

Conduction eigenchannels of atomic-sized contacts: *Ab initio* KKR Green's function formalism

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We develop a formalism for the evaluation of conduction eigenchannels of atomic-sized contacts from first principles. The multiple scattering Korringa-Kohn-Rostoker Green's function method is combined with the Kubo linear response theory. Solutions of the eigenvalue problem for the transmission matrix are proven to be identical to eigenchannels introduced by Landauer and Büttiker. Applications of the method are presented by studying ballistic electron transport through Cu, Pd, Ni, and Co single-atom contacts. We show in detail how the eigenchannels are classified in terms of irreducible representations of the symmetry group of the system as well as by orbital contributions when the channels' wave functions are projected on the contact atom.

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I. INTRODUCTION

The invention of the scanning tunneling microscope¹ in 1981 and a consequent development in the beginning of the 1990s of the remarkably simple experimental technique known as mechanically controllable break junction^{2,3} (MCBJ) led to the possibility of fabricating metallic point contacts approaching the atomic scale. A recent paper⁴ summarized the numerous achievements in this field. In the experiments, the conductance measured as a function of the elongation of the nanocontacts decreases in a stepwise fashion^{3,5-7} with steps of order of the conductance quantum $G_0=2e^2/h$. Such behavior of the conductance is attributed to atomic rearrangements that entail a discrete variation of the contact diameter.⁸⁻¹¹

The electron transport in metallic nanocontacts is purely ballistic and phase coherent because their size is much smaller than all scattering lengths of the system. According to Landauer,¹² conductance is understood as transport through nonmixing channels,

$$G = \frac{2e^2}{h} \sum_{n=1}^N T_n,$$

where T_n 's are transmission probabilities. They are defined as eigenvalues of the transmission matrix $\tau\tau^\dagger$. Here, the matrix element τ_{nm} gives the probability amplitude for an incoming electron wave in the transverse mode (channel) n on the left from the contact to be transmitted to the outgoing wave in the mode m on the right. Consequently, the eigenvectors of $\tau\tau^\dagger$ are usually called eigenchannels. It was shown in the pioneering work by Scheer *et al.*¹³ that a study of the current-voltage relation for the superconducting atomic-sized contacts allowed one to obtain transmission probabilities T_n 's for particular atomic configurations realized in MCBJ experiments. The T_n 's are found by fitting theoretical and experimental I - V curve, which has a peculiar nonlinear behavior for superconducting contacts at voltages eV smaller than the energy gap 2Δ of a superconductor.¹³ The origin of such effect is explained in terms of multiple Andreev reflections.¹⁴ The analysis of MCBJ experiments within the tight-binding (TB) model suggested by Cuevas *et al.*^{15,16} gave a strong

evidence of the relation between the number of conducting modes and the number of valence orbitals of a contact atom.

To describe the electronic and transport properties of nanocontacts, quite a big number of different methods which supplemented each other were developed during the past 15 years. Early models employed a free-electron-like approximation.^{9,17,18} Further approaches based on density functional theory (DFT) used pseudopotentials to describe atomic chains suspended between jellium electrodes.^{19,20} The TB models were applied to the problem of the conduction eigenchannels^{15,21} and to the study of the breaking processes of nanowires.⁷ The up-to-date fully self-consistent *ab initio* methods²²⁻²⁴ allowed one to treat both the leads and the constriction region on the same footing and to evaluate the non-equilibrium transport properties as well.²³⁻²⁵

The scattering waves, underlying a concept of eigenchannels introduced by Landauer and Büttiker,¹² do not form an appropriate basis for most of the *ab initio* methods. Instead, one considers conduction channels as eigenvectors of some Hermitian transmission matrix written in terms of local, atom centered basis set.^{15,24} One of the goals of the present paper is to establish a missing link between these approaches. Below, we introduce a formalism for the evaluation of conduction eigenchannels, which combines an *ab initio* Korringa-Kohn-Rostoker (KKR) Green's function method²⁶ for the electronic structure calculations and the Baranger-Stone formulation of the ballistic transport.²⁷ In recent publications,^{28,29} we have successfully applied this method to the study of the electron transport through atomic contacts contaminated by impurities. In the present paper, mathematical aspects of the problem are considered, followed by some applications. In particular, we analyze the symmetry of channels and relate our approach to the orbital classification of eigenmodes introduced by Cuevas *et al.*¹⁵

The paper is organized as follows. A short description of the KKR method is given in Sec. II. We proceed in Sec. III with a formal definition of eigenchannels for the case of realistic crystalline leads attached to atomic constriction. Section IV supplemented by Appendixes A and B (Ref. 30) contains mathematical formulation of the method. Briefly, using the equivalence of the Kubo and Landauer approaches for the conductance,^{27,31} we build the transmission matrix

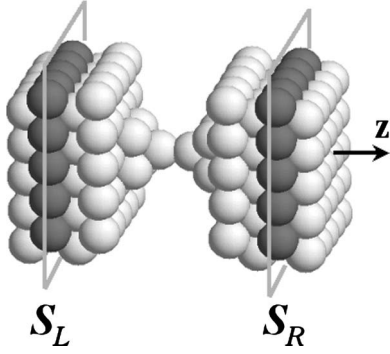


FIG. 1. Geometry of an atomic constriction: two fcc (001) pyramids are attached via apex atoms. Conductance is calculated between the two planes S_L and S_R positioned in the leads.

$\tau\tau^\dagger$ in the scattering wave representation. The angular momentum expansion of the scattering Bloch states within each cell is used further to find an equivalent, KKR representation of the transmission operator for which the eigenvalue problem can be solved. Applications of the method are presented in Sec. V. In particular, we focus on transition metal contacts (such as Ni, Co, and Pd), since experimental^{32–34} and theoretical studies^{35–39} of their transport properties have been attracting much attention during the past years. Experiments^{40–44} regarding ballistic magnetoresistance (BMR) effect in ferromagnetic contacts are commented. A summary of our results is given in Sec. VI.

II. ELECTRONIC STRUCTURE CALCULATION OF THE ATOMIC CONTACTS

The systems under consideration consist of two semi-infinite crystalline leads, left (L) and right (R), coupled through a cluster of atoms which models an atomic constriction. In Fig. 1, a typical configuration used in the calculations is shown—the two fcc (001) pyramids attached to the electrodes are joined via the vertex atoms. We employed the *ab initio* screened KKR Green’s function method to calculate the electronic structure of the systems. Since details of the approach can be found elsewhere,²⁶ only a brief description is given below.

In the KKR formalism, one divides the whole space into nonoverlapping, space-filling cells, with the atoms (and empty spheres) positioned at the sites \mathbf{R}_n , so that the crystal potential V is expressed in each cell as $V_n(\mathbf{r})=V(\mathbf{R}_n+\mathbf{r})$. The one-electron retarded Green’s function is expressed in terms of local functions centered at sites \mathbf{R}_n :

$$G^+(\mathbf{R}_n+\mathbf{r}, \mathbf{R}_{n'}+\mathbf{r}'; E) = \delta_{nn'} \sqrt{E} \sum_L R_L^n(\mathbf{r}_{<}; E) H_L^n(\mathbf{r}_{>}; E) + \sum_{LL'} R_L^n(\mathbf{r}; E) G_{LL'}^{mn'}(E) R_{L'}^{n'}(\mathbf{r}'; E), \quad (1)$$

where \mathbf{r}, \mathbf{r}' are restricted to the cells n and n' ; $\mathbf{r}_{<}, \mathbf{r}_{>}$ denote one of the two vectors \mathbf{r} or \mathbf{r}' with the smaller or the larger absolute value, and local functions $R_L^n(\mathbf{r}; E)$ and $H_L^n(\mathbf{r}; E)$ are

the regular and irregular solutions of the Schrödinger equation for the single potential $V_n(\mathbf{r})$. Here, the index $L=(l, m)$ stands for the angular momentum quantum numbers, and atomic units are used: $e=-\sqrt{2}$, $\hbar=1$, and $m=1/2$. The structural Green’s function $G_{LL'}^{mn'}(E)$ (structure constants) in Eq. (1) is related to the known structure constants of the appropriately chosen reference system by the algebraic Dyson equation, which includes the difference $\Delta t = \delta_{nn'} \delta_{LL'} \Delta t_L^n$ between local t matrices of the physical system and a reference system. In the screened KKR method,²⁶ we use a lattice of strongly repulsive, constant muffin-tin potentials (typically ~ 4 Ry height) as reference system that leads to structure constants which decay exponentially in real space.

