

Aharonov-Bohm electron interferometer in the integer quantum Hall regime

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We report experiments on a quantum electron interferometer fabricated from high mobility, low density AlGaAs/GaAs heterostructure material. In this device, a nearly circular electron island is defined by four front gates deposited in etched trenches. The island is separated from the two-dimensional (2D) electron bulk by two nearly open constrictions. In the quantum Hall regime, two counterpropagating edge channels are coupled by tunneling in the constrictions, thus forming a closed electron interference path. For several fixed front gate voltages, we observe periodic Aharonov-Bohm interference oscillations in four-terminal resistance as a function of the enclosed flux. The oscillation period ΔB gives the area of the interference path S via the quantization condition $S = h/e\Delta B$. We experimentally determine the dependence of S on the front gate voltage, and find that the Aharonov-Bohm quantization condition does not require significant corrections due to the confining potential. These results can be interpreted as a constant integrated compressibility of the island with respect to the front gates. We also analyze experimental results using two classical electrostatics models: one modeling the 2D electron density due to depletion from an etch trench, and another modeling the gate voltage dependence of the electron density profile in the island.

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I. INTRODUCTION

Quantum interference of 2D electrons around a quantum antidot subjected to a quantizing magnetic field has been used experimentally to determine the fractional charge of Laughlin quasiparticles of the surrounding quantum Hall condensate.^{1,2} Recent experiments on devices in the inverse geometry, where quantized electron paths circle a 2D electron island, have reported observation of an Aharonov-Bohm “superperiod,” implying fractional statistics of Laughlin quasiparticles.³ The layout of the present interferometer looks qualitatively similar to a “Coulomb Island,”^{4,5} but the electron island is larger. The principal difference is that the constrictions are nearly open, so that no Coulomb blockade or conductance steps are observed at zero magnetic field. In the integer quantum Hall (QH) regime, the Landau level filling in the constrictions is nearly equal to that in the 2D bulk.

In this paper we report electron quantum interference experiments in the integer QH regime performed with an electron interferometer device, Fig. 1. In this device, counterpropagating edge channels⁶⁻⁹ enclose a lithographically defined 2D electron island, and tunneling in the two nearly open, tunable constrictions completes the electron path, thus allowing an Aharonov-Bohm-type interference regime. When tunneling between the edge channels occurs, in the quantum-coherent regime, Aharonov-Bohm oscillations with period ΔB are expected in the four-terminal resistance $R_{XX} = V_X/I_X$ as a function of the magnetic field B . In the quantum limit, each oscillation signals the alignment of a quantized electron state encircling the 2D electron island with the chemical potential μ .

In each spin-polarized Landau level (LL), the single-electron states are quantized by the Aharonov-Bohm condition: The magnetic flux Φ through the area of an encircling orbital S_m satisfies $\Phi = BS_m = m\Phi_0$, where m is the quantum number of the orbital and $\Phi_0 = h/e$ is the fundamental flux quantum.^{10,11} Thus, $S_m = mh/eB = 2\pi m\ell^2$, where $\ell = \sqrt{\hbar/eB}$ is

the magnetic length, and the area for each electron state per spin-polarized LL is $S_{m+1} - S_m = 2\pi\ell^2 = h/eB$. These quantization conditions apply as well to an interacting 2D electron fluid with microscopically uniform density, so long as no phase transition to a charge density wave (such as a striped or “bubble”) ground state occurs.

The 2D electron island in this sample is large, containing ~ 2000 electrons. Thus the electron density profile is expected to be determined mostly by the classical electrostatics of neutralizing the positively charged donors and the electric field of the gates, if biased. The island basic confinement is produced by the etch trenches which remove the donors.

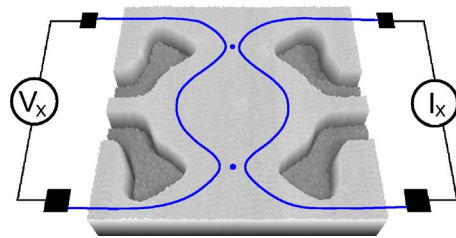


FIG. 1. (Color online) An atomic force microscope (AFM) image of the central region of an electron interferometer device. A nearly circular region of lithographic radius $R = 1300$ nm was defined in AlGaAs/GaAs heterojunction material by chemically etched trenches. Au/Ti metallization deposited in the etch trenches forms the front gates of the device. The constrictions are 1200 nm wide. Four Ohmic contacts (black squares) are in fact positioned at the corners of a $\sim 4 \times 4$ mm sample. On a quantum Hall plateau, with a quantizing magnetic field normal to the 2D electron plane, current flows along the counterpropagating edge channels (blue solid lines). Tunneling (represented by dots) occurs in the two wide constrictions, when the edge channels are close enough, thus allowing the electrons to perform a closed path around the 2DES island. The Aharonov-Bohm interference signal is detected as oscillations in $R_{XX} \equiv V_X/I_X$.

