the histogram, indicating that the bubble formation does not depend on interfacial effects arising from the finite pore length. In principle, the finite length could affect the liquid or vapor balance and the drying transition. In fact, by using an elementary macroscopic argument, $12$  the difference in freeenergy density between the liquid and vapor states is approximated by  $\Delta \Omega / \pi dL = \gamma_{lw} - \gamma_{lv} d/2L$ , where  $\gamma_{lw}$  and  $\gamma_{lv}$ are the liquid-wall and liquid-vapor surface tensions under ambient conditions, respectively, and bulk contributions to the free energy have been neglected. In other words, if finite channel effects are in place, by making the channel longer,

<span id="page-3-2"></span>

FIG. 7. Histograms as in Fig. [6](#page-3-1) but for cavity volumes larger than  $v_w$ . The curves refer to  $(d, L) = (2.0, 4.0)$  (solid line),  $(2.5, 4.0)$ (dashed line), (2.5,8.0) (long dashed line), (3.5,4.0) (dot-dashed line) at  $T = 300 \text{ K}$ , and for  $(2.5, 4.0)$  nm at  $T = 320 \text{ K}$  (dot-dotdashed line). Values in abscissa has been rescaled by the cylinder surface area.

one should move away from the vapor branch. By taking  $\gamma_{lw} = 7.4k_BT/nm^2$  and  $\gamma_{lv} = 26k_BT/nm^2$ , it is seen that the geometry  $(d, L) = (2.5, 4.0)$  nm is close to the region where the free-energy difference changes sign.<sup>5</sup> Our simulation at room temperature for  $(d, L) = (2.5, 8.0)$  nm showed that the channel remains filled as much as the  $(2.5, 4.0)$  nm geometry, without appreciable differences in the distribution of cavity volumes. Conversely, the sensitivity to the pore length appears in the fluctuations of the number of adsorbed water molecules, which approximately drops by a factor of 2 in the longer channel. We interpret the weak size dependence of cavitation as due to the corrugated, largely exposed surface of the liquid with respect to the simple macroscopic model, which renders finite size effects negligible already at *L*= 4 nm.

## **IV. LUM-CHANDLER-WEEKS PREDICTIONS**

In this section, we compare our data to the predictions of the LCW theory for an infinitely long pore. Schematically, the theory is described as follows. Let us first consider the decomposition of the microscopic density  $n(r)$  into a slowly varying component,  $n_s(r)$ , and a fast component,  $n(r) - n_s(r)$ . The LCW theory builds upon the well-known squaregradient theory for liquid-vapor coexistence<sup>25</sup> by taking into account self-consistently the fast oscillations in density. According to the square-gradient approximation, the local grand potential  $-W(n)$  is related to the Laplacian of the density via

$$
\left(\frac{dW}{dn}\right) = m\nabla^2 n(r),\tag{1}
$$

<span id="page-4-0"></span>where *m* is an effective parameter derived from the underlying interatomic potential  $v(r)$ ,  $m = -\frac{\pi}{6} \int_{0}^{\infty} dr r^{4} v(r)$  (random phase approximation<sup>25</sup>). By applying a coarse-graining procedure, the local density is replaced by the function  $n \rightarrow \bar{n}$  $=n + \frac{\lambda^2}{2} \nabla^2 n$ , where  $\lambda$  is the characteristic length of the coarsegraining procedure. Therefore, the starting equation of the LCW theory is derived from Eq. ([1](#page-4-0)) rewritten in terms of  $\bar{n}$ , and asserting that this equation holds for the slow component  $n_s$ , thus

$$
\left(\frac{dW}{dn}\right)_{n_s} = \frac{2m}{\lambda^2} [\bar{n} - n_s],\tag{2}
$$

<span id="page-4-1"></span>for which we choose  $\lambda = 0.3$  nm and  $m = 919.9$  $\times 10^{21}$  $\times 10^{21}$  $\times 10^{21}$  J nm<sup>5</sup> mol<sup>-2</sup>. To implement Eq. (2), one needs prior knowledge of the bulk equation of state of water near the liquid-vapor coexistence. Following previous studies,  $23$  we used a quartic dependence plus a linear correction term which models the proximity to coexistence,

$$
W(n) = \alpha (n - n_l)^2 (n - n_g)^2 + \beta (n - n_l),
$$
 (3)

where  $\alpha = 2.89 \times 10^{-24}$  J nm<sup>9</sup>,  $\beta = 3.04 \times 10^{-29}$  J, and the liquid and vapor densities are  $n_l$ = 32.94 nm<sup>-3</sup> and  $n_e$ = 7.7  $\times 10^{-4}$  nm<sup>-3</sup>, respectively.<sup>23</sup> By solving the equations in cylindrical coordinates and by forbidding any angular symmetry breaking, we did not attempt to observe the formation of cavities of given shape. This choice was motivated by the narrow range of numerical stability found during the solution of the LCW equations.