Within the screened KKR method, both a constriction region and the leads are treated on the same footing. This is achieved by using the hierarchy of Green’s functions connected by a Dyson equation, so that we perform the self-consistent electronic structure calculations of complicated systems in a steplike manner. First, using the concept of principal layers together with the decimation technique,⁴⁵ we calculate the structural Green’s function of the auxiliary system consisting of semi-infinite leads separated by a vacuum barrier. At the second step, the self-consistent solution of the impurity problem is found by embedding a cluster with perturbed potentials caused by the atomic contact into the auxiliary system. Due to effective screening of perturbation, the algebraic Dyson equation for the structure constants is solved in real space.²⁶

III. DEFINITION OF EIGENCHANNELS

The concept of eigenchannels is introduced in the Landauer approach to ballistic transport, where the problem of the conductance evaluation is considered from the viewpoint of scattering theory. Following Landauer,¹² we look at the system shown in Fig. 1 as consisting of two semi-infinite leads (electrodes) attached to a scattering region (atomic-sized constriction). Far away from the scattering region, the propagating states are the unperturbed Bloch waves $\Psi_k^\circ(\mathbf{r}, E)$ of the left (L , $z \rightarrow -\infty$) and right (R , $z \rightarrow +\infty$) leads, where \mathbf{k} belongs to the isoenergetic surface $E=\text{constant}$ (Fermi surface, $E=E_F$, in case of conductance) and a common notation $\mathbf{k}=(\mathbf{k}, \lambda)$ is used to denote Bloch vector \mathbf{k} and band index λ . For the eigenchannel problem, one considers incoming and outgoing states in the L and R leads normalized to a unit flux. The in states in L and out states in R are $\Phi_k^\circ = \Psi_k^\circ / \sqrt{v_k^z}$ with positive velocity $v_k \propto v_k^z > 0$ along the z axis. The conjugated states $\Phi_k^{*\circ} = \Psi_k^{*\circ} / \sqrt{|v_{-k}^z|}$ are the out states in L and in states in R with negative velocity $v_{-k} \propto v_{-k}^z < 0$. Here, v_k^z is a z component of the group velocity $\mathbf{v}_k = \partial E_k / \partial \mathbf{k}$; a proportionality factor between v_k and \mathbf{v}_k^z related to a particular choice of normalization of the Bloch waves is introduced further in Sec. IV B.

The potential $\Delta V(\mathbf{r})$ describing the constriction introduces a perturbation to the perfect conductor. Let $\Phi_k(\mathbf{r}, E)$ be a perturbed state, which is a solution of the Lippmann-Schwinger equation for an incoming state in L :

$$\Phi_{\mathbf{k}}(\mathbf{r}, E) = \Phi_{\mathbf{k}}^{\circ}(\mathbf{r}, E) + \int d^3\mathbf{r}' G_0^+(\mathbf{r}, \mathbf{r}', E) \Delta V(\mathbf{r}') \Phi_{\mathbf{k}}(\mathbf{r}', E), \quad (2)$$

where the integral goes over all space, and $G_0^+(\mathbf{r}, \mathbf{r}', E)$ is the retarded Green's function of the perfect conductor. Asymptotic behavior of $\Phi_{\mathbf{k}}(\mathbf{r}, E)$ is

$$\begin{aligned} \Phi_{\mathbf{k}}(\mathbf{r}, E)|_{z \rightarrow -\infty} &= \Phi_{\mathbf{k}}^{\circ}(\mathbf{r}, E) + \sum_{\mathbf{k}'} \rho_{\mathbf{k}\mathbf{k}'}(E) \Phi_{\mathbf{k}'}^{*\circ}(\mathbf{r}, E), \\ \Phi_{\mathbf{k}}(\mathbf{r}, E)|_{z \rightarrow +\infty} &= \sum_{\mathbf{k}'} \tau_{\mathbf{k}\mathbf{k}'}(E) \Phi_{\mathbf{k}'}^{\circ}(\mathbf{r}, E), \end{aligned} \quad (3)$$

where $\tau_{\mathbf{k}\mathbf{k}'}(E)$ and $\rho_{\mathbf{k}\mathbf{k}'}(E)$ are transmission and reflection amplitudes, assuming elastic scattering ($E_{\mathbf{k}} = E = E_{\mathbf{k}'}$). According to the Landauer-Büttiker formula,¹² conductance is given by $g = g_0 \text{Tr}(\tau\tau^\dagger)$, where $g_0 = 2e^2/h$, and trace goes over incoming states (\mathbf{k}) in the left electrode and $E = E_F$. An equivalent formulation with respect to incoming states ($-\mathbf{k}'$) from the right electrode reads as $g = g_0 \text{Tr}(\tau^\dagger\tau)$.

Eigenchannels appear from a unitary transformation of in and out states. Let ω be a unitary transform of in states in L : $\Phi_{\nu}^{\text{in}}(\mathbf{r}, E)|_{z \rightarrow -\infty} = \sum_{\mathbf{k}} \omega_{\nu\mathbf{k}}(E) \Phi_{\mathbf{k}}^{\text{in}}(\mathbf{r}, E)$. The corresponding solution $\Phi_{\nu}(\mathbf{r})$ of Eq. (2) for an arbitrary \mathbf{r} is

$$\Phi_{\nu}(\mathbf{r}, E) = \sum_{\mathbf{k}} \omega_{\nu\mathbf{k}}(E) \Phi_{\mathbf{k}}(\mathbf{r}, E). \quad (4)$$

The unitary transform ω is defined in such a way that the transmission matrix $T = \tau\tau^\dagger$ is diagonal in the basis ν :

$$\omega(\tau\tau^\dagger)\omega^\dagger = \text{diag}\{T_{\nu}\}, \quad (5)$$

and the conductance reads as $g = g_0 \sum_{\nu} T_{\nu}(E_F)$, where the T_{ν} 's are transmission probabilities of eigenchannels.

The matrix τ , however, is not diagonal in basis ν . Following Ref. 46, one can introduce a unitary matrix θ which satisfies the equation

$$\omega\tau\theta^\dagger = \theta\tau^\dagger\omega^\dagger = \text{diag}\{\sqrt{T_{\nu}}\},$$

where all quantities are energy dependent. The solution is $\theta = \text{diag}\{1/\sqrt{T_{\nu}}\}\omega\tau$. The following properties of θ can be checked: $\theta\theta^\dagger = \delta_{\nu\nu'}$, $\theta^\dagger\theta = \delta_{\mathbf{k}\mathbf{k}'}$; thus, θ is indeed the unitary matrix. It diagonalizes $\tau^\dagger\tau$:

$$\theta(\tau^\dagger\tau)\theta^\dagger = \text{diag}\{T_{\nu}\}. \quad (6)$$

Matrix θ performs a unitary transform of out states in R , so that the linear combination ν of incoming states in L , $\Phi_{\nu}^{\text{in}}(\mathbf{r}, E)|_{z \rightarrow -\infty} = \sum_{\mathbf{k}} \omega_{\nu\mathbf{k}}(E) \Phi_{\mathbf{k}}^{\text{in}}(\mathbf{r}, E)$, is reflected from the constriction and transmitted into the linear combination ν of the out states in R , $\Phi_{\nu}^{\text{out}}(\mathbf{r}, E)|_{z \rightarrow +\infty} = \sum_{\mathbf{k}} \theta_{\nu\mathbf{k}}(E) \Phi_{\mathbf{k}}^{\text{out}}(\mathbf{r}, E)$, with the transmission amplitude $\sqrt{T_{\nu}(E)}$, namely, $\Phi_{\nu}(\mathbf{r}, E)|_{z \rightarrow +\infty} = \sqrt{T_{\nu}(E)} \Phi_{\nu}^{\text{out}}(\mathbf{r}, E)$.

One can show^{27,31} that for the Bloch states at the same energy ($E_{\mathbf{k}} = E = E_{\mathbf{k}'}$) in the ideal leads, the following relations hold for the current matrix elements:

$$\int_S dS [\Psi_{\mathbf{k}}^{\circ}(\mathbf{r}, E) i \vec{\partial}_z \Psi_{\mathbf{k}'}^{*\circ}(\mathbf{r}, E)] = \frac{v_{\mathbf{k}}}{2\pi} \delta_{\mathbf{k}\mathbf{k}'}, \quad (7)$$

where the Bloch waves are either left [$v_{\mathbf{k}} \propto (\partial E_{\mathbf{k}} / \partial \mathbf{k})_z > 0$] or right traveling ($v_{\mathbf{k}} < 0$), the operator $\vec{\partial}_z$ is defined as $f \vec{\partial}_z g = f(\partial_z g) - (\partial_z f)g$, and the integral goes over infinite plane S (cross section of the lead), which is perpendicular to the current direction z .

