Stability and ordering properties of fcc alloys based on Rh, Ir, Pd, and Pt

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Stability properties and ordering trends for the six face-centered cubic binary combinations of the four transition metals Rh, Ir, Pd, and Pt are examined in the context of electronic structure calculations. The method is based on a Green's function description of the electronic structure of random alloys. Configurational order is treated within the generalized perturbation method. On one hand, the three alloys Pd-Rh, Pd-Ir, and Pt-Ir that have been studied experimentally are confirmed to behave like phase-separating systems. On the other hand, the other three mixtures Pd-Pt, Rh-Ir, and Pt-Rh, for which phase-separating trends have been inferred from experiments, are found to display chemical order with ordering of the $(1 \ 0 \ 0)$ and $(1 \ 1/2 \ 0)$ family types and a mixture of both, respectively. The origin of these results is discussed in terms of electronic structure properties.

DOI: 10.1103/PhysRevB.74.064202

PACS number(s): 61.66.Dk, 64.60.Cn, 65.40.Ba, 71.20.Be

I. INTRODUCTION

The six phase diagrams associated with the possible combinations of two elements among the four fcc-based transition metals of column VIIIA, Rh, Ir, Pd, and Pt, as presented in Ref. 1 display deceptively simple features. Indeed, for each of the six alloy systems, the phase diagram indicates a miscibility gap at relatively low temperature in the solid phase, and a region of face-centered cubic (fcc) solid solution at high temperature in the entire range of composition before melting occurs. In only three among the six cases, namely, for Pd-Rh, Pd-Ir, and Pt-Ir, the miscibility gap is represented by a solid line, indicating, by convention, that only in these cases are the assessments based on actual experiments. Interestingly enough, all these diagrams were proposed by Raub² in the 1950s in a review study on platinum metal alloys, and not much work has been done experimentally since then on Pt-Rh, Ir-Rh, and Pt-Pd as we will show below.

Hence, in this paper, a systematic study on alloy stability and ordering trends has been undertaken for these six alloys with a first-principles electronic structure approach. The configurational order was formulated within the generalized perturbation method (GPM).³⁻⁶ The electronic properties of the reference medium on which the GPM relies were described in the framework of the self-consistent tight-binding linear muffin-tin orbital (TB LMTO) multiple-scattering formulation of the coherent potential approximation (CPA).^{6,7} Finally, temperature effects on local order and stability were accounted for by means of a standard generalized mean-field approach, namely, the cluster variation method.^{4,8} From the present first-principles analysis, Pd-Rh, Pd-Ir, and Pt-Ir exhibit clustering trends in full agreement with experimental observations. On the other hand, Pd-Pt, Rh-Ir, and and Pt-Rh exhibit chemical order of the (100) and (11/20) family types, and a mixture of both, respectively (see Refs. 4 and 9 for a description of the structures). Because of the strength of the ordering tendencies, our theoretical analysis reveals that low-lying phase diagrams more complex than a miscibility gap should exist for these three systems.

The paper is organized as follows. In Sec. II, we review the results that are available in the literature, and comment on the salient features of the assessed phase diagrams of the six binary alloys. In Sec. III, we discuss the electronic structure and equilibrium properties of the six alloys based on a first-principles TB LMTO CPA description of the electronic structure of disordered alloys. In Sec. IV we present the results of the ground-state analysis of the Ising Hamiltonian based on a treatment of chemical order within the GPM. Finally, the results are summarized in Sec. V.

II. PHASE DIAGRAMS

From the commonly accepted phase diagrams¹ shown in Fig. 1 for the six binary alloys made of Rh, Ir, Pd, and Pt, only a miscibility gap at low temperature characterizes the solid portion of the phase diagrams with maximum critical temperatures reported in Table I. At higher temperatures all these alloys form a series of completely miscible solid solutions based on the fcc lattice. However note that only three among the six miscibility gaps are reported with solid lines, indicating that only these three were actually based on experiments. Most of the original work on which these phase diagrams are based was done by Raub in the late 1950s.² According to Raub, a correlation could be made between the difference in the melting points of the alloy species and the highest critical temperature of the miscibility gap, at least from the experiments performed on Pd-Ir, Pt-Ir, and Pd-Rh (see Table I). Based solely on this observation, Raub goes on and "extrapolates a possible critical temperature for the miscibility gap of the Rh-Ir, Pd-Pt, and Pt-Rh alloys." These are basically the considerations (see below for further comments) on which the very hypothetical phase diagrams given in Ref. 1 are based. Let us now comment on each alloy phase diagram.

