# Correlation between fragility and glass-forming ability of metallic alloys

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(Received 24 May 2007; revised manuscript received 25 July 2007; published 6 September 2007)

Analysis of the relaxation time of the glass forming liquids at near liquidus temperatures was conducted, correlation between the critical cooling rate for glass formation, fragility of the glass forming liquid, and reduced glass transition temperature was identified, and a glass forming ability (GFA) parameter  $(F_1 = 2[(m/m_{min})(1/T_{rg}-1)+2]^{-1})$  was proposed. This GFA parameter, which increases with a decrease in the critical cooling rate, is a function of the reduced glass transition temperature  $T_{rg}$  and a fragility index *m*, and it varies from ~0 in the case of extremely fragile liquid to  $2T_{rg}/(1+T_{rg})$  in the case of extremely strong liquid. An exponential relationship between the critical cooling rate for glass formation and the parameter  $F_1$  was identified and verified using available experimental data for metallic and nonmetallic glasses.

DOI: 10.1103/PhysRevB.76.104202

PACS number(s): 64.70.Pf, 61.43.Dq, 81.05.Kf, 83.60.-a

### **INTRODUCTION**

Over the last two decades, a number of bulk metallic glasses have been produced with the thicknesses from 1 mm to several centimeters, and empirical methods have been proposed<sup>1,2</sup> to guide the discovery of new glasses with better glass forming ability (GFA). A straightforward indicator of GFA is the critical cooling rate  $R_c$ , above which no crystallization occurs during solidification, and lower  $R_c$  always correspond to higher GFA.<sup>2,3</sup> Although this parameter allows a way to directly validate and compare GFA of different alloys, a number of solidification trials with varying cooling rates of cast material are required to determine  $R_c$ , which is a time and labor consuming process. Thus, other parameters, which can easily be determined from differential thermal analysis, have been proposed and tried to correlate with  $R_c$ .<sup>2,4–6</sup> The most extensively used empirical parameters are the reduced glass transition temperature,  $T_{rg} = T_g/T_l$ , a supercooled liquid range,  $\Delta T_x = T_x - T_g$ , and the parameter  $\gamma = T_x / (T_g + T_l)$ . Here,  $T_g$ ,  $T_x$ , and  $T_l$  are the glass transition, crystallization, and liquidus temperatures, respectively. Although each of these empirical relations can correlate quite well with GFA of some alloys, the correlation can be poor for other alloy systems.<sup>4–6</sup> There is also not yet a clear answer on what physical factors these relations are based.

It has recently been perceived that good glass forming alloys generally have strong liquids with high viscosity, while marginal glass formers have more fragile liquids.<sup>7–9</sup> Though no direct correlation between GFA and fragility has yet been identified,<sup>10,11</sup> it was suggested that GFA can be a complex function of fragility and  $T_{rg}$  (Ref. 10) or fragility and the onset driving force for crystallization.<sup>12</sup> This paper is focused on identifying a fundamental relationship between fragility and GFA in metallic and nonmetallic glass formers.

### FRAGILE BEHAVIOR OF SUPERCOOLED LIQUID

During supercooling of liquid, the relaxation time  $(\tau)$  for atom rearrangements can increase in a non-Arrhenius fashion by many orders of magnitude in a narrow temperature range. The magnitude of departure from Arrhenius behavior is called liquid fragility<sup>13,14</sup> and the non-Arrhenius behavior of  $\tau(T)$  can be described by the Vogel-Fulcher-Tammann (VFT) expression<sup>13</sup>

$$\tau = \tau_o \exp\left(\frac{DT_o}{T - T_o}\right),\tag{1}$$

where  $\tau_o$ , *D*, and  $T_o$  are parameters and *T* is the temperature in Kelvin. At  $D \ge 100$ , the behavior is very much like Arrhenius and with *D* decreasing to below 10, the behavior becomes more fragile. The parameter *D* is therefore called the strength parameter.<sup>14</sup> The parameter  $T_o$  depends on *D* in such a way that when *D* approaches infinity,  $T_o$  moves toward zero and when *D* approaches zero,  $T_o$  becomes equal to  $T_g$ . Indeed, at  $T=T_g$ , the logarithmic form of Eq. (1) reads

$$\log_{10}\left(\frac{\tau_g}{\tau_o}\right) = \frac{DT_o}{(T_g - T_o)\ln 10},\tag{2}$$