In case of the perturbed system, the orthogonality relation holds for current matrix elements in the basis of eigenchannels. Using Eqs. (3), (5), and (7), we can compute it in the asymptotic region of the right (R) lead⁴⁷

$$\int_{S_R} dS [\Phi_{\nu}(\mathbf{r}, E) i \vec{\partial}_z \Phi_{\mu}^*(\mathbf{r}, E)]_{z \rightarrow +\infty} = \frac{T_{\nu}(E)}{2\pi} \delta_{\nu\mu}. \quad (8)$$

We note that Eq. (8) holds for *any* position z of the plane S . Because the wave functions of channels are solutions of the Schrödinger equation with a real potential corresponding to the same energy, the flux through arbitrary plane S is conserved (a proof is similar to that of Appendix A of Ref. 32).

IV. CONDUCTION EIGENCHANNELS WITHIN THE KKR METHOD

A. Evaluation of conductance

To calculate the ballistic conductance, we employ the Kubo linear response theory as formulated by Baranger and Stone.²⁹

$$g = g_0 \int_{S_L} dS \int_{S_R} dS' G^+(\mathbf{r}, \mathbf{r}', E_F) \vec{\partial}_z \vec{\partial}_z' G^-(\mathbf{r}', \mathbf{r}, E_F), \quad (9)$$

where G^- and G^+ are retarded and advanced Green's functions, respectively, and $g_0 = 2e^2/h$. The integration is performed over left (S_L) and right (S_R) planes which connect the leads with the scattering region (Fig. 1). The current flows in the z direction. The implementation of Eq. (9) within the KKR method, related convergence tests, and further details were discussed in a recent publication.³¹

In this paper, we present a further extension of Ref. 31, a method for the evaluation of conduction eigenchannels. For that, we will follow closely the analysis of Refs. 27 and 31, where the equivalence of the Kubo and Landauer approaches to a conductance problem was shown. We proceed in four steps: (i) we remind the KKR representation of the Bloch functions, (ii) we build up the asymptotic expansion of the Green's function in terms of unperturbed Bloch states of the leads, (iii) we construct the transmission matrix $T = \tau\tau^\dagger$ in \mathbf{k} space, and (iv) finally, we find an equivalent representation of the transmission matrix within the local KKR basis. Further solution of the eigenvalue problem leads us to conduction channels. We mention here one aspect of the problem: for realistic calculations, the planes S_L and S_R (see Fig. 2 for details) are usually placed at a finite distance from the atomic constriction. Nevertheless, we first focus on the asymptotic limit before we discuss the realistic situation, which is considered in Sec. IV E and Appendix A.³⁰

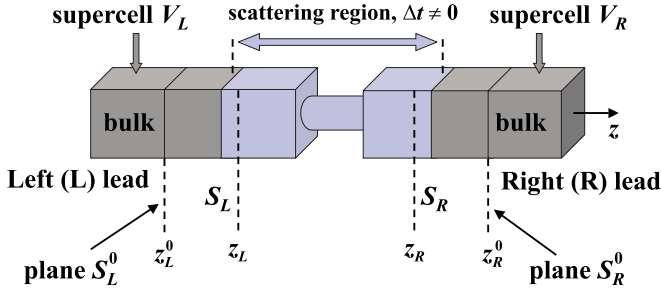


FIG. 2. (Color online) Sketch of the system under consideration. In a formal theory, left (S_L^0) and right (S_R^0) planes are placed within the leads far away from a scattering region (asymptotic limit). For all points \mathbf{r} ($z < z_L^0$) and \mathbf{r}' ($z' > z_R^0$) within the Born-von Kármán supercells (cubes), V_L and V_R asymptotic properties are achieved. When implementation of the method is considered, the conductance is calculated between the planes S_L and S_R positioned somewhere in the scattering region.

B. Atomic orbitals and Bloch functions

Let \mathbf{r} be an arbitrary point in the asymptotic region of the lead (Fig. 2). In the KKR method, the local, energy-dependent basis of atomic orbitals is defined at each unit cell n :

$$\phi_L^n(\mathbf{r}, E) = \phi_L(\mathbf{r} - \mathbf{R}_n, E) = R_L(\mathbf{r} - \mathbf{R}_n, E) \Theta(\mathbf{r} - \mathbf{R}_n), \quad (10)$$

where R_L 's are real regular solutions⁴⁸ of the Schrödinger equation for the potential $V_n(\mathbf{r})$ at cell n , and Θ function is 1 inside cell n and is 0 outside it. The unperturbed Bloch function is given by expansion over atomic orbitals at all sites n in the Born-von Kármán supercell:

$$\Psi_k^\circ(\mathbf{r}, E) = \sum_{nL} C_{k,nL}(E) \phi_L(\mathbf{r} - \mathbf{R}_n, E), \quad (11)$$

with $C_{k,nL}(E) = e^{+ik\mathbf{R}_n} C_{kL}^\circ(E)$. Here, the common notation $\mathbf{k} = (\mathbf{k}, \lambda)$ for the Bloch vector \mathbf{k} of the first Brillouin zone (BZ) and the band index λ is used. The $C_{kL}^\circ(E)$ are solutions of the KKR band structure equations⁴⁹ with energy E .

Considering a waveguide geometry, we will assume the Bloch functions to be normalized per cross section of the Born-von Kármán supercell (see Fig. 2) with open boundary conditions along the z axis. Thus, $C_{k,nL}(E) \propto 1/\sqrt{N_x N_y}$ with $N_x N_y$ being the number of atoms per cross section, and the orthogonality condition for Bloch waves takes the form³¹

$$\begin{aligned} \int_V d^3\mathbf{r} \Psi_k^\circ(\mathbf{r}, E) \Psi_{k'}^{\circ*}(\mathbf{r}, E') &= \frac{V}{(N_x N_y)} \delta_{kk'} = 2\pi A_0 \delta(k_z - k'_z) \delta_{k_{\parallel} k'_{\parallel}} \\ &= |v_k| \delta(E - E') \delta_{ss'} \delta_{k_{\parallel} k'_{\parallel}}. \end{aligned}$$

Here, $V = L_x L_y L_z$ is a volume of the supercell, $A_0 = L_x L_y / N_x N_z$ is an area of the xy unit cell in the electrode, $s, s' = \pm 1$ are signs of k_z and k'_z , relation $L_z \delta_{k_z k'_z} = 2\pi \delta(k_z - k'_z)$ has been used, and velocity v_k along current flow is defined as $v_k = 2\pi A_0 (\partial E_k / \partial \mathbf{k})_z$.

Since the Bloch waves form a complete set, a back transform of Eq. (11) exists:

$$\phi_L(\mathbf{r} - \mathbf{R}_n, E) = \sum_{k'} B_{nL,k'}^\dagger(E) \Psi_{k'}^\circ(\mathbf{r}, E_{k'}), \quad (12)$$

where \mathbf{k}' sum runs over all \mathbf{k}' points in the first BZ and over all bands λ' . The \dagger symbol means Hermitian conjugate. The expression for $B_{nL,k}^\dagger$ can be obtained⁵⁰ from known matrix $C_{k,nL}$. One can prove further that $C_{k,nL}$ and $B_{nL,k}^\dagger$ obey the following orthogonality relations:

$$\sum_{nL} C_{k,nL}(E) B_{nL,k'}^\dagger(E) = \delta_{kk'},$$

$$\sum_{\mathbf{k}} B_{nL,\mathbf{k}}^\dagger(E) C_{k,n'L'}(E) = \delta_{nn'} \delta_{LL'}, \quad (13)$$

where in the second equation a sum over \mathbf{k} is restricted to states with $E_k = E$.

