# **Systematic** *ab initio* **study of the magnetic and electronic properties of all 3***d* **transition metal linear and zigzag nanowires**

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The magnetic and electronic properties of both linear and zigzag atomic chains of all 3*d* transition metals have been calculated within density functional theory with the generalized gradient approximation. The underlying atomic structures were determined theoretically. It is found that all the zigzag chains except the nonmagnetic Ni and antiferromagnetic (AF) Fe chains, which form a twisted two-legger ladder, look like a corner-sharing triangle ribbon and have a lower total energy than the corresponding linear chains. All the 3*d* transition metals in both linear and zigzag structures have a stable or metastable ferromagnetic (FM) state. Furthermore, in the V, Cr, Mn, Fe, and Co linear chains and Cr, Mn, Fe, Co, and Ni zigzag chains, a stable or metastable AF state also exists. In the Sc, Ti, Fe, Co, and Ni linear structures, the FM state is the ground state, while in the V, Cr, and Mn linear chains, the AF state is the ground state. The electronic spin polarization at the Fermi level in the FM Sc, V, Mn, Fe, Co, and Ni linear chains is close to 90% or above, suggesting that these nanostructures may have applications in spin-transport devices. Interestingly, the V, Cr, Mn, and Fe linear chains show a giant magnetolattice expansion of up to 54%. In the zigzag structure, the AF state is more stable than the FM state only in the Cr chain. Both the electronic magnetocrystalline anisotropy and magnetic dipolar (shape) anisotropy energies are calculated. It is found that the shape anisotropy energy may be comparable to the electronic one and always prefers the axial magnetization in both the linear and zigzag structures. In the zigzag chains, there is also a pronounced shape anisotropy in the plane perpendicular to the chain axis. Nonetheless, in the FM Ti, Mn, and Co linear chains and AF Cr, Mn, and Fe linear chains, the electronic anisotropy is perpendicular, and it is so large in the FM Ti and Co linear chains as well as in AF Cr, Mn, and Fe linear chains that the easy magnetization axis is perpendicular. In the AF Cr and FM Ni zigzag structures, the easy magnetization direction is also perpendicular to the chain axis, but in the ribbon plane. Remarkably, the axial magnetic anisotropy in the FM Ni linear chain is gigantic, being  $\sim$  12 meV/atom, suggesting that Ni nanowires may have applications in ultrahigh density magnetic memories and hard disks. Interestingly, there is a spin-reorientation transition in the FM Fe and Co linear chains when the chains are compressed or elongated. Large orbital magnetic moment is found in the FM Fe, Co, and Ni linear chains. Finally, the band structure and density of states of the nanowires have also been calculated to identify the electronic origin of the magnetocrystalline anisotropy and orbital magnetic moment.

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### **I. INTRODUCTION**

Magnetism at the nanometer scale has been a very active research area in recent years, $1-4$  $1-4$  because of its novel fundamental physics and exciting potential applications. Theoretically, a great deal of research has been done on both finite and infinite chains of atoms. In particular, calculations for isotropic Heisenberg model with finite-range exchange interactions show that a one-dimensional (1D) chain cannot maintain ferromagnetism at any finite temperatures.<sup>5</sup> Nonetheless, this discouraging conclusion has to be revised when a magnetic anisotropy is present, as in, e.g., quasi-1D crystals. Experimentally, modern methods to prepare nanostructured systems have made it possible to investigate the influence of dimensionality on the magnetic properties. A fundamental idea is to exploit the geometrical restriction imposed by an array of parallel steps on a vicinal surface along which the deposited material can nucleate. For example, Gambardella *et al.*<sup>[6](#page-10-4)</sup> recently succeeded in preparing a high density of parallel atomic chains along steps by growing Co on a high-purity Pt (997) vicinal surface and also observed 1D magnetism in a narrow temperature range of 10–20 K. Structurally stable nanowires can also be grown inside tubular structures, such as the Ag nanowires of micrometer lengths grown inside self-assembled organic  $(cality[4]$ hydroquinone) nanotubes.<sup>7</sup> Short suspended nanowires have been produced by driving the tip of a scanning tunneling microscope into contact with a metallic surface and subsequent retraction, leading to the extrusion of a limited number of atoms from either tip or substrate.<sup>8</sup> Monostrand nanowires of Co and Pd have also been prepared in mechanical break junctions, and full spin-polarized conductance was observed.<sup>9</sup>

The monoatomic chains, being an ultimate 1D structure, are a testing ground for the theories and concepts developed earlier for three-dimensional systems. Furthermore, the 1D character of nanowires can cause several new physical phenomena to appear. It is of fundamental importance to understand the atomic structure in a truly 1D nanowire and how the magnetic and electronic properties change in lower dimensions. Therefore, theoretical calculations at either semiempirical tight-binding or *ab initio* density functional theory level for many infinite and/or finite chains, e.g., linear chains of Co,  $^{10-14}$  $^{10-14}$  $^{10-14}$  Fe,  $^{11,15}$  $^{11,15}$  $^{11,15}$  Ni, Pd,  $^{16}$  Pt, Cu,  $^{10}$  Ag,  $^{17,18}$  $^{17,18}$  $^{17,18}$  and Au,  $^{17,19-22}$  $^{17,19-22}$  $^{17,19-22}$ as well as zigzag chains of  $Ti^{23}$  Fe,<sup>15</sup> and Au,<sup>21</sup> have been reported. Early studies of infinite linear chains of Au,<sup>21[,22](#page-10-16)[,24](#page-10-19)[,25](#page-10-20)</sup>

<span id="page-1-0"></span>

FIG. 1. Schematic structure diagram for (a) the linear and (b) zigzag atomic chains.

Al, $^{26}$  Cu,<sup>18</sup> Ca, Pd, $^{20}$  $^{20}$  $^{20}$  and K (Ref. 20) have shown a wide variety of stable and metastable structures. Recently, the magnetic properties of transition metal infinite linear chains of Fe, Co, and Ni have been calculated.<sup>11[,12,](#page-10-23)[14,](#page-10-9)[15,](#page-10-11)[27](#page-10-24)</sup> These calculations show that the metallic and magnetic nanowires may become important for electronic and/or optoelectronic devices, quantum devices, magnetic storage, nanoprobes, and spintronics.

Despite the above mentioned intensive theoretical and experimental research, current understanding on novel magnetic properties of nanowires and how magnetism affects their electronic and structural properties is still incomplete. The purpose of the present work is to make a systematic *ab initio* study of the magnetic, electronic, and structural prop-erties of both linear and zigzag atomic chains (Fig. [1](#page-1-0)) of all 3d transition metals (TMs). Transition metals, because of their partly filled *d* orbitals, have a strong tendency to magnetize. Nonetheless, only some 3d transition metals (Cr, Mn, Fe, Co, and Ni) exhibit magnetism in their bulk structures. It is, therefore, of interest to investigate possible ferromagnetic (FM) and antiferromagnetic (AF) magnetizations in the linear chains of all 3*d* transition metals including Sc and Ti, which appear not to have been considered. As mentioned before, recent *ab initio* calculations indicate that the zigzag chain structure of, at least, Ti (Ref.  $23$ ) and Fe (Ref.  $15$ ) is energetically more favorable than the linear chain structure. Thus, we also study the structural, electronic, and magnetic properties of all 3*d* transition metal zigzag chains in order to understand how the physical properties of the monoatomic chains evolve as their structures change from linear to zigzag chain.