GaAs is known to have the “surface Fermi level pinning,” due to a large density of mid-gap surface electron states, which has been successfully modeled by self-consistent depletion of donors, including a negative surface charge density. The surface depletion results in the 2D electron density being less than the donor density (because some donor electrons go to the surface), and, important for the present samples, an additional etched mesa sidewall depletion due to the free surface of the etch trenches.

The main effect of the external confinement potential $U(r)$ is to lift the massive degeneracy of the single-electron states in each Landau level. In the first order perturbation theory, the quantization $S_m = 2\pi m \ell^2$ is not affected by the confinement [$U(r)$ is simply added to the cyclotron and spin energies]. For the QH filling¹² $i=1$ (the only QH filling presented in this paper), each R_{XX} oscillation corresponds to a change by one in the number of electron states within S_μ , the area enclosed by the path of the electron at energy μ .^{2,11} Thus, as a function of B , when S_μ is nearly fixed by the confining potential, the flux period $\Delta\Phi$ is one Φ_0 for each oscillation, similar to the quantum antidots,^{1,11} so that $S_\mu = \Phi_0 / \Delta B$.

We stress that changing B does not change appreciably the number of electrons in the large island (this would lead to an enormous Coulomb energy). Instead, changing B changes the density of states in each Landau level, so that the same number of island electrons occupies the same total number of states, but their distribution between various Landau levels changes: The Landau level filling $\nu = nh/eB$ changes while density n is fixed. On the $i=1$ QH plateau, in the 2D bulk μ is in the localized states between the lowest and the next spin-split Landau levels. Chemical potential in the island is determined by the μ in the bulk, our results (presented in this paper) show that apparently the radial position of the $i=1$ edge channel circling the island is nearly fixed by the confining potential, that is, S_μ is nearly constant. The quantum number m_μ of the state S_m corresponding to S_μ regularly changes in steps of one, $m_\mu \propto B$ since the area per state $2\pi\ell^2 \propto 1/B$. If the occupation of the states in the electron island were a step-function, 1 for $m \leq m_\mu$ and 0 for $m > m_\mu$, then S_μ must change, and the number of electrons within S_μ must change. Instead, as evidenced by the experiments reported here, both S_μ and the number of electrons within S_μ are nearly constant. What happens is that the electron occupation is not described by the step-function. Increasing B increases density of states in a LL, thus accommodating the same number of electrons is accompanied by creation of unoccupied states (that is, holes) in the otherwise filled LL. Likewise, decreasing B is accompanied by filling of the states in the next, otherwise empty LL. Such Landau level quasiparticle or quasihole creation allows to accommodate a fixed number of island electrons (as dictated by the self-consistent electrostatics of Coulomb-interacting electrons) in a nearly constant area S_μ .

Application of a front gate voltage V_{FG} produces electric field which affects the confining potential and thus changes both the electron density distribution and S_μ . The number of electrons in the island changes because both density and the area S_μ change. An increased n is accompanied by the shift to a higher B of the $i=1$ QH plateau (with Aharonov-Bohm oscillations superimposed). An increase in S_μ is observed as

a smaller Aharonov-Bohm period ΔB . Thus, the two effects are measured directly, independent of each other. From the dependence of the period ΔB , and thus S_μ , on V_{FG} we obtain the electric-field-induced ΔS_μ , the electron orbit area change corresponding to addition of one electron inside the orbital at μ . We also observe a systematic shift of the midpoint of the range of the Aharonov-Bohm oscillations B_M , which, assuming it corresponds to a fixed filling $\nu=1$, also yields the area $\Delta S_\mu = 2\pi\ell^2$ occupied by one electron. These two experimentally independent ways to obtain ΔS_μ agree very well. Additionally, we compare these experimental results to ΔS_μ obtainable from the edge depletion models of Chklovskii *et al.*¹³ and Gelfand and Halperin,¹⁴ and find a reasonable agreement between ΔS_μ obtained from these models and in the experiments.