C. Asymptotic expansion of the Green's function

Starting from the site angular momentum representation (1) of the retarded Green's function within the KKR method and using Eqs. (11) and (12), we obtain the asymptotic expansion for $G^+(\mathbf{r}, \mathbf{r}', E)$ over the unperturbed Bloch waves^{27,31}

$$G^+(\mathbf{r}, \mathbf{r}', E) \Big|_{z, z' \rightarrow \mp \infty} = \sum_{kk'} \Psi_k^{\circ*}(\mathbf{r}, E) \mathcal{A}_{kk'}(E) \Psi_{k'}^\circ(\mathbf{r}', E), \quad (14)$$

with $\mathbf{r} \in V_L$, $\mathbf{r}' \in V_R$ (see Fig. 2), and

$$\mathcal{A}_{kk'}(E) = \sum_{n \in V_L} \sum_{n' \in V_R} \sum_{LL'} B_{k,nL}(E) G_{LL'}^{nn'}(E) B_{n'L',k'}^\dagger(E), \quad (15)$$

or in a matrix form: $\mathcal{A} = B G B^\dagger$. Formally, the \mathbf{k} sums in Eq. (14) are performed over all \mathbf{k} states in the first BZ and over all bands λ . However, since the Green's function for $\mathbf{r} \neq \mathbf{r}'$ is a solution of the Schrödinger equation without a source term, only states \mathbf{k}, \mathbf{k}' at the isoenergetic surface of energy E contribute to the sum in the asymptotic expansion.^{27,31} Therefore,

$$\mathcal{A}_{kk'}(E) = \frac{1}{N_z} \bar{\delta}(E - E_k) \bar{\delta}(E - E_{k'}) \mathcal{A}_{kk'}(E), \quad (16)$$

where $\bar{\delta}(E - E_k) = (\Omega_0 / S_\lambda) |\mathbf{v}_k| \delta(E - E_k)$. Here, N_z is the number of atom sites in Born-von Kármán supercell along the z axis, $\Omega_0 = (2\pi)^3 / V_0$ is the volume of the first BZ, S_λ is the area of the isoenergetic surface corresponding to band λ and $\mathbf{v}_k = \partial E_k / \partial \mathbf{k}$. For the discrete \mathbf{k} points, the function $(1/N_z) \bar{\delta}(E - E_k)$ equals 1 if $E = E_k$, and is 0 otherwise. In addition, boundary conditions for the Green's function²⁷ constrain matrix elements $\mathcal{A}_{kk'}(E)$ to be nonzeros only if \mathbf{k} and \mathbf{k}' states are right-traveling waves (with positive velocity along the z axis) that corresponds to the in states \mathbf{k} in the left lead and out states \mathbf{k}' in the right one.

D. Transmission matrix: Asymptotic limit

We proceed further and use the asymptotic representation (14) of the Green's function to evaluate conductance accord-

ing to Eq. (9). Assuming the integration planes to be placed within the leads infinitely far from the scattering region, we obtain

$$g = g_0 \text{Tr}_{(k)}[V_L \mathcal{A}(E_F) V_R \mathcal{A}^\dagger(E_F)], \quad (17)$$

where the diagonal operators of velocities V_L and V_R (related to the left and right planes) acting in the \mathbf{k} space were introduced: $[V_{L(R)}]_{kk'} = (v_k/2\pi)\delta_{kk'}$. Formally, the trace (Tr) in Eq. (17) goes over all \mathbf{k} states, and the Fermi surface is taken into account by means of Eq. (16) where $E=E_F$.

The velocity operators can be decomposed into sum of two operators related to the Bloch states with positive and negative velocities along z : $\hat{V} = \hat{V}^+ + \hat{V}^-$, where \hat{V}^+ is nonzero for right-traveling waves only, while \hat{V}^- is nonzero for left-traveling ones. In the asymptotic limit, only incoming and outgoing \mathbf{k} states with positive velocities contribute to the sums in Eq. (17). Using the relation between expansion coefficients $A_{kk'}$ and the transmission amplitudes $\tau_{kk'}$ derived in Refs. 27 and 31,

$$A_{kk'}(E) = -2\pi i \frac{\tau_{kk'}(E)}{\sqrt{v_k v_{k'}}}, \quad (18)$$

we obtain

$$g = g_0 \text{Tr}_{(k)}[V_L^+ \mathcal{A}(E_F) V_R^+ \mathcal{A}^\dagger(E_F)] = g_0 \text{Tr}_{(k)}[T(E_F)], \quad (19)$$

where a representation of $T = \tau\tau^\dagger$ in \mathbf{k} space is given by

$$T(E) = (V_L^+)^{1/2} \mathcal{A}(E) V_R^+ \mathcal{A}^\dagger(E) (V_L^+)^{1/2} \quad (20)$$

with a positive definite operator under square roots.

The \mathbf{k} representation is formal but not suitable for implementation. To solve the eigenvalue problem for $T = \tau\tau^\dagger$, the mapping on the site-angular momentum (n, L) space of the KKR method should be presented. Such mapping is realized through the expansion (11) of the Bloch functions over atomic orbitals, so that velocity operators in \mathbf{k} space take a form

$$[V_{L(R)}]_{kk'} = \sum_{nm' \in S_{LL}^0} \sum_{LL'} C_{k,nL} [D_{L(R)}]_{LL'}^{nm'} C_{n'L',k'}^\dagger,$$

where site-diagonal operators D_R and D_L , defined on atomic orbitals, are the KKR analog of velocities:⁵¹

$$[D_{L(R)}(E)]_{LL'}^{nm'} = \pm \delta_{nm'} \int_{S_{L(R)}^n} dS [R_L^n(\mathbf{r}, E) i \vec{\partial}_z R_L^n(\mathbf{r}, E)]. \quad (21)$$

Here, the integral is restricted to the cross section of the unit cell around site n . Now we can evaluate conductance according to Eq. (17). Taking into account that $B^\dagger C = C^\dagger B = \delta_{nm'} \delta_{LL'}$ [Eq. (13)], we obtain

$$g = g_0 \text{Tr}_{(n,L)}(D_L G D_R G^\dagger). \quad (22)$$

Here (and further), all matrices are assumed to be taken at the Fermi energy, $G = \{G_{LL'}^{nm'}\}$ stands for matrix notation of the structural Green's function introduced in Eq. (1), and trace

(Tr) involves sites and orbitals related to the atomic plane S_L^0 (Fig. 2).

The operators D_L, D_R are antisymmetric and Hermitian, thus their spectrum consists of pairs of positive and negative eigenvalues: $\pm \delta_i^0$. Let U be the unitary transform of matrix D (either D_L or D_R) to a diagonal form

$$D^0 = U^\dagger D U = \text{diag}\{\pm \delta_i^0\}. \quad (23)$$

Decomposition of operator D into two terms, $D = D^+ + D^-$, related to the right- and left-traveling waves, is naturally given in the basis of eigenvectors:

$$D^\pm = U D^{0(\pm)} U^\dagger, \quad (24)$$

with

$$D^{0(+)} = \begin{pmatrix} \Delta^+ & 0 \\ 0 & 0 \end{pmatrix}, \quad D^{0(-)} = \begin{pmatrix} 0 & 0 \\ 0 & -\Delta^- \end{pmatrix},$$

where Δ^+, Δ^- are positive (non-negative) diagonal matrices. The analog of Eq. (19) reads as

$$g|_{z,z' \rightarrow \mp \infty} = g_0 \text{Tr}_{(n,L)}(D_L^+ G D_R^+ G^\dagger). \quad (25)$$

Now we are ready to build the (n, L) representation for transmission matrix $T = \tau\tau^\dagger$. For that, one should extract a square root from the positive definite operator $V_L^+ = C D_L^+ C^\dagger$ defined on \mathbf{k} space with the help of (n, L) space. Namely, because the V_L^+ is positive definite, it can be represented in the following form:⁵² $V_L^+ = \Omega_L \Omega_L^\dagger$. Here, an operator Ω_L maps the \mathbf{k} space on the (n, L) space, $\Omega_L: \{\mathbf{k}\} \rightarrow \{n, L\}$. The solution for Ω_L is

$$\Omega_L = C(D_L^+)^{1/2} \mathcal{E},$$

where \mathcal{E} is an arbitrary unitary matrix ($\mathcal{E}\mathcal{E}^\dagger = 1$) and $(D_L^+)^{1/2} = U_L [D_L^{0(+)}]^{1/2} U_L^\dagger$ with $[D_L^{0(+)}]^{1/2}$ being the square root of the positive definite diagonal matrix [Eq. (24)].

To find $T = \tau\tau^\dagger$, we start from Eq. (19) and proceed as follows:

$$\begin{aligned} g &= g_0 \text{Tr}_{(n,L)}(\Omega_L \Omega_L^\dagger \mathcal{A} V_R^+ \mathcal{A}^\dagger) = g_0 \text{Tr}_{(n,L)}(\Omega_L^\dagger \mathcal{A} V_R^+ \mathcal{A}^\dagger \Omega_L) \\ &= g_0 \text{Tr}_{(n,L)}[(D_L^+)^{1/2} C^\dagger (B G B^\dagger) (C D_R^+ C^\dagger) (B G^\dagger B^\dagger) C (D_L^+)^{1/2}], \end{aligned}$$

where Eq. (15) was used. Because of $B^\dagger C = \delta_{nm'} \delta_{LL'}$ [Eq. (13)], we obtain

$$g = g_0 \text{Tr}_{(n,L)}(\mathcal{T}), \quad (26)$$

where, in the asymptotic limit, the transmission matrix $T = \tau\tau^\dagger$ in (n, L) representation is given by

$$\mathcal{T} = (D_L^+)^{1/2} G D_R^+ G^\dagger (D_L^+)^{1/2}. \quad (27)$$

The trace in Eq. (26) goes over all sites n and orbitals L of the atomic plane S_L^0 in the left lead (Fig. 2). An equivalent formula can be written for the right lead. To conclude, one can prove that the spectrum of the obtained matrix coincides with the spectrum of transmission matrix T [Eq. (20)] defined in \mathbf{k} space (see Appendix B for details³⁰). Therefore, solution of the eigenvalue problem for \mathcal{T} gives us the required transmission probabilities.