Relativistic electron spin-orbit coupling (SOC) is the fundamental cause of the orbital magnetization and also the magnetocrystalline anisotropy energy (MAE) of solids. The MAE of a magnetic solid is the difference in total electronic energy between two magnetization directions, or the energy required to rotate the magnetization from one direction to another. It determines whether a magnet is a hard or soft one. Furthermore, knowledge of the MAE of nanowires is a key factor that would determine whether the nanowires have potential applications in, e.g., high-density recording and magnetic memory devices. *Ab initio* calculations of the MAE have been performed mainly for the Fe and Co linear chains, $12,28-30$  $12,28-30$  $12,28-30$  while semiempirical tight-binding calculations have been reported for both linear chains and two-legger ladders of Fe and Co[.30–](#page-10-26)[32](#page-10-27) Unlike 4*d* and 5*d* transition metals, the SOC is weak in 3*d* transition metals. Nonetheless, the MAE could be very large in certain special 3*d* transtion metal structures such as tetragonal FeCo alloys.<sup>33</sup> Therefore, as an endeavor to find nanowires with a large MAE, we have calculated the MAE and also the magnetic dipolar (shape) anisotropy energy for all 3*d* transition metals in both the linear and zigzag structures. Indeed, we find that the FM Ni linear chain has a gigantic MAE, as will be reported in Sec. V. Although in this paper we study only freestanding 3*d* transition metal chains, the underlying physical trends found may also hold for monoatomic nanowires created transiently in break junctions,<sup>9</sup> encapsulated inside 1D nanotubes, $7.29$  $7.29$  or deposited on weakly interacting substrates,  $34$  albeit with the actual values of the physical quantities being modified.

## **II. THEORY AND COMPUTATIONAL METHOD**

In the present first principles calculations, we use the accurate frozen-core full-potential projector augmented-wave (PAW) method,<sup>35</sup> as implemented in the Vienna *ab initio* simulation package (VASP).<sup>[36,](#page-10-32)[37](#page-10-33)</sup> The calculations are based on density functional theory with the exchange and correlation effects being described by the generalized gradient approxi-mation (GGA).<sup>[38](#page-10-34)</sup> We adopt the standard supercell approach to model an isolated atomic chain, i.e., a freestanding atomic chain is simulated by a two-dimensional array of infinitely long, straight or zigzag atomic wires. For both linear and zigzag chains, the nearest wire-wire distance between the neighboring chains is, at least, 10 Å. This wire-wire separation should be wide enough to decouple the neighboring wires, since the energy bands, density of states, magnetic moments, and MAE from our test calculations with a larger separation of 15 Å for the linear Fe atomic chain are nearly identical to those obtained with the wire-wire distance of 10 Å. A large plane-wave cutoff energy of  $\sim$ 340 eV is used for all 3*d* transition metal chains.

The equilibrium bond length (lattice constant) of the linear atomic chains in the nonmagnetic (NM), FM, and AF states is determined by locating the minimum in the calculated total energy as a function of the interatomic distance. The results are also compared with those obtained by structural optimizations, and the differences are small (within 0.4%) for, e.g., the Mn, Fe, and Ni chains. For the zigzag chains, the theoretical atomic structure is determined by structural relaxations using the conjugate gradient method. The equilibrium structure is obtained when all the forces acting on the atoms and the axial stress are less than  $0.02$  eV/Å and 2.0 kbar, respectively. The  $\Gamma$ -centered Monkhorst-Pack scheme with a *k* mesh of  $1 \times 1 \times n$  (*n*=20) in the full Brillouin zone (BZ), in conjunction with the

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FIG. 2. (Color online) (a) Equilibrium bond lengths, (b) magnetization energy  $(\Delta E)$  (i.e., the total energy of a magnetic state relative to that of a nonmagnetic state)  $(\Delta E = E^{FM(AF)} - E^{NM})$ , and (c) spin magnetic moments  $(\mu_B)$  of all the 3*d* transition metal linear atomic chains in the NM, FM, and AF states.

Fermi-Dirac smearing method with  $\sigma$ =0.01 eV, is used to generate *k* points for the BZ integration. With this *k*-point mesh, the total energy is found to converge to within  $10^{-3}$  eV.

Because of its smallness, *ab initio* calculation of the MAE is computationally very demanding and needs to be carefully carried out (see, e.g., Refs. [39](#page-10-35) and [40](#page-10-36)). Here, we use the total energy difference approach rather than the widely used force theorem to determine the MAE, i.e., the MAE is calculated as the difference in the full self-consistent total energies for the two different magnetization directions (e.g., parallel and perpendicular to the chain) concerned. The total energy convergence criteria is 10−6 eV/atom. A very fine *k*-point mesh with  $\sigma$ =0.001 eV is used, with *n* being 500 for the linear atomic chains and 800 for the zigzag chains. The same *k*-point mesh is used for the band structure and density of states calculations.

## **III. LINEAR ATOMIC CHAINS**

#### **A. Bond length and spin magnetic moment**

The calculated equilibrium bond lengths  $(d)$  and atomic spin magnetic moments of all the 3*d* transition metal linear chains in the NM, FM, and AF states are displayed in Fig. [2](#page-2-0) and also listed in Table [I.](#page-2-1) The calculated total energy relative to that of the NM state (i.e., the magnetization energy) of the FM and AF linear atomic chains are also shown in Fig. [2](#page-2-0) and Table [I.](#page-2-1) It is clear from Fig. [2](#page-2-0) that all the 3*d* TM elements which are nonmagnetic in their bulk structures become magnetic in the linear chain structures, though the FM Cu has a very small magnetic moment and is almost degenerate with

<span id="page-2-1"></span>TABLE I. Calculated equilibrium bond lengths (d) (in Å), total energies  $(E_t)$  (in eV/atom) in the FM and AF states (relative to the NM state), and spin magnetic moments  $(m<sub>s</sub>)$  (in  $\mu_B$ /atom) of the 3*d* transition metal linear chains.

	$d_{NM}$	$E_t^{FM}$	$m_s^{FM}$	$d_{FM}$	$E_t^{AF}$	$m_s^{AF}$	$d_{AF}$
Sc	2.71	$-0.057$	1.79	2.88			
Ti	2.21	$-0.036$	0.77	2.22			
V	2.00	0.116	4.06	2.60	$-0.021$	1.13	2.05
Cr	1.82	$-0.363$	5.60	2.80	$-0.683$	3.30	2.32
Mn	1.86	$-0.673$	4.75	2.60	$-0.748$	2.95	2.29
Fe	1.94	$-0.530$	3.41	2.25	$-0.235$	1.82	2.15
Co	2.02	$-0.393$	2.24	2.15	$-0.066$	1.15	2.15
Ni	2.13	$-0.153$	1.11	2.18			
Cu	2.30	$-0.001$	0.06	2.30			

the NM state (Table [I](#page-2-1)). Furthermore, for all the 3*d* TM elements, the NM state is metastable and the ground state is either FM and AF (see Fig. [2](#page-2-0) and Table [I](#page-2-1)). The V linear chain appears to be unique in that it has a large FM magnetic moment of 4.8  $\mu_B$ /atom, but its FM state is higher in energy than the NM state [Table [I](#page-2-1) and Fig.  $2(b)$  $2(b)$ ]. Interestingly, Fig. [2](#page-2-0) also shows that in all the cases, the equilibrium bond length is larger in a magnetic state than in the NM state. This is due to the larger kinetic energy in a magnetic state which make magnetic materials softer and larger in size. This magnetism induced increase in the bond length (or magnetolattice expansion) can be as large as 54%, as in the case of the Cr linear chain. The ground states for the Sc, Ti, Fe, Co, and Ni chains are ferromagnetic, while that for the V, Cr, and Mn chains are antiferromagnetic.