II. EXPERIMENTAL RESULTS

Our device is based on a very low disorder, high mobility modulation-doped AlGaAs/GaAs heterojunction,¹⁵ which had a 2D electron system (2DES) with density $n_0 = 9.7 \times 10^{10} \text{ cm}^{-2}$ (achieved after exposing the sample to red light at 4.2 K). Ohmic contacts were prepared on a pre-etched mesa. Next, a 2DES island of lithographic radius $R=1300 \text{ nm}$ was defined by electron beam lithography (using proximity correction) and a self-aligned lift-off process (see Fig. 1). The 50 nm thick Au/Ti gate metal was deposited in chemically etched shallow trenches, 82 nm deep, reaching below the δ -doping, while the 2DES is 215 nm below the surface. The four independent front gates are contacted separately.

All the measurements presented here were performed with the device in the 10.2 mK ^3He — ^4He bath in the tail of the mixing chamber of a top-loading into mixture dilution refrigerator. Extensive cold filtering in the electrical leads reduces the electromagnetic background incident on the sample to $5 \times 10^{-17} \text{ W}$.¹⁶ We measure $R_{XX} = V_X / I_X$ as a function of magnetic field B using a lock-in technique at 5.4 Hz. We typically use $I_X = 200 \text{ pA}$ rms in this paper, although reducing the current to 100 pA reveals moderate electron heating effects. Each R_{XX} versus B trace was measured at a fixed value of V_{FG} , defined as the average front gate voltage. A small differential front gate bias was applied in order to fine-tune the two constrictions for symmetry of tunneling amplitudes (to increase the amplitude of the oscillations).

In this paper we focus exclusively on the $i=1$ QH plateau in the island. The experimental results in this regime are summarized in Figs. 2 and 3 and in the inset of Fig. 4. In general, we observe the Aharonov-Bohm oscillations in R_{XX} , superimposed on a smooth background magnetoresistance coming from the 2D bulk outside the island.³ Fig. 2 presents a typical directly measured R_{XX} vs. B trace. The oscillations are clearly periodic with period ΔB ; for example, the trace shown in Fig. 2 ($V_{FG} \approx 0$) has $\Delta B = 1.87 \text{ mT}$. Figure 3 presents the oscillatory δR_{XX} as a function of B (that is, R_{XX} with the smooth background subtracted), for several positive values of V_{FG} . The period ΔB for each of these traces decreases with increasing V_{FG} . It is evident that the magnetic field intervals where the Aharonov-Bohm oscillations occur shift to

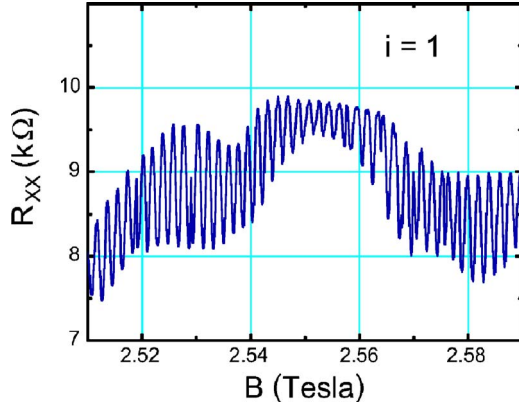


FIG. 2. (Color online) Directly measured Aharonov-Bohm oscillations in R_{XX} on $i=1$ quantum Hall plateau. Front gate voltage $V_{FG} \approx 0$, bath temperature of 10.2 mK. Oscillations are superimposed on a smooth background due to conduction in the 2D electron “bulk,” outside of the island.

higher magnetic fields when V_{FG} is increased. To quantify this behavior, we define B_M as the midpoint of the magnetic field range in which the oscillations occur (for the given V_{FG}). For example, $B_M \approx 2.80$ T for the $V_{FG}=150$ mV trace. The inset in Fig. 4 shows the dependence of thus determined B_M on V_{FG} , which is approximately linear in the range of the voltages studied.

