

First-principles study of the mixed oxide α -FeCrO₃

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We have investigated the electronic and magnetic properties of the mixed oxide α -FeCrO₃ and compared it to the parent oxides α -Fe₂O₃ and α -Cr₂O₃. Density functional theory B3LYP calculations with the nonlocal Hartree-Fock exchange contribution reduced from 20% to 10% were found to reproduce the band gaps of α -Fe₂O₃ and α -Cr₂O₃ remarkably well. Optimized cell constants also agreed very well with experimental values. Thus, this method was used to study α -FeCrO₃. α -FeCrO₃ is predicted to be a charge-transfer insulator with O(2*p*) and Cr(3*d*) predominating in the upper edge of the valence band and Fe(3*d*) in the lower edge of the conduction band. The direct band gap of α -FeCrO₃ is predicted to be close in value to that of α -Fe₂O₃. For ordered α -FeCrO₃, the lowest energy is found for chromium ions occupying the sites related by the *c* glide plane. The antiferromagnetic ground state of this oxide is found to be that with magnetic ordering as in α -Fe₂O₃.

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I. INTRODUCTION

α -Fe₂O₃ and α -Cr₂O₃ both adopt a corundumlike structure, but display differences in the magnetic ordering of the cations and in the nature of the bands on either side of the Fermi level. In the primitive rhombohedral unit cell of the nonmagnetic or ferromagnetic corundum structure, there are four symmetry-related metal ions aligned on the three-fold axis with *z* coordinates of 0.15, 0.35, 0.65, and 0.85 (Fig. 1). Following Catti and Sandrone,¹ we label these 1, 2, 3, and 4 in the order of increasing *z* coordinate, as indicated in the figure. The pairs 1, 2 and 3, 4 are related by two-fold axes at *z*=0.25 and *z*=0.75; the pairs 2, 3 and 4, 1 are related by symmetry centers at *z*=0 and *z*=0.5, and the pairs 1, 3 and 2, 4 are related by the *c* glide plane. The ferromagnetic state retains the full $R\bar{3}c$ symmetry. For the antiferromagnetic state, there are three possibilities of lower symmetry, $R3c(\uparrow\downarrow\uparrow\downarrow)$, $R\bar{3}(\uparrow\downarrow\downarrow\uparrow)$, and $R32(\uparrow\uparrow\downarrow\downarrow)$, where the arrows represent the relative orientation of spins on positions 1, 2, 3, and 4 in that order. Neutron diffraction experiments^{2,3} have shown that below the Néel temperature, α -Cr₂O₃ adopts the $R3c$ structure and α -Fe₂O₃ the $R\bar{3}$ structure. Thus, for both oxides, spin coupling is antiferromagnetic between the pairs of cations with the longer separation (1, 2 and 3, 4) but is ferromagnetic for pairs separated by the shorter distance (2, 3 and 4, 1) in α -Fe₂O₃ and antiferromagnetic in α -Cr₂O₃. Spectroscopic evidence⁴ suggests that α -Fe₂O₃ is a charge-transfer insulator with a band gap between a lower predominantly O 2*p* band and an upper Fe 3*d* band. By contrast, photoemission studies^{5,6} and inverse photoemission experiments⁶ support the classification of α -Cr₂O₃ as an intermediate-type insulator between charge-transfer and Mott-Hubbard insulators.

The mixed oxides α -Fe_{2-x}Cr_xO₃ also adopt the corundum structure, forming a solid solution retaining this structure throughout the range from 100% α -Cr₂O₃ to 100% α -Fe₂O₃ with a smooth increase in unit cell volume⁷ but a very strong deviation from the Vegard behavior, suggesting either cation ordering or specific magnetic interactions between cations. The solid solutions are antiferromagnetic with a single Néel

temperature that decreases linearly with an increasing proportion of Cr. There is no evidence of superstructure peaks in the diffraction pattern,⁸ suggesting that Fe and Cr occupy the cation sites in a random manner, although an earlier study of the vibrational spectrum⁹ suggested that α -FeCrO₃ adopted an ilmenitelike $R\bar{3}$ structure. For *x*=0.8, 1.0, and 1.2, powder neutron diffraction lines are consistent with the spin ordering of α -Fe₂O₃.⁸ There are, however, changes in the magnetic ordering below the Néel temperature for *x*=1.6⁸.

