Two- and three-dimensional incommensurate modulation in optimally-doped $Bi_2Sr_2CaCu_2O_{8+\delta}$

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X-ray scattering measurements on optimally doped single crystal samples of the high-temperature superconductor Bi₂Sr₂CaCu₂O_{8+ δ} reveal the presence of three distinct incommensurate charge modulations, each involving a roughly fivefold increase in the unit cell dimension along the **b** direction. The strongest scattering comes from the well known (*H*, *K*±0.21, *L*) modulation and its harmonics. However, we also observe broad diffraction which peak up at the *L* values complementary to those which characterize the known modulated structure. These diffraction features correspond to correlation lengths of roughly a unit cell dimension, $\xi_c \sim 20$ Å in the **c** direction, and of $\xi_b \sim 185$ Å parallel to the incommensurate wave vector. We interpret these features as arising from three-dimensional incommensurate domains and the interfaces between them, respectively. In addition we investigate the recently discovered incommensurate modulations which peak up at (1/2, *K*±0.21, *L*) and related wave vectors. Here we explicitly study the *L* dependence of this scattering and see that these charge modulations are two dimensional in nature with weak correlations on the scale of a bilayer thickness, and that they correspond to short-range, isotropic correlation lengths within the basal plane. We relate these new incommensurate modulations to the electronic nanostructure observed in Bi₂Sr₂CaCu₂O_{8+ δ} using STM topography.

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I. INTRODUCTION

High-temperature superconductivity is observed and has been extensively studied across several families of layered copper oxides.¹ While the structure of families of these materials differs in detail, they are all comprised of stackings of CuO₂ rectangular layers, with so-called charge reservior layers in between. The CuO₂ layers can occur in isolation, or appear in bilayer or trilayer assemblies. One of the most extensively studied of these materials is Bi₂Sr₂CaCu₂O_{8+ δ}, which is known to display an optimal superconducting T_C of ~93 K.¹ As shown in Fig. 1, it is a bilayer superconductor with orthorhombic symmetry and lattice parameters of *a* ~*b*~5.4 Å, and *c*=30.8 Å.² As such two CuO₂ bilayers appear within the unit cell separated by ~15.4 Å along **c**.

 $Bi_2Sr_2CaCu_2O_{8+\delta}$ has been the high-temperature superconducting sample of choice for studies using surfacesensitive techniques such as photoemission³ and scanning tunneling microscopy (STM).⁴ This is due to the relative ease of producing clean, cleaved surfaces of $Bi_2Sr_2CaCu_2O_{8+\delta}$ at low temperature, a consequence of its extreme quasi-two-dimensionality, even compared with other families of layered high-temperature superconductors, such as YBa₂Cu₃O_{7- δ} and La_{2-x}Sr_xCuO₄. These techniques and the information they provide on electronic structure have been very important to the general field of high-temperature superconductivity, and $Bi_2Sr_2CaCu_2O_{8+\delta}$ has been crucial to these studies. Unfortunately, the two-dimensional nature of the material has also resulted in relatively thin single crystals being grown (with thicknesses in the **c** direction of as much as, but typically smaller than, a few millimeters). This has precluded, or made very difficult, the study of the $Bi_2Sr_2CaCu_2O_{8+\delta}$ family by experimental techniques which require a large volume of material, such as single crystal neutron scattering.⁵

The structural detail for which $Bi_2Sr_2CaCu_2O_{8+\delta}$ is perhaps best appreciated is the incommensurate modulation it possesses within its basal plane. This incommensurate modulation has been observed by different techniques including, x-ray,⁶ neutron,⁷ and electron diffraction;⁸ scanning tunneling microscopy;⁹ and electron microscopy.¹⁰ This complex crystal structure has been described in terms of two interpenetrating periodic crystals, each of which modulate the other,¹¹ with supporting experimental evidence from neutron scattering.¹²

The modulation is one dimensional, running along the **b** direction in the basal plane, and it is the modulation (as opposed to a difference between *a* and *b* lattice parameters) that is responsible for the lower-than-tetragonal symmetry of the structure. The incommensurate modulation is characterized by multiple harmonics, and the first order harmonic corresponds to a periodicity of roughly five unit cells along **b**. Interestingly, it appears that Bi₂Sr₂CaCu₂O_{8+ δ} crystals typically grow untwinned, likely a consequence of strains which would develop between orthogonal modulations. This is in contrast to other families of high-temperature superconductors which can be produced in an untwinned state, but only with considerable effort in preparation.