III. ANALYSIS AND DISCUSSION

A. The edge depletion models

The 2D electron island is defined by the depletion potential of the etch trenches. We use a model based on that of Gelfand and Halperin¹⁴ (GH) to calculate the resulting elec-

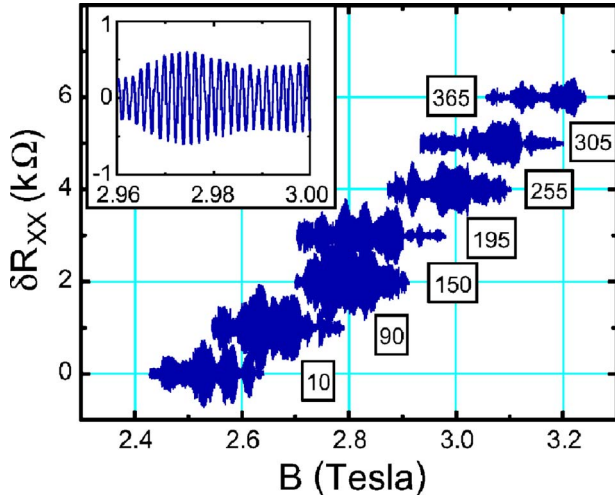


FIG. 3. (Color online) Aharonov-Bohm oscillations δR_{XX} as a function of B for several values of positive front gate voltage V_{FG} , given in the labels next to each trace (in mV). All the traces occur on the $i=1$ quantum Hall plateau, and have been displaced vertically in steps of 1 kΩ for clarity (1 kΩ corresponds to tunneling conductance $0.04e^2/h$). Each trace contains approximately 100 oscillations with a well defined period ΔB , which depends on V_{FG} . Inset: A blow up of the $V_{FG}=255$ mV trace shows the regularity of the oscillations.

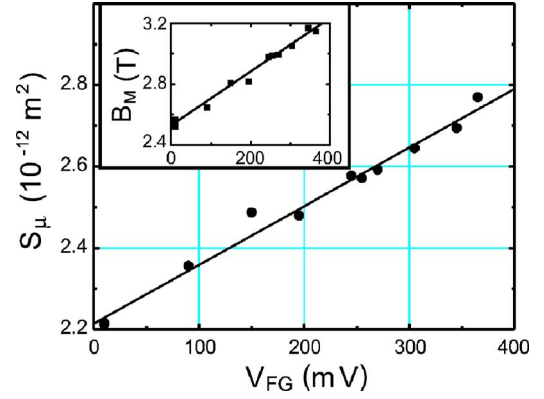


FIG. 4. (Color online) Dependence of island area S_μ on V_{FG} . Each value of S_μ (circles) was determined from the Aharonov-Bohm period ΔB . The dependence is approximately linear in the range of V_{FG} studied; the solid line is a least squares fit to $S_\mu = a + bV_{FG}$, giving $a = 2.21 \times 10^{-12} \text{ m}^2$ and $b = 1.44 \times 10^{-12} \text{ m}^2/\text{V}$. Diameter $\sqrt{4S_\mu/\pi} \approx 1.8 \mu\text{m}$. Inset: The midpoint of the oscillations B_M vs V_{FG} . A linear fit $B_M = c + dV_{FG}$ gives $c = 2.53$ T and $d = 1.77$ T/V.

tron density profile $n(r, V_{FG}=0)$, assumed to be rotationally symmetric. Briefly, this $B=0$ classical electrostatics model includes effects of the surface charge on the side wall of the etched mesa due to the GaAs surface states, and the resulting ionized donors of the intentional 2D δ -doping. GH obtain an analytic expression for the density profile $n_{GH}(x) = F_{GH}(x/W)n_0$ for a linear edge, where x is the coordinate normal to the edge ($x=-W$ at the lithographic edge), W is the depletion length, n_0 is the 2D “bulk” electron density, and F_{GH} is the function given in their Eq. (7). In a strong magnetic field $W \gg \ell$, the magnetic length, and this analytic expression agrees very well with the profile obtained in a Hartree-Fock calculation¹⁴ for x such that $n_{GH}(x)/n_0 > 0.3$. Since $W \ll R$, the island lithographic radius, we adapt the GH density profile to our circular geometry:

$$n_{GH}(r) = F_{GH}[(R-r)/W]F_{GH}[(R+r)/W]n_0, \quad (1)$$

where r is the radial distance from the center of the island.

