

Magnetic phase transitions in the two-dimensional frustrated quantum antiferromagnet Cs_2CuCl_4

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We report magnetization and specific heat measurements in the two-dimensional frustrated spin-1/2 Heisenberg antiferromagnet Cs_2CuCl_4 at temperatures down to 0.05 K and high magnetic fields up to 11.5 T applied along a , b , and c axes. The low-field susceptibility $\chi(T) \approx M/B$ shows a broad maximum around 2.8 K characteristic of short-range antiferromagnetic correlations and the overall temperature dependence is well described by high temperature series expansion calculations for the partially frustrated triangular lattice with $J=4.46$ K and $J'/J=1/3$. At much lower temperatures (≤ 0.4 K) and in in-plane field (along b and c axes) several new intermediate-field ordered phases are observed in between the low-field incommensurate spiral and the high-field saturated ferromagnetic state. The ground state energy extracted from the magnetization curve shows strong zero-point quantum fluctuations in the ground state at low and intermediate fields.

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I. INTRODUCTION

Cs_2CuCl_4 is a quasi-two-dimensional (2D) Heisenberg antiferromagnet with $S=1/2$ Cu^{2+} spins arranged in a triangular lattice with spatially anisotropic couplings.¹ The weak interlayer couplings stabilize magnetic order at temperatures below 0.62 K into an incommensurate spin spiral. The ordering wave vector is largely renormalized from the classical large- S value and this is attributed to the presence of strong quantum fluctuations enhanced by the low spin, geometric frustrations, and low dimensionality.^{2,3} The purpose of the thermodynamic measurements reported here is to probe the phase diagrams in applied magnetic field and see how the ground state spin order evolves from the low-field region, dominated by strong quantum fluctuations, up to the saturated ferromagnetic phase, where quantum fluctuations are entirely suppressed by the field. Intermediate fields are particularly interesting as the combination of (still) strong quantum fluctuations, potentially degenerate states due to frustration and an effective “canceling” of small anisotropies by the applied field may stabilize nontrivial forms of magnetic order.

The Hamiltonian of Cs_2CuCl_4 has been determined from measurements of the magnon dispersion in the saturated ferromagnetic phase.⁴ The exchanges form a triangular lattice with spatially anisotropic couplings as shown in Fig. 1(b) with exchanges $J=0.374(5)$ meV (4.34 K) along b , $J'=0.34(3)J$ along the zig-zag bonds in the bc plane, and weak interlayer couplings $J''=0.045(5)J$ along a . In addition there is also a small Dzyaloshinskii-Moriya interaction $D=0.053(5)J$, which creates an easy-plane anisotropy in the (bc) plane (for details see Ref. 4). Neutron diffraction measurements have shown rather different behavior depending on the field direction with respect to the easy plane. For perpendicular fields (along the a axis) incommensurate cone order with spins precessing around the field axis is stable up

to ferromagnetic saturation, however, for fields applied along the c axis (in-plane) the incommensurate order is suppressed by rather low fields, 2.1 T compared to the saturation field of 8.0 T along this axis.¹ The purpose of the present magnetization and specific heat measurements is to explore in detail the phase diagram in this region of intermediate to high fields. From anomalies in the thermodynamic quantities we observe that for in-plane field several phases occur in-between the low-field spiral and the saturated ferromagnetic states. From the magnetization curve we extract the work required to fully saturate the spins and from this we derive the total ground state energy in magnetic field and the component due to zero-point quantum fluctuations.

II. EXPERIMENTAL DETAILS

dc magnetization of a high-quality single crystal of Cs_2CuCl_4 grown from solution was measured at temperatures down to 0.05 K and high fields up to 11.5 T using a high-resolution capacitive Faraday magnetometer.⁵ A commercial superconducting quantum interference device magnetometer (Quantum Design MPMS) was used to measure the magnetization from 2 to 300 K. The specific heat measurements were carried out at temperatures down to 0.05 K in magnetic fields up to 11.5 T using the compensated quasi-adiabatic heat pulse method.⁶

III. MEASUREMENTS AND RESULTS

A. Temperature dependence of susceptibility

We first discuss the temperature dependence of the magnetic susceptibility at low field and compare with theoretical predictions for an anisotropic triangular lattice as appropriate for Cs_2CuCl_4 . Figure 1(a) shows the measured susceptibility

