Spin-exchange interaction in ZnO-based quantum wells

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Wurtzitic ZnO/(Zn, Mg)O quantum wells grown along the (0001) direction permit unprecedented tunability of the short-range spin exchange interaction. In the context of large exciton binding energies and electron-hole exchange interaction in ZnO, this tunability results from the competition between quantum confinement and giant quantum confined Stark effect. By using time-resolved photoluminescence we identify, for well widths under 3 nm, the redistribution of oscillator strengths between the *A* and *B* excitonic transitions, due to the enhancement of the exchange interaction. Conversely, for wider wells, the redistribution is canceled by the dominant effect of internal electric fields, which dramatically reduces the exchange energy.

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Exchange interaction energy naturally appears in quantum mechanics whenever one has to deal with identical interacting particles. This interaction is important for understanding particle physics, interpreting small energy splittings in atoms, and for describing spin-related excitonic fine structure in condensed matter. In this latter case, a prerequisite to the interpretation of the overall optical properties of pure solids has been the definition of the short-range and long-range contributions to this interaction.¹

In this paper, we address a report on a modification of the short-range electron-hole exchange interaction with well width, in ZnO-ZnMgO wurtzitic quantum wells (WQWs). We provide a good description of our results by using a three-band model, an extension of the model found to be useful for a quantitative analysis of the optical properties of bulk ZnO.^{2[,3](#page-3-3)} Due to an efficient quantum confined Stark effect (QCSE), the short-range electron-hole exchange interaction redistributes oscillator strengths among exciton states built from different valence bands in a way that depends on well width.

For Group III nitride WQWs, due to excessive inhomogeneous broadening effects, 4 the optical properties and their evolution with time are treated in the context of a band to band model. The short-range electron-hole exchange interaction is not identified as an important issue although it plays, for micrometric epilayers, 5 a role in the mixing of the excitonic states that originate from the different valence bands. The short-range electron-hole exchange interaction γ equals 0.69 meV for GaN (Ref. [5](#page-3-5)) and 0.02 meV for GaAs.⁶ Gil³ has established for ZnO, by using a model including the appropriate excitonic symmetry, that the weak oscillator strength of the low energy *A* exciton compared to the oscillator strength of the higher energy *B* exciton results, in particular, from an extremely efficient A-B coupling. This coupling is due to the giant magnitude of the short-range electron-hole exchange interaction energy $(\gamma = 4.7 \text{ meV}$ in ZnO). Such quantum beat oscillations cannot be studied in the context of a band to band model. This indicates that the ZnO-ZnMgO WQW is the adequate system for proving the need to use *a true excitonic description*, of the optical properties. They cannot be interpreted out of the context of a model that includes the short-range exchange interaction *and* the tuning of its magnitude by varying well widths.

When reducing the width of a quantum well (L_W) , given a recombination process, one generally observes a blueshift of the emission, as well as an enhancement of the excitonic binding energy, $\frac{7}{7}$ and of the electron-hole exchange inter-action.^{8,[9](#page-3-9)} However, internal electric fields which are spontaneously generated in (0001)-grown WQW structures, from the breaking of on-axis translational symmetry at the heterointerfaces¹⁰, produce a huge QCSE that drastically reduces the excitonic oscillator strength by separating the wave functions of the electron and hole, while smoothly reducing the excitonic binding energy via the extension of the in-plane relative motion of the electron-hole pair. $11,12$ $11,12$

Let us first consider Group III nitride semiconductors for comparison. They exhibit particularly large coefficients of both spontaneous and piezoelectric polarizations (comparable to those of ZnO ^{[13](#page-3-13)[–15](#page-3-14)} and thus can generate internal fields of several MV/cm. For wide enough nitride WQWs (above a few nanometers, in practice), the QCSE is so strong that it can counteract the quantum confinement and therefore can push the fundamental transition *below* the natural excitonic gap of the WQW material. 14 Two regimes of well widths can be defined:

(i) for narrow WQWs, the quantum confinement dominates, yielding large emission energies and typical excitonic lifetimes of nanoseconds, or slightly less,

(ii) for wide enough WQWs, the QCSE dominates and the emission energy decreases almost linearly with increasing L_W , whereas the exciton lifetime increases (its oscillator strength decreases) almost exponentially.

Similar effects are expected in case of $ZnO/(Zn, Mg)O$, but enriched from short-range interaction effects.