The ground state bond lengths for the Sc, Ti, V, Cr, Mn, Fe, Co, Ni, and Cu chains are 2.88, 2.22, 2.05, 2.32, 2.29, 2.25, 2.15, 2.18, and 2.30 Å, respectively. These bond lengths are generally shorter than their counterparts in the bulk structures. For example, the calculated bond lengths for AF bcc Cr, FM bcc Fe, FM fcc Co, and FM fcc Ni are 2.43, 2.45, 2.48, and 2.49 Å, respectively. The chemical bonding environment in a wire is not the same as that in a bulk structure. In particular, the coordination number in a linear wire is certainly lower than in a bulk material, and this may result in a shorter bond length. Our predictions of the FM ground state for Fe, Co, Ni, and Cu are in good agreement with Refs. [15,](#page-10-11) [18,](#page-10-14) [19,](#page-10-15) and [27.](#page-10-24) Our calculated bond lengths of the 3*d* TM linear chains in the FM state (Table [I](#page-2-1)) agree well with many previous calculations. For example, previous theoretical bond lengths reported for the Fe, Ni, and Co chains are 2.28 Å (Ref. [27](#page-10-24)) and 2.25 Å (Ref. [15](#page-10-11)) for Fe, 2.18 Å (Ref.  $27$ ) for Co, 2.18 Å (Ref. 27) and 2.16 Å (Ref. [19](#page-10-15)) for Ni, and 2.33 Å (Ref. [19](#page-10-15)) and 2.29 Å (Ref. [18](#page-10-14)) for Cu. Our predictions of the AF ground state for the Cr and Mn linear chains are also consistent with the previous reports.<sup>41</sup> Nonetheless, the energy difference between the FM and AF states in the Fe chain being 0.29 eV/atom is somewhat smaller than previous results[.28](#page-10-25)

## **B. Spin-orbit coupling and orbital magnetic moment**

The relativistic SOC is essential for the orbital magnetization and magnetocrystalline anisotropy in solids, though it

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FIG. 3. (Color online) Spin (left panels) and orbital (right panels) magnetic moments as a function of interatomic distance of the ferromagnetic Fe, Co, and Ni linear atomic chains. "Parallel" and "perpendicular" denote the results from fully relativistic calculations with the magnetization parallel and perpendicular to the chain axis, respectively. In the left panels, "no SOC" denotes the results of the scalar-relativistic calculations.

may be weak in the 3*d* transition metal systems. Therefore, unlike several previous studies of the magnetic properties of the  $3d$  TM chains,  $15,27,41$  $15,27,41$  $15,27,41$  we include the SOC in our selfconsistent calculations. When the SOC is taken into account, the spin moments for the linear atomic chains become  $1.79\mu_B$  (Sc),  $0.76\mu_B$  (Ti),  $4.06\mu_B$  (V),  $5.65\mu_B$  (Cr),  $4.74\mu_B$  $(Mn)$ , 3.41 $\mu_B$  (Fe), 2.21 $\mu_B$  (Co), 1.17 $\mu_B$  (Ni), and 0.08 $\mu_B$ (Cu), respectively. These values are almost identical to the corresponding ones obtained without the SOC (see also Fig. [3](#page-3-0)). This is due to the weakness of the SOC in the 3*d* transition metals. However, including the SOC does give rise to a significant orbital magnetic moment in some atomic chains and, importantly, allows us to determine the easy magnetization axis in these 3*d* atomic chains. For the magnetization along the chain direction, the calculated orbital magnetic moments in the FM state are 0.42, 0.23, and 0.45  $\mu_B$ /atom for the Fe, Co, and Ni chains, respectively, though they are only −0.04, −0.02, −0.16, −0.02, −0.04, and 0.0  $\mu_B$ /atom for the Sc, Ti, V, Cr, Mn, and Cu chains, respectively. The orbital moments in the Fe, Co, and Ni atomic chains are, therefore, considerably enhanced, when compared with the bulk materials, $^{42}$  and are also larger than the orbital moments in the Fe, Co, and Ni monolayers. $43,44$  $43,44$ 

To see how the magnetic properties of the atomic chain evolve with the interatomic distance, we plot the spin and orbital moments for the Fe, Co, and Ni chains in the FM state as a function of the bond length in Fig. [3.](#page-3-0) For all three 3*d* TM chains, the spin moment remains almost unchanged as the bond length is increased (Fig. [3](#page-3-0)). As mentioned before, the spin moment is also unaffected when the SOC is taken into account, due to the weakness of the SOC in 3*d* transition

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FIG. 4. Band structures of the Fe (upper panels) and Ni (lower panels) linear chains at the equilibrium bond length. Left panels: The scalar-relativistic band structures. Middle and right panels: The fully relativistic band structures with the magnetization parallel to and perpendicular to the chain axis, respectively. In the left panels, the solid and dashed lines represent spin-up and spin-down bands, respectively. The Fermi level (the dotted horizontal line) is at zero energy.

metals. The same result is found even in the 4*d* (Refs. [29](#page-10-29) and [45–](#page-11-3)[47](#page-11-4)) and 5*d* (Ref. [20](#page-10-22)) TM linear atomic chains. Nonetheless, the SOC gives rise to rather pronounced orbital moments in all three cases, and these orbital moments increase significantly with the bond length, as can be seen in Fig. [3.](#page-3-0) Significantly, the orbital moment shows a strong dependence on the magnetization orientation (Fig. [3](#page-3-0)). The orbital moment for the magnetization along the chain is higher than that for the magnetization perpendicular to the chain. The orbital moments of the Fe, Co, and Ni chains at its equilibrium bond length with a perpendicular magnetization are only 0.15, 0.17, and  $0.12\mu_B$ , respectively. This anisotropy in the orbital moment is especially pronounced in the Ni chain. It is well known that, in general, the magnetization direction with a larger orbital moment would be lower in total energy. Therefore, the easy magnetization direction in the Fe, Co, and Ni chains is expected to be along the chain, as will be reported in Sec. V. Finally, we notice that our results for the spin and orbital moments are in good agreement with previ-ous calculations for the Fe (Refs. [29](#page-10-29) and [30](#page-10-26)) and Co (Ref. [13](#page-10-38)) linear chains.