II. MATERIALS AND EXPERIMENTAL METHODS

The $Bi_2Sr_2CaCu_2O_{8+\delta}$ single crystal samples were grown by the traveling solvent floating zone techniques using a



FIG. 1. (Color online) A schematic diagram depicting one and a half unit cells of Bi₂Sr₂CaCu₂O_{8+ δ} is shown. The light (orange) pyramids represent CuO₂ plus apical oxygen complexes, while the dark (blue) octahedra represent BiO₂ plus apical oxygen atom complexes. The Cu ions reside at the center of the base of the light pyramids, while the Bi ions reside at the center of the octahedra. The CuO₂ and BiO₂ bilayer thicknesses are indicated as 3.3 and 3.2 Å, respectively, while the bilayer-bilayer separation of $c/2 \sim 15.4$ is also shown.

Crystal Systems, Inc., image furnace. The growth was performed from premelted polycrystalline rods in 2 atmospheres of flowing O₂. The rods were counter-rotated at 30 rpm and the growth speed was 0.2 mm/h. The resulting single crystals were carefully extracted from a large boule, and had approximate dimensions of 10 mm × 5 mm × 0.1 mm, where the thin dimension was parallel to the **c** axis. Although thin, the single crystals were of excellent quality with mosaic spreads less than 0.07°, and a superconducting transition temperature, determined by superconducting quantum interference device (SQUID) magnetomery, of $T_C \sim 92$ K with a width of ~2 K.

Two sets of x-ray scattering measurements were performed on these samples. Measurements were made using a Cu-rotating anode source and a triple axis spectrometer at McMaster University. These measurements employed Cu- $K\alpha$ radiation and utilized a pyrolitic graphite monochromator. The sample was mounted in a closed cycle refrigerator and placed in a four-circle goniometer. Four sets of slits were employed to define the incident and scattered beams.

A high-resolution diffraction setup at the Advanced Photon Source synchrotron radiation facility was used to study a subset of the modulations with greater precision. These measurements were performed on the 4-ID-D beamline at an x-ray energy of 16 keV. This beamline is equipped with a double-crystal Si(111) monochromator. A Pd-coated bent mirror was used to focus the beam to a spot size of 180 $\times 220 \ \mu m$ at the sample. A flat Pd mirror was used to further



FIG. 2. Synchrotron x-ray scattering scans on a logarithmic intensity scale along [0, K, 0] (top panel) and [0, K, 1] (lower panel) in Bi₂Sr₂CaCu₂O_{8+ δ}. A total of four harmonics of the modulated structure with the form $(0, 4-n \times \tau, L)$ are observed at both L=0 and L=1, and they clearly alternate between resolution-limited and broad along both *K* and *L* (see Fig. 3). The broad component to the scattering is well described by a Lorentzian-squared line shape (see Fig. 4).

suppress higher order harmonics. The thin single crystal sample was placed in a closed cycle refrigerator. A Ge(111) analyzer was used to reduce background and to improve resolution.

III. EXPERIMENTAL RESULTS

A. Three-dimensional modulated structure

Synchrotron x-ray scattering scans of the form (0, K, 0)and (0, K, 1) are shown in Fig. 2. These data are plotted on a logarithmic intensity scale, and were taken at T=10 K, although no significant temperature dependence was observed to this scattering to temperatures as high as 300 K. A clear pattern of diffraction peaks is observable at incommensurate wave vectors of the form $(0, 4-n \times \tau, L)$ for $\tau=0.21$, corresponding to a roughly five unit cell modulation, and at all harmonics (n=1,2,3,4) which we studied. Two distinct line shapes are clearly present. One is very sharp, resolution limited, and these peaks alternate in harmonic for a particular L. This is to say that the even harmonic, n=2 (K=3.58), is clearly sharp in K for L=0, while it is the odd harmonics, n=1 (K=3.79) and n=3 (3.37), which are sharp for L=1.