where  $\tau_g$  is the relaxation time at  $T_g$ . By definition,  $\tau_g = 100 \text{ s}$ ,<sup>13</sup> while experimental data indicate that for many liquids,  $\tau_o \approx 10^{-14} \text{ s}$ .<sup>14–17</sup> This leads to the following relationship between *D* and  $T_o$ :

$$D = \frac{m_{\min}(T_g - T_o)}{T_o} \ln 10,$$
 (3)

where  $m_{min} \equiv \log_{10}(\tau_g/\tau_o) \approx 16$ . By combining Eqs. (1) and (3), we obtain a modified VFT relation,

$$\log_{10}\left(\frac{\tau}{\tau_o}\right) = m_{\min}\frac{T_g - T_o}{T - T_o}.$$
(4)

A convenient method to measure fragility of glass forming liquids has recently been suggested<sup>14–16</sup> by using a fragility index m,

$$m = \frac{d \log_{10} \tau}{d(T_g/T)_{T=T_g}}.$$
 (5)

Liquids with  $m \approx m_{\min}$  show the Arrhenius behavior, and larger departure of *m* from  $m_{\min}$  indicates higher fragility. A relation between *m* and  $T_o$  is obtained by differentiating Eq. (4),



FIG. 1. Time-temperature transformation diagram for the onset of crystallization of a glass forming liquid (schematic). Crystallization occurs between  $T_l$  and  $T_g$ , and it can be avoided when the liquid is chilled with the cooling rate  $R \ge R_c$ .

$$\frac{1}{m} = \frac{1}{m_{\min}} \left( 1 - \frac{T_o}{T_g} \right). \tag{6}$$

A relation between m and D can be obtained by combining Eqs. (3) and (6),

$$D = \frac{m_{\min}^2}{m - m_{\min}} \ln 10.$$
 (7)

# CORRELATION BETWEEN LIQUID FRAGILITY AND THE CRITICAL COOLING RATE FOR GLASS FORMATION

We will now identify the correlation between the liquid fragility and glass forming ability. Liquid can be undercooled and form the glassy state only if crystallization is kinetically constrained due to a rapid increase in the viscosity and relaxation time during quenching. Crystallization may occur in the temperature interval between  $T_l$  and  $T_g$  and an incubation time is required to start the crystallization.4,18 The temperature dependence of the incubation time [a so-called timetemperature transformation (TTT) diagram, Fig. 1] has a C shape, and the minimum time  $t_n$ , which is required to start crystallization, occurs at a temperature  $T_n$  located between  $T_g$ and  $T_l$ . This temperature can be expressed in terms of  $T_g$  and  $T_l$  as  $T_n = a(T_g + T_l)$ , where parameter *a* is between 0.45 and 0.55, and it is generally close to 0.5.18-20 To avoid crystallization, the cooling curve should not intersect the TTT curve, and the minimum (critical) cooling rate  $R_c$  required to form a glass is the cooling rate needed to bypass the nose of the TTT curve (see Fig. 1).

Therefore,  $R_c$  is inversely proportional to  $t_n$  and can be virtually defined as  $R_c \approx (T_l - T_n)/t_n$ . It is reasonably to assume that  $t_n$  is proportional to the relaxation time  $\tau_n$  of the supercooled liquid at  $T=T_n$ , which can be determined from Eq. (4) as

$$\log_{10}\left(\frac{\tau_{n}}{\tau_{o}}\right) = \frac{m_{\min}(T_{g} - T_{o})}{T_{n} - T_{o}} \approx \frac{m_{\min}(T_{g} - T_{o})}{0.5(T_{l} + T_{g}) - T_{o}}.$$
 (8)

Therefore,  $\log_{10}(R_c) \sim \log_{10}(1/\tau_n) = -m_{\min}(T_g - T_o)/[0.5(T_l + T_g) - T_o]$ . Because the glass forming ability increases with a decrease in  $R_c$ , a GFA parameter  $F_1$ , which is proportional to  $-\log_{10}(R_c)$ , can be defined,

$$F_1 = \frac{(T_g - T_o)}{0.5(T_l + T_g) - T_o} \sim -\log_{10}(R_c).$$
(9)

According to Eq. (9),  $F_1$  increases and  $R_c$  decreases with an increase in  $T_g$  and a decrease in  $T_o$  and  $T_l$ . In the extreme case of very strong liquid  $(T_o \approx 0)$ ,  $F_1 = 2T_{rg}/(1 + T_{rg})$ , where  $T_{rg} = T_g/T_l$ . For very fragile liquids, when  $T_o$  approaches  $T_g$ ,  $F_1$  will be close to zero.