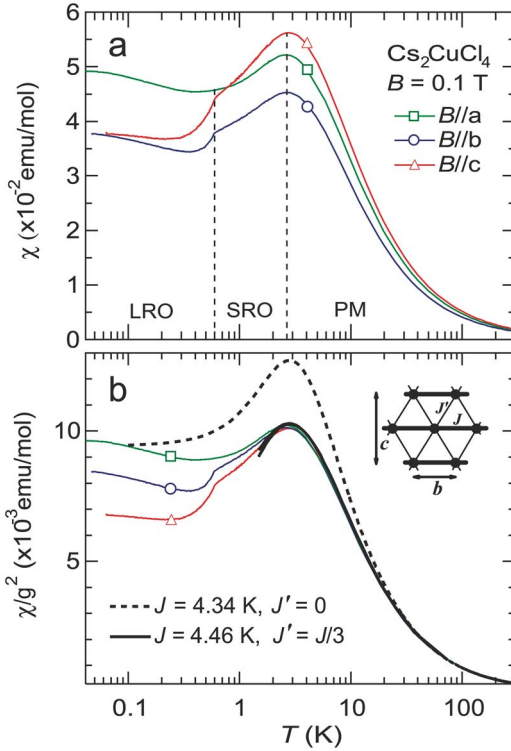


FIG. 1. (Color online) (a) Temperature dependence of the susceptibility $\chi \approx M/B$ of Cs_2CuCl_4 along the three crystallographic axes. Labels indicate magnetic long range order (LRO), short range order (SRO), and paramagnetic (PM). (b) Susceptibility divided by the g factor squared compared to calculations for a 2D anisotropic triangular lattice (see inset) with $J'/J=1/3$ and $J=4.46$ K (thick solid line), and noninteracting one-dimensional (1D) chains with $J'=0$ and $J=4.34$ K (thick dashed line).

$\chi \approx M/B$ in a field of 0.1 T. A Curie-Weiss local-moment behavior is observed at high temperatures and a broad maximum, characteristic of short-range antiferromagnetic correlations, occurs around $T_{\text{max}}=2.8(1)$ K, in agreement with earlier data.⁷ Upon further cooling the b -axes and c -axes susceptibilities show a clear kink at $T_N=0.62$ K, indicating the transition to long-range magnetic order. No clear anomaly at T_N is observed for $B\parallel a$. This is because the magnetic structure has ordered moments spiralling in a plane which makes a very small angle ($\sim 17^\circ$) with the bc plane.⁸ In this case the near out-of-plane (a -axis) susceptibility is much less sensitive to the onset of magnetic order compared to the in-plane susceptibility (along b and c). Fitting the high-temperature data ($T \geq 20$ K) to a Curie-Weiss form $\chi(T)=C/(T+\Theta)$ with $C=N_A g^2 \mu_B^2 S(S+1)/3k_B$ gives $\Theta=4.0 \pm 0.2$ K and g factors $g_a=2.27$, $g_b=2.11$, and $g_c=2.36$ for the a , b , and c axes, respectively. The g factors are in good agreement with the values obtained by low-temperature electron spin resonance (ESR) measurements $g=(2.20, 2.08, 2.30)$.⁹ When the susceptibility is scaled by the determined g values, χ/g^2 , the data along all three crystallographic directions overlap within experimental accuracy onto a common curve for temperatures above the peak, indicating that the small anisotropy term in the Hamiltonian (estimated to $\sim 5\%$ J) are only relevant at much lower tempera-

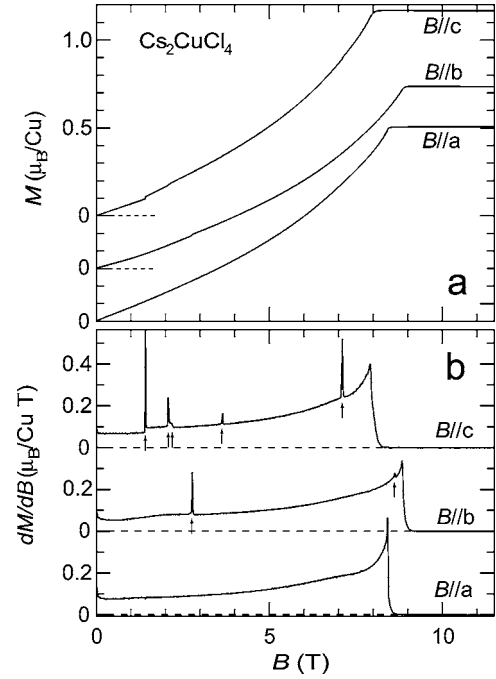


FIG. 2. (a) Magnetization curves of Cs_2CuCl_4 measured at the base temperature for the field applied along the three crystallographic axes. The curves for $B\parallel b$ and c are shifted by 0.3 and 0.6 μ_B/Cu , respectively. (b) Susceptibility dM/dB vs field. Vertical arrows indicate anomalies associated with phase transitions (see text).

tures. In the temperature range $T \geq T_{\text{max}}$ we compare the data with high-temperature series expansion calculations¹⁰ for a 2D spin-1/2 Hamiltonian on an anisotropic triangular lattice [see Fig. 1(b) inset]. Very good agreement is found for exchange couplings $J'/J=1/3$ and $J=4.46$ K (0.384 meV) [solid line in Fig. 1(b)]. In contrast, the data depart significantly from the expected Bonner-Fisher curve for one-dimensional chains ($J'=0$ and $J=4.34$ K).¹⁰