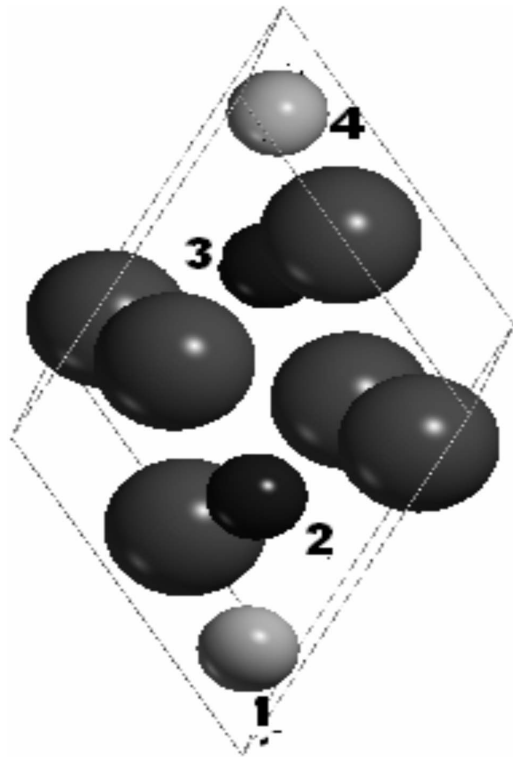


FIG. 1. Primitive unit cell for corundum-type oxides, α -M₂O₃, showing the labeling of the cation sites used in this paper; large sphere oxide ions and smaller sphere metal ions.

These oxides pose a challenge to computation because the metal d electrons are strongly correlated. There have been a number of computational studies of the pure transition metal sesquioxides using both unrestricted Hartree-Fock (UHF) and density functional theory (DFT) methods. Catti *et al.*¹⁰ used the UHF method within the linear combination of crystalline orbitals (LCCO) approach. This grossly overestimated the size of the band gap but correctly predicted that Fe_2O_3 was a charge-transfer insulator and Cr_2O_3 a borderline charge-transfer/Mott-Hubbard insulator. The overestimation of the band gap is due to a complete neglect of correlation. A DFT study¹¹ using the augmented spherical wave method with a local spin density approximation (LSDA) functional underestimated the band gap but, when the results were adjusted for this, produced a good fit to the spectroscopic data. Using an LSDA functional with a tight-binding approach,¹² Punkkinen *et al.* obtained a value of 1.42 eV for the energy band gap by including a Hubbard-type on-site Coulomb repulsion in the Hamiltonian (LSDA+ U method). It should be noted, however, that these two latter studies fixed the cell parameters at the experimental values. Bandyopadhyay *et al.*¹³ found that using LSDA and LSDA+ U within a plane wave code using projector augmented wave based pseudopotentials and relaxing the structure yielded values of 0.31 and 1.88 eV, respectively, for the band gap. A standard pseudopotential plane-wave study of $\alpha\text{-Cr}_2\text{O}_3$ (Ref. 14) reproduced the structural properties well, but the band gap was underestimated at ~ 1.5 eV. Using a generalized gradient approximation (GGA) density functional¹⁵ gives band gaps that are too small for both $\alpha\text{-Fe}_2\text{O}_3$ and $\alpha\text{-Cr}_2\text{O}_3$. However, including strong correlation effects described by a Hubbard-type on-site Coulomb repulsion (GGA+ U) leads to a very good agreement with the size of the band gap and the nature of the orbitals contributing to the bands,¹⁵ although the predicted band gaps of the two solids are closer to each other than found experimentally. Using the hybrid DFT functional B3LYP within the LCCO approach has been shown to predict correctly the ground states of strongly correlated electronic systems and the band gap, including that of $\alpha\text{-Cr}_2\text{O}_3$.¹⁶ B3LYP corresponds to Becke's GGA exchange functional¹⁷ with the correlation potential of Lee *et al.*¹⁸ and with 20% of the exchange functional replaced by the exact Hartree-Fock exchange.

One of our aims is to investigate how well the B3LYP functional describes $\alpha\text{-Fe}_2\text{O}_3$ and $\alpha\text{-Cr}_2\text{O}_3$ in terms of band gap, nature of the valence and conduction bands, and magnetic ordering. Given the differing magnetic ordering and nature of the bands on either side of the band gap, particularly the valence band, in these two oxides, we were also interested in investigating the properties of the mixed oxide $\alpha\text{-FeCrO}_3$. Ordered structures of the mixed oxide with the same number of ions in the unit cell were chosen for study. This enabled us to consider antiferromagnetic solutions without recourse to supercells. The chosen structures are sufficient to determine whether coupling between Fe and Cr ions will be ferromagnetic or antiferromagnetic for both the long and short separations of the ions and are thus relevant to spin ordering in both random and ordered $\alpha\text{-Fe}_{2-x}\text{Cr}_x\text{O}_3$. In addition, although $\alpha\text{-Fe}_{2-x}\text{Cr}_x\text{O}_3$ produced via a high temperature route may well have a random ordering of Fe and Cr

over the cation sites, it is possible that the most energetically favored state at low temperatures, where calculations of this kind are valid, would be ordered. A study¹⁹ of Cr-doped $\alpha\text{-Fe}_2\text{O}_3$ using LSDA+ U , with one Cr substituting for Fe in a 30-atom unit cell, suggested that the filled Cr impurity level lay close to the top of the valence band and that, consequently, the band gap was unchanged from that of $\alpha\text{-Fe}_2\text{O}_3$. We were interested to see if this would remain the case for 50% substitution on the Fe sites.