E. General case: Arbitrary positions of planes

In practical calculations of conductance with the use of the Kubo formula, the left (L) and right (R) planes are positioned *somewhere* in the leads (Fig. 2). Expression (22) is valid in the general case and the result is exactly the same as in Ref. 31. Operator D_L in Eq. (22) is sum of the two terms: $D_L = D_L^+ + D_L^-$. Therefore, we can write down

$$g = g_0 \text{Tr}(D_L^+ G D_R G^\dagger) + g_0 \text{Tr}(D_L^- G D_R G^\dagger) = g^+ + g^-, \quad (28)$$

where g^+ and g^- denote two contributions. In a formal theory, when the atomic plane S_L is placed in the asymptotic region of the left lead far from the atomic constriction, the second term g^- in Eq. (28) is equal to zero. In practice, the real space summation of current contributions includes only a finite number of sites at both atomic planes, because the current flow along the z direction is localized in the vicinity of the contact. Due to numerical effort, we are forced to take integration planes closer to the constriction in order to obtain convergent value for the conductance with respect to number of atoms included in summation. In addition, even better convergence for matrix elements is required to solve the eigenvalue problem. A compromise can usually be achieved, but positions of the atomic planes S_L and S_R do not meet the asymptotic limit criterion. However, since the electron current through the structure is conserved, any position of the planes is suitable for the calculation of conductance. If S_L is placed somewhere in the scattering region, we have to sum up all multiple scattering contributions. We show in Appendix A (Ref. 30) that all multiple scattering contributions in the direction of the current cause g^+ , whereas all scattering contributions in the opposite direction give rise to g^- . Thus, the first term, g^+ , in Eq. (28) is always positive, while the second one, g^- , is always negative. To make this statement clear, an illustration of scattering events is shown in Fig. 3 assuming a simple free-electron model. In the region of the lead where the potential is a small perturbation with respect to the bulk potential, the contribution to the conductance due to g^- is 1 order of magnitude smaller than g^+ .

To find transmission probabilities of eigenchannels, one has to apply the procedure introduced in the previous section independently for both terms g^+ and g^- . We refer to Appendix A (Ref. 31) for a mathematical justification. Expression for conductance takes a form

$$g = g_0 \text{Tr}_{(n,L)}(T^+) + g_0 \text{Tr}_{(n,L)}(T^-), \quad (29)$$

with

$$T^\pm = \pm (\pm D_L^\pm)^{1/2} G D_R G^\dagger (\pm D_L^\pm)^{1/2}. \quad (30)$$

We show in Appendix A (Ref. 30) that all eigenvalues of T^+ are either positive or zero, whereas all eigenvalues of T^- are negative or zero. To identify transmission probabilities T_n of channels, the spectra of operators T^+ and T^- have to be arranged in a proper way. Then transmission of the n th channel is given by $T_n = \tau_n^+ - \tau_n^-$, where $\pm \tau_n^\pm$ are positive and negative eigenvalues of the operators T^+ and T^- , respectively. The T_n does not depend on the positions of the left (S_L) and right (S_R) planes, while τ_n^\pm are z dependent. In the asymptotic

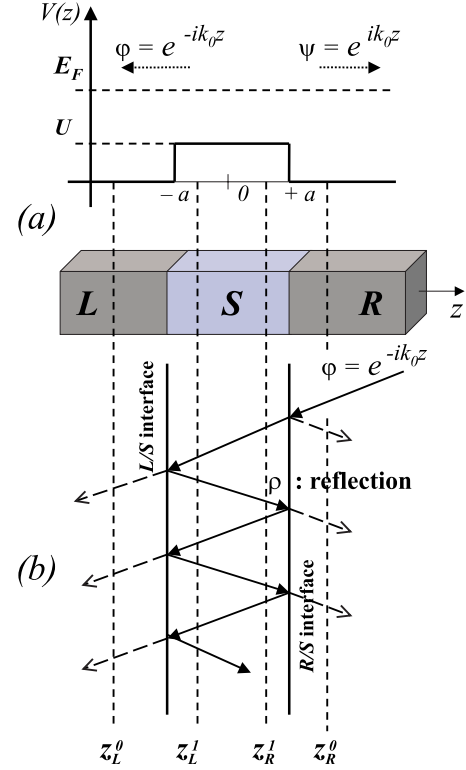


FIG. 3. (Color online) (a) A model steplike potential for the free-electron gas within the $L/S/R$ structure having two-dimensional periodicity. The electrons moving with energy $E = E_F$ from the leads (L and R) are scattered at the potential step U . The k_{\parallel} momentum is conserved, while the momentum k_z along the z axis is $k_0 = [2mE - k_{\parallel}^2]^{1/2}$ in the leads and $k_1 = [2m(E - U) - k_{\parallel}^2]^{1/2}$ in the S layer. (b) A multiple reflection of the incoming state from the R lead wave $e^{-ik_0 z}$ within the spacing layer S , where it is a linear combination $\phi(z) = \chi_+(z) + \chi_-(z) = \alpha e^{-ik_1 z} + \beta e^{+ik_1 z}$ of two functions. If z_L^1 is the position of one of the planes taken for the conductance evaluation, transmission $T(k_{\parallel})$ of channel k_{\parallel} is proportional to the current $j = \phi(z) i \partial_z \phi^*(z) = 2k_0 = 2k_1 |\alpha|^2 - 2k_1 |\beta|^2 = j_+ - j_-$, which is the sum of two terms (positive and negative) due to contributions from two functions, $\chi_+(z)$ and $\chi_-(z)$. The value $\rho = \beta/\alpha = (k_1 - k_0)/(k_1 + k_0) e^{+2ik_1 a}$ has a meaning of the reflection coefficient of the S/R or S/L interface. However, if the plane is chosen in the asymptotic region of the lead, at point z_L^0 , transmission $T(k_{\parallel}) \sim 2k_0$ contains only one positive contribution.

limit $\tau_n^-|_{z_L \rightarrow -\infty} \rightarrow 0$ and $T_n = \tau_n^+|_{z_L \rightarrow -\infty}$, so that the Landauer picture is restored.

In the general case, the direct way to find the pairs of eigenvalues is not evident without a back transform to the \mathbf{k} space. However, from the point of view of applications to the extremely small symmetric atomic contacts, same as the ones we are studying in this work, the problem is easy to handle. Since the number of contributing eigenmodes is limited, the pairs of eigenvalues can be found by symmetry analysis of the eigenvectors of T^+ and T^- . Namely, using the symmetry properties of the structural Green's function $G_{LL}^{nn'}$, and current matrix elements $D_{LL}^{nn'}$, one can show that the channel's transmission T_n bounded between 0 and 1 is defined by eigenvalues τ_n^+ and τ_n^- , which belong to the same irreducible representation of the symmetry point group.

V. APPLICATIONS OF THE METHOD

In recent papers,^{28,29} we have verified the method described here by studying systematic changes in the conductance of metallic constrictions in the presence of defect atoms. Illustrative examples presented below focus on single-atom contacts made of pure metals such as Cu, Ni, Co, and Pd.

Copper serves mainly for test purposes. It is a representative of the noble metals and has electronic properties similar to Ag and Au, for which a lot of experimental results^{9,32,53–56} as well as DFT based calculations^{21,23} are available. In particular, a large number of experiments for alkali metals^{32,56,57} (Li, Na, and K) and noble metals (Au, Ag, and Cu),^{32,54–56} employing different techniques under room and liquid-He temperatures, show that conductance histograms have a dominant peak very close to one conductance quantum $G_0 = 2e^2/h$ and smaller peaks close to integer values.

However, for transition metal contacts (examples of which are Ni, Co, and Pd), the situation differs significantly.^{32,55} Only one broad maximum centered somewhere between $1G_0$ and $3G_0$ is usually observed in conductance histograms.^{4,56} That is a signature of the nontrivial decomposition of conductance consisting of more than one perfectly transmitting channel,^{15,16} since for transition metal atoms d states of different symmetries are available at the Fermi level. The question on half-integer conductance quantization has been addressed.^{33,58} However, recent experiments⁵⁹ do not confirm this hypothesis, thus pointing to the conclusion that the electron transport through ferromagnetic contacts can never be fully spin polarized. Another issue is a large magnetoresistance (MR) effect^{40,42} observed for metallic point contacts made of different magnetic materials. This field is known to be full of controversy. There is still a continuing discussion on whether or not the enormous MR values found experimentally could be of electronic origin^{35,37,60–64} or the effect is just due to atomic rearrangements in the neck region of a contact as a response to the applied magnetic field.^{65,66} Extensive discussion on this topic can be found in the recent paper by Marrows.⁶⁷ We will comment further on the above issues.