B. Magnetization curve and ground-state energy

Figure 2 shows the magnetization $M(B)$ and its derivative $\chi=dM/dB$ as a function of the applied field at a base temperature of 0.05 K for the a and b axes and 0.07 K for the c axis. For all three axes the magnetization increases linearly at low field but has a clear overall convex shape and saturates above a critical field $B_{\text{sat}}=8.44(2)$, $8.89(2)$, and $8.00(2)$ T along the a , b , and c axis, respectively. When normalized by the g values the saturation fields are the same within 2% for the three directions, the difference being the same order of magnitude as the relative strength 5% of the anisotropy terms in the Hamiltonian.⁴ The saturation magnetizations $M_{\text{sat}}/g=\langle S_z \rangle$ are obtained to be only 1%–2.5% below the full spin value of 1/2, which might be due to experimental uncertainties in the absolute units conversion or a slight overestimate of the g values by this amount. Including such a small uncertainty in the g values has only a small effect on the normalized susceptibility χ/g^2 in Fig. 1(b) and does not

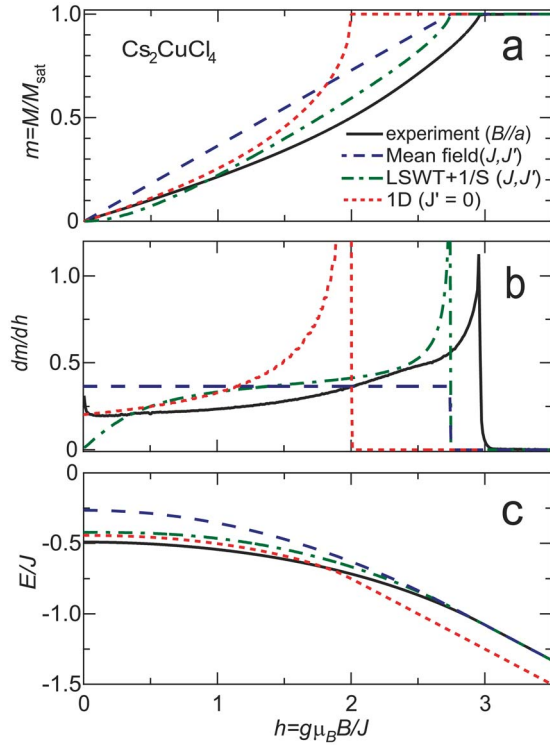


FIG. 3. (Color online) (a) Reduced magnetization, (b) susceptibility, and (c) ground-state energy vs reduced field. Black (solid), blue (dashed), green (dash-dotted), and red (dotted) lines show experimental data for $B\parallel a$, semiclassical mean-field prediction, linear spin-wave theory including first order quantum corrections and Bethe-ansatz prediction for 1D chains $J'=0$, respectively.

significantly change the results of the comparison with the series expansion calculation for the anisotropic triangular lattice.

Before analyzing in detail the various transitions in field identified by anomalies in the susceptibility $\chi=dM/dB$ [vertical arrows in Fig. 2(b)] we briefly discuss how the ground-state energy varies with the applied field, as this gives important information about the effects of quantum fluctuations. The ground state energy is obtained by direct integration of the magnetization curve, i.e.,

$$E(B) = E(0) - \int_0^B M(B)dB, \quad (1)$$

where the energy (per spin) above the saturation field takes the classical value $E(B > B_{\text{sat}}) = J(0)S^2 - g\mu_B BS$ because the ferromagnetic state is an exact eigenstate of the Hamiltonian with no fluctuations.⁴ Here $J(0) = \frac{1}{2} \sum_{\delta} J_{\delta}$ is the sum of all exchange interactions equal to $J+2J'$ for the main Hamiltonian in Cs_2CuCl_4 [see Fig. 1(b) inset]. Figure 3 shows comparisons between the experimental data for $B\parallel a$ (black solid lines), similar results obtained using b -axis or c -axis data), a mean field calculation (blue dashed lines), a linear spin-wave theory (LSWT) with first order quantum correction (green dash-dotted lines) and Bethe-ansatz prediction for 1D chains $J'=0$ (red dotted lines). In magnetic field, a cone structure is predicted by the classical mean field calculation³