<span id="page-4-3"></span>

FIG. 8. Radial density profiles divided by the density of liquid water  $n_l$ . The radial coordinate is rescaled with the effective thermal radius (MD data, upper panel) and the value  $\overline{d/2}$  (LCW data, lower panel). Upper panel: MD profiles at 300 K for nominal pore diameter  $d=2.0$  nm (solid line),  $2.5$  nm (dashed line),  $3.0$  nm (longdashed line), and  $3.5$  nm (dot-dashed line) and length  $L=4$  nm. Lower panel: LCW profiles for  $\bar{d}$  equal to 2.8 nm (solid line), 3.0 nm (dashed line), 3.4 nm (long-dashed line), and 3.6 nm (dotdashed line).

The link between the slowly varying and the complete density fields is established within the Gaussian density fluctuations approximation by writing $24$ 

$$
n(\mathbf{r}) = n_s(\mathbf{r}) - \int d\mathbf{r}' c(\mathbf{r}') \chi(\mathbf{r}, \mathbf{r}'), \tag{4}
$$

<span id="page-4-2"></span>where the response function  $\chi(\mathbf{r}, \mathbf{r}') \equiv \langle \delta n(\mathbf{r}) \delta n(\mathbf{r}') \rangle$  is approximated by  $\chi(\mathbf{r}, \mathbf{r}') \approx n_s(\mathbf{r}) \delta(\mathbf{r} - \mathbf{r}') + n_s(\mathbf{r}) n_s(\mathbf{r}')h(|\mathbf{r} - \mathbf{r}'|),$ and  $h(|\mathbf{r}-\mathbf{r}'|)-1$  is the bulk pair correlation function. Moreover,  $c(\mathbf{r})$  is the water-wall direct correlation function. Given  $n_s(\mathbf{r})$ , Eq. ([4](#page-4-2)) is solved to obtain  $c(\mathbf{r})$  and  $n(\mathbf{r})$  via the Nystrom numerical procedure. $26$  The two coupled integrodifferential equations  $[(2)$  $[(2)$  $[(2)$  and  $(4)]$  $(4)]$  $(4)]$  are solved iteratively. We did not include the correction to the LCW theory due to the attractive part of the wall-oxygen potential. $2<sup>3</sup>$  Vice versa, the effective diameter of MD and the diameter used in LCW calculations  $\overline{d}$  were considered as equivalent control parameters.

We have found that for diameter  $\bar{d}$  < 2.6 nm, the LCW equations predict complete pore emptying, in agreement with previous simulation and experimental results, but below our MD data which exhibit emptying (or eventually intermittency) for effective diameter  $\leq 2.0$  nm, as shown in Fig. [8.](#page-4-3) However, in this geometry, the LCW predictions do not distinguish between intermittent and cavitating behavior. In the range of  $2.6 < \bar{d} < 3.8$  nm, the theory predicts partial filling of the pore, as illustrated by the density profiles in Fig. [4,](#page-2-2) where the microphase coexistence is accompanied by a significant density depletion near the wall. Moreover, the LCW equations predict a gradual increase of the vapor layer as the

<span id="page-5-0"></span>

FIG. 9. Number of water molecules occupying channels of length 4 nm at  $T = 300$  K obtained from MD (filled circles), LCW solutions (open squares), and a uniform filling of the channel (dashed curve). The vertical jump in the LCW curve signals the crossover between empty and partially filled states.

diameter lowers, while the MD results show a maximum which varies slowly with the pore diameter. Following Ref. [23,](#page-6-23) we attribute this difference to the presence of the weak attractive tail in the water-wall potential. Finally, at larger diameters, the LCW curves show weakly structured profiles, with a characteristic nonwetting shape near contact. In the essence, the LCW theory predicts a crossover between empty and partially filled states for  $\overline{d}$  = 2.6 nm, larger than the MD results where the crossover appears in the 1.5:2.0 nm interval. This discrepancy may be attributed to the onedimensional solution of the LCW equations and to the missing attractive tail in our theoretical treatment, causes which artificially stabilize the vapor phase, or to the undetermined location of the confining surface, whose diameter can vary by about 0.5 nm.