II. COMPUTATIONAL METHODS

Electronic and magnetic properties and the band structure of the oxides were calculated using CRYSTAL03 (Ref. 20) and CRYSTAL06 (Ref. 21) on the LINUX Beowulf cluster at The Open University and on the LINUX Opteron Beowulf cluster (formerly COMPAQ 8400), Columbus, at The Rutherford Appleton Laboratory. The basis sets used for Fe, Cr, and O were taken from the literature.¹⁰ The tolerances used as the truncation criteria for bielectronic integrals were 10^{-7} , 10^{-7} , 10^{-7} , 10^{-7} , and 10^{-14} . Calculations were performed on the ferromagnetic state and the possible antiferromagnetic states. For $\alpha\text{-FeCrO}_3$, all arrangements of the metal ions within the unit cell were studied. Cell constants and atomic positions were both optimized for $\alpha\text{-Fe}_2\text{O}_3$, $\alpha\text{-Cr}_2\text{O}_3$, and $\alpha\text{-FeCrO}_3$ using the DFT method with the hybrid functional B3LYP in CRYSTAL06. A recent study²² showed that using B3LYP, with the nonlocal Hartree-Fock exchange contribution increased from 20% to 35%, gave very accurate values for spin-spin coupling constants in a series of transition metal compounds. However, it was subsequently suggested that the optimum exchange contribution differed for direct exchange and superexchange²³ and that for the solids studied, 35% was a compromise between the two.

The effect of changing the percentage of the nonlocal Hartree-Fock contribution was therefore investigated. A series of runs on $\alpha\text{-Fe}_2\text{O}_3$ with the experimental cell parameters and varying Hartree-Fock exchange contributions was performed. Values of the energy band gap decreased roughly linearly with decreasing percentage of Hartree-Fock exchange contribution with a discontinuity between 25% and 22%. This coincided with a change from a pure O $2p$ character of the top levels of the valence band to a mixed Fe $3d$ /O $2p$ character. A Hartree-Fock exchange contribution of 10% gave a band gap close to the experimental one. Consequently, runs were performed on $\alpha\text{-Fe}_2\text{O}_3$, $\alpha\text{-Cr}_2\text{O}_3$, and $\alpha\text{-FeCrO}_3$ with optimization of both cell constants and atomic positions using a 10% Hartree-Fock exchange correlation.

III. RESULTS AND DISCUSSION

A. Crystal structure

The calculated energies of the ferromagnetic and the possible antiferromagnetic states for FeCrO_3 with the different possible arrangements of Fe and Cr on the cation sites are given in Table I.

The lowest energy state of $\alpha\text{-FeCrO}_3$ is found to be that with the cations arranged as FeCrFeCr in ascending order of

TABLE I. Calculated energies of the ferro- and antiferromagnetic states of α -FeCrO₃ relative to that of the lowest energy antiferromagnetic state as 0. The ordering of spins and cations is given as 1, 2, 3, 4 along the c axis. Cell constants and atomic positions are relaxed.

Arrangement of cations	Energy (meV/f.u.)		
	Antiferromagnetic		Ferromagnetic
	($\uparrow\downarrow\uparrow\downarrow$)	($\uparrow\downarrow\downarrow\uparrow$)	($\uparrow\uparrow\downarrow\downarrow$)
CrFeFeCr			
B3LYP	110.00		118.48
B3LYP (10%)	125.76		144.72
FeCrFeCr			
B3LYP		0	81.87
B3LYP (10%)		0	99.47
FeFeCrCr			
B3LYP	157.69	79.02	
B3LYP (10%)	173.81	85.20	

z coordinate along the threefold axis. We have also obtained this arrangement of cations as the lowest energy arrangement using interatomic potential calculations. The determining factor in the distribution of Fe and Cr ions is thus likely to be steric rather than electronic. We note that our calculations show that the centrosymmetric arrangement is not the most stable ordered form as an early experimental report suggested.⁹