## **C. Band structure and density of states**

In order to understand the calculated magnetic properties, let us now examine the band structure of the 3*d* transition metal linear chains. Plotted in Fig. [4](#page-3-1) is the band structure obtained without and also with the SOC for the Fe and Ni linear chains in the FM state at the equilibrium interatomic distance. In the absence of the SOC, because of the linear chain symmetry, the bands may be grouped into three sets, namely, the nondegenerate  $s$ - and  $d<sub>z</sub>$ <sup>2</sup>-dominant bands, doubly degenerate  $(d_{xz}, d_{yz})$  bands, and  $(d_{x^2-y^2}, d_{xy})$  dominant bands (see the left panels in Fig. [4](#page-3-1)). The  $(d_{x^2-y^2}, d_{xy})$  bands are narrow because the  $d_{x^2-y^2}$  and  $d_{xy}$  orbitals are perpendicular to the chain, thus forming weak  $\delta$  bonds. The  $(d_{xz}, d_{yz})$ bands, on the other hand, are more dispersive due to the stronger overlap of the  $d_{xz}$  and  $d_{yz}$  orbitals along the chain, which gives rise to the  $\pi$  bonds. The *s*- and  $d_{z}$ <sup>2</sup>-dominant bands are most dispersive since these orbitals form strong  $\sigma$ bonds along the chain. In the FM state, these bands are exchange split, and this splitting into the spin-up and spindown bands is 0.64, 0.57, 2.58, 3.44, 3.67, 2.99, 1.94, 0.96, and 0.04 eV for the Sc, Ti, V, Cr, Mn, Fe, Co, Ni, and Cu chains. The size of this spin splitting could be correlated with the spin moment in the FM state (see Table [I](#page-2-1)). Also, Fig. [4](#page-3-1) shows that when the band filling increases, as one moves from Fe to Ni, the  $(d_{x^2-y^2}, d_{xy})$  bands, which are partially occupied in the Fe chain, now lie completely below the Fermi level in the Ni chain, and hence, play no role in magnetism.

The directional dependence of the magnetization can be explained by analyzing the fully relativistic band structures (see Fig. [4](#page-3-1)). For the Fe linear chain with the axial magneti-zation [Fig. [4](#page-3-1)(b)], the doubly degenerate  $d_{x^2-y^2}$ ,  $d_{xy}$  bands are split into two with angular momenta  $m_l = \pm 2$ . If one of them is fully occupied and the other is empty, the resulting orbital moment is 2. Nonetheless, in the Fe linear chain, both are partially occupied with different occupation numbers Fig.  $4(b)$  $4(b)$ ], resulting in an orbital moment of 0.42  $\mu_B$ /atom. Of course, the larger the SOC splitting, the larger the difference in the occupation number and, hence, the larger the orbital moment. However, for the perpendicular magnetization, the  $d_{x^2-y^2}$ ,  $d_{xy}$  bands remain degenerate [Fig. [4](#page-3-1)(c)] and, hence, do not contribute to orbital magnetization. Therefore, the Fe linear chain would have a smaller orbital magnetic moment. Of course, when the SOC is included, the degenerate  $d_{xz}$ ,  $d_{yz}$ bands are also split into the  $m_l$ =−1 and +1 bands for the axial magnetization, but remain degenerate for the perpen-dicular magnetization (see Fig. [4](#page-3-1)). This SOC splitting of the  $(d_{xz}, d_{yz})$  band and  $(d_{x^2-y^2}, d_{xy})$  band is proportional to  $\langle d_{xz} | H_{SO} | d_{yz} \rangle$ <sup>2</sup> and  $\langle d_{x^2-y^2} | H_{SO} | d_{xy} \rangle$ <sup>2</sup>, respectively. Here, *HSO* is the SOC Hamiltonian. Since  $|\langle d_{xz}|H_{SO}|d_{yz}\rangle|^2$ : $|\langle d_{x^2-y^2}|H_{SO}|d_{xy}\rangle|^2$ =1:4,<sup>48</sup> the SOC splitting of the  $(d_{xz}, d_{yz})$  bands is much smaller than the  $(d_{x^2-y^2}, d_{xy})$ bands (see Figs. [4](#page-3-1) and 5). Therefore, the  $(d_{xz}, d_{yz})$  bands would make a much smaller contribution to the orbital magnetization and also the magnetocrystalline anisotropy, which will be discussed in Sec. V.

In Fig. [5,](#page-4-0) the band structure of the Fe linear chain at several different interatomic distances with the magnetization along the chain direction is displayed. Figure  $3(b)$  $3(b)$  shows that the Fe orbital moment for both magnetization orientations increases with the interatomic distance. However, the increase for the magnetization along the chain axis is much more dramatic than for the perpendicular magnetization. The

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FIG. 5. Band structures of the Fe linear chain with the magnetization along the chain axis at several interatomic distances. The Fermi level (the dotted horizontal line) is the zero energy.

reason for this variation of the orbital moment with the interatomic distance is twofold: one is due to the increase in the localization of the 3*d* orbital wave function with the interatomic distance; the other is due to the detailed change in the band structure. For example, as the interatomic distance goes from 2.4 Å [Fig.  $5(c)$  $5(c)$ ] to 2.6 Å [Fig.  $5(d)$ ], one of the SOC split  $(d_{x^2-y^2}, d_{xy})$  bands becomes fully occupied, resulting in the increase in the occupation number difference in the two  $m_l = \pm 2$  bands and, hence, in a larger orbital moment.

Electric and spin current transports are determined by the characteristics of the band structure near the Fermi level  $(E_F)$ in the systems concerned. Therefore, it would be interesting to examine the energy bands and density of states (DOS) of the atomic chains in the vicinity of the  $E_F$ . The spindecomposed DOS for the FM Sc, V, Cr, Mn, Fe, Co, and Ni linear chains are displayed in Fig. [6.](#page-5-0) In the Fe, Co, and Ni cases, the spin-up states are nearly completely filled and, hence, the DOS at the  $E_F$  is low. On the other hand, the spin-down states are only partially occupied, resulting in a large DOS at the  $E_F$ . Therefore, the density of states at the  $E_F$ in these systems are highly spin polarized. This is usually quantified by the spin polarization *P* defined as

$$
P = \frac{N_{\uparrow}(E_F) - N_{\downarrow}(E_F)}{N_{\uparrow}(E_F) + N_{\downarrow}(E_F)},
$$
\n(1)

where  $N_{\uparrow}(E_F)$  and  $N_{\downarrow}(E_F)$  are the spin-up and spin-down DOS at the  $E_F$ , respectively. The most useful materials for the spintronic applications are the so-called half-metallic materials, in which one spin channel is metallic and the other spin channel is insulating. The spin polarization for these half-metals is either 1.0 or −1.0, and the electric conduction would be fully spin polarized. The calculated spin polarization and also the numbers of the conduction bands that cross

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FIG. 6. (Color online) Density of states of the FM 3*d* TM linear atomic chains at the equilibrium bond length. The Fermi level (dotted vertical lines) is at the zero energy.

the Fermi level in the 3*d* TM chains are listed in Table [II.](#page-5-1) It is clear that the FM V, Fe, Co, and Ni linear chains have a very high spin polarization, though none of the 3*d* TM linear chains in the FM state is half-metallic. Our calculated spin polarizations for the bulk FM bcc Fe, fcc Co, and fcc Ni are −0.55, −0.77, and −0.81, respectively, being considerably smaller than the spin polarization of the corresponding linear chains. This suggests that the Sc, V, Mn, Fe, Co, and Ni nanowires may be good potential materials for spintronic devices[.49](#page-11-6) Interestingly, the FM V chain has a large positive spin polarization (Table [II](#page-5-1) and Fig.  $6$ ).

The magnetic properties and spin polarization near the Fermi level in the linear Fe, Co, and Ni chains have been

<span id="page-5-1"></span>TABLE II. Numbers  $(n_c^{\dagger} \text{ and } n_c^{\dagger})$  of the spin-up and spin-down conduction bands crossing the Fermi level, and spin polarization *P* at the Fermi level in the 3*d* TM atomic chains in the FM state. The spin polarizations  $P$  for the bulk FM bcc Fe, fcc Co, and fcc Ni are −0.55, −0.77, and −0.81, respectively.