Figure 3 shows x-ray scattering data, plotted on a logarithmic intensity axis, taken with the rotating anode source. These data examine the systematic *L* dependence of the scattering shown in Fig. 2. Once again these data are taken at 10 K and scans of the form (0, 4, L), (0, 3.79, L), and (0, 3.58, L) are shown in the top, middle and bottom panels of Fig. 3, respectively. Consistent with the data shown in Fig. 2, two sets of incommensurate diffraction peaks are seen, in



FIG. 3. Rotating anode x-ray scattering measurements on a logarithmic intensity scale show the *L* dependence of the principal Bragg peaks, such as [0,4,L] (top panel); the first order harmonic of the modulated structure [0, 3.79, L] (middle panel); and the second order harmonic of the primary modulated structure [0, 3.58, L] (bottom panel). The harmonics alternate with *L* between resolution-limited Bragg scattering and broad scattering which is well described by a Lorentzian-squared line shape (see Fig. 4).

the bottom two panels, which alternate with L, between a sharp, resolution-limited line shape, and a broad diffraction feature.

Clearly, at alternate harmonics one observes a much broader line shape. This is considered quantitatively in Fig. 4, where broad diffraction features at (0, 3.58, 1) and (0, 3.58, 5) are plotted as a function of *K* and *L* on a linear intensity scale. These data were fit to a Lorentzian-squared form along both \mathbf{b}^* and \mathbf{c}^* :

$$S(\mathbf{Q}) = \frac{A}{\left[1 + \frac{(\mathbf{Q} - \mathbf{Q}_0)^2}{\kappa^2}\right]^2}$$
(1)

yielding correlation lengths of $\xi_b = \frac{1}{\kappa_b} \sim 185$ Å and $\xi_c = 20$ Å.

Together these data illustrate two coexisting incommensurate structures one of which displays resolution-limited longrange order in three dimensions, while the other displays three-dimensional, albeit highly anisotropic, short-range order. We interpret the anisotropic, short-range order diffraction peaks as arising from stacking faults in the incommensurate modulation.



FIG. 4. X-ray scattering scans along K (top) and L (bottom) taken from Figs. 2 and 3 and plotted on a linear intensity scale. Both plots show the second order harmonics of the primary modulation [0, 3.58, 1] and [0, 3.58, 5]. These positions correspond to wave vectors with broad (as opposed to resolution-limited) line shapes. Also shown is the fit to each line shape using a Lorentzian-squared form, Eq. (1), which is clearly excellent. As described in the text, this line shape is typically used to describe the three-dimensional random field domain state in disordered magnets.

For simplicity, we discuss this three-dimensional scattering as if a single harmonic characterized the incommensurate structure. Domains of well ordered modulated regions give rise to the resolution-limited peaks at say (0, 3.79, L) with L= odd. The L= odd requirement implies a phase shift of π , $3 \times \pi$, $5 \times \pi$, between either CuO₂ bilayers (or equivalently BiO₂ bilayers) which are separated from each other by half a unit cell along **c** (see Fig. 1). That is, the modulated structure within a particular bilayer is π out of phase with that immediately above and below it.

In contrast, the L dependence of the broad diffraction peaks, such as (0, 3.79, L) with L=even, implies that this incommensurate modulation is in phase with that in the bilayer immediately above and below it. Also, as the correlation length along c is roughly a unit cell dimension, we have a very natural interpretation that these diffraction features arise from the interface between two bulk domains, but which are out of phase with respect to each other. While the domain interfaces, attributed to the broad diffraction peaks, are anisotropic with $\xi_c \sim 20$ Å and $\xi_a \sim 185$ Å, we classify all of the $(0, 4 \pm n \times \tau, L)$ superlattice diffraction peaks as being three dimensional in nature, as all of the superlattice peaks are localized around a particular point in reciprocal space, as opposed to being organized into rods or sheets of scattering, as is known to be relevant to two- and onedimensional structures, respectively.