The phase diagram of Pd-Rh has been described in Ref. 10. The results were confirmed by electrical resistivity



FIG. 1. (Color online) Assessed phase diagrams of the Rh-Ir, Pd-Pt, Rh-Pd, Ir-Pt, Rh-Pt, and Ir-Pd binary alloy systems, taken from Ref. 1.

measurements,¹¹ and the thermodynamic mixing properties have been investigated to confirm the solid-state immiscibility.¹²⁻¹⁴

TABLE I. For each A-B alloy, the table indicates the number of valence electrons for each species i, N_i , and the difference in the number of valence electrons, $\Delta N_v = N_B - N_A$, the maximum value of the temperature of the miscibility gap, T_{MG} , and the melting point of each species i, T_M^i . Temperatures are given in °C.

A - B alloy	N_A	N_B	$\Delta N_{ m v}$	$T_{\rm MG}$	$T^A_{\rm M}$	T^B_{M}
Rh-Ir	9	9	0	850	2447	1963
Pd-Pt	10	10	0	770	1555	1769
Rh-Pd	9	10	1	845	1963	1555
Rh-Pt	9	10	1	760	1963	1769
Ir-Pd	9	10	1	1482	2447	1555
Ir-Pt	9	10	1	975	2447	1769

The phase diagram of Pt-Rh redrawn¹⁵ in 1992 with practically no input from experiment has been challenged in a recent study.¹⁶ In this experimental work based on emf measurements the authors found a moderate negative deviation from Raoult's law for the activities, and relatively large negative enthalpies of mixing and negative excess entropy in the 900-1300 K temperature range. These results do not support the existence of a solid-state miscibility gap but instead point to the existence of some kind of ordering, and are in agreement with the shape of the solidus-liquidus lines. However, no systematic characterization of the chemical order has been reported yet. It is worth noting that the author of the originally suggested phase diagram reconsidered the Pt-Rh system at a later time in a study on the ternary Au-Pt-Rh alloys, and concluded that long-time annealing of Pt-Rh samples for more than four years at 600 °C corroborated the existence of a continuous solid solution with no initiation of decomposition.¹⁷ Only recently was a diffuse x-ray and small-angle neutron scattering analysis performed on a Pt-47 at. % Rh sample.¹⁸ The results point to very "faint" ordering of the $(1 \ 1/2 \ 0)$ family that seems to support the existence of the so-called "phase 40" (Refs. 4 and 9) around the equiatomic composition with an estimated critical order-disorder temperature of about 185 K.

The phase diagram of Pd-Ir originally investigated by Raub^{2,19} in 1959 and 1964 has been reconsidered since then.^{20,21} These experimental studies have confirmed the clustering trend in this system.

The phase diagram of Pt-Ir was also originally proposed by Raub^{2,22} and was based on experimental work. The phase diagram has been redrawn recently with a much higher maximum critical temperature of 1370 °C (instead of 975 °C around 25 at. % Ir).²³ The positive departure from Raoult's law for the activities that was measured experimentally^{24,25} confirmed the clustering tendency in this system.

A recently assessed phase diagram of Rh-Ir has been proposed²⁶ on the basis of thermodynamic data²⁷ that seem to confirm the clustering trend in this system. However, the highest critical temperature of the miscibility gap was set at 1335 °C instead of the 850 °C suggested by Raub.² Although a large negative deviation from the ideal solution is observed in this system, this is only an indication that a miscibility gap may exist since no direct measurement of short-range order (SRO) has been performed so far on this system.

Finally, the Pd-Pt phase diagram suggested by Raub² was reconsidered in the 1970s.²⁸ The results of vapor pressure by a torsion-effusion method and of calorimetric heat-of-solution measurements indicated a small negative deviation of the activities from ideal solution lines, moderately negative enthalpies of formation over the whole range of alloy composition, and positive entropies of formation smaller than the ideal entropies. These results have been confirmed by calorimetric investigation²⁹ and reviewed in Refs. 30 and 31. Finally, x-ray diffuse scattering measurements were performed in the late 1960s.³² Although this study concluded that SRO in Pd-Pt should exist, no detailed work has yet been reported to fully characterize it.³³

As said in Ref. 27, "a complete set of good thermodynamic data for all the binary systems discussed here would



FIG. 2. DOSs of the pure elements (solid line) Rh, Pd, Ir, and Pt based on the fcc structure. The dotted line indicates the variation of the integrated density of states with energy. The Fermi energy E_F is indicated by a vertical line and taken as the zero of energy.

form a testing ground for the models of metallic phase stability." Here we will adopt the complementary view that theoretical analysis of this class of systems may motivate further thorough experimental work on these alloys by pointing out situations that may depart from commonly accepted or suggested propositions on alloy stability and chemical order.