		Linear chain	Zigzag chain			
	$(n_c^{\uparrow}, n_c^{\downarrow})$	P	$(n_c^{\uparrow}, n_c^{\downarrow})$	P		
Sc	(4, 1)	0.881	(3, 0)	0.610		
Ti	(5, 4)	0.416	(4, 4)	0.181		
V	(6, 1)	0.930	(3, 3)	0.085		
Cr	(3, 1)	0.777	(4, 2)	0.481		
Mn	(1, 3)	$-0.869$	(2, 1)	$-0.829$		
Fe	(1, 6)	$-0.961$	(2, 4)	$-0.643$		
Co	(1, 6)	$-0.920$	(2, 7)	$-0.884$		
Ni	(1, 6)	$-0.951$	(2, 2)	$-0.890$		

calculated *ab initio* by several groups.<sup>12,[27,](#page-10-24)[30](#page-10-26)</sup> In particular, the freestanding FM Fe, Co, and Ni linear chains are reported to be nearly half-metallic in Ref. [27,](#page-10-24) in agreement with our findings (Table [II](#page-5-1)). Experimentally, a clear peak at  $0.5G_0$  (  $G_0 = 2e^2/h$  being the conductance quantum) was observed recently in the conductance of the Co chain, $9$  indicating a fully polarized conduction in this monoatomic chain system.

## **IV. ZIGZAG CHAINS**

The zigzag structure for monoatomic wires has already been observed in experiments<sup>50</sup> and also proposed in theo-retical calculations.<sup>15[,17,](#page-10-13)[23](#page-10-17)[,24](#page-10-19)</sup> However, among 3*d* transition metals, only the Ti and Fe zigzag chains have been studied theoretically.<sup>15[,23](#page-10-17)</sup> In the present paper, we perform a systematic *ab initio* study of the structural, electronic, and magnetic properties of the zigzag chain structure of all the 3*d* transition metals.

### **A. Structure and magnetic moment**

The calculated equilibrium structural parameters (Fig.  $1$ ), spin magnetic moment, and magnetization energy of the 3*d* TM zigzag chains are listed in Table [III.](#page-6-0) First of all, the bond length between two nearest ions  $(d_2)$  in the zigzag chains is generally similar to that  $(d)$  of the corresponding linear chains, though the distance  $(d_1)$  between two ions in the zigzag chains along the chain direction (*z* axis) is somewhat larger than in the linear chains (see Table [III](#page-6-0)). Interestingly, most of the zigzag chains are like planar equilateral triangle ribbons [Fig.  $1(b)$  $1(b)$ ] except the AF Fe and NM Ni zigzag chains which look more like a sheared two-legger ladder  $(\alpha \ge 71^{\circ}, d_1 < d_2$ ; see Table [III](#page-6-0)). Note that the calculated structural parameters  $(d_1, d_2,$  and  $\alpha$  in Table [III](#page-6-0)) of the NM Ti zigzag chain are similar to those  $(d_1=2.58 \text{ Å}, d_2)$ =2.41 Å, and  $\alpha$ =57.6) reported previously in Ref. [23.](#page-10-17) For a FM state of the Fe zigzag chain,  $\alpha = 56$  and  $m_s = 2.9 \mu_B$  were reported in Ref. [15,](#page-10-11) close to the corresponding values listed in Table [III](#page-6-0) here.

Secondly, all the 3*d* TM zigzag chains, except that of Cu, have magnetic solutions. Furthermore, one can see that the Sc, Mn, Fe, Co, and Ni zigzag chains are most stable in the FM state, while the ground state of the Ti and V chains is the NM state and that of the Cr chain is the AF state. Note that the ground state of the linear Ti (V, Mn) chain is the FM (AF) state (Table [I](#page-2-1)). Thirdly, the spin magnetic moments in the zigzag chains (Table [III](#page-6-0)) are generally smaller than in the corresponding linear chains (Table [I](#page-2-1)). This is due to the increase in the coordination number in the zigzag chains because most of them form a planar equilateral triangle ribbon. Note that our calculated spin magnetic moments for bulk FM Fe, Co, and Ni are 2.19, 1.60, and 0.63  $\mu_B$ /atom, respectively, considerably smaller than both the linear and zigzag chains. Nonetheless, as for the linear chains, the Cr zigzag chain still has the largest spin magnetic moment (Table [III](#page-6-0)).

When the SOC is taken into account, the spin magnetic moments of the zigzag chains remain almost unchanged, same as for the linear chain cases. The orbital magnetic moments of the FM zigzag chains with the magnetization along

<span id="page-6-0"></span>TABLE III. Equilibrium structural parameters [see Fig.  $1(b)$  $1(b)$  for symbols  $d_1$ ,  $d_2$ , and  $\alpha$ ], spin magnetic moment  $(m_s)$ , and magnetization energy  $(\Delta E)$  (i.e., the total energy of a magnetic state relative to that of the NM state) of the 3*d* transition metal zigzag chains.  $d_1$  and  $d_2$  are in Å, and  $\alpha$  is in degree.  $\Delta E$  is in eV/atom, and  $m_s$  in  $\mu_B$ /atom.

<b>State</b>		<sub>Sc</sub>	Ti	V	Cr	Mn	Fe	Co	Ni	Cu
<b>NM</b>	d <sub>1</sub>	2.911	2.718	2.627	2.213	2.264	2.271	2.258	2.067	2.371
	$d_2$	2.910	2.364	2.067	2.162	2.079	2.095	2.228	3.275	2.334
	$\alpha$	60.01	54.91	50.55	59.23	57.02	57.18	59.56	71.60	59.56
<b>FM</b>	d <sub>1</sub>	2.910	2.720	2.626	2.831	2.700	2.429	2.318	2.288	
	$d_2$	2.938	2.366	2.066	2.766	2.480	2.240	2.218	2.275	
	$\alpha$	59.68	54.91	50.55	59.23	57.02	57.18	58.50	59.82	
	m <sub>s</sub>	1.050	0.571	0.027	5.904	4.368	3.006	2.049	0.867	
	$\Delta E$	$-0.527$	0.002	0.000	0.049	$-0.574$	$-0.779$	$-0.485$	$-0.714$	
AF	d <sub>1</sub>				2.587	2.628	2.179	2.313	2.262	
	$d_2$				2.531	2.413	3.765	2.213	2.301	
	$\alpha$				59.27	57.00	73.18	58.50	60.55	
	m <sub>s</sub>				3.478	3.208	3.062	1.311	0.563	
	$\Delta E$				$-0.336$	$-0.565$	0.098	$-0.139$	$-0.647$	

the *z* axis are  $-0.003$  (Sc),  $-0.005$  (Ti), 0.000 (V), 0.000 (Cr), 0.025 (Mn), 0.087 (Fe), 0.149 (Co), and 0.096 (Ni)  $\mu_B$ /atom, significantly smaller than those of the corresponding linear chains (see Sec. III B).