$E_{cl}(B < B_{\text{sat}}) = S^2[J(Q)\cos^2\theta + J(0)\sin^2\theta] - g\mu_B BS \sin\theta$ (blue dashed lines) where Q is the classical ordering wave vector $Q = \cos^{-1}[-J'/(2J)]$, $\theta = \sin^{-1}(B/B_{\text{sat}})$, the saturation field is $g\mu_B B_{\text{sat}} = 2S[J(0) - J(Q)]$ and $J(Q) = J\cos(2Q) + 2J'\cos(Q)$. Here we use $J = 0.374$ meV and $J'/J = 0.34$ for the main Hamiltonian in Cs_2CuCl_4 . The experimentally determined ground state energy (black solid line) is lower than the classical value (blue dashed line) due to zero-point quantum fluctuations. The energy difference in zero field is 85% of the expected classical energy $E_{cl}(B=0) = J(0)S^2$, indicating rather strong quantum fluctuations in the ground state. The strongly nonlinear (convex) shape of the magnetization curve compared to the classically expected linear form $M/M_{\text{sat}}(B < B_{\text{sat}}) = B/B_{\text{sat}}$ [see Fig. 3(a)] is a direct indication of the importance of zero-point quantum fluctuations. Including first order quantum correction to the classical result in a linear spin-wave approach gives³

$$E_{\text{LSWT}+1/S} = S(S+1)[J(Q)\cos^2\theta + J(0)\sin^2\theta] - g\mu_B B(S+1/2)\sin\theta + \langle\omega_{\mathbf{k}}\rangle/2$$

where $\langle\omega_{\mathbf{k}}\rangle$ is the average magnon energy in the 2D Brillouin zone of the triangular lattice. This improves the agreement with the data (green dash-dotted lines). Particularly at high fields it better captures the divergence of the susceptibility [see Fig. 3(b)] at the transition to saturation. The saturation field is underestimated slightly because we have neglected here the weak interlayer couplings $J'' = 4.5\% J$ and the DM interaction $D = 5.3\% J$, both of which increase the field required to ferromagnetically align the spins. It is also illuminating to contrast the data with a model of noninteracting chains ($J'=0$, red dotted lines). This would largely (by 48%) underestimate the observed saturation field and would predict a rather different functional form for the magnetization $M_{1D}(B < B_{\text{sat}}) = M_{\text{sat}}/2 \pi \sin^{-1}(1 - \pi/2 + \pi J/g\mu_B B)^{-1}$, $B_{\text{sat}} = 2J/g\mu_B$, and susceptibility $\partial M_{1D}/\partial B$ compared to the data, indicating that the 2D frustrated couplings are important.

C. Phase diagrams in in-plane field

When the magnetic field is applied along the a axis perpendicular to the plane of the zero-field spiral the ordered spins cant towards the field axis and at the same time maintain a spiral rotation in the bc plane thus forming a cone. The cone angle closes continuously at the transition to saturation and as expected in this case the susceptibility dM/dB observes a sharp peak followed by a sudden drop as the field crosses the cone to saturated ferromagnet transition, see Fig. 2(b). However, for fields applied along the b and c axes several additional anomalies are present in the magnetization curve apart from the sharp drop in susceptibility upon reaching saturation, indicating several different phases stabilized at intermediate field.

Before discussing in detail the experimental phase diagrams we note that for all field directions the magnetization increases in field up to saturation and no intermediate-field plateaus are observed, in contrast to the isostructural material Cs_2CuBr_4 , where a narrow plateau phase occurs for in-plane field when the magnetization is near 1/3rd of saturation.¹¹

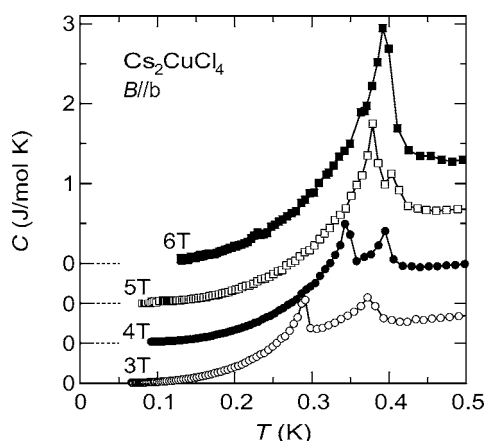


FIG. 4. Specific heat as a function of temperature in magnetic fields along the b axis. Specific heat data in fields 4, 5, and 6 T are shifted upwards by 0.5, 1.0, and 1.5 J/mol K², respectively.

Such a plateau phase is expected for the fully frustrated ($J'/J=1$) triangular antiferromagnet and originates from the formation of the gapped collinear up-up-down state in field. The absence of a plateau in Cs_2CuCl_4 is probably related to the weaker frustration [$J'/J=0.34(3)$] compared to Cs_2CuBr_4 ($J'/J \sim 0.5$).¹¹

A difference in the phase diagrams in the field applied along the a axis and in the bc plane in Cs_2CuCl_4 is expected based on the presence of small DM terms in the spin Hamiltonian, which create a weak easy-plane anisotropy in the bc plane.⁴ Semiclassical calculations which take this anisotropy into account predict two phases below saturation:³ a distorted spiral at low field separated by a spin-floppike transition from a cone at intermediate field. The data in Fig. 2(b), however, observe more complex behavior with several different intermediate-field ordered phases. Also early neutron scattering measurements did not observe the characteristic incommensurate magnetic Bragg peaks expected for a cone structure at $B > 2.1 \text{ T} \parallel c$ axis,¹ suggesting that the magnetic structure at the intermediate field may be quite different from the classical prediction and may be stabilized by quantum fluctuations beyond the mean-field level. To map out the extent of the various phases in the in-plane field we have made a detailed survey of the B - T phase diagram using both the temperature and field scans in magnetization and specific heat and the resulting phase diagrams are shown in Fig. 10. Below we describe in detail the signature of those transitions in specific heat and magnetization data, first for field along the b axis, then the c axis.