Optimization of both the cell constants and atomic positions for the lowest energy antiferromagnetic state using DFT with the hybrid B3LYP functional gave values very close to experimental values. Optimizations for both α -Fe₂O₃ and α -Cr₂O₃ were also performed for comparison, and the results are given in Table II. Our results show considerable improvement over the published UHF optimized structure and are comparable to the results of Rohrbach *et al.* using the plane wave GGA method with the addition of Hubbard-type on-site Coulomb repulsion.¹⁵ We note that our values for a and c show a marked decrease from α -Fe₂O₃ to α -Cr₂O₃, in agreement with experiment and in contrast to the GGA+ U results which give very similar structures for these two oxides. Calculations using B3LYP, with the Hartree-Fock exchange contribution decreased from 20% to 10%—

TABLE II. Lattice constants, axial ratio (c/a), magnetic moments, and direct band gap (E_g) for antiferromagnetic corundum-related α -Fe₂O₃, α -FeCrO₃, and α -Cr₂O₃.

Method	a (pm)	c (pm)	c/a	μ (μ_B /cation)	E_g (eV)
α-Fe₂O₃					
UHF (Ref. 12)	511.2	13.820	2.70	4.74	~11
B3LYP	505.7	1388.3	2.75	4.21	3.31
B3LYP (10%)	505.5	1393.9	2.76	4.04	1.93
GGA+ U (Ref. 16)	506.7	1388.2	2.74	4.11	2.0
Expt.	503.5	1374.7	2.73	4.9 ^a	2
α-FeCrO₃					
FeCrFeCr					
B3LYP	504.6	1374.2	2.72	4.21, 2.88	3.26
B3LYP (10%)	505.1	1377.9	2.73	4.06, 2.81	1.95
CrFeFeCr					
B3LYP	505.0	1380.5	2.73	4.25, 2.93	3.15
B3LYP (10%)	505.5	1385.9	2.74	4.11, 2.86	1.63
FeFeCrCr					
B3LYP	504.7	1374.8	2.72	4.24, 2.86	3.29
B3LYP (10%)	505.3	1378.1	2.73	4.09, 2.78	1.65
Expt.	501.0	1362.8	2.72		
α-Cr₂O₃					
UHF (Ref. 12)	504.8	1373.5	2.72	2.99	~15
B3LYP	500.6	1374.8	2.75	2.92	4.4
B3LYP (10%)	501.2	1377.9	2.75	2.87	3.0
GGA+ U (Ref. 16)	507.3	1383.9	2.73	3.01	2.6
Expt.	495.9	1359.3	2.74	2.76 ^b	3.4

^aReference 25.

^bReference 26.

which gave the most accurate band gaps (see below)—gave a slightly less good agreement with the experimental structure, although there was still a marked decrease in the parameters for α -Fe₂O₃ and α -Cr₂O₃ in line with experiment. Even for these calculations, the largest error (in the c axis of α -Fe₂O₃ and α -Cr₂O₃) was only 1.4%, which is an extremely good agreement for calculated lattice parameters.

The cation arrangements FeCrFeCr and FeFeCrCr gave very similar lattice parameters for the lowest energy antiferromagnetic state. For CrFeFeCr, the cell constants were slightly larger. All three results are, however, sufficiently close that a mixture of all three in the crystal would be feasible without causing substantial strain.

B. Magnetic properties

In the nonmagnetic or ferromagnetic corundum structure, the primitive rhombohedral unit cell contains four symmetry-related cations aligned along the threefold axis which, following Catti and Sandrone,¹ we labeled 1, 2, 3, 4 with increasing z coordinate in Fig. 1. The stable antiferromagnetic state for α -Fe₂O₃ is characterized by the spin sequence $\uparrow\downarrow\downarrow\uparrow$, and that for α -Cr₂O₃ by the spin sequence $\uparrow\downarrow\uparrow\downarrow$. In both cases, the spin sequence $\uparrow\uparrow\downarrow\downarrow$ is the next most stable antiferromagnetic state.

Table I presented results for all arrangements of both Fe and Cr ions and all possible spin states. The positions of Fe and Cr ions in the structure are given in the order 1, 2, 3, 4. The blank entries refer to spin states in which both Cr ions have the same spin which is opposed to that on both Fe ions. In these cases, since the Fe and Cr ions have different numbers of unpaired electrons, the solids will be ferrimagnetic rather than antiferromagnetic. From Table I, we predicted that the lowest energy antiferromagnetic state of α -FeCrO₃ is one with Fe on sites 1 and 3 and with Cr on sites 2 and 4. The lowest energy magnetic ordering for this arrangement of cations is the same as for pure hematite, $\uparrow\downarrow\uparrow\downarrow$. We also considered the spin states of other orderings of Fe and Cr on the cation sites. For the cation order FeFeCrCr, the lowest energy spin arrangement is again $\uparrow\downarrow\uparrow\downarrow$, the same as that for CrFeFeCr. However, for the order FeCrCrFe, this arrangement would not be antiferromagnetic. The lowest antiferromagnetic state for this arrangement is $\uparrow\downarrow\uparrow\downarrow$. The energy difference between this state and the higher energy antiferromagnetic state is much smaller than the comparable energy difference for the other two cation orders.