Quantum confinement is known to change this interaction by a factor that is inversely proportional to the squeezed volume occupied by the confined exciton wave function. For quantum wells, the modification factor is given by $\frac{8}{3}$

$$
\alpha = \pi a_{3D}^3 W_{eh} |\varphi_\lambda(0)|^2, \tag{1}
$$

where a_{3D} is the excitonic effective Bohr radius for the bulk material. The exciton relative motion is described by the product of envelope functions $f_e(z_e)$ and $f_h(z_h)$ describing the electron and hole confinement along the QW growth axis, by the two-dimensional hydrogenic term $\varphi_{\lambda}(\rho) = (\sqrt{2/\pi}/n)$ λ)exp(- ρ/λ), where ρ is the in-plane relative coordinate. The *z*-dependent factor is given by

$$
W_{eh} = \int_{-\infty}^{+\infty} dz [f_e(z) f_h(z)]^2.
$$
 (2)

From Eqs. (1) (1) (1) and (2) (2) (2) it is obvious that, in any case of on-axis separation of the electron and hole, the $\alpha\gamma$ factor may become smaller than unity and even vanish with increasing *LW*, in presence of a longitudinal electric field.

Due to large spontaneous and piezoelectric polarization parameters,¹⁵ WQWs based on ZnO, such as ZnO-(Zn, Mg)O WQWs, are thus expected to materialize the unprecedented situation where *both* large internal electric fields *and* giant exchange interaction terms are present. To face this situation, competitive effects of confinement and electric fields on the large exciton binding energy $(\sim 60 \text{ meV})$ have to be properly considered.

The samples were grown by plasma-assisted molecular beam epitaxy, the metals (Zn and Mg) being evaporated using Knudsen cells and atomic O being activated in a radiofrequency plasma cell. After thermal cleaning of the *c*-oriented sapphire substrates, the latter were exposed to the O beam for 5–10 min prior to the deposition of ZnO. The growth of a ZnO template was then carried out at a growth temperature of 520 °C and a growth rate of \sim 0.45 μ m/h. In order to minimize the effect of Al diffusion, which acts as a shallow donor from the substrate and to ensure a low carrier concentration in the QW area, templates with thicknesses of $1 \mu m$ were grown. Based on previous electrochemical capacitance-voltage measurements of ZnO epilayers grown using the same growth conditions, we estimate the residual carrier concentration in the vicinity of the QWs to be less than 1016 cm−3. The QW heterostructures consist in the growth of a 0.2 μ m thick $(Zn, Mg)O$ layer, a ZnO QW with thicknesses varying from sample to sample, and a 0.1 μ m thick (Zn, Mg)O cap layer. QW thicknesses were varied from 1.6 to 9.5 nm; the Mg content of the barrier layers was in the range of 21–22%, varying slightly from sample to sample. More details can be found in Ref. [16.](#page-3-16)

In the following, we use results of time-integrated photoluminescence (PL), obtained under pulsed excitation, instead of continuous wave (cw) PL. The 2 ps laser pulses were provided by the third harmonic (260 nm) of a titaniumsapphire laser, with typical energy densities of \sim 50 nJ/cm² per pulse. It is important to outline that unintended photoinduced screening of electric field easily occurs in such wide band gap WQWs (Refs. 13-[15](#page-3-14)) and that correct observation of an unscreened situation (and correct measurement of a photoluminescence energy) requires that one works using pulsed excitation conditions at a repetition rate slow enough to reach a situation where both exponential intensity decay

FIG. 1. Time-integrated photoluminescence spectra obtained under pulsed excitations for four different WQW widths and the band profiles, energy levels, and envelope functions for electrons and heavy holes that we calculate for two extreme situations, namely narrow and wide WQWs.

time and absence of any redshift of the photoluminescence are reached. Therefore the repetition rate was adapted to the slowness of the observed decay, by use of an acousto-optical modulator, between 800 Hz and 80 kHz, thus allowing for a full deexcitation between two consecutive pulses. The PL signal was collected and focused by two parabolic mirrors onto the entrance slit of a 50 cm spectrometer. A grating with 150 grooves/mm disperses the PL signal, which is then detected by a Hamamatsu synchroscan streak camera.