Magnetization and differential susceptibility dM/dB in the field along b are shown in Fig. 2. dM/dB shows a sharp peak at $B=2.76 \text{ T}$ and an additional small peak at $B=8.57 \text{ T}$ and those two anomalies indicate two new phases at the base temperature below the saturation field and above the spiral phase. To probe the extent in the temperature of those phases we show in Fig. 4 specific heat measurements as a function of temperature at constant magnetic field. At 3 T two peaks are clearly observed indicating two successive phase transitions upon cooling from high temperatures. The lower critical temperature increases rapidly with increasing

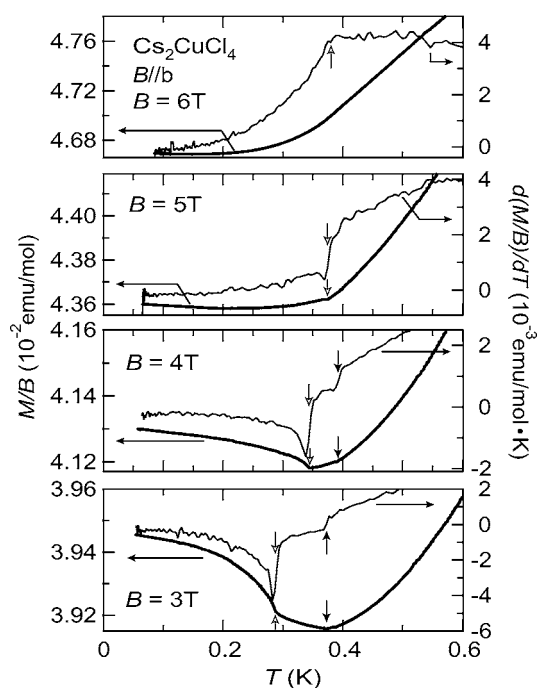


FIG. 5. Magnetization normalized by applied field M/B (thick solid lines, left axis) and its derivative $d(M/B)/dT$ (thin solid lines, right axis) as a function of temperature for $B \parallel b$. Vertical arrows indicate anomalies.

the field and gradually approaches the upper transition at 5 T and the two peaks appear to merge at 6 T.

Complementary magnetization data versus temperature for the field along b is shown in Fig. 5. At 3 and 4 T two anomalies are observed also in $M/B(T)$ and its derivative $d(M/B)/dT$, at essentially the same temperatures as the peaks in specific heat, indicating that those two anomalies are associated with magnetic phase transitions. The anomalies appear as kinks in $M/B(T)$ and steps in $d(M/B)/dT$. At 5 T, however, the scaled magnetization $M/B(T)$ only observes a clear anomaly at the lower of the two critical temperatures observed in specific heat. At 6 T no anomaly is visible in $M/B(T)$, but only the derivative $d(M/B)/dT$ shows a kink. The missing anomalies can, however, be seen in the raw capacitance data, plotted in Fig. 6, which also contain information not only on the (longitudinal) magnetization but also the transverse spin components. At 4 T the capacitance in both the zero and nonzero gradient field show two successive transitions indicated by solid and open arrows. Those are in good agreement with the peaks observed in specific heat. Although there is no anomaly visible in the magnetization at 6 T, the raw capacitance shows an anomaly (see derivative of dC/dT in the inset of Fig. 6) at the same temperature as the peak in specific heat. The capacitance in the nonzero gradient field contains information on the torque of the sample in addition to the magnetization, while that in the zero gradient field does not depend on the magnetization but only on the torque. The torque contribution is subtracted by measuring the capacitance in the zero gradient field (details of measurement technique are described in Ref. 5). The fact that there is no anomaly in the magnetization implies that the

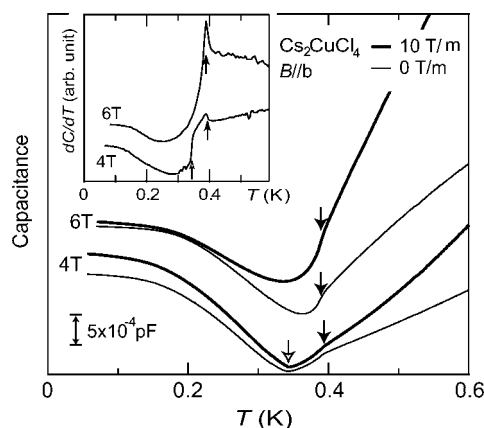


FIG. 6. Raw capacitance data as a function of temperature in magnetic field of 4 and 6 T applied along the b axis. Data are vertically shifted for clarity. Filled and open arrows indicate anomalies. Thick (thin) solid lines correspond to measurements with (without) the gradient field. The inset shows the temperature derivative of the capacitance data in the gradient field 10 T/m. The curves are shifted vertically for clarity.

subtraction of the torque effect cancels out the anomaly in the raw data. Therefore, only the torque (transverse magnetization) has an anomaly and the longitudinal magnetization has no anomaly at the critical temperatures for these missing anomalies.