For the lowest energy states for all three orders of cations, coupling between the cations separated by the longer distance is antiferromagnetic. This is not unexpected as both FeFe coupling and CrCr coupling are antiferromagnetic across this distance. From the results for the arrangements FeFeCrCr and FeCrFeCr, we conclude that coupling between Fe and Cr ions separated by the shorter distance is ferromagnetic. For CrFeFeCr, we would thus expect cations on sites 1 and 2 and on sites 3 and 4 to be antiferromagnetically coupled, the Cr ions on sites 4 and 1 to be antiferromagnetically coupled, and the Fe ions on sites 2 and 3 to be ferromagnetically coupled. It is impossible for all these couplings to be satisfied. Thus, this is a potentially spin-frustrated situation and may give rise to a spin glass.

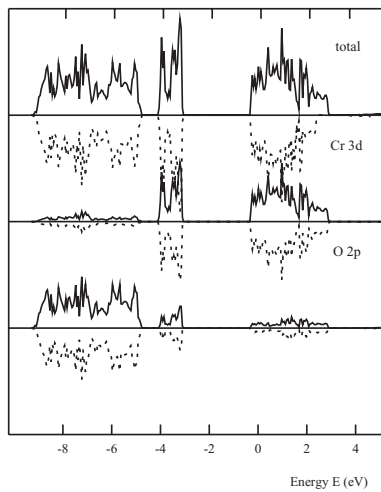
The difference in the signs of the various spin couplings in these oxides can be rationalized by considering the nature of the superexchange in these oxides. It has previously been noted¹ that superexchange in corundum-type structures is not simply a function of cation-cation distance. In the corundum-type structure, the M -O- M' angle is less than the ideal σ -type superexchange value of 180° and is smaller for the cations separated by the shorter distance. However, π -type superexchange, while weaker than the σ -type superexchange at 180°, is still effective at an M -O- M' angle of 90°. In α -Fe₂O₃, the $3d$ orbitals that contribute to π -type superexchange are low in energy and do not interact well with O $2p$ orbitals. Consequently, superexchange in Fe₂O₃ is dominated by σ -type interactions. The Fe-O-Fe angle for the shorter Fe-Fe distance is close to 90°, where such interaction is ineffective and the spin-spin interaction is dominated by direct exchange giving ferromagnetic coupling. In α -Cr₂O₃, by contrast, the superexchange is π type and the cations separated by the shorter distance are antiferromagnetically coupled via the superexchange. From our results, it would appear that Fe-O-Cr interactions are dominated by the σ -type superexchange. This is not unexpected as the π -type superexchange would still be inhibited by the lack of strong interaction between the relevant Fe $3d$ orbitals and O $2p$ orbitals. Calculated magnetic moments tend to be close to experimental for UHF calculations but low for DFT calculations, and this is true here. The calculated magnetic moments are included in Table II.

C. Band structure

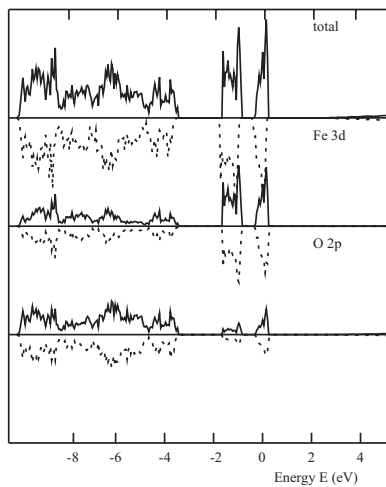
UHF calculations are known to give band gaps that are far too large, but calculations on α -Fe₂O₃ and α -Cr₂O₃ (Ref. 10) correctly predict the nature of the orbitals on either side of the band gap. DFT calculations generally give band gaps that are too small, but recent calculations^{13,15} involving the addition of a Hubbard-type on-site Coulomb interaction give band gaps close to experiment for these oxides.