B. Two-dimensional modulated structure

X-ray scattering measurements using the rotating anode source were also extended to look for additional charge



FIG. 5. X-ray scattering scans of the form [H, 3.58, 5] which show the new modulated structure corresponding to a doubling of the unit cell along **a** is shown. The dashed line in the upper panel shows where the scans reside in reciprocal space, passing through the second order harmonic of the primary modulation. The middle and lower panels show these scans on logarithmic (middle) and linear (bottom) intensity scales, with Lorentzian line shapes [Eq. (2)] fit to the data. The bottom panel also demonstrates the lack of temperature dependence to this scattering below room temperature.

modulation. Additional modulation, distinct from that at $(0, 4-n \times \tau, L)$ and discussed above, involving a doubling of the periodicity along a have recently been reported in $Bi_2Sr_2CaCu_2O_{8+\delta}$ by Megtert and co-workers,¹³ and also by ourselves.¹⁴ Scans performed along H, going through the second order harmonic of the three-dimensional modulation, $(0, 4-2 \times 0.21, 5)$, are shown in the bottom two panels of Fig. 5. The (0, 3.58, 5) second order harmonic of the threedimensional modulation is easily observable at the ~ 10 counts/s level. However, we also observe peaks at $(\pm 1/2, 3.58, 5)$ at the 0.4 counts/s level on а ~ 0.2 counts/s background. While weak, this H=1/2 modulation is clearly resolved in the middle panel of Fig. 5. The bottom panel of Fig. 5 shows three data sets at T=10, 100,and 250 K, at the (-1/2, 3.58, 5) wave vector and demonstrates that, similar to the H=0 modulations discussed above, the new H=1/2 modulations have little or no temperature dependence to temperatures as high as room temperature. The peaks shown in Fig. 5 were fit to a resolution-convoluted Lorentzian form

$$S(\mathbf{Q}) = \frac{A}{\left[1 + \frac{(\mathbf{Q} - \mathbf{Q}_0)^2}{\kappa^2}\right]}$$
(2)

and the (±1/2, 3.58, 5) peaks were found to be characterized by a correlation length of $\xi_a \sim 27$ Å along **a**.



FIG. 6. X-ray scattering scans of the form [1/2, K, 5] which display the new modulated structure corresponding to a doubling of the unit cell along **a** is shown. The upper panel shows where the scans reside in reciprocal space, passing through the first four harmonics of this new modulated structure. The data in the bottom panel is fit to Lorentzian line shapes [Eq. (2)] centered at each of the four harmonic positions along **K**. Also shown for comparison in the same panel are **K** scans of the first and second harmonics of the instrumental resolution.

Figure 6 shows x-ray scattering scans of the form (1/2, K, 5) passing between K=3 and 4, and showing $(1/2, 4-n \times \tau, 5)$ for $\tau=0.21$ and n=1,2,3, and 4. The top panel of Fig. 6 locates these scans in reciprocal space as the dashed lines. Also shown in the bottom panel of Fig. 6, are scans of the form (0, K, 0) and (0, K, 1) taken under precisely the same experimental conditions as the (1/2, K, 5)scan. This data shows K scans through (0, 3.58, 0) and (0, 3.58, 0)3.79, 1) which are both resolution-limited Bragg peaks (see Fig. 2). We therefore conclude that the peaks shown in the (1/2, K, 5) scans of Fig. 6 are not resolution limited. We can provide an excellent fit to this data, shown as the solid line in Fig. 6, with a resolution-convoluted Lorentzian line shape, Eq. (2). We then extract a relatively short correlation length along **b** for this H=1/2 modulation of $\xi_b \sim 27$ Å, very similar to the correlation length ξ_a , extracted from the (H, 3.58, 5) scans of Fig. 5.

Figure 7 shows *L* scans of the form $(1/2, 4-n \times \tau, L)$ for n=2 in the top panel, that is (1/2, 3.58, L), and for n = 1, 2, 3, and 4 in the bottom panel. Also shown in the top panel is a background scan taken at (0.3, 3.45, L). Remarkably these scans, from L=-10 to 10, show almost no *L* dependence at all; that is rods of scattering characteristic of two-dimensional structures. The scattering is weakly peaked at $L \sim \pm 5$, but extends over all *L* values measured. These scans were also carried out as a function of temperature, and again, as seen in the top panel of Fig. 7, one sees little or no temperature. These results on the new $(1/2, 4-n \times \tau, L)$ modulations extend those reported earlier^{13,14} by explicitly determining *L* dependencies. We also see that our results give approximately isotropic correlation lengths within the