The effect of the front gate bias is modeled following Chklovskii, Shklovskii, and Glazman¹³ (CSG). They obtain an analytic expression for the electron density profile $n_{CSG}(x) = F_{CSG}(x/L)n_0$ for a linear edge ($x=-L$ at the gate edge), where $F_{CSG} = [(x+L)/(x-L)]^{1/2}$, and the length parameter $L = \epsilon\epsilon_0 V_{FG} / \pi e n_0$. Again, since $L \ll R$ for our V_{FG} range, we adapt the CSG density profile to our circular geometry:

$$n_{CSG}(r) = F_{CSG}(r/L)n_0 = \left(\frac{(R+2L)^2 - r^2}{R^2 - r^2} \right)^{1/2} n_0. \quad (2)$$

The main effect of a quantizing magnetic field is to open the QH gap at μ , causing creation of “incompressible” and “compressible” regions.^{13,14,17} The effect on electron transport properties is great, but the $B=0$ electron density profile is not perturbed very much. This is because a variation of electron density produces large electrostatic charging energy, which must be compensated by the fraction of the QH gap energy gained per displaced electron. Recently, Hartree-Fock

calculations for up to 300 electrons confined in an island for QH filling $i=2$ have been reported for both parabolic and a bell-shaped confining potentials.¹⁸ Certain qualitative similarities to the behavior in our samples are apparent, and perhaps future Hartree-Fock work can more closely model confinement in the electron interferometer samples.

B. The Aharonov-Bohm quantization

As mentioned in the Introduction, in this sample, in the integer QH regime, the Aharonov-Bohm oscillations arise from the modulation of quantum interference of electron paths by magnetic flux Φ enclosed by the two counterpropagating edge channels, coupled by tunneling (Fig. 1). The edge channels follow the equipotentials of the edge depletion potential, where the resulting electron density is such that Landau level filling $\nu = \hbar n / eB \approx i=1$ (note that $\nu \propto n$ in a given B). These approximately circular electron island states are quantized by the Aharonov-Bohm condition of one state per Φ_0 per spin-polarized LL:

$$\Phi = BS_m = m\Phi_0, \quad (3)$$

where the azimuthal quantum number $m=0,1,2,\dots$, $\Phi_0=2\pi\hbar/e=h/e$, and S_m is the area enclosed by the m th electron state. This quantization follows from equating the Aharonov-Bohm Berry phase of the m th electron state to $2\pi m$, required for single-valued wave functions. In the low temperature, low excitation extreme quantum limit, the current is carried by electrons at the chemical potential μ , and each oscillation in R_{XX} signals the crossing of a single-electron quantized state with μ . Consequently, the Aharonov-Bohm oscillation period ΔB corresponds to a flux change by one Φ_0 through S_μ (the area enclosed by the electron state at μ):

$$S_\mu = \Phi_0 / \Delta B. \quad (4)$$

Thus determined S_μ are plotted in Fig. 4 for several V_{FG} .

In a magnetic field sweep, at a fixed V_{FG} , as discussed in the Introduction, the density of the electron states in each LL is proportional to B . The electron density is pretty much constant, because disturbing the electron density results in a huge charging energy. For example, if each of the 100 observed oscillations resulted from transfer of one electron to the island, the total charging by $100e$ would result in ~ 10 eV charging energy; if an $i=2$ ring containing 100 “extra” electrons were to form just within the $i=1$ edge channel, thus allowing shrinkage of S_μ , the charging energy would be ~ 2 eV, still enormous.

The chemical potential μ in the open island follows μ in the 2D bulk; LLs crossing μ results in de Haas-van Alphen and Shubnikov-de Haas oscillations. On a QH plateau, where the Aharonov-Bohm oscillations are observed, μ resides in the localized states between two LLs. The fixed number of N electrons occupying the nearly constant area S_μ is accomplished by creating localized LL quasiparticles or quasiholes within the island edge ring. The Aharonov-Bohm oscillations result from a quantized single-electron state crossing μ , which modulates the tunneling amplitude, accompanied by a microscopic electron population redistribution within S_μ .

Each oscillation corresponds to a change by one Φ_0 in the flux through S_μ , but at the higher field $B + \Delta B$ the area per Φ_0 is less; thus the area S_μ remains nearly constant, and the number of electrons within S_μ is constant too. Since the quantization condition Eq. (3) is equivalent to the increment by 2π of the Berry phase of the electron wave function, we recover the Aharonov-Bohm periodicity of the constructive-destructive interference.