Taking into account the relation between  $T_o$  and D [Eq. (3)] or between  $T_o$  and m [Eq. (6)],  $F_1$  can also be expressed in terms of  $T_{rg}$  and D or  $T_{rg}$  and m,

$$F_1 = \frac{2T_{rg}D}{D(1+T_{rg}) + m_{\min}(1-T_{rg})\ln 10}$$
(10)

1

or

$$F_1 = 2 \left[ \frac{m}{m_{\min}} \left( \frac{1}{T_{rg}} - 1 \right) + 2 \right]^{-1}.$$
 (11)

The data presented in Tables I and II were used to validate the GFA parameter  $F_1$  and identify the correlation between  $F_1$  and  $R_c$ . To illustrate generality of the present analysis, not only a broad range of metallic glasses but also several nonmetallic glasses were used for which  $R_c$  values are known and other parameters, which are required to determine  $F_1$ , are also available experimentally. Table I lists glasses for which reliable parameters  $T_o$  and D are available, and m was calculated using  $m=DT_oT_g/(T_g-T_o)^2 \ln 10.^{15}$  Two values of the parameter  $F_1$ ,  $F_1(T_o)$  and  $F_1(D)$ , listed in this table for each alloy, were calculated using Eqs. (9) and (10), respectively, and their average values were used for validation.

Table II lists the glasses for which reliable *m* values are available or they can be determined using Eq. (5) from the experimentally accessible temperature dependences of the relaxation time or viscosity near  $T_g$ . Correspondingly, Eq. (11) was used to calculate  $F_1$  listed in this table. Figure 2 shows correlation between  $R_c$  and the GFA parameter  $F_1$ . The best linear fit of these experimental data points in the coordinates  $\log_{10}(R_c)$  vs  $F_1$  was conducted using the least squares method regression analysis, and the following relation was identified:

$$R_c = R_{co} \exp(-AF_1), \tag{12}$$

where  $R_{co} \approx 2.7 \times 10^{11}$  K/s and  $A \approx 48.7$ . A rather high value of the correlation coefficient (or the coefficient of determination,  $R^2 = 0.962$ ) indicates that Eq. (12) fits the experimental points very well. If relation (12) is valid within a whole range of  $F_1$ , then it predicts  $R_c$  maximum for the extremely fragile liquid  $(F_1=0)$ ,  $(R_c)_{max} \equiv R_{co} \approx 2.7 \times 10^{11}$  K/s. This value is in good agreement with the critical cooling rate range for pure metals.<sup>2,4</sup> For the extremely strong liquid, when  $T_{rg} \approx 2/3$  (Ref. 21) and  $F_1 \approx 0.8$ , Eq. (12) predicts the minimum critical cooling rate  $(R_c)_{min} \approx 2.3 \times 10^{-6}$  K/s, which can be compared with  $R_c \approx 10^{-5}$  K/s for SiO<sub>2</sub>.<sup>31,32</sup>

TABLE I. The critical cooling rate  $R_c$ , characteristic temperatures  $(T_g, T_l, T_o)$ , reduced glass transition temperature  $T_{rg}$ , strength parameter D, fragility index m, and GFA parameter  $F_1$  for several bulk metallic glasses and two oxide glasses.

Glass formers	<i>R</i> <sub>c</sub> (K/s)	Т <sub>g</sub> (К)	<i>T</i> <sub><i>l</i></sub> (K)	Т <sub>о</sub> (К)	D	т	$F_1 \\ (D)$	$F_1 \\ (T_o)$
$Mg_{65}Cu_{25}Y_{10}^{a}$	50	402	730	260	22.1	50	0.479	0.464
$Pd_{40}Ni_{40}P_{20}^{b}$	1.6	578	973	390	18.1	50	0.491	0.488
$Pd_{48}Ni_{32}P_{20}^{c}$	10	590	985	392	16.6	43	0.481	0.501
$Pd_{77.5}Cu_6Si_{16.5}^{d}$	500	637	1058	493	11.1	73	0.412	0.406
$Cu_{47}Ti_{34}Zr_{11}Ni_8^e$	250	673	1128	500	12.0	59	0.421	0.432
Zr <sub>41.2</sub> Ti <sub>13.8</sub> Cu <sub>12.5</sub> Ni <sub>10</sub> Be <sub>22.5</sub> <sup>f</sup>	1.2	625	993	412.5	18.5	46	0.532	0.536
Zr <sub>46.75</sub> Ti <sub>8.25</sub> Cu <sub>7.5</sub> Ni <sub>10</sub> Be <sub>27.5</sub> <sup>g</sup>	8.0	590	1020	372	22.7	46	0.511	0.503
SiO <sub>2</sub> <sup>h</sup>	$10^{-5}$	1452	1999	530	63.3	25	0.770	0.771
GeO <sub>2</sub> <sup>h</sup>	$10^{-3}$	816	1388	199	112.6	21	0.683	0.683

<sup>a</sup>Reference 22.