A. Computational details

An atomic configuration of a constriction used in our calculations is presented in Fig. 1. The single-atom contact was modeled by a small cluster attached to the semi-infinite fcc (001) leads. The cluster consists of two pyramids joined via the vertex atoms separated by a distance $a_0/\sqrt{2}$. Here, a_0 is the experimental lattice constant of fcc metals: 6.83 a.u. for Cu, 6.66 a.u. for Ni, 6.70 a.u. for Co, and 7.35 a.u. for Pd. The metals under consideration do not have a tendency to form chains.⁶⁸ An atomic bridge is most likely to be broken just after the single-atom limit is achieved. Thus, a configuration shown in Fig. 1 resembles one of limiting configurations of point contacts which could appear in the MCBJ experiments.

Our calculations are based on DFT within the local density approximation. The of Vosko-Wilk-Nusair parametrization (Ref. 69) for the exchange and correlation energy was

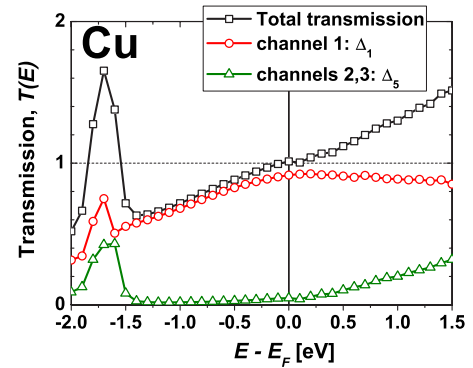


FIG. 4. (Color online) Energy-dependent transmission and its decomposition to the conduction eigenchannels for the Cu single-atom contact shown in Fig. 1.

used. The potentials were assumed to be spherically symmetric around each atom [atomic sphere approximation (ASA)]. However, the full charge density, rather than its spherically symmetric part, was taken into account. To achieve well converged results, the angular momentum cutoff for the wave functions and the Green's function was chosen to be $l_{\max} = 3$ that imposed a natural cutoff $2l_{\max} = 6$ for the charge density expansion. In the case of heavy element Pd, the scalar relativistic approximation⁷⁰ was employed. For the conductance calculation, the surface Green's function was computed using a small imaginary part $\text{Im } E = 0.04$ mRy and about 250 000 k points were taken in the two-dimensional Brillouin zone. Instead of integration over planes, current matrix elements (21) were averaged over atomic layers as described in detail in Ref. 31. A typical error in the calculation of conductance was $\sim 5\%$.

B. Symmetry analysis of eigenchannels

To understand the relation between the electronic structure and the transport properties of atomic contacts, we consider the energy-dependent total transmission, $T(E)$, and its decomposition to the conduction eigenchannels, $T_i(E)$. Results are shown in Figs. 4, 6, 8, and 9 for the case of Cu, Ni, Co, and Pd point contacts, respectively. The investigated structure (Fig. 1) has a C_{4v} symmetry. Further, we denote individual channels by the indices of irreducible representations of this group using notations of Ref. 71, common in band theory. In addition, each channel can be classified according to the angular momentum contributions when the channel wave function is projected on the contact atom of the constriction. This is very helpful since the channel transmission can be related to the states of the contact atom.¹⁵ For example, the identity representation Δ_1 of the C_{4v} group is compatible with the s , p_z , and d_{z^2} orbitals (here, z is perpendicular to the surface and passes through the contact atom), while the two-dimensional representation Δ_5 is compatible with the p_x , p_y , d_{xz} , and d_{yz} orbitals. The basis functions of Δ_2 and Δ_2' are $d_{x^2-y^2}$ and d_{xy} harmonics, respectively.

C. Cu contacts

The energy-dependent transmission of Cu atomic contact (shown in Fig. 1) is presented in Fig. 4 together with the

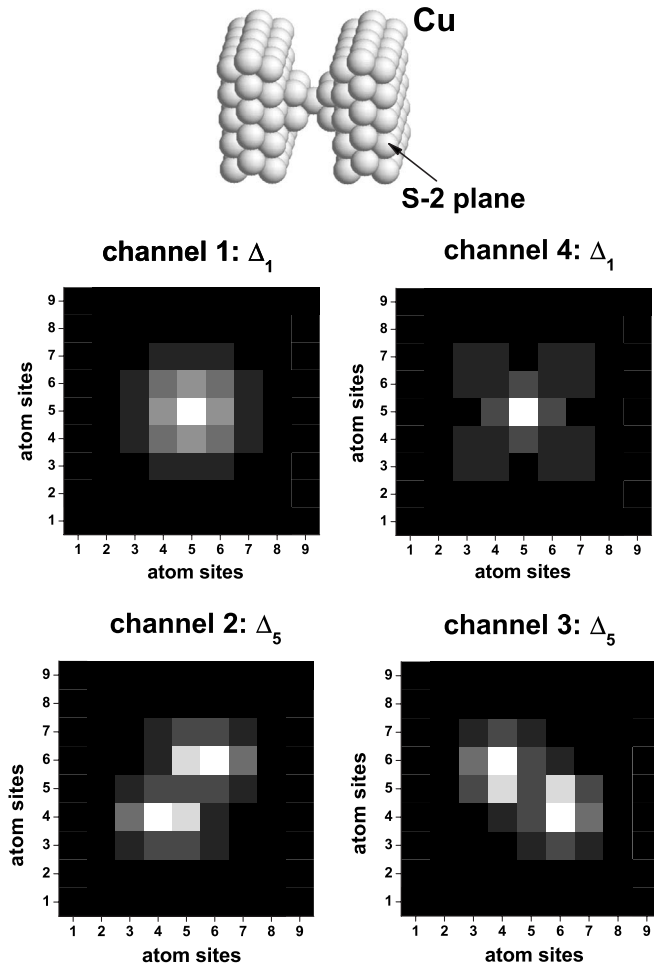


FIG. 5. Wave functions $|\Psi_i(\mathbf{r})|^2$ (probability densities) of the four dominating eigenchannels for the pyramidal Cu contact shown on the top. Wave functions resolved to atoms are visualized two atomic planes below the surface plane (S-2). Colors from white to black correspond to consequently decreasing positive values. Transmission probabilities of channels are $T_1=0.90$ (Δ_1), $T_2=T_3=0.71$ (Δ_5), and $T_4=0.08$ (Δ_1), which are summed up to conductance $G=2.57G_0$. Further details are given in the text.

eigenchannel decomposition. At the Fermi energy, the calculated conductance value is $G=1.01G_0$. It mainly consists of one open channel of Δ_1 symmetry which arises locally from s , p_z , and d_{z^2} orbitals when the wave function is projected on the contact atom. This result is in good agreement with a lot of experiments^{32,56} mentioned previously as well as with other calculations involving different approaches.^{21,23} The additional twofold degenerate channel has Δ_5 symmetry. Transmission of this channel increases at energies above the Fermi level (E_F) together with an increase of the p_x, p_y contribution to the local density of states (LDOS) at the contact atom. However, at $E < -1.5$ eV below the E_F , the Δ_5 channel is built mainly from the d_{xz}, d_{yz} orbitals of the Cu atom.

We would like to point out that in the case of noble metals, the conductance of single-atom contact is not necessarily restricted to one channel. An example of a configuration which has more channels (but still has only one Cu atom at the central position) is presented on the top of Fig. 5. Because of the larger opening angle for incoming waves as

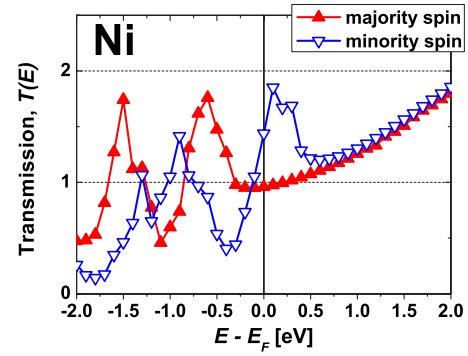


FIG. 6. (Color online) Spin-dependent transmission as a function of energy for the Ni single-atom contact shown in Fig. 1.

compared with the preceding case, conductance of such system is $G=2.57G_0$ with major contribution from four channels (Fig. 5 and its caption). The value $2.57G_0$ correlates with a position of the third peak in the conductance histogram of Cu, which is shifted from $3G_0$ to smaller values.^{32,56} As is seen from the presented example, conductance quantization does not occur for the metallic atomic-sized contacts. In general, even for noble metals, conduction channels are only partially open³² in contrary to the case of quantum point contacts realized in the two-dimensional electron gas where a clear conductance quantization was observed.⁷²

For illustration, we present in Fig. 5 probability amplitudes of the eigenchannels $|\Psi_i(\mathbf{r})|^2$ in real space resolved with respect to atoms of the second plane (S-2) below the surface. We see that the wave functions of the first and fourth channels with the highest symmetry (Δ_1) obey all eight symmetry transformations of the C_{4v} group, while two different wave functions of the double degenerate channel (Δ_5) are transformed to each other after some symmetry operations.