III. ELECTRONIC STRUCTURE MODELING AND EQUILIBRIUM PROPERTY RESULTS

For the six chemically random fcc-based alloys electronic structure calculations were carried out on the basis of a charge self-consistent fully relativistic version of the tightbinding-linear muffin-tin orbital-coherent potential approximation method within the atomic sphere approximation and the local density approximation (LDA) of density functional theory.⁶ The LDA calculations were based on the exchangecorrelation energy of Ceperley and Alder³⁴ as parametrized by Perdew and Zunger.³⁵ To eliminate the charge transfer effects, at each lattice parameter and alloy composition, the atomic sphere radii of the two species were adjusted in such a way that atoms were charge neutral while preserving the total volume of the alloy. The densities of states were evaluated on a line 0.005 Ry above the real axis (with an energy step of about 5 mRy) and then deconvoluted on the real axis. The CPA equations were solved iteratively using the method described in Ref. 6.

Calculations of the density of states (DOS), using the TB LMTO CPA method, have been performed as functions

of composition for the six chemically random alloys based on the fcc lattice at their respective equilibrium lattice parameter. We show the DOS for the fcc-based pure elements in Fig. 2, and for the alloys at the three compositions A_3B , AB, and AB_3 in Fig. 3. For the pure metals, the DOSs are typical of the underlying fcc lattice, with a high DOS of *d* character close to the filled *d* band. The number of *d* electrons is about 8 for Rh and Ir, and 9 for Pd and Pt, whereas the numbers of valence electrons are 9 and 10, respectively (cf. the plot of the integrated density of states versus energy in Fig. 2). These values are located on both sides of a high peak of electron density. In addition, one can expect stronger relativistic effects for the 5*d* series (Ir and Pt) than for the 4*d* one (Rh and Pd) that tend to decrease the DOS at the Fermi energy, $n(E_F)$, as shown in Fig. 2.

Since the difference in the number of valence electrons, $\Delta N_{\rm v}$, is unity in the case of X-Pd and X-Pt (X=Rh,Ir), and zero for Rh-Ir and Pd-Pt, the scattering properties of the electrons vary very little in the alloys as functions of composition, and when compared to those of the pure elements. Indeed, as shown in Fig. 3, the DOSs are quite similar to those of the pure elements, especially in the case of Rh-Ir and Pd-Pt at equiatomic composition. For these two alloys, $N_{\rm v}$ is constant and equal to the value associated with the species constituting the alloy. The alloying effect only causes a small smearing in the sharpness of the DOSs of the alloy components. The partial DOSs also displayed in Fig. 3 are quite similar to those of the pure elements. Hence the main role of alloying is to fine-tune the location of the Fermi energy that is proportional to the average number of valence electrons, $N_{\rm v}$. The results for the DOS at the Fermi energy,



FIG. 3. Total (solid line) and partial (dotted and dashed lines) DOSs of fcc-based A_3B (left panels), AB (central panels), and AB_3 (right panels) alloys. The Fermi energy E_F is indicated by a vertical line and taken as the zero of energy.

 $n(E_{\rm F})$, reported in Fig. 4 are strongly indicative of what the variation of the electronic coefficient γ that contributes a γT term to the heat capacity should be as a function of alloy composition, since³⁶

$$\gamma = 2/3 \,\pi^2 k_{\rm B}^2 n(E_{\rm F}), \qquad (3.1)$$

where $k_{\rm B}$ is Boltzmann's constant. However, for quantitative comparison of the predicted values of the DOS at the Fermi



FIG. 4. Variation of the DOS at the Fermi energy, $n(E_{\rm F})$, as a function of alloy composition for the six fcc-based alloys Pd-Rh, Pd-Ir, Pt-Rh, Pt-Ir, Ir-Rh, and Pd-Pt.

energy to experimental results, an enhancement factor $(1 + \lambda)$ has to be included in the right-hand side of Eq. (3.1) to account for electron-phonon coupling. Note that since the *d* band of Pd is completely below the Fermi level (see Fig. 2), and $E_{\rm F}$ is located in a region of high DOS, a substantial decrease in γ can be expected when Rh, Ir, or Pt solute is added to Pd. In the case of the isoelectronic alloys Rh-Ir and Pd-Pt, a similar trend in γ is expected and reflects the transition from the 4*d* to 5*d* series that results in a moderate decrease in the DOS at the Fermi energy, as said before.

Based on TB LMTO CPA calculations the equilibrium properties have been obtained for the six chemically random alloys based on a fcc lattice, and the results are reported in Fig. 5 for the lattice parameter, and in Fig. 7 below for the bulk modulus. As usually observed, the results that correspond to the actually observed structures are within about 1% for the lattice constant and 15% for the bulk modulus. Note that for the fcc-based disordered alloys, a slight negative departure from Vegard's law is observed for all alloys in the entire range of composition, except for Pt-Rh and Pt-Ir. Usually, a positive (negative) departure from linearity is associated with a tendency toward phase decomposition (for-



FIG. 5. Variation of the lattice constant (Å) for the six fcc-based alloys as a function of composition.