FIG. 7. X-ray scattering scans of the form [1/2, K, L] which observe the new modulated structure corresponding to a doubling of the unit cell along **a** are shown. The top panel shows *L* scans of the second order (*K*=3.58) harmonic of this scattering, at different temperatures below 250 K, as well as a background scan of the form [0.3, 3.45, L]. The lower panel shows the *L* dependence of each of the first four harmonics of this structure at 10 K. Remarkably over the 10 Brillouin zones from *L*=10 to *L*=-10, a near complete rod of scattering is observed for the first order harmonic (*K*=3.79), while higher order harmonics peak up weakly at *L*=±5.

a-**b** plane a factor of two smaller than those reported by Megtert and collaborators.¹³ However, the Megtert *et al.* work does not discuss the form to which the scattering was fit to extract their correlation length, and hence a quantitative comparison is not possible at present.

The extreme extended nature of this scattering in *L* helps us understand why the scattering is so weak at any one position, and therefore why it is difficult to observe, and has escaped observation until recently. As the scattering is broad in both *H* and *K* (with correlation lengths $\xi_{ab} \sim 27$ Å and rodlike in *L*, the *integrated* intensity of these H=1/2 incommensurate modulations is in fact quite appreciable. However the scattering is sufficiently diffuse so as to make its *peak* intensity very weak, down by a factor of 10⁶ compared with principal Bragg peaks of the three-dimensional structure, such as (0, 4, 0). The characteristics of the three sets of scattering from incommensurate modulations are summarized in Table I.

IV. DISCUSSION AND RELATION TO STM IMAGING

Our results show three distinct sets of incommensurate modulation in optimally doped Bi₂Sr₂CaCu₂O_{8+ δ}, which coexist at all temperatures below room temperature. Two of these are three dimensional in nature, with scattering centered on definite Bragg points in reciprocal space. This scattering is peaked up at $(H, 4-n \times \tau, L)$ and alternates as a TABLE I. The characteristics of the scattering at the incommensurate wave vectors with three distinct line shapes is summarized. As discussed in the text, (0, 3.79, 0), (0, 3.37, 0), and (0, 3.58, 1)are typical of $(0, 4-\delta$, even) wave vectors; while (0, 3.58, 0), (0, 3.79, 1), and (0, 3.37, 1) are typical of $(0, 4-\delta, \text{ odd})$ wave vectors (see Figs. 2 and 3).

	$(0, 4-\delta, \text{even})$	$(0, 4-\delta, \text{ odd})$	$(1/2, 4-\delta, L)$
In-plane	$\xi_b \sim 185$ Å	Res. lim.	$\xi_a \sim \xi_b \sim 27$ Å
correlations	(Lorentzian) ²		Lorentzian
Out of plane	$\xi_c \sim 20 \text{ Å}$	Res. lim.	Rodlike
correlations	(Lorentzian) ²		

function of harmonic at a particular L, and as a function of L at a particular harmonic, between resolution-limited peaks and those characterized by finite and anisotropic correlation lengths in all three directions.

The broad, $(H, 4-n \times \tau, L)$, incommensurate peaks are extremely well described by a Lorentzian-squared line shape (Fig. 4). This is an interesting result in itself, as a sum of Lorentzian plus Lorentzian-squared terms is typically used to model diffuse magnetic scattering in random field Ising model (RFIM) magnets, which display random local symmetry breaking.¹⁵ Three-dimensional RFIM systems, such as $Co_x Zn_{1-x}F_2$ (Ref. 16) and $Fe_x Zn_{1-x}F_2$ (Ref. 17) in the presence of an applied magnetic field, show magnetic diffraction features with negligible Lorentzian weight, and thus their diffuse scattering is also very well described by a Lorentzian-squared form. Such a scattering form implies a pair-correlation function in three dimensions which falls off with distance as $\exp(-\kappa r)$, and is characteristic of a domain wall state.¹⁵ Our results for κ_{ab} imply these domains are hundreds of angstroms across, with domain walls which are a single unit cell in extent in the c direction. This small spatial extent, $\xi_c \sim 20$ Å in the **c** direction is consistent with local stacking defects. As Bi2Sr2CaCu2O8+8 is more generally the m=2 member of the Bi₂Sr₂Ca_{m-1}Cu_mO_{4+2 $m+\delta$} family, the nature of the stacking fault is likely a missing Ca layer. As such the domain wall itself is expected to locally be the m=1 member of the family: Bi₂Sr₂CuO_{6+ δ}. This is a relatively low T_C superconductor ($T_C \sim 10$ K) with a smaller c axis, c = 24.6 Å (Ref. 18) than Bi₂Sr₂CaCu₂O_{8+ δ}. Such a scenario has recently been proposed from high resolution electron microscopy measurements performed on the same crystals as those studied here.¹⁹