D. Transition metal contacts

We turn to transition metals, and consider the ferromagnetic Ni assuming a uniform magnetization of the sample. Transmission $T(E)$ split per spin of a Ni contact is shown in Fig. 6. A shift ~ 0.8 eV along the energy axis between transmission curves is seen that is in agreement with exchange splitting of the Ni d states. Similar computational results regarding transmission of Ni constrictions were reported by Solanki *et al.*,³⁶ Rocha *et al.*,²⁴ and Smogunov *et al.*³⁹ Exchange splitting estimated from their works varies from 0.8 to 1.0 eV, but fine details differ because of different atomic configurations and employed methodologies. In this regard, exchange splitting about 2.0 eV observed in transport calculations of Jacob *et al.*³⁷ in the case of Ni contact seems to be overestimated.

The shift in energy due to different spins is observed as well for the transmissions of individual channels (Fig. 7). We see from Fig. 7 and Table I that at the Fermi energy the spin-up (majority) conductance of Ni contact is mainly determined by one open Δ_1 channel (similar to the case of Cu), while three partially open channels, of Δ_1 and Δ_5 symmetries, contribute to the spin-down (minority) conductance. The minority Δ_5 channel arises locally from d_{xz} and d_{yz}

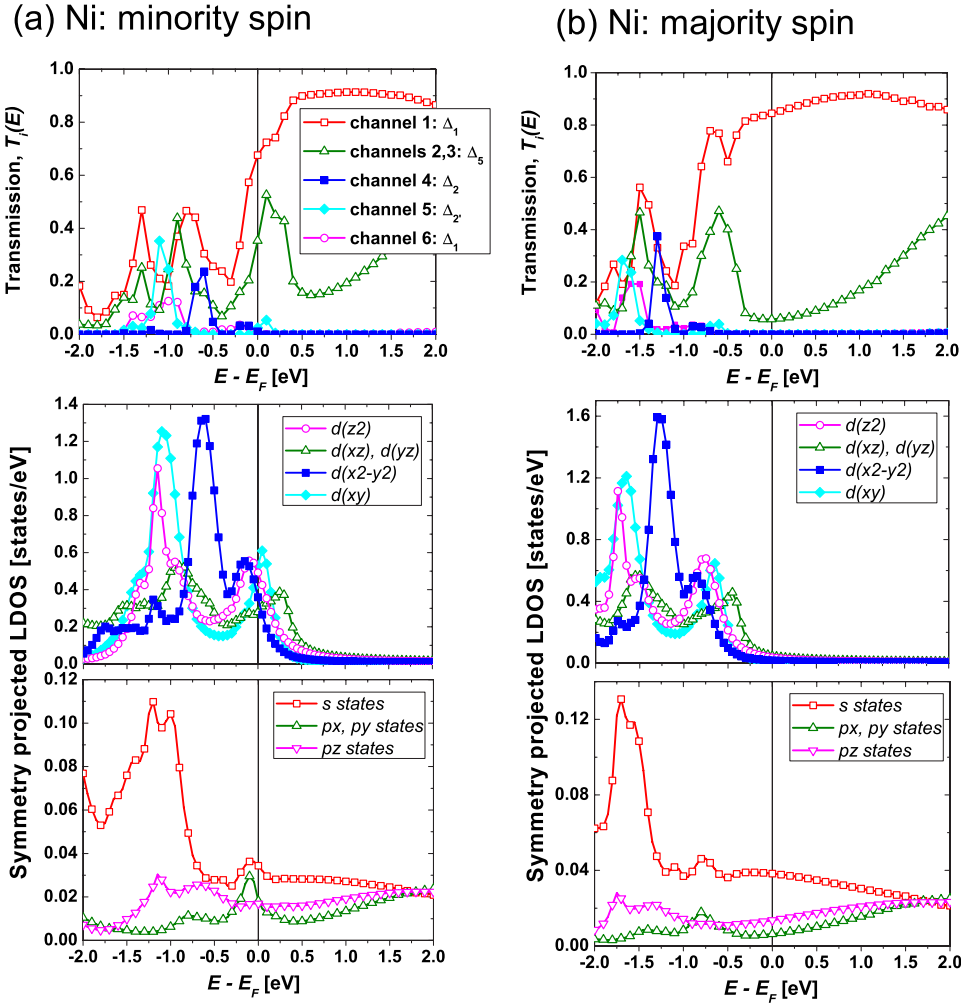


FIG. 7. (Color online) Spin- and energy-dependent transmission decomposed to conduction eigenchannels for the Ni atomic-sized constriction in comparison with the symmetry projected local density of states at the contact atom (i.e., apex atoms in Fig. 1).

states, rather than from p_x and p_y states whose contribution to the spin-down LDOS at the Fermi energy is much smaller (Fig. 7). The calculated conductance, $G=1.20G_0$, correlates with a position of the wide peak in the conductance histogram of Ni centered between $1G_0$ and $2G_0$.^{56,59}

Within the energy range shown in Figs. 6 and 7 (± 2 eV around E_F), we count six eigenmodes of different symmetries for both spins. At energies well above the Fermi level

($E > 1.0$ eV), the spin splitting of Ni sp states is lost, and the picture is similar to what we have seen for Cu. Three channels are present: one open Δ_1 (sp_z -like) channel with transmission around 0.9 and a partially open double degenerate Δ_5 (p_x, p_y) channel whose transmission increases monotonically as a function of energy. However, below the Fermi energy, all eigenmodes $T_i(E)$ display a complicated behavior (Fig. 7, upper plots) that reflects a complex structure of the

TABLE I. Transmission probabilities of eigenchannels at the Fermi energy of Ni and Co atomic contacts shown in Fig. 1 for two different (P and AP) orientations of magnetizations in the leads. Only transmissions of the dominant channels are presented. Magnetoresistance ratio defined as $MR=[(G_P-G_{AP})/G_{AP}]100\%$ is given in the last line.

Channel	Ni			Co		
	P	AP	(\uparrow) or (\downarrow) spin	P	AP	(\uparrow) or (\downarrow) spin
T_1 (Δ_1)	0.68	0.84	0.82	0.36	0.89	0.58
$T_2=T_3$ (Δ_5)	0.35	0.06	0.31	0.14	0.07	0.09
T_4 (Δ_2)				0.17		
Transmission	1.44	0.96	1.45	0.83	1.03	0.76
MR ratio		-17%			+23%	

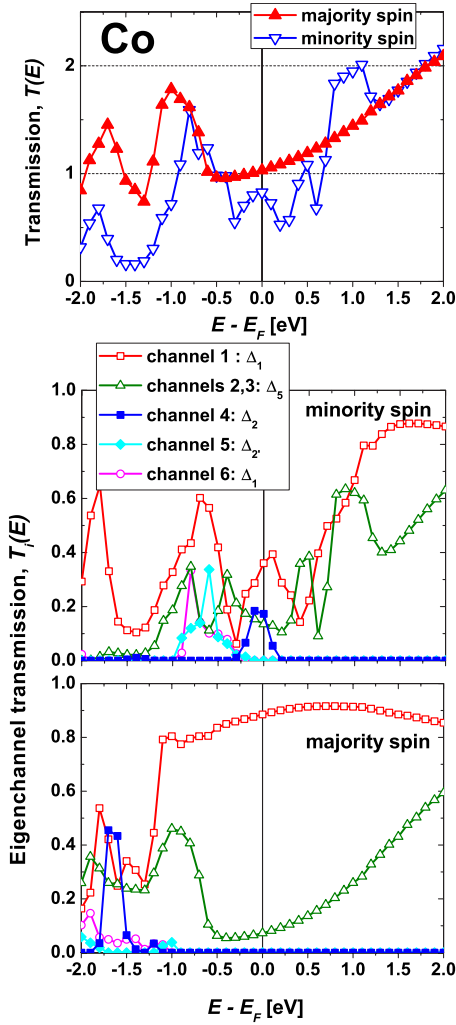


FIG. 8. (Color online) Spin- and energy-dependent transmission decomposed to conduction eigenchannels for the Co single-atom contact shown in Fig. 1.