FIG. 6. Variation of the departure of the lattice constant from Vegard's law, $\delta a = a_{alloy}^{eq} - \sum_{i=A,B} c_i a_i^{eq}$ [plotted as $10^3 \delta a$ (Å)] with Rh composition in the case of Pt-Rh alloys. The solid line corresponds to the theoretical results and the dotted line to the experimental data from Ref. 17.

mation). However, here, since the departure is so insignificant very little can be inferred from the results, although this departure well reproduces the experimental data¹⁷ as shown in Fig. 6 in the case of the Pt-Rh alloys. For the bulk modulus (see Fig. 7), there is a noticeable evolution with alloy composition since $B_{Pd} < B_{Pt} ~ B_{Rh} < B_{Ir}$, with Ir exhibiting the highest cohesive properties. Alloying effects beyond linear behavior with composition are here also very minor, except for Ir-Rh. For the pure metals, the theoretical values of 2.04, 2.68, 2.79, and 3.57 Mbar for the bulk modulus of Pd, Pt, Rh, and Ir, respectively, compare well with 1.93,³⁷ 2.83,³⁸ 2.67,³⁹ and 3.73,⁴⁰ obtained experimentally. It should be noted that the evolution with alloy composition of the calculated bulk modulus (cf. Fig. 7), should translate in a similar variation of the Debye temperature $\Theta_{\rm D}$ since both quantities are a good measure of the degree of cohesion in the solid state. Since the Debye temperature is related to the coefficient β that contributes a βT^3 term to heat capacity³⁶ according to



FIG. 7. Variation of the bulk modulus (Mbar) for the six fccbased alloys as a function of composition.

TABLE II. Three-term Redlich-Kister analysis of the mixing energy (mRy/atom) for each of the six fcc-based alloys.

A-B alloy	^{0}L	^{1}L	^{2}L
Ir-Rh	-17.97915	-1.02461	-0.21934
Pd-Pt	-15.64755	-0.48400	-0.09801
Pd-Rh	+16.37361	-0.63817	-0.23707
Pt-Rh	+1.90672	+1.40107	-0.97414
Ir-Pd	-2.03042	-0.82296	-1.66072
Ir-Pt	+18.63975	+0.74137	+0.37826

$$\Theta_{\rm D} = (1.944/\beta)^{1/2} \tag{3.2}$$

the predictions presented here on the γ and β coefficients of the specific heat should be fairly well confirmed experimentally.

IV. STABILITY AND ORDERING TRENDS

Ordering trends have been predicted^{3,4} with the GPM in the context of the TB LMTO CPA electronic structure description of chemically disordered alloys. Within the GPM the ordering part of the total energy for a binary alloy $A_{1-c}B_c$ is given, at zero temperature and to second order in perturbation, by³⁻⁵

$$\Delta E_{\rm ord}(\{q_s\}) \simeq \sum_s q_s V_s(c) \tag{4.1}$$

with $q_s = c/2(n_s^{BB} - cn_s)$, where n_s^{BB} and n_s refer to the number of *BB* pairs and the total number of pairs per site, respectively, associated with the *s*th-neighbor shell, and *c* is the concentration of the *B* species. In this last equation, V_s represents an *s*th-neighbor effective pair interaction (EPI) given by $V_s = V_s^{AA} + V_s^{BB} - 2V_s^{AB}$. Therefore, the sign convention is such that when $V_s > 0$ (<0), *AB* (*AA* or *BB*) pairs associated with one species at the origin and the other in the *s*th-neighbor shell are favored. Within this formalism, the formation (or mixing) energy of the chemically random alloy is given by

$$\Delta E_{\text{mix}}(\{c_i\}) = E_{\text{alloy}}^{\text{CPA}} - \sum_i c_i E_i^{\text{eq}}$$
(4.2)

where c_i is the concentration of species *i*, and $E_{\text{alloy}}^{\text{CPA}}$ and E_i^{eq} are the energies of the chemically random alloy and of the pure element *i*, respectively, at their corresponding equilibrium lattice parameters.

For practical purposes, this energy can be conveniently expressed by a so-called Redlich-Kister polynomial⁴¹ as follows:

$$\Delta E_{\min}(\{c_i\}) = c_i c_j \sum_p {}^p L_{ij} (c_i - c_j)^p$$
(4.3)

where by definition the two species *i* and *j* that form the alloy are in alphabetical order. For the six alloys studied the values of the three interaction parameters ${}^{p}L; p=[0,2]$ that enter Eq. (4.3) are reported in Table II.