Notwithstanding the negligible correlations emerging from the LCW solutions, we can compare MD and LCW data regarding the number of water molecules filling a channel of 4 nm length as a function of the channel effective diameter  $\overline{d}$ . From Fig. [9,](#page-5-0) it is apparent that the LCW model shows systematically lower values than the MD data in the region where the theory exhibits partial filling. The MD data are intermediate between the LCW values and the simple model of uniform filling of the pore at the water liquid density. As for the discrepancy in the crossover diameter, the lack of longitudinal symmetry breaking and the weak attractive tail in the simulated water-wall potential might explain the smaller number of water molecules predicted by the LCW theory.

#### **V. CONCLUSIONS**

The behavior of water in contact with an extended hydrophobic surface has attracted considerable attention on account of the intrinsic thermodynamic problem, which has significant implications in protein folding, $^{23}$  ionic transport in biological channels, $3$  and the specification of boundary conditions for water flow in microchannels.<sup>28</sup>

Our study clearly demonstrates the spontaneous formation of vapor microcavities on the nanometer scale for water in contact with a concave cylindrical surface of diameter *d*  $\geq$  2.0 nm. The cavities are localized both in the angular and, more importantly, in the longitudinal directions.

The results are particularly interesting for the on-going debate on the hydrophobic effect, in which a number of different interpretations have been put forward, such as entropic effects due to molecular rearrangement, electrostatic effects, and spontaneous cavitation due to the metastability of the fluid.<sup>10</sup> Recent experiments have focused on analyzing water in contact with a hydrophobic surface and found contrasting results. In particular, either cavitation $14,15$  $14,15$  or an extended low-density depletion layer<sup>16</sup> have been observed. Our observations that water around a concave, but smooth, hydrophobic surface forms short-ranged islands of vapor, modulated by the surface curvature, suggests that the contrasting experimental observations arise from the sensitive structural response of water to the roughness of the solid surface.

Moreover, our study sheds some light on the experimental observation of hysteresis in water intrusion or extrusion cycles in pores and on the interpretation based on homogenous nucleation.<sup>18</sup> The simulation data underline the metastable character of highly confined water. However, the rich structural patterns exhibited by the interface are absent in a simple fluid and, therefore, are unlikely to be explained in terms of a macroscopic approach. When comparing the simulation data with a quasimicroscopic treatment, namely, the Lum-Chandler-Weeks theory, the density profiles and the crossover diameter between empty and partially filled states of the latter were found to agree only qualitatively with the simulation data. The discrepancies were explained mostly on the basis of the one-dimensional solution of the LCW equations.

Finally, we wish to comment on some recent measurements on ionic conductance in nanopores of diameter *d*  $\approx$  10 nm showing that transport displays an anomalous response, with a 5 orders of magnitude reduction in the current spectral density power and a strongly noisy response with respect to bulk behavior.<sup>29</sup> This behavior was attributed to the presence of spherical shaped air bubbles trapped inside the nanopores such that the translocating ions encounter a two-phase filled region. Although the differences in pore diameter between the presently simulated and the experimental systems might seem large, we expect that water cavitation is still effective in wider pores or that cavitation is locally enhanced by the translocating ion. The effect of such cavitation would induce nontrivial wall-ion dielectric interactions, modulated by the imperfect screening of water, and nontrivial hydrodynamic forces. Such scenario could imply a coupled ion-bubble transport mediated by the microscopic liquid-vapor coexistence.

### **ACKNOWLEDGMENTS**

We wish to thank Jean-Pierre Hansen and Francesco Sciortino for critical reading of the paper and Mauro Chinappi for help with the simulation setup.