For the field along c it has been reported from a neutron scattering study that the spiral phase at the zero field is suppressed by magnetic field of 1.4 T and above this field ordered spins form an incommensurate elliptical structure with elongation along the field direction.¹ The elliptical phase is suppressed at 2.1 T where the intensity of incommensurate magnetic Bragg peaks vanishes and the properties of the phase above 2.1 T are still unknown. As shown in Fig. 2(b), the suppression of the spiral phase is clearly seen as a step in magnetization (a sharp peak in dM/dB) at 1.40 T. In Fig. 7 the magnetization at 0.07 K and its derivative dM/dB are expanded in order to show the four anomalies above the spiral phase. In Fig. 7(a), $M(B)$ shows a small step [a peak in $\chi(B)$] at 2.05 T, corresponding to the suppression of the elliptical phase. As indicated by an open arrow in Fig. 7(a), a step in susceptibility at 2.18 T is clearly seen, possibly indicating a new phase which may exist only in a very small range of fields from 2.05 to 2.18 T. The next transition occurs at 3.67 T (for the increasing field) shown in Fig. 7(b). $M(B)$ has a step accompanied by a hysteresis, indicative of a first order transition. Figure 7(c) shows another transition at 7.09 T with a clear hysteresis.

Figure 8 shows specific heat in magnetic fields along the c axis. At 3 T only one transition is observed upon cooling, whereas at 4 and 5 T two successive transitions are observed. The lower temperature transition is very sharp, related to the first order behavior (hysteresis) on this transition line also observed in the magnetization data $M(B)$ at 3.67 T shown in Fig. 7(b). The lower temperature transition shifts to higher temperatures with the increasing field and almost merges with the upper transition at 6 T.

Figure 9 shows complementary magnetization data versus temperature. 3 T $M/B(T)$ and $d(M/B)/dT$ show a kink and a

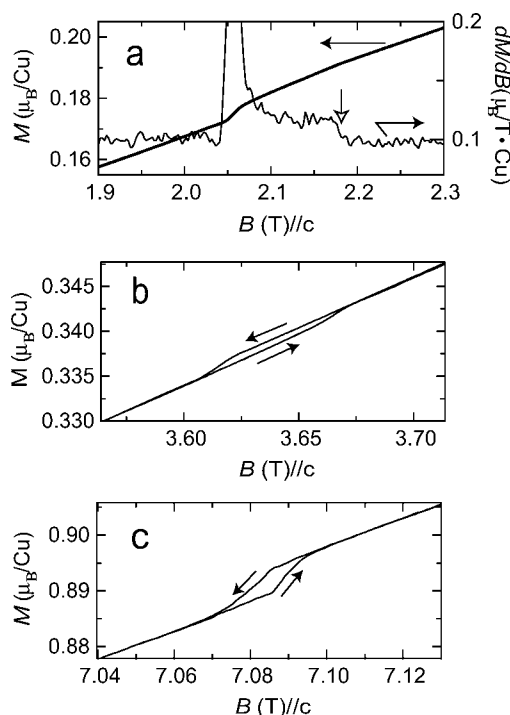


FIG. 7. Expanded plots of magnetization and susceptibility $\chi = dM/dB$ as a function of field along the c axis. Data are identical to those from Figs. 2(a) and 2(b).

step at 0.35 K, respectively. At 4 T the position of the kink [step in $d(M/B)/dT$] is shifted to a slightly higher temperature and another steplike anomaly [a negative peak in $d(M/B)/dT$] appears at lower temperatures 0.22 K. At 5 T this lower temperature step shifts to higher temperatures and the upper temperature anomaly (kink) cannot be seen in $M/B(T)$ but is manifested as a kink in $d(M/B)/dT$ at 0.38 K. Again the anomaly is missing in $M/B(T)$, but the raw capacitance data (not shown) exhibit an anomaly at 0.38 K in good agreement with the specific heat result. As shown in the top panel of Fig. 9, $M/B(T)$ and $d(M/B)/dT$ have two anomalies at 6 T. Note that due to the first order character of the lower

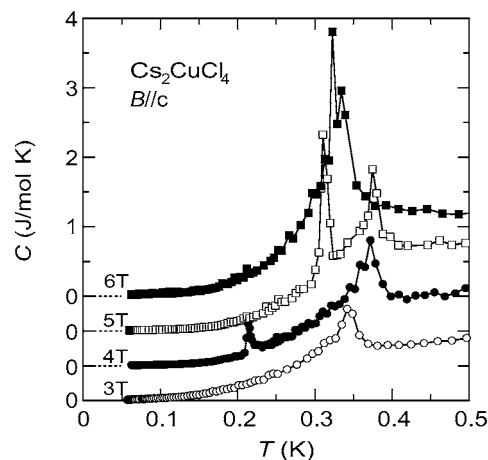


FIG. 8. Specific heat as a function of temperature in magnetic fields along the c axis. Specific heat data in fields 4, 5, and 6 T are shifted upwards by 0.5, 1.0, and 1.5 J/mol K², respectively.