Our DFT B3LYP calculations give band gaps that are reasonably close to experiment but are too large. In the light of the success of the $+U$ method calculations, the effect of varying the percentage of the nonlocal Hartree-Fock exchange contribution was studied. Following our exploration of the effect of varying the percentage on the band gap of α -Fe₂O₃ (see Sec. II), fully optimized calculations with a nonlocal Hartree-Fock exchange contribution of 10% were performed and it was found that this gave a band gap close to experiment for both α -Fe₂O₃ and α -Cr₂O₃. The results of our calculations, with both standard DFT B3LYP and nonlocal Hartree-Fock exchange contribution changed to 10%, are given in Table II. The band gap for α -FeCrO₃ is predicted to be close to that of α -Fe₂O₃ for both standard B3LYP and B3LYP with the nonlocal Hartree-Fock exchange contribution changed to 10%, for all distributions of Fe and Cr over the cation sites.

Figure 2 compares the total density of states and the projections of metal $3d$ and O $2p$ onto the density of states for the pure oxides. This figure shows clearly that the bottom of the conduction band is dominated by metal $3d$ orbital contri-



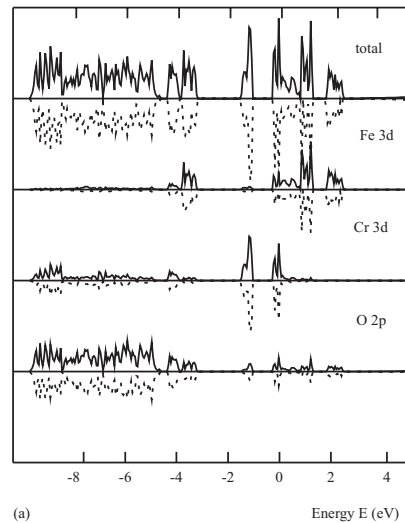
(a)



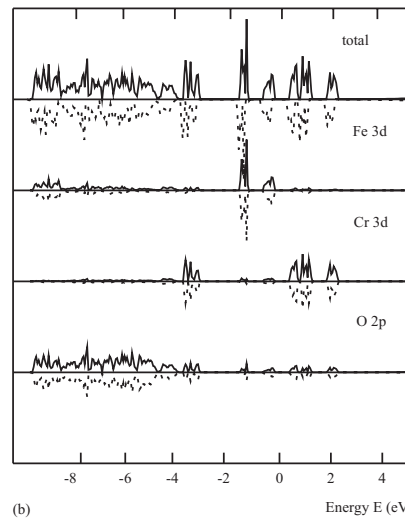
(b)

FIG. 2. Total density of states and projection of $M 3d$ and $O 2p$ on the density of states for the most stable antiferromagnetic configurations of (a) $\alpha\text{-Fe}_2\text{O}_3$ and (b) $\alpha\text{-Cr}_2\text{O}_3$ from calculations using B3LYP, with the Hartree-Fock exchange contribution reduced to 10%. Continuous line refers to “spin-up” electrons and dotted line to “spin-down” electrons.

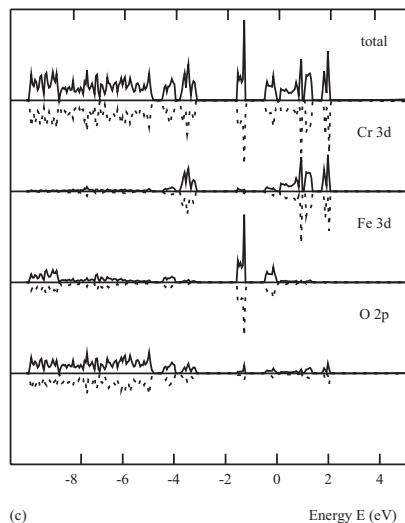
butions. However, whereas in $\alpha\text{-Fe}_2\text{O}_3$ two narrow $Fe 3d$ -dominated bands arise, in $\alpha\text{-Cr}_2\text{O}_3$ the empty $Cr 3d$ -dominated band is much broader. The valence band of $\alpha\text{-Cr}_2\text{O}_3$ is dominated by $Cr 3d$ orbitals with some admixture of $O 2p$ orbitals in line with the experimental description of this oxide being an intermediate-type insulator between charge-transfer and Mott-Hubbard insulators. By contrast, the valence band of $\alpha\text{-Fe}_2\text{O}_3$ contains both $Fe 3d$ and $O 2p$ orbitals with a predominance of $O 2p$ at the band edge. The $Fe 3d$ orbitals at the top edge of the valence band come from a different set of atoms (on sites 2 and 3) from those (on sites 1 and 4) contributing to the lower edge of the conduction band. Thus, we would predict this oxide to be a charge-transfer insulator, as is found experimentally. The appearance and nature of the $\alpha\text{-Fe}_2\text{O}_3$ bands are very similar to those