The most remarkable result we report is the confirmation and characterization of the incommensurate modulation corresponding to a doubling of the periodicity along *H* and giving rise to rods of scattering of the form $(1/2, 4-n \times \tau, L)$ at all *L*. The scattering tends to be weakly peaked near *L* =±5. This indicates out-of-phase, or π , correlations within a bilayer. As shown schematically in Fig. 1, the CuO₂ and BiO₂ bilayer thicknesses are almost identical, at ~3.3 Å. Such correlations give rise to weak peaks at wave vectors of $\pi/(bilayer thickness) \sim \pi/3.3$ Å=0.95 Å⁻¹~*L*=5×2 π/c . As can be seen in Fig. 7, this tendency for the twodimensional rods of scattering to peak up near *L*~±5 seems to be strongest for the second and third order harmonics



FIG. 8. (Color online) The correlation areas of the new modulated structure corresponding to a doubling of the unit cell along **a** extracted from our x-ray scattering analysis are superposed on STM topographs (Ref. 9) of the surface of Bi₂Sr₂CaCu₂O_{8+ δ}. Our measurements indicate isotropic short range correlations with a correlation length of ~27 Å, and these correspond very well to the extent of the "S" microstructure which appears to be imprinted on the primary modulated structure of Bi₂Sr₂CaCu₂O_{8+ δ}, as observed in real space with the STM measurements.

of this incommensurate structure (1/2, 3.58, L) and (1/2, 3.375, L), and is not seen at all for the first order harmonic (1/2, 3.79, L) which appears to be truly rodlike in nature.

Several interesting questions arise from the observation of this two-dimensional incommensurate structure. First, from what does it arise? For example, is it a surface effect, or can it arise from an intrinsically two-dimensional charge inhomogeneity which exists throughout the full volume of the crystal?

The scattering geometry employed in all of the measurements presented in this paper is *transmission* geometry, and hence it is very unlikely that the rodlike incommensurate scattering we observe in Figs. 5–7 is due to surface structure of any kind, even though it is two dimensional in nature. We are then left with the intriguing conclusion that the scattering originates from the bulk of the crystal, but is nonetheless two dimensional in nature.

A second question which arises is, given that the $Bi_2Sr_2CaCu_2O_{8+\delta}$ family of superconductors have been studied for more than 15 years, has this type of structure been observed in previous experiments? We believe the answer to this question is yes, and consider earlier STM measurements of the surface structure of $Bi_2Sr_2CaCu_2O_{8+\delta}$. Roomtemperature measurements by Sugita et al.20 identified a superstructure with periodicity of two unit cells along the a direction. In addition, we reconsider higher resolution, low temperature STM images of the surface structure of $Bi_2Sr_2CaCu_2O_{8+\delta}$ discussed several years ago by Pan and co-workers.⁹ Figure 8 shows an STM image of the [001] cleaved surface of near-optimally doped Bi2Sr2CaCu2O8+8 from Pan et al.⁹ The well known (0, 0.21, L) modulation is seen as the periodic lighter stripes which run along the vertical direction in the STM image and which have an approximate periodicity of five unit cells dimensions along b. However, superposed on the light stripes is an "S-like" dark modulation, which has a periodicity of two unit cells along the stripe; that is along the **a** direction. This additional modulation in the structure appears superposed on every light stripe within the field of view. As such one expects its manifestation in reciprocal space to appear at wavevectors of the form (1/2, 0.21, L), exactly where we observe the twodimensional rods of scattering.