LDOS projected on orbitals of the contact atom (Fig. 7, bottom plots). Below E_F , the existing s , p_z , and d_{z^2} states are strongly hybridized, giving rise to two channels of Δ_1 symmetry at energies about $E \approx -1.0$ eV and $E \approx -1.5$ eV for minority and majority spins, respectively. A clear correlation between the symmetry projected LDOS and $T_i(E)$ is seen for the pure d channels, Δ_2 ($d_{x^2-y^2}$) and Δ_2' (d_{xy}). For example, the minority spin $d_{x^2-y^2}$ resonance centered around $E = -0.7$ eV and majority spin $d_{x^2-y^2}$ resonance at $E = -1.3$ eV reflect themselves as peaks in the transmission of the minority and majority Δ_2 channels. The same is valid for the d_{xy} states at $E = -1.1$ eV (spin down) and $E = -1.7$ eV (spin up), that causes the increase of transmission of the Δ_2' channel at the same energies. However, even at the resonances, the Δ_2 and Δ_2' channels are only partially open because the $d_{x^2-y^2}$ and d_{xy} orbitals are spread perpendicular to the wire (z) axis, that prevents effective coupling with the neighboring atoms.

Our results for Co constriction are presented in Fig. 8. As compared with Ni, the shift between the spin-up and spin-down $T(E)$ curves becomes larger (~ 1.7 eV) because of the stronger exchange field of cobalt. At the Fermi energy, ma-

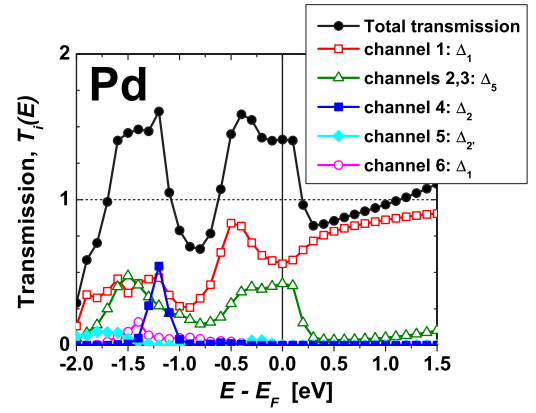


FIG. 9. (Color online) Eigenchannel decomposition of the transmission for the Pd contact shown in Fig. 1.

majority spin conductance is still dominated by one highly transmitted Δ_1 channel (Table I), while for the minority spin the $d_{x^2-y^2}$ resonance is pinned to the Fermi level and results in the additional (as compared with Ni) channel of Δ_2 symmetry. Thus four channels with moderate transmission probabilities contribute to the minority spin conductance (Table I).

Figure 9 shows the results for Pd. According to recent theoretical predictions,⁷³ monatomic Pd wires might exhibit magnetic properties. However, in this work we considered nonmagnetic solution, since a coordination number even for the contact atom was already big enough (Fig. 1) to suppress magnetism.⁷³ Pd is isovalent to Ni. The Fermi level crosses the partially filled d band. Therefore, the eigenchannel decomposition resembles the minority spin channels of Ni. However, due to a larger occupation number, transmission curves are shifted ~ 0.5 eV downward in energy as compared with spin-down Ni modes. The conductance $G = 1.41G_0$ is a sum of three channels. This value is in agreement with the conductance histogram of Pd,⁷⁴ which shows a broad maximum around $\approx 1.7G_0$.

We turn back to Ni and Co contacts, and consider a situation when a relative orientation of magnetizations in the leads is antiparallel (AP), so that an abrupt atomic-scale domain wall is formed as shown in Table II. We see from Table

TABLE II. Spin magnetic moments (in μ_B) at atoms forming Ni and Co contacts shown in Fig. 1 for the parallel (P) and the antiparallel (AP) orientation of magnetizations in the leads. Bulk magnetic moments are $0.62\mu_B$ for Ni and $1.62\mu_B$ for Co.

Atom	Ni		Co	
	P	AP	P	AP
Surface	0.66	0.66	1.78	1.78
Contact-1	0.70	0.69	1.83	1.83
First contact	0.68	0.54	1.76	1.64
Second contact	0.68	-0.54	1.76	-1.64
Contact+1	0.70	-0.69	1.83	-1.83
Surface	0.66	-0.66	1.78	-1.78

I that, both for Ni and Co, the AP conductance reflects the structure of the minority spin channels and consists of a Δ_1 channel and a Δ_5 channel. For the atomic configuration shown in Fig. 1, we obtained “optimistic” MR values: -17% in the case of Ni and $+23\%$ in the case of Co, which are quite small in accordance with our previous study.³⁵ However, the precise MR values as well as transmission curves for Co differ from the results reported in our earlier work because of the different geometrical configurations of atomic contacts. The reason is that the transmission of d -like channels is quite sensitive to the exact geometry.³⁵ We mention here that a more accurate full-potential approach and an improved description of the electron correlations for localized d electrons can somewhat affect presented results. That is also valid for the effects of atomic relaxations which were neglected. In particular, the exact values for the transmission probabilities and MR at the Fermi level reported in this study for different systems could be slightly changed. However, more precise calculations obviously will not affect the physical results of the present work.

Evident conclusions follow from presented examples. First, in contrast to earlier studies,^{33,58} the ferromagnetic Ni and Co contacts do not show any tendency to close one spin channel. On the contrary, both spin channels contribute to the conductance that gives only moderate magnetoresistance values. Independent of the geometry of the atomic contact, the minority spin channel will include a sum of fractional contributions from many modes because the d states are always present at the Fermi level. That agrees with later experiments by Untiedt *et al.*,⁵⁹ where the absence of conductance quantization for ferromagnetic Fe, Co, and Ni contacts was clearly confirmed.

Second, an abrupt, atomic-scale domain wall pinned to the constriction does not show an impressive MR effect. For a fixed atomic configuration, the P and AP conductances are of the same order. Most likely that more sophisticated calculations, involving relaxation effects and noncollinear magnetic moments in the domain wall, will not be able to change this statement.^{75,76} A recent research⁷⁷ toward transport in nanocontacts with noncollinear moments shows that energetically preferable noncollinear magnetic order results in a larger domain wall width as compared to the abrupt, collinear wall considered in the present paper. That leads to weakened scattering of electrons and a further reduction of the MR values.

Turning to the experimental situation on BMR effect in ferromagnetic contacts, we point out that large MR values^{41,42} were usually measured for much thicker constrictions (as compared with atomic-sized contacts) with resistance in the range of hundreds of Ohms. It is believed,^{65,66}

that such experiments suffer from many unavoidable artifacts induced by magnetomechanical effects that mimic the real MR signal, which would come from the spin-polarized transport alone. However, recent studies by Sullivan *et al.*⁴³ and Chopra *et al.*⁴⁴ on Ni and Co atomic-sized contacts report BMR values in the range of 200% – 2000% , with discussion on the electronic origin of the effect due to domain wall scattering. In spite of the fact that attempts to minimize magnetostriuctive effects were undertaken, we just can repeat⁶⁵ that a natural explanation of these^{43,44} and similar experiments^{34,40} is that, due to magnetization reversal processes, unstable in time atomic constriction changes its contact area when magnetic field is applied. Characteristic steps and jumps in the measured field-dependent conductance (Fig. 4 of Ref. 43) or resistance (Fig. 3a of Ref. 44, Fig. 3 of Ref. 34) are distinct evidence of atomic reconstructions and fractional changes of the contact cross section. For example, just eliminating one contact atom from the configuration shown in Fig. 1 changes the conductance of a Ni constriction from $1.2G_0$ (chain of two atoms, see Table I) up to $\sim 2.8G_0$ (one contact atom only, see Ref. 29), thus producing $\sim 130\%$ MR. Further increase of a contact area can give arbitrarily high MR values, that supports the hypothesis on the mechanical nature of the effect.

VI. CONCLUSIONS

To summarize, we have presented a formalism for the evaluation of conduction eigenchannels of metallic atomic-sized contacts from first principles. We have combined the *ab initio* KKR Green’s function approach with the Kubo linear response theory. Starting from the scattering wave formulation of the conductance problem, we have built a special representation of the transmission matrix in terms of local, energy and angular momentum dependent basis inherent to the KKR method. We have proven that solutions of the eigenvalue problem for the obtained matrix are identical to conduction eigenchannels introduced by Landauer and Büttiker. Applications of the method have been presented by studying ballistic electron transport through Cu, Pd, Ni, and Co single-atom contacts. The symmetry analysis of eigenchannels and its connection to the orbital classification known from the tight-binding approach was discussed in detail. Experiments on the electron transport through magnetic contacts were commented.

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$$\int_{S_L} dS [\bar{\Phi}_\nu(\mathbf{r}, E) i \partial_z \bar{\Phi}_\mu^*(\mathbf{r}, E)]_{z \rightarrow -\infty} = -\frac{T_\nu(E)}{2\pi} \delta_{\nu\mu}.$$

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