Figure [1](#page-1-2) shows, for four different QW widths, the timeintegrated photoluminescence (PL) spectra obtained under pulsed excitation. Insets in Fig. [1](#page-1-2) show the band profiles, energy levels, and envelope functions for electrons and heavy holes that we calculate for two extreme situations, namely narrow and wide QWs. A very good agreement is obtained between our variational "one band" excitonic calculation¹⁵ and the experimental PL energies, as shown in Fig. 3 of Ref. [15,](#page-3-14) when we include an electric field of 0.9 MV/cm.

The well-width dependence of the oscillator strength is usually considered to be roughly the same as that of quantity $f = |\varphi_{\lambda}(0)|^2 I_{eh}^2$, where

$$
I_{eh} = \int_{-\infty}^{+\infty} dz f_e(z) f_h(z)
$$

is the envelope-function overlap integral. So, in this approach, we can readily see how fast the oscillator strength is expected to decrease: when the QCSE becomes dominant, we obtain a drop of more than seven orders of magnitude between $L_W = 2$ and 7 nm. Wide WQWs show very large PL decay times, at a temperature of $T=8$ K, and they grow almost exponentially with L_W . As an illustration the data for the 7.1 nm wide WQW is shown in the right-hand plot in Fig. [2.](#page-2-0)

Experimentally, things are a little more complicated, for narrow WQWs, as reported in Ref. [15.](#page-3-14) The left-hand plot in Fig. [2](#page-2-0) indicates that the PL dynamics of WQWs emitting at energies above the band gap of ZnO exhibits two characteristic times. Typically, a first decay occurs with a slightly

FIG. 2. Photoluminescence decay for a wide well (right-hand plot), and for a narrow well (left-hand plot). Note the different time scales in top and bottom in the left-hand plot. In this case, the PL decay time is obtained by fitting the result to the single exponential function for the two regimes (see text). For the wide well, a background value of 2×10^{-2} is used in the fit.

subnanosecond time (τ_1) , followed by a second one, with decay time of a few tens of nanoseconds (τ_2) . We have checked that the slower part of this dynamics was not induced by a slow carrier transfer from the barriers: timeresolved PL (TR-PL) from these barriers revealed much slower decay times, on orders of hundreds of microseconds. These τ_1 and τ_2 are accurately measured if recording the decays using different, appropriate times scales as shown here in the case of the 1.6 nm thin WQW. The measured decay times are reported in Fig. 3 (dots).

We explain these results by the superposition of two radiative mechanisms related to the two fundamental excitonic ground states, usually referred to as the *A* and *B* excitons, in the bulk material. As explained above, the *e*-*h* exchange interaction mixes the Γ_5 exciton states, defined in Ref. [3,](#page-3-3) that are dipole allowed in the present σ -polarization.^{2[,3](#page-3-3)} The shortrange exchange energy, $\gamma = 4.7$ meV for bulk ZnO, strongly

FIG. 3. (Color online) Measured (dots) and computed decay times vs well width. Right-hand bottom inset: short-range exchange energy in $\alpha\gamma$ meV. Left-hand top inset: the computed *A-B* splitting vs well width to be compared with widths of photoluminescence lines.

depends on well width for the present WQWs, as illustrated by the right-hand bottom inset in Fig. [3,](#page-2-1) which presents the changes of the e -*h* exchange energy, $\alpha\gamma$ calculated from Eqs. (1) (1) (1) and (2) (2) (2) versus L_W . For narrow enough QWs, the confine-ment enhances both direct Coulomb (see Ref. [15](#page-3-14)) and shortrange exchange energies. But they both become smaller than their bulk value for QW widths larger than \sim 2–3 nm.

For narrow QWs, the mixing of the two fundamental Γ_5 states by $\alpha\gamma$ necessarily redistributes some oscillator strength from the *A* exciton to the benefit of the *B* exciton, such as in the case³ for bulk ZnO , but more strongly, since in that case, the exchange energy $\alpha\gamma$ is enhanced. To describe this for our samples, we have used an adapted version of the formalism presented in Ref. [3,](#page-3-3) for Γ_5 states. More specifically, as we did in Ref. [15,](#page-3-14) we assume, for simplicity, equal on-axis effective masses for the so-called heavy and light holes. This warrants that, even for QWs, the energy difference between diagonal terms for these two types of holes is independent of the well width. We assume, too, that the bulk binding energies are equal for *A*, *B*, and *C* excitons for all QW widths. Again, this permits the energy separation of diagonal terms in the Γ_5 excitonic Hamiltonian of Ref. [3](#page-3-3) to be kept constant. We mimic internal strain by our choice of the Δ_1 crystal-field parameter. Finally, we consider a single confined state for electrons as well as for each of the three hole bands, which is reasonable in view of the band profiles sketched in Fig. [1.](#page-1-2)