<sup>b</sup>References 23 and 24. <sup>c</sup>Reference 25. <sup>d</sup>References 25 and 26. <sup>e</sup>References 7 and 25. <sup>f</sup>References 27–29.

<sup>g</sup>References 25 and 30. <sup>h</sup>References 31 and 32.

$R_c$ (K/s)	$T_g$ (K)	<i>Т</i> <sub><i>l</i></sub> (К)	т	$F_1$
89	491	941	42	0.455
109	456	896	43	0.435
20	472	900	37	0.485
10	467	835	35	0.540
43	459	878	42	0.453
7.9	466	823	37	0.530
0.1	577	836	52	0.578
1.5	656	1168	35	0.539
$10^{-4}$	1393	2003	28	0.687
$10^{-2}$	820	1383	24	0.660
169	995	1664	66	0.419
$1.7 \times 10^{-3}$	708	1135	29	0.647
1.0	710	1316	33	0.532
1.0	218	313	66	0.521
	$\begin{array}{c} R_c \\ (\text{K/s}) \\ \\ 89 \\ 109 \\ 20 \\ 10 \\ 43 \\ 7.9 \\ 0.1 \\ 1.5 \\ 10^{-4} \\ 10^{-2} \\ 169 \\ 1.7 \times 10^{-3} \\ 1.0 \\ 1.0 \\ 1.0 \end{array}$	$\begin{array}{c cccc} R_c & T_g \\ (\text{K/s}) & (\text{K}) \\ \hline & 89 & 491 \\ 109 & 456 \\ 20 & 472 \\ 10 & 467 \\ 43 & 459 \\ 7.9 & 466 \\ 0.1 & 577 \\ 1.5 & 656 \\ 10^{-4} & 1393 \\ 10^{-2} & 820 \\ 169 & 995 \\ 1.7 \times 10^{-3} & 708 \\ 1.0 & 710 \\ 1.0 & 218 \\ \hline \end{array}$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$

TABLE II. The critical cooling rate  $R_c$ , glass transition  $T_g$ , and liquidus  $T_l$  temperatures, fragility index m, and GFA parameter  $F_1$  for several bulk metallic glasses and nonmetallic glasses.

<sup>a</sup>References 33–35.

<sup>b</sup>References 33 and 34.

<sup>c</sup>References 34 and 35.

<sup>d</sup>References 6, 8, and 36.

<sup>e</sup>References 6, 8, and 37.

<sup>f</sup>References 14, 38, and 39.

<sup>g</sup>References 39 and 40.

<sup>h</sup>References 41 and 42.

<sup>i</sup>Reference 43.

<sup>j</sup>References 31, 40, and 44.



FIG. 2. Correlation between the critical cooling rate  $R_c$  and the glass forming ability parameter  $F_1$  for several glass forming systems listed in Tables I and II. Solid circles correspond to the bulk metallic glasses and open diamonds correspond to the nonmetallic glasses.

Figure 3(a) shows correlation between  $R_c$  and  $T_{rg}$  for the glass formers from Tables I and II. Although there is a trend for  $R_c$  to decrease with an increase in  $T_{rg}$ , the correlation is not very good ( $R^2$ =0.451). This indicates that  $T_{rg}$  cannot be a reliable GFA parameter. Similar conclusion regarding  $T_{rg}$  was also made in other publications.<sup>6,10,12</sup> In accord to Eqs. (9)–(11),  $T_{rg}$  can be used as a GFA indicator only for glass forming systems in which fragility weakly depends on the composition.