The energy associated with a chemical configuration C, defined by the set $\{q_s^{C}\}$ at 0 K, is given by

$$\Delta E^{\mathcal{C}}(\{q_s\}) = \Delta E_{\text{mix}}(\{c_i\}) + \Delta E_{\text{ord}}(\{q_s\}). \tag{4.4}$$

Note that in the same way that an ordering energy has been defined in the case of order, one can define a clustering (segregation) energy ΔE_{seg} , with the same expression as the one given by Eq. (4.1) but with $n_s^{BB} = n_s$. However, the formation energy of the alloy will be approximately given by

$$\Delta E_{\rm form} \sim -\Delta E_{\rm seg}.\tag{4.5}$$

The clustering energy is estimated from the concentrationweighted average of the DOSs of the pure metals, each calculated at the average Fermi level of the average CPA medium, in the spirit of the GPM. On the other hand, $\Delta E_{\rm form}$ is obtained from the contribution of the two subbands that are associated with each species and its own Fermi level. As long as the interfacial energies are negligible (which would be the case for alloy species exhibiting similar electron scattering properties, an assumption that is applicable to the present alloys), we expect the total energies that correspond to both situations (i.e., segregation within an alloy sample and juxtaposition of two metals) to be the same.

The variation of the first two EPIs V_1 and V_2 with alloy composition is shown in Fig. 8. The more distant EPIs are an order of magnitude lower than the first two, and therefore contribute little to the ordering energy (see below). These results can also be displayed as trajectories in a ground-state map spanned by the first- and second-nearest^{9,4} EPIs that are shaped by composition effect. From Fig. 9 and Table III, the clustering trends that are experimentally observed for Rh-Pd, Ir-Pd, and Ir-Pt are confirmed since in all three cases V_1 <0 and $V_2/V_1 < -1$. However, for the other three alloys, the situation is quite different. All three systems Rh-Pt, Rh-Ir, and Pd-Pt exhibit ordering tendencies, contrary to suggestions made in the past (see Sec. II). More specifically, for the Rh-Pt system, the (100) family of ordered states that consists of L1₂ for Rh₃Pt and RhPt₃ and L1₀ for RhPt is predicted. On the other hand Rh-Ir and Pd-Pt should display ordered states of the $(1 \ 1/2 \ 0)$ family, i.e., $D0_{22}$ at the A_3B and AB_3 compositions, $C11_h$ order (of Pt₂Mo type) at the compositions A_2B and AB_2 , phase 40 at equiatomic composition,^{9,4} and finally A_5B type of order.⁹ It is interesting to note that in the case of Rh-Pt, the mixing energy is slightly positive whereas in the case of Ir-Pd the mixing energy is slightly negative, although the former has a clear tendency to order whereas the latter displays a definite tendency toward phase separation.

By including in the ground-state analysis EPIs up to the fourth-neighbor distance, the results are unchanged except for Pd-Pt, which should exhibit order of the $(1\ 0\ 0)$ family, as indicated in Table IV. Note also that in the case of Rh-Pt below 50 at. % Rh the ordering trends switch from the $(1\ 1/2\ 0)$ to the $(1\ 0\ 0)$ family of ordered states.

The expected ground states together with the values of the EPIs and the use of Eq. (4.1) allow us to predict the magnitude of the ordering energies, which controls the shape of the phase diagram at finite temperature. The combined variation of the mixing energy [see Eqs. (4.2) and (4.3)], and of the



FIG. 8. Variation of the first- and second-nearest-neighbor effective pair interactions (mRy/atom) for the six fcc-based alloys with composition.

ordering energy [Eq. (4.1)], with alloy composition provides the phase diagram of each alloy at T=0 K, as shown in Fig. 10. From this study it can be concluded that, as observed experimentally, the three alloys Rh-Pd, Ir-Pd, and Ir-Pt should definitely phase separate, in accordance with experimental facts. On the other hand, Rh-Ir and Pd-Pt should exhibit all the ordered states that belong to the (1 1/2 0) and (1 0 0) families of order, respectively. Finally, in the case of Rh-Pt, despite a slightly positive mixing energy, this system should exhibit a $D0_{22}$ ordered state and the so-called⁹ phase 40 at the compositions Rh₃Pt and RhPt, respectively.

Our predictions are in qualitative agreement with those obtained for all six systems based on the calculation of the total energy for some alloy configurations carried out with an "exact" muffin-tin orbital method within the LDA or the generalized gradient approximation (GGA) of density functional theory.⁴² For the sake of quantitative comparison, we also report in Table IV the formation energies of Ref. 43 for Pd-Pt, Rh-Pd, and Rh-Pt alloys. These results were obtained from the application of the semirelativistic linearized aug-



FIG. 9. Variation of the effective pair interactions with alloy composition in a ground-state map representation (first versus second effective pair interaction) for the six fcc-based alloys. For each trajectory, the filled square corresponds to the null composition of the underlined element.

mented plane-wave method.⁴⁴ Considering that our approach is solely based on the knowledge of the properties of the random state of an alloy, our results compare favorably in a quantitative sense with those of Ref. 43. Our predictions obtained for Pd-Pt and Pt-Rh are also in qualitative agreement with those based on recent ultrasoft pseudopotential LDA and projector-augmented wave GGA calculations.⁴⁵ For both alloys, the latter results also predict the existence of ordered structures not yet seen experimentally. In the case of Pd-Pt alloys, Pd₃Pt and PdPt₃ prototype ordered structures, and an $L1_1$ PdPt, close in energy to $L1_0$, have been found with small heats of formation not exceeding -3 mRy/atom. In the case of Pt-Rh alloys, $D1_a$ Pt₄Rh and PtRh₄, $D0_{22}$ Pt₃Rh and PtRh₃, C49 PtRh₂, and ordered PtRh were predicted with a minimum heat of formation of about -1.8 mRy/atom found for PtRh.