(a)



(b)



(c)

FIG. 3. Total density of states and projection of $M 3d$ and $O 2p$ on the density of states for the most stable antiferromagnetic configurations of $\alpha\text{-FeCrO}_3$ with (a) cation ordering FeCrFeCr , (b) cation ordering CrFeFeCr , and (c) cation ordering FeFeCrCr from calculations using B3LYP, with the Hartree-Fock exchange contribution reduced to 10%. Continuous line refers to spin-up electrons and dotted line to spin-down electrons.

obtained by several authors^{12,13,15} using GGA+*U* or LSDA+*U* methods.

The total density of states and projections of metal 3*d* and O 2*p* onto the density of states are shown for all the lowest energy antiferromagnetic states of ordered α -FeCrO₃ in Fig. 3. These are very similar. The lower edge of the conduction band is dominated by two narrow Fe 3*d* bands, similar to α -Fe₂O₃. Cr 3*d* bands lie above this. In α -FeCrO₃, there are two distinct Cr 3*d* bands as opposed to the continuous broad band found for α -Cr₂O₃. The top of the valence band is dominated by Cr 3*d*, but this overlaps the O 2*p*-dominated mixed Fe/O bands. The upper edge of this band thus remains at roughly the same energy as in the pure oxides, and because the direct band gap is taken as the difference between the bottom of the conduction band and the top of the valence band, the predicted band gap is very similar to that of α -Fe₂O₃. This band structure resembles that of the Cr-doped hematite.¹⁹ We consider the most likely lowest energy transition across the band gap to be from O 2*p* to Fe 3*d* and therefore classify α -FeCrO₃ as a charge-transfer insulator.

IV. CONCLUSIONS

Ab initio LCCO DFT B3LYP calculations, with the non-local Hartree-Fock exchange contribution decreased to 10%, gave values close to experiment for the band gaps of both α -Fe₂O₃ and α -Cr₂O₃. Optimized cell parameters were slightly greater than the experimental values, but the errors were less than 1.5% in both *a* and *c*, and there was a clear decrease in both *a* and *c* from Fe₂O₃ to Cr₂O₃. Standard DFT B3LYP calculations gave slightly better optimized cell parameters but overestimated the band gaps. In both cases, the calculated band gaps for the mixed oxide α -FeCrO₃ were close to that of α -Fe₂O₃. An inspection of the band structure showed that this was due to the lower edge of the conduction band being dominated by Fe 3*d* in the two oxides. The upper edge of the valence band was dominated by Cr 3*d* in the case

of α -FeCrO₃, but this did not substantially alter the energy of the upper edge of the band. The band structure resembled that of Cr-doped α -Fe₂O₃.

The lowest energy arrangement of Fe and Cr ions on the cation sites in α -FeCrO₃ is that with the ions ordered as FeCrFeCr for the cations of the unit cell in ascending order of *z* coordinate along the threefold axis. This does not support the suggestion of an ordered centrosymmetric arrangement.

Our calculations show that there is little or no Fe-O-Cr π -type superexchange interaction and that the dominant coupling mechanism between Fe and Cr ions on sites 2 and 3 (and 1 and 4) is direct exchange giving a ferromagnetic coupling. Hence, for cells with the cations arranged as FeCrFeCr or FeFeCrCr along the threefold axis, the lowest energy spin ordering was that characteristic of α -Fe₂O₃, $\uparrow\downarrow\downarrow\uparrow$. For CrFeFeCr, we would expect cations on sites 1 and 2 and on sites 3 and 4 to be antiferromagnetically coupled, the Cr ions on sites 4 and 1 to be antiferromagnetically coupled, and the Fe ions on sites 2 and 3 to be ferromagnetically coupled. It is impossible for all these couplings to be satisfied; thus, this is a potentially spin-frustrated situation and may give rise to a spin glass. A sample of α -FeCrO₃, with each unit cell containing two Fe ions and two Cr ions but with the cation sites randomly occupied, would be expected to show a net magnetic ordering similar to that of α -Fe₂O₃, as is observed experimentally.

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¹M. Catti and G. Sandrone, *Faraday Discuss.* **106**, 189 (1997).

²B. N. Brockhouse, *J. Chem. Phys.* **21**, 961 (1953).

³C. G. Shull, W. A. Strauser, and E. O. Wollan, *Phys. Rev.* **83**, 333 (1951); T. G. Worton, R. M. Brugger, and R. B. Bewman, *J. Phys. Chem. Solids* **29**, 435 (1968).