Further, careful examination of the STM image shows that the S modulation along **a** is not a perfect pattern, but is characterized by phase slips both along **a** and between S modulations imposed on adjacent light stripes. Consequently, such substructure would not give rise to resolution-limited Bragg peaks, but rather to diffuse peaks characterized by relatively short correlation lengths. Again, this is fully consistent with the two-dimensional rods of scattering which we have observed at $(1/2, 4-n \times \tau, L)$, wherein the correlation length measured in the *ab* plane was found to be approximately isotropic, $\xi_{ab} \sim 27$ Å. We have superposed correlation areas within the *ab* plane using the correlation lengths extracted from our x-ray scattering measurements, onto the STM images⁹ of the structure of the cleaved [001] plane of optimally doped $Bi_2Sr_2CaCu_2O_{8+\delta}$, and the agreement between the two is remarkably good. The S modulation within the STM image was not commented on by Pan et al.9 However, as STM is a very surface sensitive probe, it provides little information as to the behavior of this substructure into the bulk of the material. It would therefore be possible to associate such structure in an STM experiment with a surface effect. However, we reiterate that our x-ray scattering measurements, performed in transmission geometry, are very insensitive to the surface. We conclude that the twodimensional modulated structure we observe in x-ray scattering is the same as the electronic inhomogeneity observed with STM, and that it originates from charge inhomogeneity within the bulk of the $Bi_2Sr_2CaCu_2O_{8+\delta}$ superconductor.

Finally, one can ask how general is the phenomenon of charge inhomogeneity in different families of high-temperature superconductors? Of course, electronic phase separation is implied within a variety of models for high-temperature superconductivity, most prominently those involving "stripes."²¹ However, is there related diffuse scattering evidence in other high-temperature superconductors?

The answer again appears to be yes, with the recent reports of a four unit cell superstructure with correlation lengths of ~ 20 Å within the *ab* plane and very short-range correlations along **c** in optimally doped $YBa_2Cu_3O_{7-\delta}$,²² and related superstructure in underdoped $YBa_2Cu_3O_{7-\delta}^{23}$ In these cases, the short range ordered superstructure is periodic along the shorter Cu-Cu bond, whereas the two unit cell superstructure we report here for $Bi_2Sr_2CaCu_2O_{8+\delta}$ is periodic along a diagonal of the CuO₂ basal plane cell, and thus at 45° to either Cu-Cu bond. This difference, however, may simply be a consequence of the electronic inhomogeneity following the appropriate template for $Bi_2Sr_2CaCu_2O_{8+\delta}$ or $YBa_2Cu_3O_{7-\delta}$. That template would be set by the threedimensional modulation in $Bi_2Sr_2CaCu_2O_{8+\delta}$ and by the short-range oxygen-vacancy ordered superstructures in the case of $YBa_2Cu_3O_{7-\delta}{}^{23}$ which are present throughout the superconducting region of its phase diagram.²⁴ We also note

that recent STM measurements on Bi₂Sr₂CaCu₂O_{8+ δ} (Ref. 25) and Ca_{2-x}Na_xCuO₂Cl₂ (Ref. 26) have also observed a checkerboard pattern to the local density of electronic states with a 4 to 5 lattice constant periodicity within the basal plane. These results have been interpreted as being related to static, crossed stripes.²⁷ It may therefore be the case that such quasi-two-dimensional, short-range charge inhomogeneity is a general property of cuprate high-temperature superconductors and related materials.

V. CONCLUSIONS

We report the observations of three sets of incommensurate modulation to the structure of the high-temperature superconductor Bi₂Sr₂CaCu₂O_{8+ δ}. Two of these are the well known modulation characterized by wave vectors (0, 4–*n* × τ , *L*). These Bragg features alternate in both harmonic *n* for the same *L*, and in *L* for the same harmonic, between resolution-limited Bragg peaks and diffuse scattering line shapes which are very well described by a Lorentziansquared profile. We also confirm and extend the characterization of the recently discovered (1/2, 4–*n*× τ , *L*) modula-

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tions. These charge correlations are quasi-two-dimensional. The rodlike character of this scattering along c^* is weakly peaked at L=5, and this scattering is characterized by finite and relatively short correlation lengths of ~ 27 Å within the *ab* plane. We contend that the charge inhomogeneity underlying this diffuse scattering is that previously observed in STM measurements.⁹ These new x-ray scattering measurements, in transmission geometry, establish that this charge inhomogeneity is a bulk property of the system, and is not due to any reconstruction or related surface effect. We have also thoroughly investigated any possible temperature dependence to all three of these structural modulations below room temperature and find no such effect.

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