Despite these predictions on chemical order in Rh-Ir, Pd-Pt, and Pt-Rh, it may be difficult to characterize longrange order, and even to identify SRO with x-ray or neutron diffuse scattering experiments. Indeed, the ordering trends that have been predicted in this work are rather weak, and the ordering energies themselves are less than 2 mRy/atom (see Table IV). In addition, since all the order-disorder transitions that would be involved are first order, the SRO is expected to decrease rapidly with increasing temperature above the lowlying critical order-disorder transition. Altogether, it means that thermal annealing of samples at temperatures where SRO should still exist may not be possible, or takes a very long time due to slow diffusion kinetics. A recent diffuse x-ray and small-angle neutron scattering analysis performed on a Pt-47 at.% Rh sample revealed very weak maxima of diffuse intensity in the $(1 \ 1/2 \ 0)$ positions in reciprocal space that are associated with the existence of a phase $40.^{18}$ The extraction of the EPIs by an inverse Monte Carlo method led to an estimate of the critical order-disorder temperature of about 185 K, a lower bound according to the authors of this work since the relaxation-time effect may cause the actual magnitude of the EPIs to slightly increase. It is worth noting that the first two EPIs of 2.35 and -0.41 mRy/atom obtained experimentally with the Borie-Sparks separation technique¹⁸ compare favorably with our theoretical values of 3.73 and -0.28 mRy/atom for a Pt₅₀Rh₅₀ alloy, cf. Fig. 11. This figure also confirms the rapid convergence of the EPIs with distance beyond the second nearest neighbor distance, as is the case for the other alloys at any composition.

To examine temperature effects on ordering trends and tie them to phase diagrams, critical order-disorder temperatures were estimated with the generalized mean-field CVM within

TABLE III. Ground-state analysis up to the second-nearest-neighbor EPI for the six fcc-based alloys. For each ordered state the ordering and formation energies (in parentheses) are given in mRy/atom. The ordering energy associated with phase separation (PS; see text) is also indicated for all alloys at equiatomic composition.

A-B	Rh-Ir	Pd-Pt	Rh-Pd	Rh-Pt	Ir-Pd	Ir-Pt
A - B	-0.37 (-2.78)	-0.51 (-2.74)	0.82 (2.98)	-0.74 (-0.40)	1.29 (0.86)	0.71 (3.37)
$L1_2(A_3B)$	-0.52 (-3.82)	-0.81 (-3.79)	1.42 (4.55)	-1.73 (-1.54)	3.08 (2.55)	1.46 (5.02)
$D0_{22} (A_3 B)$	-0.62 (-3.92)	-0.90 (-3.88)	1.54 (4.66)	-1.68 (-1.49)	3.02 (2.49)	1.52 (5.08)
$C11_b (A_2B)$	-0.68 (-4.57)	-0.88 (-4.37)	1.52 (5.17)	-1.37 (-1.07)	2.62 (+2.05)	1.46 (+5.64)
$L1_0 (AB)$	-0.80 (-5.28)	-1.01 (-4.92)	2.01 (6.11)	-2.08 (-1.61)	4.17 (3.66)	2.06 (6.73)
$40 (A_2B_2)$	-0.97 (-5.46)	-1.19 (-5.10)	2.22 (6.31)	-1.94 (-1.47)	4.02 (3.51)	2.17 (6.83)
$L1_1(AB)$	-0.27 (-4.75)	-0.26 (-4.17)	0.31 (4.40)	0.21 (0.68)	-0.22 (-0.73)	0.16 (4.82)
PS(AB)	3.45	4.08	-7.28	5.39	-11.62	-6.83
$C11_b (AB_2)$	-0.73 (-4.80)	-0.83 (-4.26)	1.58 (5.15)	-1.15 (-0.66)	2.62 (2.21)	1.48 (5.56)
$L1_2 (AB_3)$	-0.68 (-4.15)	-0.74 (-3.63)	1.61 (4.61)	-1.44 (-0.98)	2.96 (2.58)	1.54 (4.98)
$D0_{22} (AB_3)$	-0.75 (-4.22)	-0.82 (-3.71)	1.69 (4.69)	-1.36 (-0.91)	2.93 (2.55)	1.59 (5.04)
AB_5	-0.396 (-3.00)	-0.44 (-2.57)	0.75 (2.65)	-0.52 (-0.61)	1.14 (0.85)	0.74 (3.23)

TABLE IV. Ground-state analysis up to the fourth-nearest-neighbor EPI for the six fcc-based alloys. For each ordered state the ordering and formation energies (in parentheses) are given in mRy/atom. The ordering energy associated with phase separation (PS; see text) is also indicated for all alloys at equiatomic composition. For comparison purposes, a second line indicates the formation energy from Ref. 43 whenever available.