With such hypotheses, we are left with the resolution of the following matrix:

$$
\begin{pmatrix}\n| \Gamma_{5A} \rangle & | \Gamma_{5B} \rangle & | \Gamma_{5C} \rangle \\
\epsilon^* - \Delta_1 - \Delta_2 + \alpha \gamma/2 & \alpha \gamma & 0 \\
\alpha \gamma & E^* - \Delta_1 + \Delta_2 + \alpha \gamma/2 & -\sqrt{2}\Delta_3 \\
0 & -\sqrt{2}\Delta_3 & E^* - \alpha \gamma/2\n\end{pmatrix}.
$$
\n(3)

Here, the bulk-like term is simply the one that is plotted in the right-hand bottom inset in Fig. 3 and E^* is an energy which accounts for the band gap, augmented by the confinement energies of the electron and the hole and reduced by the size-dependent binding energy. Within our approximations, the *B* line remains a few meV above the fundamental *A* line. In fact, some L_W dependency (left-hand top inset in Fig. [3](#page-2-1)) is only obtained for $L_W < 3$ nm and the maximum separation of these lines is of 12 meV, which is rather small, if compared to the PL linewidths for the two narrower QWs, comprised between 25 and 35 meV. These inhomogeneous linewidths result from the fluctuations of Mg concentration in the barriers and of strain along the QW plane. We thus understand that, for all well widths, including the smaller ones, the observed PL lines correspond to the superposition of the two unresolved transitions, which we may still call "*A*" and "*B*." These transitions correspond to well-width dependent combinations of $|\Gamma_{5A}\rangle$ and $|\Gamma_{5B}\rangle$ states, both dipole allowed in σ polarization.

Coming to the oscillator strengths—thus PL decay times—of these transitions for the narrower QWs, exchangeinduced mixings now have the same kind of effect as for ZnO epilayers: reduction of oscillator strength for the ground state *A* to the benefit of *B*. For each of these two transitions, using the notation in Ref. [3,](#page-3-3) the eigenstates of the matrix in Eq. ([3](#page-2-2)) have the general form $u(L_W)|\Gamma_{5A}\rangle + v(L_W)|\Gamma_{5B}\rangle$ $+ w(L_W) | \Gamma_{5C}$. Owing to spin-flip effects,³ the oscillator strengths in σ polarization are proportional to $[u(L_W)]$ $+v(L_W)^2$ multiplied by the envelope factor *f*, calculated above. The L_W dependency lies essentially, here, on the variation of the $\alpha\gamma$ off-diagonal term.

Figure [3](#page-2-1) is a plot of a quantity inversely proportional to the calculated oscillator strengths for the two lower-lying optical transitions versus L_W . The case of wide QWs (dominating QCSE) is rather simple: having nearly no exchange coupling means that the oscillator strengths of confined states built upon the Γ_{5A} and Γ_{5B} states are nearly equal, in σ polarization. The only difference arises from the mixing of Γ_{5B} and Γ_{5C} states via spin-orbit off-diagonal terms in the Hamiltonian. Therefore, the oscillator strengths of these quantized states should follow together the well-width dependence of the "envelope term." A factor has been applied

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to this quantity in order to fit the experimental PL decay times for the 5.2 and 7.1 nm wide QWs. For the two narrower QWs, two decay times have been plotted, resulting from the detailed measurements shown in Fig. [2.](#page-2-0)

The double-exponential PL decays measured for narrow QWs (and the single one for wide QWs) are well explained by the superposition, within the same line, of two exciton states having different recombination rates. We thus assign this observation to the exciton state mixing induced by the enhanced (or reduced) e-h exchange interaction.

In summary, we report a quantitative measurement of the impact of quantum confined short-range spin-exchange interaction on the optical properties of wurtzitic ZnO/(Zn,Mg)O quantum wells. For well widths smaller than 3 nm, it manifests itself via a double exponential decay that we have explained by the redistribution of oscillator strengths between the two lower-lying excitonic transitions. This effect disappears for well widths larger than 3 nm, due to the presence of the strong electric field.

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