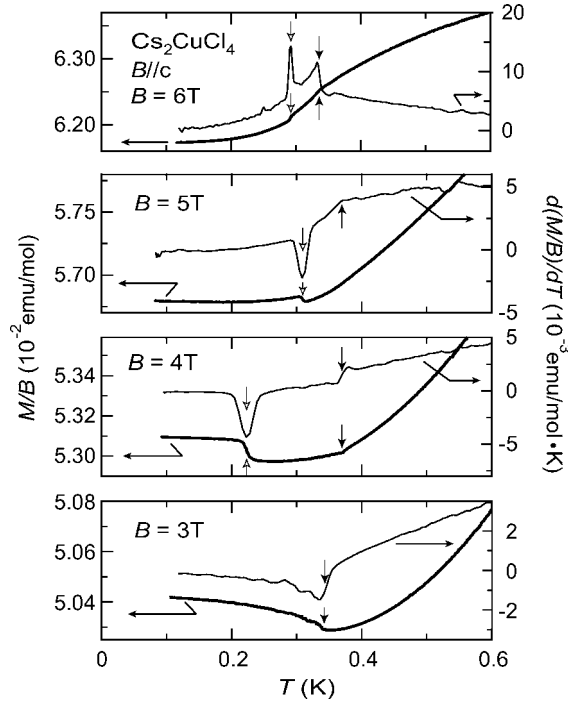


FIG. 9. Magnetization normalized by the applied field M/B (thick solid lines, left axis) and its derivative $d(M/B)/dT$ (thin solid lines, right axis) as a function of temperature for $B \parallel c$. Vertical arrows indicate anomalies.

temperature transition the anomalies of M/B ($d(M/B)/dT$) indicated by open arrows in Fig. 9 are steps (peaks) rather than kinks (steps).

The phase diagrams for the $B \parallel b$ and c axis constructed using the anomalies discussed above are shown in Fig. 10. The new data agree with and complement earlier low-field neutron diffraction results (open triangles).¹ Apart from the phase transition boundaries identified above we have also marked the cross-over line between the paramagnetic and antiferromagnetic SRO region, determined by the location of the peak in the temperature dependence of the magnetization such as in Fig. 1(a). The peak position T_{max} decreases with the increasing field and disappears above B_c , indicating the suppression of antiferromagnetic correlations by the magnetic field. For the field along the b and c axis the phase diagrams are much more complicated than that for $B \parallel a$ which shows only one cone phase up to the saturation field.^{4,12} For $B \parallel b$ three new phases appear above the spiral phase. Two of these phases occupy small areas of the B - T phase diagram. For $B \parallel c$ four new phases are observed in addition to the spiral and elliptical phases.

We note that the absence of an observable anomaly in the temperature dependence of the magnetization upon crossing the phase transitions near certain fields (6 T along b and 5 T along c) is consistent with Ehrenfest relation and is related to the fact that the transition boundary $T_c(B)$ is near flat around those points. The relation between the shape of the phase boundary and the anomaly in $M(T)$ was discussed by Tayama *et al.*¹³ and is

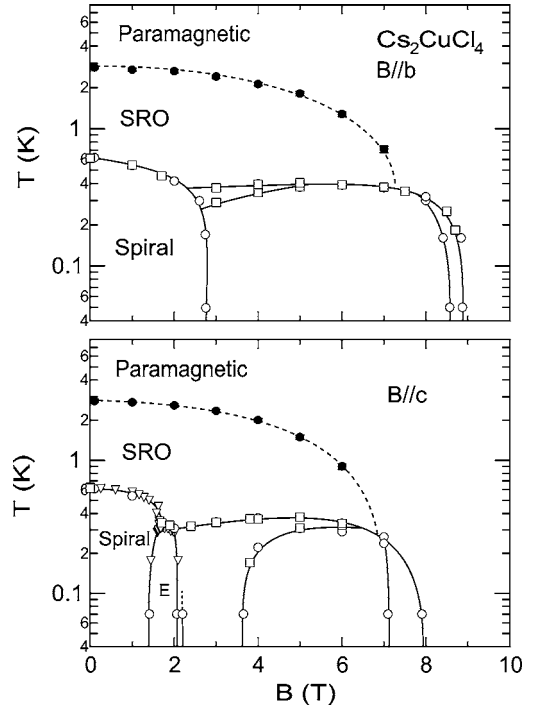


FIG. 10. B - T phase diagrams of Cs_2CuCl_4 for the $B \parallel b$ and c axis. Data points of open circles (magnetization), squares (specific heat), and triangles [neutrons (see Ref. 1)] connected by solid lines indicate phase boundaries. Solid circles show the positions of the maximum in the temperature dependence of the magnetization and indicate a crossover from paramagnetic to SRO. "E" on the phase diagram for the $B \parallel c$ axis denotes the elliptical phase (see Ref. 1).