A-B	Rh-Ir	Pd-Pt	Rh-Pd	Rh-Pt	Ir-Pd	Ir-Pt
A_5B	-0.46 (-2.88)	-0.59 (-2.82)	0.53 (2.69)	-0.74 (-0.41)	0.75 (0.32)	0.49 (3.15)
$L1_2(A_3B)$	-0.32 (-3.62)	-1.33 (-4.32)	2.48 (5.61)	-1.55 (-1.36)	4.45 (3.92)	2.86 (6.42)
		(-2.23)	(6.25)	(-1.50)		
$D0_{22} (A_3 B)$	-0.70 (-3.99)	-1.02 (-4.00)	1.40 (4.53)	-1.67 (-1.48)	2.62 (2.08)	1.45 (5.00)
		(-1.62)	(4.69)	(-1.85)		
$C11_b (A_2B)$	-0.86 (-4.75)	-0.78 (-4.28)	0.89 (4.54)	-1.45 (-1.15)	1.50 (0.93)	0.75 (4.93)
		(-2.07)	(4.72)	(-0.74)		
$L1_0 (AB)$	-0.56 (-5.05)	-1.80 (-5.71)	3.00 (7.09)	-1.94 (-1.47)	5.56 (5.05)	3.50 (8.16)
		(-2.90)	(6.06)	(-1.21)		
$40 (A_2B_2)$	-1.23 (-5.72)	-0.97 (-4.88)	1.35 (5.45)	-2.04 (-1.58)	2.37 (1.87)	1.17 (5.83)
		(-2.36)	(5.20)	(-1.21)		
$L1_1(AB)$	-0.31 (-4.80)	-1.11 (-5.03)	0.49 (4.58)	0.26 (0.73)	-0.60 (-1.11)	0.81 (5.47)
		(-2.14)	(5.81)	(-0.29)		
PS(AB)	2.58	3.01	-9.53	5.15	-17.32	-8.56
$C11_b (AB_2)$	-0.89 (-4.96)	-0.83 (-4.26)	1.03 (4.60)	-1.15 (-0.66)	1.51 (1.11)	0.84 (4.92)
		(-2.23)	(5.33)	(-0.32)		
$L1_2 (AB_3)$	-0.53 (-4.01)	-1.36 (-4.25)	2.18 (5.17)	-1.43 (-0.98)	3.91 (3.53)	2.40 (5.85)
		(-2.58)	(4.91)	(-0.79)		
$D0_{22} (AB_3)$	-0.82 (-4.29)	-0.88 (-3.77)	1.61 (4.60)	-1.39 (-0.94)	2.41 (2.03)	1.41 (4.85)
		(-2.14)	(5.07)	(-0.96)		
AB_5	-0.48 (-3.08)	-0.42 (-2.55)	0.52 (2.42)	-0.52 (-0.61)	0.51 (0.22)	0.46 (2.95)

the tetrahedron-octahedron approximation.^{4,8} This allowed us to properly describe the ordering contribution to the Gibbs energy up to the second-nearest EPI as well as the configurational entropy as functions of temperature. The more distant interactions, third and fourth EPIs, were also accounted for in the ordering energy with a Bragg-Williams treatment. For the three alloys Rh-Ir, Pt-Rh, and Pd-Pt at equiatomic composition, the critical order-disorder temperatures are 246 K ($40 \rightarrow$ disordered), 325 K ($40 \rightarrow$ disordered), and 422 K ($L1_0 \rightarrow$ disordered), respectively. These low values just reflect the weak ordering tendencies found for this class of alloys.