Figure 3(b) shows dependence of  $R_c$  on the fragility index m. There is a trend for  $R_c$  to decrease with a decrease in m. However, for metallic glasses, a "correct" tendency for  $R_c$  to decrease with a decrease in m is observed only at  $R_c$  of  $\sim 10$  K/s and higher. At the lower  $R_c$ , a reverse correlation can be noticed, when  $R_c$  decreases with an increase in m. Overall, the correlation between these two parameters is not very good, and the correlation coefficient is low,  $R^2$ =0.454. No correlation between  $R_c$  and fragility for bulk metallic glasses was also reported in other works,<sup>10–12,45</sup> although some tendency for  $R_c$  to increase with an increase in the fragility index was noticed for the glass forming alloys with  $R_c > 10$  K/s.<sup>45</sup>

### DISCUSSION

Many researchers use  $T_{rg}$  or *m* to estimate GFA of different systems.<sup>3-6</sup> These parameters, when used independently, correlate well with the GFA (i.e., with  $R_c$ ) of some glass forming systems but the correlations are poor for other glass forming systems,<sup>6,9–12,45</sup> and Fig. 3 is an example. Until now, there was no clear explanation of such unpredictable behavior. The analysis conducted in the present work explains the reason of such inconsistency. Indeed, this analysis shows that  $R_c$  is a function of both  $T_{rg}$  and *m* and, therefore, these parameters must be used together to estimate GFA. The parameter  $T_{rg}$  alone can be a good GFA indicator only for glass forming systems which have similar fragility values. However,  $T_{rg}$  cannot be a reliable GFA parameter for materials with significantly different fragilities [see Fig. 3(a)]. Simi-



FIG. 3. Dependence of the critical cooling rate  $R_c$  on (a) the reduced glass transition temperature  $T_{rg}=T_g/T_l$  and (b) the fragility parameter *m* for several glass formers listed in Tables I and II. Solid circles correspond to the bulk metallic glasses and open diamonds correspond to the nonmetallic glasses.

larly, good correlation between GFA and liquid fragility can be observed only for the systems which have nearly the same  $T_{rg}$  values. In general, however, both the reduced glass transition temperature and the fragility must be known in order to predict GFA ( $R_c$ ) of a liquid. As a result, a GFA parameter  $F_1$ , which is proportional to  $-\log_{10}(R_c)$  and is a function of  $T_{rg}$  and m, was introduced [see Eqs. (9)–(11)].

The physical background for such GFA behavior is illustrated in Figs. 4 and 5. Figure 4 illustrates the dependence of the GFA parameter  $F_1$  on m for hypothetical liquids, which have three different  $T_{rg}$  values: 0.4, 0.55, and 0.67. Two horizontal dotted lines corresponding to  $F_1=0.4$  ( $R_c=940$  K/s) and  $F_1 = 0.6$  ( $R_c = 0.06$  K/s) are also drawn, indicating that the liquids with a higher  $F_1$  value have better GFA. These dotted lines cross the  $F_1(m, T_{rg})$  lines at given values of m, which decrease with a decrease in  $T_{rg}$ . Taking into account that liquid fragility increases with an increase in *m*, one can see that liquids with higher  $T_{rg}$  must be more fragile in order to have the same  $R_c$  values. This figure illustrates that (a) each specific value of  $F_1$  defines a particular critical cooling rate  $R_c$ , (b) liquids with different *m* values can have the same  $R_c$ , (c) liquids with different  $T_{rg}$  values can have the same  $R_c$ , and (d) liquids with higher fragility (higher m) must have higher  $T_{rg}$  values in order to have the same GFA  $(R_c)$ . This



FIG. 4. (Color online) Dependence of the glass forming ability parameter  $F_1$  [=0.54-0.047 log<sub>10</sub>( $R_c$ )] on the fragility index *m* at three different  $T_{rg}$  values.

clearly explains why, when they are used individually, the parameters  $T_{rg}$  and *m* cannot predict the glass forming ability. However, when these two parameters are combined into the GFA parameter  $F_1$  through Eq. (11), they predict the glass forming ability of different families of glass forming liquids very well (see Fig. 2).