$$\Delta\left(\frac{dM}{dT}\right) = -\frac{dT_c}{dB}\Delta\left(\frac{C}{T}\right), \quad (2)$$

where $\Delta(X)$ is the discontinuity of quantity X , C is the specific heat, and T_c is the field-dependent critical temperature of the second order phase transition. This shows that the discontinuity in dM/dT vanishes when $dT_c/dB=0$, i.e., when the phase boundary is flat in the field. This is indeed the case for 6 T $\parallel b$ and at 5 T $\parallel c$ (see Fig. 10), and here only a kink and no discontinuity is seen in dM/dT .

IV. CONCLUSIONS

We have studied the magnetic phase diagrams of Cs_2CuCl_4 by measuring magnetization and specific heat at low temperatures and high magnetic fields. The low-field susceptibility in the temperature range from below the broad maximum to the Curie-Weiss region is well described by high-order series expansion calculations for the partially frustrated triangular lattice with $J'/J=1/3$ and $J=0.385 \text{ meV}$. The extracted ground state energy in the zero field obtained directly from integrating the magnetization curve is nearly a factor of 2 lower compared to the classical mean-field result. This indicates strong zero-point quantum fluctuations in the ground state, captured in part by including

quantum fluctuations to order $1/S$ in a linear spin-wave approach. The obtained B – T phase diagrams for the in-plane field ($B\parallel b$ and c -axis) show several new intermediate-field phases. The difference between the phase diagrams for $B\parallel a$, b , and c cannot be explained by a semiclassical calculation for the main Hamiltonian in Cs_2CuCl_4 , of a frustrated 2D Heisenberg model on an anisotropic triangular lattice with small DM terms. Further neutron scattering

experiments are needed to clarify the magnetic properties of these new phases.

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¹R. Coldea, D. A. Tennant, A. M. Tsvelik, and Z. Tylczynski, *Phys. Rev. Lett.* **86**, 1335 (2001).

²Z. Weihong, R. H. McKenzie, and R. R. P. Singh, *Phys. Rev. B* **59**, 14367 (1999); C. H. Chung, J. B. Marston, and R. H. McKenzie, *J. Phys.: Condens. Matter* **13**, 5159 (2001).

³M. Y. Veillette, J. T. Chalker, and R. Coldea, *Phys. Rev. B* **71**, 214426 (2005).

⁴R. Coldea, D. A. Tennant, K. Habicht, P. Smeibidl, C. Wolters, and Z. Tylczynski, *Phys. Rev. Lett.* **88**, 137203 (2002).

⁵T. Sakakibara, H. Mitamura, T. Tayama, and H. Amitsuka, *Jpn. J. Appl. Phys., Part 1* **33**, 5067 (1994).

⁶H. Wilhelm, T. Lühmann, T. Rus, and F. Steglich, *Rev. Sci. Instrum.* **75**, 2700 (2004).

⁷R. L. Carlin, R. Burriel, F. Palacio, R. A. Carlin, S. F. Keij, and D. W. Carnegie, *J. Appl. Phys.* **57**, 3351 (1985).

⁸R. Coldea, D. A. Tennant, R. A. Cowley, D. F. McMorrow, B. Dorner, and Z. Tylczynski, *J. Phys.: Condens. Matter* **8**, 7473 (1996).

⁹S. Bailleul, J. Holsa, and P. Porcher, *Eur. J. Solid State Inorg. Chem.* **31**, 432 (1994).

¹⁰W. Zheng, R. R. P. Singh, R. H. McKenzie, and R. Coldea, *Phys. Rev. B* **71**, 134422 (2005).

¹¹T. Ono, H. Tanaka, O. Kolomiyets, H. Mitamura, T. Goto, K. Nakajima, A. Oosawa, Y. Koike, K. Kakurai, J. Klenke, P. Smeibidl, and M. Meißner, *J. Phys.: Condens. Matter* **16**, S773 (2004).

¹²T. Radu, H. Wilhelm, V. Yushankhai, D. Kovrizhin, R. Coldea, Z. Tylczynski, T. Lühmann, and F. Steglich, *Phys. Rev. Lett.* **95**, 127202 (2005).

¹³T. Tayama, T. Sakakibara, K. Kitami, M. Yokoyama, K. Tenya, H. Amitsuka, D. Aoki, Y. Ōnuki, and Z. Kletowski, *J. Phys. Soc. Jpn.* **70**, 248 (2001).