Finally, let us review the points that could help us rationalize the stability and ordering trends that we found for these six substitutional alloys in the context of electronic structure properties. On one hand, for the two isoelectronic systems Rh-Ir and Pd-Pt that involve elements from the 4*d* and 5*d* series, a definite and similar tendency toward order is predicted. It is interesting to note that a standard *d*-band tight-binding analysis (with only the diagonal-disorder effect included) of ordering for these two alloys would predict a clustering tendency since the average numbers of valence *d* electrons are 8 and 9 electrons, respectively.⁴ The trend from *ab initio* calculations can be attributed to *s*-*d* hybridization, and to relavistic effects that cannot be ignored for elements of the 5*d* series. On the other hand, for the two alloys that exhibit a ΔN_v of unity with elements belonging to the same series (4d or 5d), i.e., for Rh-Pd and Ir-Pt, a tendency toward phase separation is predicted, in accordance with the d-band TB analysis since, in this case, the *s*-*d* hybridization and the relativistic effect cancel out, in accordance with the assumption made in a standard TB analysis. For these first two classes of systems, the alloys are located in a similar region of Fig. 9. Finally, for the last two alloys that mix elements belonging to the 4d and 5d series with a $\Delta N_{\rm v}$ of unity, i.e., Rh-Pt and Pd-Ir, a mixed situation is encountered. Indeed, whereas the sign of the mixing energy indicates favorable (unfavorable) phase formation for Ir-Pd (Rh-Pt), the ordering trends indicate the opposite, i.e., phase separation for Ir-Pd and order for Rh-Pt. This ambiguity can be lifted if one notes that the difference in d-band widths ΔW_d of the pure elements is about 0.015 Ry for Rh-Pt whereas it is 0.250 Ry for Ir-Pd (for the other four alloys this difference is 0.140, 0.125, 0.110, and 0.125 Ry for Rh-Ir, Pd-Pt, Rh-Pd, and Ir-Pt, respectively).⁴⁶ Since ΔW_d is a measure of the off-diagonal disorder in the TB language, a large value of this quantity favors clustering. This would explain why Ir-Pd displays a tendency toward phase separation whereas Rh-Pt shows a tendency toward order. Hence, for all six alloy systems studied, the combined effects of *s*-*d* hybridization, relativity, and off-diagonal disorder lead to the definition of three classes of alloys. It should be noted that here $N_{\rm y}$ has little effect on the chemical trends, and only a small impact on the magnitude of the mixing energy. The same can be said of $\Delta N_{\rm v}$ which is



FIG. 10. Formation energy of the disordered state as a function of alloy composition (dotted line) for the six fcc-based alloys. Configuration energies of the most likely ground states (full circles), including the values minus the energies of the segregated state (solid curve, when applicable) have also been reported.

a measure of the difference in the scattering properties of the electrons that control the strength of stability. Here $\Delta N_v \leq 1$, and therefore this leads overall to weak magnitudes for the mixing energies and the ordering (or segregation) energies for the six alloy systems.

It is worth mentioning that, based on these trends, and the arguments put forward to explain them, the ordering tendency predicted and observed in the Ni-Pt system should not come as a surprise. Indeed, the Pt-Pd system belongs to the (1 0 0) family of order, and the same is true for Ni-Pt. Despite the theoretical controversy that arose about this system,⁴⁷ the diagonal disorder parameter ΔW_d =0.243 Ry, relativistic effects that particularly apply to Pt and its alloys,

and *s*-*d* hybridization are all responsible for the chemical order observed in this isoelectronic alloy.

V. CONCLUSIONS

An *ab initio* alloy theory has been applied to the study of the relation between constitution (phase) diagrams, electronic structure, and stability and ordering properties for the binary systems made of the four fcc-based transition metals Rh, Ir, Pd, and Pt. For three of the six binary alloys, namely, Rh-Pd, Ir-Pd, and Ir-Pt, the phase-separation trend that was observed experimentally is fully confirmed by our calcula-



FIG. 11. Variation of the effective pair interaction (mRy/atom) with distance (in units of the equilibrium fcc lattice parameter a) for a Pt₅₀Rh₅₀ alloy.

tions. On the other hand, for the other three binary alloys Rh-Pt, Rh-Ir, and Pd-Pt, ordering trends are predicted, in contradiction with suggested and accepted phase-separation tendencies. For Pd-Pt, Rh-Ir, and Rh-Pt, the $(1\ 0\ 0)$ and $(1\ 1/2\ 0)$ family types of order and a mixture of both, respectively, are predicted. The impact of relativistic effects

and *s*-*d* hybridization explains to some extent the ordering trends that are predicted for these three alloys, a finding that could not be anticipated on the basis of semiphenomenological tight-binding calculations that rely only on *d*-band analysis. The predictions made about the variation with alloy composition of the electron and phonon contributions to the specific heat, if confirmed experimentally, should validate the electronic structure description of these alloys. Finally, detailed analysis of short-range order from diffuse scattering measurements should validate the ordering trends discussed here. If confirmed, these predictions should impact the way these alloys and the higher-order component alloys that contain them are considered in a thermodynamic analysis, even at high temperature, since short-range order has important consequences on physical properties.

ACKNOWLEDGMENTS

The work of P.T. has been performed under the auspices of the U.S. Department of Energy by the University of California Lawrence Livermore National Laboratory under Contract No. W-7405-ENG-48. The work of V.D. and J.K. was carried out within the Project No. AV0Z1-010-914 of the Academy of Sciences of the Czech Republic, and supported by the Grant Agency of the Academy of Sciences of the Czech Republic under Project No. AV0Z10100520.

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