<span id="page-6-0"></span>\*simone.melchionna@roma1.infn.it

- <span id="page-6-1"></span><sup>1</sup> S. Iijima, Nature (London) **56**, 354 (1991).
- <span id="page-6-2"></span><sup>2</sup> J. J. Kasianowicz, E. Brandin, D. Branton, and D. W. Deamer, Proc. Natl. Acad. Sci. U.S.A. 93, 13770 (1996).
- <span id="page-6-3"></span><sup>3</sup>B. Hille, *Ionic Channels of Excitable Membranes* (Sinauer, Sunderland, MD, 1992).
- <span id="page-6-4"></span><sup>4</sup>G. Hummer, J. C. Rasaiah, and J. P. Nowortya, Nature (London) 414, 188 (2001).
- <span id="page-6-5"></span>5R. Allen, S. Melchionna, and J.-P. Hansen, Phys. Rev. Lett. **89**, 175502 (2002); J. Chem. Phys. 119, 3905 (2003).
- <span id="page-6-6"></span><sup>6</sup> J. Dzubiella and J.-P. Hansen, J. Chem. Phys. **122**, 234706  $(2005).$
- <span id="page-6-7"></span>7O. Beckstein, K. Tai, and M. S. P. Sansom, J. Am. Chem. Soc. 126, 14694 (2004).
- <span id="page-6-8"></span>8P. Attard, C. P. Ursenbach, and G. N. Patey, Phys. Rev. A **45**, 7621 (1992).
- 9D. R. Bérard, P. Attard, and G. N. Patey, J. Phys. Chem. **98**, 7236  $(1992).$
- <span id="page-6-9"></span>10E. E. Meyer, K. J. Rosenberg, and J. Israelachvili, Proc. Natl. Acad. Sci. U.S.A. 103, 15739 (2006).
- <span id="page-6-10"></span><sup>11</sup>P. Attard, Adv. Colloid Interface Sci. 104, 75 (2003).
- <span id="page-6-11"></span><sup>12</sup> J.-L. Barrat and J.-P. Hansen, *Basic Concepts for Simple and Complex Liquids* Cambridge University Press, Cambridge, 2003).
- <span id="page-6-12"></span><sup>13</sup> T. Pompe and S. Herminghaus, Phys. Rev. Lett. **85**, 1930 (2000).
- <span id="page-6-13"></span><sup>14</sup> J. Yang, H. Duan, D. Fornasiero, and J. Ralston, J. Phys. Chem. B 107, 6139 (2003).
- <span id="page-6-27"></span>15N. Ishida, R. Inoue, M. Miyahara, and K. Higashitani, Langmuir

16, 6377 (2000).

- <span id="page-6-14"></span>16A. Poynor, L. Hong, I. K. Robinson, S. Granick, Z. Zhang, and P. A. Fenter, Phys. Rev. Lett. 97, 266101 (2006).
- <span id="page-6-15"></span>17K. Lum, D. Chandler, and J. D. Weeks, J. Phys. Chem. B **103**, 4570 (1999).
- <span id="page-6-16"></span>18B. Lefevre, A. Saugey, J.-P. Barrat, L. Bocquet, E. Charlaix, P. F. Gobin, and G. Vigier, J. Chem. Phys. 120, 4927 (2004).
- <span id="page-6-18"></span>19U. Essmann, L. Perera, M. L. Berkowitz, T. Darden, and H. Lee, and L. G. Pedersen, J. Chem. Phys. **103**, 8577 (1995).
- <span id="page-6-19"></span>20H. J. C. Berendsen, J. P. M. Postma, W. F. van Gunsteren, A. Di Nola, and J. R. Haak, J. Chem. Phys. 81, 3684 (1984).
- <span id="page-6-20"></span>21D. Frenkel and B. Smit, *Understanding Molecular Simulation* (Academic, London, 1996).
- <span id="page-6-17"></span>22W. L. Jorgensen, J. Chandrasekhar, J. D. Madura, R. W. Impey, and M. L. Klein, J. Chem. Phys. 79, 926 (1983).
- <span id="page-6-23"></span>23D. M. Huang and D. Chandler, J. Phys. Chem. B **106**, 2047  $(2002).$
- <span id="page-6-24"></span><sup>24</sup>D. Chandler, Phys. Rev. E **48**, 2898 (1993).
- <span id="page-6-22"></span><sup>25</sup> J. P. Hansen and I. R. McDonald, *Theory of Simple Liquids*, 3rd ed. (Academic, Amsterdam, 2006).
- <span id="page-6-25"></span>26W. H. Press *et al.*, *Numerical Recipes in C: The Art of Scientific* Computing (Cambridge University Press, Cambridge, 2002).
- <span id="page-6-21"></span>27W. Humphrey, A. Dalke, and K. Schulten, J. Mol. Graphics **14**, 33 (1996).
- <span id="page-6-26"></span><sup>28</sup> P.-G. de Gennes, Langmuir **18**, 3413 (2002).
- <span id="page-6-28"></span>29R. M. M. Smeets, U. F. Keyser, M. Y. Wu, N. H. Dekker, and C. Dekker, Phys. Rev. Lett. 97, 088101 (2006).