#### **B. Band structures and density of states**

The scalar-relativistic band structures of the FM Cr, Fe, and Co zigzag chains are displayed in Fig. [7](#page-6-1) as representatives. Compared with the corresponding band structures of the linear chains [Fig.  $4(a)$  $4(a)$ ], the number of bands become doubled in the zigzag chains because of the doubling of the number of atoms. Furthermore, unlike the linear chains where the  $d_{xy}$   $(d_{xz})$  and  $d_{x^2-y^2}$   $(d_{yz})$  bands [Figs. [4](#page-3-1)(a) and  $4(d)$  $4(d)$  are degenerate because of rotational invariance, the  $d_{xy}$  $(d_{xz})$  and  $d_{x^2-y^2}$   $(d_{yz})$  bands are now split because of the

<span id="page-6-1"></span>

FIG. 7. Scalar-relativistic band structures of the Cr, Fe, and Co zigzag atomic chains in the FM state. The Fermi level (the dotted horizontal line) is at the zero energy.

strong anisotropy in the *x*-*y* plane perpendicular to the chain axis. It is clear that the energy bands are also highly spin split and the separation of the spin-up and spin-down bands may be correlated with the spin magnetic moment. For example, the spin splitting of the lowest bands is 1.78 eV in the Cr chain, but is only 0.89 and 0.50 eV for the Fe and Co chains, respectively.

As for the linear chains, we calculate the spin polarization  $(P)$  and count the numbers of spin-up and spin-down conduction bands at the Fermi level in the FM zigzag chains, as listed in Table [II.](#page-5-1) Nevertheless, the *P* in the V, Mn, Fe, Co, and Ni zigzag chains all gets reduced (Table  $II$ ). The largest reduction is in the V zigzag chain, being reduced from 0.939 to 0.085. The reduction is small for the Mn, Co, and Ni chains (Table  $II$ ), suggesting that the FM Mn, Co, and Ni zigzag chains are still useful for spintronic applications.

#### **C. Stability of linear chain structures**

Let us now compare the total energies of the linear and zigzag chains and examine the relative stability of the two structures. The ground state cohesive energy of the linear chains and the cohesive energies of the zigzag chains in the NM, FM, and AF states are displayed in Fig. [8.](#page-7-0) The cohesive energy  $(E_c)$  of an atomic chain is defined as the difference between the sum of the total energy of the free constituent atoms  $(E_a)$  and the total energy of the chain  $(E_t)$ , i.e.,  $E_c$  $=E_a-E_t$ . A positive value of the  $E_c$  means that the formation of the chain from the free atoms would save energy, i.e., the chain would be stable against breaking up into free atoms. The total energies of the free atoms are calculated by the cubic box supercell approach with the cell size of 10 Å. The electronic configurations used are  $3d^14s^2$  (Sc),  $3d^34s^1$  (Ti),  $3d^44s^1$  (V),  $3d^54s^1$  (Cr),  $3d^64s^1$  (Mn),  $3d^74s^1$  (Fe),  $3d^84s^1$  $(Co)$ ,  $3d^9 4s^1$  (Ni), and  $3d^{10} 4s^1$  (Cu).

<span id="page-7-0"></span>

FIG. 8. (Color online) The cohesive energy of the 3*d* TM zigzag chains in the NM, FM, and AF states. For comparison, the ground state cohesive energy of the corresponding linear chains is also plotted (solid circles). The ground state magnetic configuration of the linear chains is labeled as NM, FM, or AF near each solid circle.

Remarkably, Fig. [8](#page-7-0) shows that in all the cases, the ground state cohesive energy of the linear chain is smaller than that of the zigzag chain in a magnetic state. This suggests that the 3*d* linear chains are unstable against the zigzag structural distortion, as may be expected from the Peierls instability of linear one-dimensional monoatomic metals.<sup>51</sup> The difference in the ground state energy between the linear and zigzag structures for all the 3*d* elements is rather large, ranging from 0.8 to 1.1 eV/atom. This shows that the freestanding 3*d* TM linear chains would not be the stable state, and the linear chains may occur only in constrained conditions such as on the steps on a vicinal surface $6$  and under tensile stress in the breakpoint experiments.<sup>9,[52–](#page-11-9)[55](#page-11-10)</sup> Only the zigzag structure of Fe has been considered before in Ref. [15.](#page-10-11) The zigzag structure of Fe was also found to be lower in energy than the linear chain by 1.01 eV/atom, a value close to 0.99 eV/atom found in the present calculations.

Interestingly, we find that for some 3*d* transition metals, the ground state magnetic configuration changes when the structure changes from the linear to zigzag chain. For example, the ground state of the Sc and Ti chains is ferromagnetic in the linear chain but becomes nonmagnetic in the zigzag structure (Table  $III$ ). On the other hand, the ground state of the Mn chain changes from the AF state in the linear chain to the FM state in the zigzag structure. Nevertheless, the total energy difference between the FM and AF states in the Mn zigzag chain is small (within  $\sim 0.01$  eV/atom). The ground state of the V chain also changes, from the AF state in the linear chain to the FM state in the zigzag chain.

#### **V. MAGNETIC ANISOTROPY ENERGY**

The total energy as a function of the magnetization orientation  $(\theta, \phi)$  of a 1D wire may be written, in the lowest nonvanishing terms, as

$$
E_t = E_0 + \sin^2 \theta (E_1 - E_2 \cos^2 \phi),
$$
 (2)

<span id="page-7-1"></span>where  $\theta$  is the polar angle of the magnetization away from the chain axis (*z* axis) and  $\phi$  is the azimuthal angle in the *x*-*y* 

plane perpendicular to the wire, measured from the *x* axis. For the freestanding linear atomic chains, the azimuthal anisotropy energy constant  $E_2$  is zero because of the rotational invariance. The axial anisotropy energy constant  $E_1$  is then given by the total energy difference between the magnetization along the *y* (*x*) and *z* axes, i.e.,  $E_1 = E^y - E^z$  ( $E^x = E^y$ ). A positive value of  $E_1$  means that the chain  $(z)$  axis is the easy magnetization axis. For the zigzag chains which are in the  $x-z$  plane,  $E_2$  is not zero and can be calculated as the total energy difference between the magnetization along the *x* and *y* axes, i.e.,  $E_2 = E^y - E^x$ .

The magnetic anisotropy energy for a magnetic solid consists of two contributions. One comes from the magnetocrystalline anisotropy in the electronic band structure caused by the simultaneous occurrence of the electron spin-orbit interaction and spin polarization in the magnetic system. This is known as the electronic contribution, and *ab initio* calculation of this part has already been described in Sec. II. The other is the magnetostatic (or shape) anisotropy energy due to the magnetic dipolar interaction in the solid. The shape anisotropy energy is zero for the cubic systems such as bcc Fe and fcc Ni, and also negligibly small for weakly anisotropic solids such as hcp Co. However, for the highly anisotropic structures such as magnetic Fe and Co monolayers,  $43,44$  $43,44$  the shape anisotropy energy can be comparable to the electronic MAE, and therefore, cannot be neglected. Furthermore, as will be reported immediately below, the shape anisotropy energy of the 3*d* TM atomic chains are also large and cannot be ignored. Therefore, in this work, following Ref. [43,](#page-11-1) we use Ewald's lattice summation technique<sup>56</sup> to calculate the magnetic dipole-dipole interaction energy. For the collinear magnetic systems (i.e.,  $\mathbf{m}_q \parallel \mathbf{m}_{q'}$ , this magnetic dipolar energy  $E_d$  is given by<sup>43</sup> (in atomic Rydberg units-

and

$$
M_{qq'} = \sum_{\mathbf{R}}' \frac{1}{|\mathbf{R} + \mathbf{q} + \mathbf{q'}|^3} \left\{ 1 - 3 \frac{\left[ (\mathbf{R} + \mathbf{q} + \mathbf{q'}) \cdot \hat{\mathbf{m}}_{\mathbf{q}} \right]^2}{|\mathbf{R} + \mathbf{q} + \mathbf{q'}|^2} \right\},\tag{4}
$$

 $\frac{m_q m_{q'}}{c^2} M_{qq'}$  (3)

 $E^d = \sum_{qq'}$ 

where  $M_{qa'}$  is called the magnetic dipolar Madelung constant, which is evaluated by Ewald's lattice summation technique.<sup>56</sup> The speed of light  $c = 274.072$ . **R** are the lattice vectors, **q** are the atomic position vectors in the unit cell, and  $m_q$  is the atomic magnetic moment on site  $q$ . Note that in atomic Rydberg units, one Bohr magneton  $(\mu_B)$  is  $\sqrt{2}$ . Therefore, the magnetic dipolar energy  $E^d$  for the multilayers obtained previously by Guo *et al.*[43,](#page-11-1)[44](#page-11-2)[,57–](#page-11-12)[59](#page-11-13) is too small by a factor of 2.