With increasing V_{FG} , more electrons are attracted to the 2DES island and the constrictions. Since tunneling amplitude is exponentially sensitive to the tunneling distance, the position of the tunneling links at the saddle points in the constrictions is nearly fixed, but the electron density n_C at these positions increases with increasing V_{FG} . Accordingly, in order to remain on the $i=1$ QH plateau, the applied B must be increased. Within the island, the edge channels must follow the constant electron density contours with density equal that in the constrictions, n_C , and move outward, away from the island center. This edge channel density increase is confirmed by the shift to higher B of the midpoint of the range of the Aharonov-Bohm oscillations: $n(r_\mu) \approx B_M / \Phi_0$ at QH filling $i=1$, where r_μ is the radius of the electron orbit at μ . The B_M vs V_{FG} dependence is shown in the inset of Fig. 4; the slope $dB_M/dV_{FG}=1.77$ T/V corresponds to $dn(r_\mu)/dV_{FG}=4.3 \times 10^{14}$ 1/m²V. Similarly, the area S_μ is expected to increase with increasing V_{FG} because of reduced mesa depletion. An approximately linear dependence of S_μ on V_{FG} is indeed obtained from the Aharonov-Bohm period ΔB , see Fig. 4, the slope $dS_\mu/dV_{FG}=1.44 \times 10^{-12}$ m²/V.

Reference 5 reported and analyzed Aharonov-Bohm oscillations observed in a Coulomb Island of lithographic radius $R=750$ nm, separated from the 2D bulk by two narrow (300 nm wide) point contacts, showing conductance steps at $B=0$. The gates were deposited on GaAs surface, with no etch trenches; a fixed negative V_{FG} was applied to produce the confining potential. The analysis of Ref. 5 invoked a large negative correction to the Aharonov-Bohm period, Eq. (4), which was justified by a seemingly strong dependence of the product $i\Delta B$ on the island QH filling i , assumed equal to that in the bulk. Actually, from the data in Figs. 2 and 3 and the text of Ref. 5, it is clear that the island edge ring filling was ~ 1.7 times smaller than in the bulk. Accordingly, the Aharonov-Bohm oscillations regions centered on $B=5.1, 2.6, 1.85$, and 1.4 T should be identified as belonging to the $i=1, 2, 3$, and 4 QH plateaus, respectively. Using this filling factor assignment, the corresponding periods $\Delta B=5.3, 2.7, 2.0$, and 1.3 mT scale well, so that the product $i\Delta B \approx 5.4$ mT is constant (within the experimental uncertainty). This yields the area $S_\mu = \Phi_0 / i\Delta B = 7.6 \times 10^{-13}$ m² and the radius $r_\mu = 495$ nm, values independent of i and reasonable. The $i=1, 2$, and 4 Aharonov-Bohm oscillations reported¹⁹ for the device of Ref. 3 also yield a constant product $i\Delta B \approx 2.7 \pm 0.1$ mT. This analysis involves no correction to our Eq. (4) due to the confining potential.

C. The front gate voltage period

Although not done in experiments reported here, in principle it is possible to sweep front gate voltage V_{FG} continu-

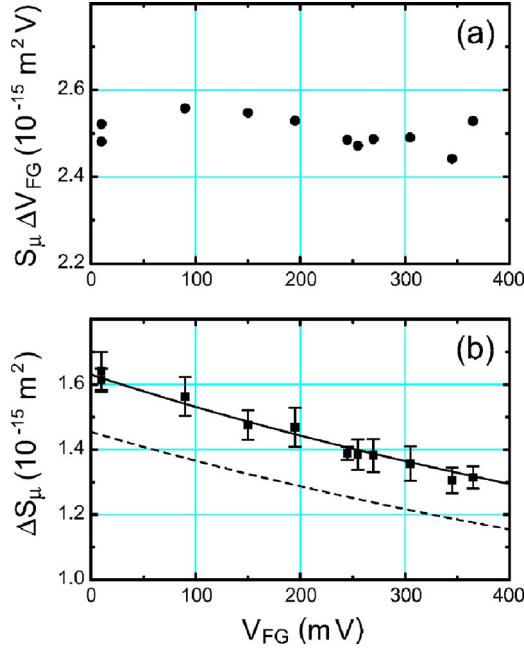


FIG. 5. (Color online) (a) Dependence of the product $S_\mu \Delta V_{FG}$ on V_{FG} , where the increment ΔV_{FG} induces one more electron within the area S_μ at a fixed B . The product $S_\mu \Delta V_{FG}$ is constant within $\pm 2\%$ in the range of V_{FG} from 0 to 400 mV, while S_μ increases by 27% in the same range (Fig. 4). (b) One electron state area ΔS_μ vs V_{FG} . The squares with error bars (ΔS_μ) are determined from the experiment as $\Phi_0/B_M = 2\pi\ell^2$, Eq. (5), while the solid line (ΔS_μ^*) is obtained from the fit of the experimental Aharonov-Bohm periods ΔB , Eq. (7). The dashed line gives ΔS_μ calculated by integrating the edge depletion model electron density profile with no adjustable parameters. The 13% discrepancy between the model calculation and the experiment is surprisingly small, considering the several approximations made and the idealized, simplified geometry of the model.