Figure 5 shows the temperature dependences of the relaxation time of seven glass forming liquids from Table I in the vicinity of the liquidus temperatures. It can be seen from this figure that the alloy Zr<sub>41.2</sub>Ti<sub>13.8</sub>Cu<sub>12.5</sub>Ni<sub>10</sub>Be<sub>22.5</sub> is the strongest and the alloy Pd<sub>77.5</sub>Cu<sub>6</sub>Si<sub>16.5</sub> is the most fragile among these seven alloys. At a given normalized reciprocal temperature  $(T_g/T)$ , a stronger liquid has a longer relaxation time  $\tau$  and, therefore, longer incubation period for starting crystallization. However, at the normalized temperature  $T_n$  $[T_g/T_n \cong 2T_{rg}/(1+T_{rg})]$ , which corresponds to the nose of the TTT crystallization curve (see Fig. 1) and which values are different for different alloys (they are shown as open points on the respective relaxation curves in Fig. 5), the straight dependence of the relaxation time  $\tau_n$  (and, therefore, GFA, which is proportional to  $\log_{10}\tau_n$ ) on liquid fragility may no longer be valid. A stronger liquid with a smaller  $T_{rg}$ may have a shorter  $\tau_n$  and start to crystallize faster than a more fragile liquid with a higher  $T_{rg}$ . For example, the liquid is stronger Zr<sub>46.75</sub>Ti<sub>8.25</sub>Cu<sub>7.5</sub>Ni<sub>10</sub>Be<sub>27.5</sub> than Zr<sub>41.2</sub>Ti<sub>13.8</sub>Cu<sub>12.5</sub>Ni<sub>10</sub>Be<sub>22.5</sub> (compare, respectively, lines 7 and 5 in Fig. 5). However, the latter alloy has higher  $T_{rg}$ (=0.629 versus 0.578), which leads to a higher value of the relaxation time at  $T_g/T_n$  and, therefore, better GFA of the Zr<sub>41,2</sub>Ti<sub>13,8</sub>Cu<sub>12,5</sub>Ni<sub>10</sub>Be<sub>22,5</sub> alloy (see Fig. 5 and Table I). On the other hand, alloys  $Pd_{77.5}Cu_6Si_{16.5}$ ,  $Cu_{47}Ti_{34}Zr_{11}Ni_8$ ,  $Pd_{40}Ni_{40}P_{20}$ , and  $Pd_{48}Ni_{32}P_{20}$  have almost the same  $T_{rg}$  (i.e., the same  $T_g/T_n$  values, see Fig. 5. Therefore, for these four alloys, the GFA increases with a decrease in fragility.



FIG. 5. Fragility plot of the relaxation times  $\tau$  (lines) of seven glass forming alloys. The lines, in the order from the bottom to the top, correspond to (1) Pd<sub>77.5</sub>Cu<sub>6</sub>Si<sub>16.5</sub>, (2) Cu<sub>47</sub>Ti<sub>34</sub>Zr<sub>11</sub>Ni<sub>8</sub>, (3) Pd<sub>40</sub>Ni<sub>40</sub>P<sub>20</sub>, (4) Pd<sub>48</sub>Ni<sub>32</sub>P<sub>20</sub>, (5) Zr<sub>41.2</sub>Ti<sub>13.8</sub>Cu<sub>12.5</sub>Ni<sub>10</sub>Be<sub>22.5</sub>, (6) Mg<sub>65</sub>Cu<sub>25</sub>Y<sub>10</sub>, and (7) Zr<sub>46.75</sub>Ti<sub>8.25</sub>Cu<sub>7.5</sub>Ni<sub>10</sub>Be<sub>27.5</sub>. Open circles on the lines correspond to the nose temperatures  $T_n$  [i.e.,  $T_g/T_n \approx 2T_{rg}/(T_{rg}+1)$  in this plot] of the respective alloys. The  $F_1$  values of these alloys are also plotted here (as crosses) versus respective  $T_g/T_n$  values.

### CONCLUSIONS

Analysis of the fragile behavior and relaxation time of glass forming liquid in the temperature range between the liquidus temperature and glass transition temperature allowed us to identify unique correlation between the critical cooling rate for glass formation  $R_c$ , liquid fragility index m, and reduced glass transition temperature  $T_{rg}$ . Correspondingly, a GFA parameter  $F_1$ , which is proportional to  $-\log_{10}(R_c)$  and is a function of  $T_{rg}$  and m, was proposed. This GFA parameter increases with an increase in  $T_{rg}$  and a decrease in *m* in accord to Eq. (11) and varies from  $\sim 0$  in the case of the extremely fragile liquid (e.g., pure metals) to  $\sim 0.8$  in the case of the extremely strong liquid (e.g., SiO<sub>2</sub>). Validity and universality of this GFA parameter  $F_1$  was experimentally verified for a number of bulk metallic and nonmetallic glasses. On the other hand, when used alone,  $T_{rg}$  and *m* were shown to be able to predict GFA only in special cases.

#### ACKNOWLEDGMENTS

Discussions with D. B. Miracle, S. Gorsse, A. L. Greer, C. A. Angell, and J. M. Scott are very much appreciated. This work was conducted under the Air Force Research Laboratory Contract No. FA8650-04-D-5233.

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