⁴T. Uozumi, K. Okada, and A. Kotani, *J. Electron Spectrosc. Relat. Phenom.* **78**, 103 (1996); A. Fujimori, M. Saeki, N. Kimizuka, M. Taniguchi, and S. Suga, *Phys. Rev. B* **34**, 7318 (1986); F. Ciccacci, L. Braicovich, E. Puppin, and E. Vescovo, *ibid.* **44**, 10444 (1991).

⁵T. Uozumi, K. Okada, and A. Kotani, *J. Electron Spectrosc. Relat. Phenom.* **78**, 103 (1996); R. Zimmerman, P. Steiner, and S. Hüfner, *ibid.* **78**, 49 (1996); X. Li, L. Liu, and V. E. Heinrich, *Solid State Commun.* **84**, 1103 (1992).

⁶T. Uozumi, K. Okada, A. Kotani, R. Zimmerman, P. Steiner, S. Hüfner, Y. Tezuka, and S. Shin, *J. Electron Spectrosc. Relat.*

Phenom. **83**, 9 (1997).

⁷T. Grygar, P. Bezdička, and E. G. Caspary, *J. Electrochem. Soc.* **146**, 3234 (1999); H. E. V. Steinwehr, *Z. Kristallogr.* **125**, 377 (1967).

⁸T. Grygar, P. Bezdička, J. Dědeček, E. Petrovsky, and O. Schneeweis, *Ceramics - Silikáty* **47**, 32 (2003).

⁹K. F. McCarty and D. R. Boehme, *J. Solid State Chem.* **79**, 19 (1989); G. Busca, G. Ramis, M. del Carmen Prieto, and V. S. Escribano, *J. Mater. Chem.* **3**, 665 (1993); M. I. Baraton, G. Busca, M. C. Prieto, G. Ricchiardi, and V. Sanchez Escibano, *J. Solid State Chem.* **112**, 9 (1994).

¹⁰M. Catti, G. Sandrone, G. Valerio, and R. Dovesi, *J. Phys. Chem. Solids* **57**, 1735 (1996); M. Catti, G. Valerio, and R. Dovesi, *Phys. Rev. B* **51**, 7441 (1995).

¹¹L. M. Sandratskii, M. Uhl, and J. Kübler, *J. Phys.: Condens. Matter* **8**, 983 (1996).

¹²M. P. J. Punkkinen, K. Kokko, W. Hergert, and I. J. Värynen, *J.*

- Phys.: Condens. Matter **11**, 2341 (1999).
- ¹³A. Bandyopadhyay, J. Velev, W. H. Butler, S. K. Sarker, and O. Bengone, Phys. Rev. B **69**, 174429 (2004).
- ¹⁴A. Y. Dobin, W. Duan, and R. M. Wentzcovitch, Phys. Rev. B **62**, 11997 (2000).
- ¹⁵A. Rohrbach, J. Hafner, and G. Kresse, Phys. Rev. B **70**, 125426 (2004).
- ¹⁶J. Muscat, A. Wander, and N. M. Harrison, Chem. Phys. Lett. **342**, 397 (2001).
- ¹⁷A. D. Becke, J. Chem. Phys. **98**, 5648 (1993); S. H. Vosko, L. Wilk, and M. Nusair, Can. J. Phys. **58**, 1200 (1980).
- ¹⁸C. Lee, W. Yang, and R. G. Parr, Phys. Rev. B **37**, 785 (1988).
- ¹⁹J. Velev, A. Bandyopadhyay, W. H. Butler, and S. J. Sarker, Phys. Rev. B **71**, 205208 (2005).
- ²⁰V. R. Saunders *et al.*, CRYSTAL2003 User's Manual, University of Torino, Torino, 2003.
- ²¹R. Dovesi *et al.*, CRYSTAL06 User's Manual, University of Torino, Torino, 2006.
- ²²X. Feng and N. M. Harrison, Phys. Rev. B **70**, 092402 (2004).
- ²³F. Cora, M. Alfredsson, G. Mallia, D. S. Middlemiss, W. C. Mackrodt, R. Dovesi, and R. Orlando, Struct. Bonding (Berlin) **113**, 171 (2004).
- ²⁴P. Ugliengo, D. Viterbo, and G. Chiari, Z. Kristallogr. **207**, 9 (1993); P. Ugliengo, <http://www.moldraw.unito.it>
- ²⁵E. Kren, P. Szabo, and G. Konczos, Phys. Lett. **19**, 103 (1965).
- ²⁶M. Corliss, J. M. Hastings, R. Nathans, and G. Shirase, J. Appl. Phys. **36**, 1099 (1965).