ously (at a fixed B). We denote ΔV_{FG} the expected period, which induces a change $\Delta N = 1$ in the number of electrons N within S_μ . Application of ΔV_{FG} results in a change ΔS_μ , which can be linearized as $\Delta S_\mu = (dS_\mu/dV_{FG})\Delta V_{FG}$ for large $N \gg 1$ (in this device $N \approx 2000$). Since the area ΔS_μ can be occupied by precisely one electron per spin-polarized Landau level, ΔS_μ can be identified with the area between consecutive quantized electron orbits $S_{m+1} - S_m$ in the vicinity of μ . Hence, from the Aharonov-Bohm quantization condition Eq. (3), substituting B_M for B :

$$\Delta S_\mu = \Phi_0/B_M. \quad (5)$$

Note that Eq. (5) simply gives $\Delta S_\mu = 2\pi\ell^2$ with magnetic length corresponding to B_M . Combining these two expressions for ΔS_μ , we get an expression for ΔV_{FG} in terms of experimentally obtained quantities:

$$\Delta V_{FG} = \Phi_0/(dS_\mu/dV_{FG})B_M. \quad (6)$$

We calculated ΔV_{FG} using the experimental value of dS_μ/dV_{FG} and the values of B_M (see Fig. 4). We find that ΔV_{FG} decreases with increasing V_{FG} , but the product $S_\mu \Delta V_{FG}$ is approximately constant, independent of V_{FG} (within the

experimental uncertainty of 2%), see Fig. 5(a). The product $S_\mu \Delta V_{FG}$ is proportional to the inverse integrated compressibility of the 2D electrons in the island: $dn/d\mu \propto dn/dV_{FG} \propto (dN/dV_{FG})/S_\mu = \Delta N/S_\mu \Delta V_{FG} = 1/S_\mu \Delta V_{FG}$. In this perspective, the constancy of $S_\mu \Delta V_{FG}$ is very fundamental: It stems from the fixed density of states in the island area encircled by the $i=1$ edge channel, that is, in one spin-split Landau level. The Aharonov-Bohm signal originates in the interference of electrons moving in the current-carrying edge channel. Under increasing positive V_{FG} , the edge channel radius increases, but, so long as the island remains on the $i=1$ plateau, the opening of the QH gap precludes population of the next Landau level in the interior of the island (recall that B is fixed). That is, the population of the island by additional electrons occurs by an enlargement of the edge channel radius, as opposed to the $B=0$ case, where additional electrons are induced throughout the area of the island.

The constancy of the product $S_\mu \Delta V_{FG}$ can also be viewed as a constant differential capacitance per unit area, $C/S_\mu = 64 \mu\text{F}/\text{m}^2$, where $C = dQ/dV = e/\Delta V_{FG}$ is the differential capacitance between the front gates and the 2D electron island. The effect must be quantum, since the classical island capacitance can be estimated to change by a factor of 1.5, from the data of Fig. 4. A constant differential capacitance in QH regime has been reported in quantum antidots²⁰ and in mesoscopic Si MOSFETs.²¹

Using the experimental fact that the product $S_\mu \Delta V_{FG}$ does not depend on V_{FG} , and the linearization $\Delta S_\mu = (dS_\mu/dV_{FG})\Delta V_{FG}$, we obtain:

$$\Delta S_\mu^*(V_{FG}) = \left. \frac{dS_\mu}{dV_{FG}} \right|_{V_{FG}} \frac{S_\mu(0)\Delta V_{FG}(0)}{S_\mu(V_{FG})}, \quad (7)$$