The calculated shape anisotropy energies  $(E^d)$  for the linear and zigzag chains are listed in Tables [IV](#page-8-0) and [V,](#page-8-1) respectively. Tables [IV](#page-8-0) and [V](#page-8-1) show that in both the linear and zigzag chains and in both the FM and AF states, the shape anisotropy energies can be comparable to the electronic contributions. Furthermore, they always prefer the chain direc-

<span id="page-8-0"></span>TABLE IV. Total  $(E_1^t)$ , electronic  $(E_1^e)$ , and dipolar  $(E_1^d)$  magnetic anisotropy energies (in meV/atom) of the 3*d* transition metal linear chains. If  $E_1^t$  is positive, the easy magnetization axis is along the chain; otherwise, the easy magnetization axis is perpendicular to the chain.

		FM		AF				
	$E_1^t$	$E_1^e$	$E_1^d$	$E_1^t$	$E_1^e$	$E_1^d$		
Sc	0.06	0.01	0.05					
Ti	$-0.22$	$-0.27$	0.05					
V	0.81	0.45	0.36	0.183	0.138	0.045		
Cr	0.62	0.07	0.55	$-0.006$	$-0.259$	0.253		
Mn	0.22	$-0.28$	0.50	$-0.487$	$-0.698$	0.212		
Fe	2.65	2.25	0.40	$-0.817$	$-0.917$	0.100		
Co	$-0.48$	$-0.68$	0.20	5.194	5.155	0.039		
Ni	11.44	11.39	0.05					

tion  $(z$  axis) as the easy magnetization axis, and this may be expected since the shape anisotropy energy always favors the direction of the longest dimension. Therefore, any perpendicular magnetic anisotropy must originate from the electronic magnetocrystalline anisotropy when it overcomes the shape anisotropy. In the zigzag chains, there is also a significant magnetic anisotropy in the *x*-*y* plane perpendicular to the chain axis. For the FM state, the *x* axis is favored in all the zigzag chains, i.e., the *y* axis would be the hard magnetization axis if the magnetic anisotropy were determined by the  $E^d$  alone. In contrast, for the AF state, the *x* axis would be the hard axis (see Table  $V$ ).

The calculated electronic anisotropy energies of the linear and zigzag atomic chains are also listed in Tables [IV](#page-8-0) and [V,](#page-8-1) respectively. Interestingly, Table [IV](#page-8-0) shows that in the FM linear chains, the electronic anisotropy energy would favor a perpendicular anisotropy in the Ti, Mn, and Co chains but prefer the chain axis in the Sc, V, Cr, Fe, and Ni chains. Nevertheless, the easy magnetization direction is predicted to be the chain axis in all the 3*d* FM linear chains except for Ti and Co because the perpendicular electronic anisotropy in the Mn chain is not sufficiently large to overcome the axial shape anisotropy (Table [IV](#page-8-0)). In the AF state, in contrast, the

<span id="page-8-2"></span>

FIG. 9. (Color online) Magnetocrystalline anisotropy energy  $(E_1^e)$  of the 3*d* transition metal linear atomic chain as a function of interatomic distance. A positive value of  $E_1^e$  means that the magnetization would be parallel to the chain axis, while a negative value would mean that the easy magnetization axis would be perpendicular to the chain.

Cr, Mn, and Fe linear chains would have the easy axis perpendicular to the chain, while the V and Co linear chains still prefer the axial anisotropy. Remarkably, the FM Ni linear chain has a gigantic axial anisotropy energy (Table [IV](#page-8-0)), in the same order of magnitude to that in the 4*d* transition metal linear chains.<sup>60</sup> In the 4*d* transition metals, the SOC splittings are large, about ten times larger than the 3*d* transition metals, and thus, a large MAE in the 4*d* transition metal linear chains may be expected. The axial anisotropy energies for the FM V, Cr, and Fe linear chains and AF Co linear chains are also rather large, generally a few times larger than the corresponding monolayers[.43,](#page-11-1)[44](#page-11-2)

In Fig. [9,](#page-8-2) the electronic anisotropy energy for the linear 3*d* atomic chains is displayed as a function of the lattice constant (bond length). It is clear that in all the 3*d* linear chains except those of Fe and Co, the easy axis of magnetization remains the same regardless of whether the chain is elongated or compressed. When compressed, the FM Fe linear chain would undergo a spin-reorientation transition from

<span id="page-8-1"></span>TABLE V. The total  $(E_1^t, E_2^t)$ , electronic  $(E_1^e, E_2^e)$ , and dipolar  $(E_1^d, E_2^d)$  magnetic anisotropy energy constants (in meV/atom) as well as the easy magnetization axis **(M)** of the 3*d* transition metal zigzag chains.  $E_1 = E^y - E^z$ ,  $E_2 = E^y - E^x$  $E_2 = E^y - E^x$  $E_2 = E^y - E^x$ , [see Eq. (2)].

	FM							AF						
	$E_1^e$	$E_2^e$	$E_1^d$	$E_2^d$	$E_1^t$	$E_2^t$	M	$E_1^e$	$E_2^e$	$E_1^d$	$E_2^d$	$E_1^t$	$E_2^t$	M
Sc	0.000	0.000	0.022	0.011	0.022	0.011	$Z_{\cdot}$							
Ti	0.000	0.000	0.010	0.006	0.010	0.006	$Z_{\cdot}$							
V	0.000	0.000	0.000	0.000	0.000	0.000								
Cr	$-0.158$	$-0.158$	0.857	0.418	0.699	0.260	$Z_{\cdot}$	$-2.663$	$-2.754$	0.152	$-0.190$	$-2.511$	$-2.944$	$\mathcal{V}$
Mn	$-0.194$	$-0.256$	0.578	0.299	0.384	0.043	$Z_{\cdot}$	0.898	1.024	0.091	$-0.190$	0.989	0.834	$Z_{\rm c}$
Fe	$-0.700$	$-0.584$	0.374	0.193	$-0.326$	$-0.391$	$\mathcal{V}$	0.012	0.006	0.315	$-0.071$	0.327	$-0.065$	$Z_{\rm c}$
Co	1.317	1.122	0.192	0.096	1.509	1.218	Z.	8.763	6.992	0.029	$-0.040$	8.792	6.952	$Z_{\rm c}$
Ni	0.636	1.741	0.035	0.017	0.671	1.758	$\mathcal{X}$	6.911	5.126	0.006	$-0.007$	6.917	5.119	$Z_{\rm c}$

<span id="page-9-0"></span>

FIG. 10. (Color online) d-orbital-decomposed density of states of the FM (a) Fe, (b) Co, and (d) Ni linear chains at the equilibrium bond length. In (c), *d*-orbital-decomposed density of states of the FM Co linear chain at an elongated bond length of 2.6 Å is displayed.

the axial to perpendicular direction at the bond length of  $\sim$  2.06 Å. In contrast, the FM Co linear chain would transform from the perpendicular to axial direction at  $\sim$ 2.31 Å when elongated.