where $S_\mu(0)$ and $\Delta V_{FG}(0)$ are evaluated at $V_{FG}=0$. The asterisk in ΔS_μ^* serves to distinguish it from ΔS_μ calculated using Eq. (5). Equation (7) is of interest because it can be used to obtain ΔS_μ^* from entirely different experimental input, the dependence of the Aharonov-Bohm period ΔB on V_{FG} , than those used in Eq. (5), that is, the dependence of B_M (positions of QH filling $i=1$ in the island) on V_{FG} . The results obtained from these two routes are given in Fig. 5(b), where ΔS_μ^* (solid line) is calculated using the slope dS_μ/dV_{FG} of the linear dependence of S_μ on V_{FG} (Fig. 4) and $\Delta V_{FG}(0) = 1.13$ mV, Eq. (6). The error bars in ΔS_μ are most likely overestimated by taking an error in B_M equal to half the range of the magnetic field at which the oscillations occur. As can be seen, the agreement between ΔS_μ and ΔS_μ^* is very good, well within the error bars. This agreement confirms that the Aharonov-Bohm quantization condition, Eqs. (3) and (4), describes well the basic physics of the electron interferometer devices in the QH regime studied in this work and in Ref. 3.

D. Comparison to the edge depletion models

As stated in Sec. III A, the primary 2D electron confining potential is created by the depletion potential of the etch trenches. The resulting 2D electron density profile is affected by the electric field of the front gates. A relatively robust way

to evaluate the effect of V_{FG} on the electron island is to calculate ΔS_μ due to ΔV_{FG} , the voltage increment needed to attract one more electron to S_μ . To this end, we evaluate $n_{GH}(r)$ from Eq. (1), using the known heterostructure and lithographic parameters and dimensions as input. We then calculate $n(r, V_{FG}) = n_{GH}(r) F_{CSG}(r, V_{FG})$, using F_{CSG} from Eq. (2), where the V_{FG} -dependence is contained in $L \propto V_{FG}$ (for the present device, $L/V_{FG} = 0.23$ nm/mV). Such a calculation is not self-consistent, but, in the absence of a self-consistent result, is justified by: (i) In this paper, front gate voltage in the range of $0 < V_{FG} < 400$ mV is only a perturbation to the larger depletion effect of the etch trenches, and (ii) we use only $n(r, V_{FG})$ integrated over the area of S_μ , which excludes the low density tail of $n(r, V_{FG})$, and thus should reduce relative error due to nonself-consistency of the calculation, because such an error is larger for nearly depleted regions of small electron density.

Integrating $n(r, V_{FG})$ over the experimental Aharonov-Bohm area S_μ , we determine ΔV_{FG} such that the number of electrons within S_μ increments by one: $\Delta N = \int n(V_{FG} + \Delta V_{FG}) dS - \int n(V_{FG}) dS = 1$. In particular, we obtain $\Delta V_{FG}(0) = 1.01$ mV starting at $V_{FG} = 0$. Using Eq. (7), the increment $\Delta V_{FG}(0)$ gives the one electron state area ΔS_μ , shown by the dashed line in Fig. 5(b). The model calculation described above involves no adjustable parameters, has experimental input via S_μ , and uses an idealized device geometry. The surprisingly small difference (13%) between the experimental and the calculated ΔS_μ indicates that the CSG model adequately describes the effect of front gates on electron density profile for moderate V_{FG} .

IV. CONCLUSIONS

We reported electron quantum interference experiments on the $i=1$ quantum Hall plateau performed with an electron

interferometer device. When tunneling between edge channels occurs, in the quantum-coherent regime, Aharonov-Bohm oscillations with period ΔB were observed as a function of magnetic field B . In this regime, the electron states encircling the island are quantized by the Aharonov-Bohm condition: The magnetic flux through the area of the closed electron path at the chemical potential μ satisfies $\Delta \Phi = \Delta B S_\mu = \Phi_0$, where $\Phi_0 = h/e$. Each oscillation corresponds to a change by one Φ_0 in the flux through S_μ . Microscopically, each Landau level has one electron state per Φ_0 , and addition of flux Φ_0 leads to the outermost empty state crossing μ , that is, becoming occupied. Simultaneously, addition of Φ_0 to the interior of the island creates a hole state in the otherwise occupied LL. Thus the area S_μ remains nearly invariable, and the number of electrons within S_μ is constant, too. We experimentally determined the dependence of S_μ on the front gate voltage, and conclude that the Aharonov-Bohm quantization condition does not require significant corrections due to the confining potential. These results can be interpreted as a constant integrated compressibility of the island (on a quantum Hall plateau) with respect to the front gates. We also analyzed experimental results using two classical electrostatics models: One modeling the 2D electron density due to depletion from an etch trench, and another modeling the gate voltage dependence of the electron density profile in the island. We conclude that the models adequately describe the effect of front gates on electron density profile for moderate biases.

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