To help in identifying the electronic origin of the magnetocrystalline anisotropy, we plot the scalar-relativistic *d*-orbital-decomposed DOS for the FM Fe, Co, and Ni linear chains in Fig. [10.](#page-9-0) According to perturbation theory analysis, the occupied and empty *d* states in the vicinity of the Fermi level which are coupled by the SOC are most important to the magnetocrystalline anisotropy. $61$  Furthermore, the SOC matrix elements  $\langle d_{xz} | H_{SO} | d_{yz} \rangle$  and  $\langle d_{x^2-y^2} | H_{SO} | d_{xy} \rangle$  are found to contribute to the axial anisotropy, while  $\langle d_{x^2-y^2} | H_{SO} | d_{yz} \rangle$ ,  $\langle d_{xy} | H_{SO} | d_{xz} \rangle$ , and  $\langle d_{3z^2-r^2} | H_{SO} | d_{yz} \rangle$  prefer a perpendicular anisotropy[.48](#page-11-5) The ratio of these matrix elements are  $\langle d_{xz} | H_{SO} | d_{yz} \rangle^2 : \langle d_{x^2-y^2} | H_{SO} | d_{xy} \rangle^2 : \langle d_{x^2-y^2} | H_{SO} | d_{yz} \rangle^2 :$  $\langle d_{xy}|H_{SO}|d_{xz}\rangle^2$ :  $\langle d_{3z^2-r^2}|H_{SO}|d_{yz}\rangle|^2=1:4:1:1:3.^48$  Figures  $10(a) - 10(d)$  $10(a) - 10(d)$  show that in the FM Fe and Ni chains, the  $E_F$ sits on, respectively, the lower and upper sharp peaks of the spin-down  $d_{x^2-y^2}$  and  $d_{xy}$  DOSs. Consequently, the SOC near the  $E_F$  between the  $d_{x^2-y^2}$  and  $d_{xy}$  bands would give rise to a dominating contribution to the magnetocrystalline anisotropy and, therefore, the FM Fe and Ni chains would prefer the chain axis. On the other hand, in the FM Co chain, the  $E_F$  lies in the valley of the spin-down  $d_{x^2-y^2}$  and  $d_{xy}$  DOS [Fig. [10](#page-9-0)(b)]. As a result, the  $\langle d_{x^2-y^2} | H_{SO} | d_{xy} \rangle$  contribution does not dominate and the FM Co chain would perfer a perpendicular anisotropy. Nonetheless, the spin-down  $d_{x^2-y^2}$  and  $d_{xy}$  DOSs near the  $E_F$  increase dramatically when the FM Co chain is stretched [Fig.  $10(c)$  $10(c)$ ]. This would enhance the  $\langle d_{r^2-v^2}|H_{SO}|d_{vv}\rangle$  contribution considerably and the FM Co chain would then prefer the axial anisotropy when the bond length is larger than  $\sim$  2.23 Å (Fig. [9](#page-8-2)).

Generally speaking, the magnetic anisotropy in at least the FM 3*d* chains becomes smaller as the structure moves from the linear to zigzag structure (see Tables [IV](#page-8-0) and [V](#page-8-1)). The most dramatic reduction in the magnetic anisotropy occurs in the FM Ni chain. The axial anisotropy constant  $E_1$  in the zigzag Ni chain is one order of magnitude smaller than that in the linear chain. There is now a large anisotropy energy  $(E_2)$  in the *x*-*y* plane perpendicular to the chain axis (see Table  $V$ ). As a result, the easy magnetization axis in the zigzag FM Ni chain is in the zigzag chain plane, but perpendicular to the chain axis, i.e., the  $x$  axis (see Fig. [1](#page-1-0)). For the FM Ti and Co chains, the easy magnetization changes from the perpendicular to axial direction (Tables [IV](#page-8-0) and [V](#page-8-1)). Strikingly, no AF state could be stabilized in the linear Ni chain, and in contrast, the AF state not only can be stabilized but also has gigantic magnetic anisotropy energies in the zigzag chain (see Table [V](#page-8-1)). Table V also shows that the magnetic anisotropy energies in the zigzag AF Co chain are considerably enhanced compared with those in the linear AF Co chain.

#### **VI. CONCLUSIONS**

We have performed a systematic *ab initio* study of the magnetic and electronic properties of both linear and zigzag atomic chains of all 3*d* transition metals within density functional theory with GGA. The accurate frozen-core fullpotential PAW method is used. The underlying atomic structures were determined theoretically. All the zigzag chains except the NM Ni and AF Fe chains, which form a twisted two-legger ladder, look like a corner-sharing triangle ribbon and have a lower total energy than the corresponding linear chains.

We find that all the 3*d* transition metals in both linear and zigzag structures have a stable or metastable FM state. Furthermore, in the V, Cr, Mn, Fe, and Co linear chains and Cr, Mn, Fe, Co, and Ni zigzag chains, a stable or metastable AF state exists, too. In the Sc, Ti, Fe, Co, and Ni linear structures, the FM state is the ground state, while in the V, Cr, and Mn linear chains, the AF state is most energetically favorable. The electronic spin polarization at the Fermi level in the FM Sc, V, Mn, Fe, Co, and Ni linear chains is close to 90% or above, suggesting that these nanostructures may have applications in spin-transport devices. Only in the Cr zigzag structure is the AF state energetically more favorable than the FM state. Surprisingly, the V, Cr, Mn, and Fe linear chains show a giant magnetolattice expansion of up to 54%.

Both the electronic magnetocrystalline anisotropy energy and magnetic dipolar anisotropy energy have been calculated. We find that shape anisotropy energy can be comparable to the electronic one and always prefer the axial magnetization in both the linear and zigzag structures. Furthermore, in the zigzag chains, there is also a pronounced shape anisotropy in the plane perpendicular to the chain axis. Nonetheless, in the FM Ti, Mn, and Co linear chains and AF Cr, Mn, and Fe linear chains, the electronic anisotropy is perpendicular, and it is sufficiently large in the FM Ti and Co linear chains, as well as in the AF Cr, Mn, and Fe linear chains such that the easy magnetization axis is perpendicular. In the AF Cr, FM Fe, and FM Ni zigzag structures, the easy magnetization direction is also perpendicular to the chain axis. Remarkably, the axial magnetic anisotropy in the FM Ni linear chain is gigantic,  $\sim$  12 meV/atom, suggesting that Ni nanowires could have important applications in ultrahigh density magnetic memories and hard disks. The axial magnetic anisotropy energy of the FM V, Cr, and Fe linear chains and FM Cr, Mn, and Co zigzag structures is also sizable. Interestingly, there is a spin-reorientation transition in the FM Fe and Co linear chains when the chains are compressed or elongated. Large orbital magnetic moment is found in the FM Fe, Co, and Ni linear chains. Finally, the electronic band structure and density of states of the nanowires have also been calculated mainly in order to understand the electronic origin of the large magnetocrystalline anisotropy and orbital magnetic moment.

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