# **Frustrated magnetism in the two-dimensional triangular lattice of Li<sub>r</sub>CoO<sub>2</sub>**

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Magnetism of the simplest layered cobaltite  $Li<sub>x</sub>CoO<sub>2</sub>$  with  $x=1.0$ , 0.95, and 0.7 has been investigated by positive muon spin rotation and relaxation  $(\mu^+$ SR) spectroscopy together with magnetic susceptibility measurements, using polycrystalline samples in the temperature range between 300 and 1.8 K. Weak transverse field  $\mu$ <sup>+</sup>SR showed the appearance of magnetism below ~65 K (= $T_c^{\text{on}}$ ) for the sample with *x*=1.0. The volume fraction of the magnetic phase at 1.8 K is determined to be  $\sim$ 20% for LiCoO<sub>2</sub>, strongly suggesting that the observed magnetism is not induced by impurities but is an intrinsic behavior. This indicates that either a charge disproportionation  $(2Co^{3+} \rightarrow Co^{2+} + Co^{4+})$ , a spin state transition  $(t_{2g}^6 \rightarrow t_{2g}^5 e_g^1)$ , or an appearance of magnetic  $Co<sup>3+</sup>$  at surface occurs below 65 K. Zero field  $\mu$ <sup>+</sup>SR spectra of LiCoO<sub>2</sub> consist mainly of a slow relaxing signal due to random fields even at 1.8 K plus a small amount of a fast relaxing signal and an oscillating component, implying the presence of an antiferromagnetic order, as in the case of  $Na_{x}CoO_{2}$  with  $x \ge 0.75$ . For Li-deficient Li<sub>x</sub>CoO<sub>2</sub> samples,  $T_c^{on}$  decreases with decreasing x from 50 K for  $x=0.95$  to 25 K for  $x=0.7$ . The volume fraction of the magnetic phase is however almost independent of *x* and is estimated as 20% at 1.8 K, but no oscillations were observed in the zero field spectrum.

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## **I. INTRODUCTION**

Layered cobaltites with  $CoO<sub>2</sub>$  planes, in which Co ions form the two-dimensional triangular lattice 2DTL by the connection of edge-sharing  $CoO<sub>6</sub>$  octahedra, have been intensively investigated originally due to reversible insertion and extraction of  $Li^+$  in  $LiCoO_2$ ,<sup>1</sup> then due to good thermoelectric properties in  $Na<sub>x</sub>CoO<sub>2</sub>$  (Refs. 2–4) and  $\left[\text{Ca}_2\text{CoO}_3\right]_{0.62}\left[\text{CoO}_2\right],$ <sup>5-7</sup> and very recently due to superconductivity in  $\text{Na}_{0.35}\text{CoO}_2$  \* 1.3H<sub>2</sub>O.<sup>8–10</sup> Among several layered cobaltites,  $LiCoO<sub>2</sub>$  is doubtlessly the most basic compound, because  $Li<sup>+</sup>$  is the smallest alkali ion.  $LiCoO<sub>2</sub>$  belongs to the rhombohedral system (space group  $\overline{R3m}$ ) with the layered  $\alpha$ -NaFeO<sub>2</sub> structure, similarly to  $\gamma$ -Na<sub>x</sub>CoO<sub>2</sub>.

For stoichiometric LiCoO<sub>2</sub>, magnetic susceptibility  $(\chi)$ measurements, $11$  x-ray photoelectron spectroscopic (XPS) analysis, $12$  and band-structural calculations $13$  indicate that  $Co^{3+}$  ions are in a low spin state  $(t_{2g}^6)$  with  $S=0$  at ambient temperature. It is thus believed that  $LiCoO<sub>2</sub>$  does not exhibit magnetic transitions at low *T*. This was also confirmed by  $\chi$ and NMR experiment down to 4.2 K.<sup>14</sup> Although LiCoO<sub>2</sub> is known to be an insulator, Li deficient  $Li<sub>x</sub>CoO<sub>2</sub>$  with  $x=0.7-0.55$ , in which Li was removed/deintercalated by an electrochemical reaction similar to Li batteries, exhibits metallic behavior above 50 K.<sup>15</sup> In other words, as  $x$ decreases from 1, an insulator-to-metal transition was found at around  $x=0.95$  by resistivity ( $\rho$ ) measurements;  $\rho(275 \text{ K}) \sim 2000 \Omega \text{ cm}$  for LiCoO<sub>2</sub>, ~6  $\Omega \text{ cm}$  for  $Li_{0.96}CoO_2$ , and  $\sim$ 1  $\Omega$  cm for  $Li_{0.94}CoO_2$ . The lowest  $\rho$ (275 K) was observed in Li<sub>0.7</sub>CoO<sub>2</sub> to be ~33 m $\Omega$  cm. The value of  $\rho$ (275 K) increased with further lowering *x*, such as ~80 m $\Omega$  cm for Li<sub>0.55</sub>CoO<sub>2</sub>, although the  $\rho(T)$  curve was

almost independent of *T* for  $Li<sub>x</sub>CoO<sub>2</sub>$  with  $x \le 0.7$ .<sup>15</sup>

This behavior is well explained by hole doping in the triple degenerate  $t_{2g}$  states with decreasing *x*, because Li deintercalation increases Co valence, i.e., the population of  $Co<sup>4+</sup>$  ions. This is also consistent with the thermopower  $(II)$  measurements;<sup>15</sup> that is, at ambient temperature,  $\Pi$  ~ 190 μVK<sup>-1</sup> for LiCoO<sub>2</sub>, ~80 μV K<sup>-1</sup> for Li<sub>0.7</sub>CoO<sub>2</sub> and  $\sim$ 40  $\mu$ V K<sup>-1</sup> for Li<sub>0.6</sub>CoO<sub>2</sub>. Considering that  $\rho$  was measured using polycrystalline pellets, the transport properties of  $Li<sub>0.7</sub>CoO<sub>2</sub>$  seem to be almost comparable to those of  $\gamma$ -Na<sub>0.7</sub>CoO<sub>2</sub>, which is known to be a good thermoelectric material.<sup>8-10</sup>

In  $\text{Na}_x\text{CoO}_2$  with  $x \ge 0.75$ , a long-range magnetic order which is clearly incommensurate (IC) spin density wave (SDW) in single crystalline samples—was found at low temperatures by positive muon spin rotation and relaxation  $(\mu^+$ SR) experiments.<sup>17,18</sup> The existence of long-range magnetic order in Na<sub>x</sub>CoO<sub>2</sub> was reconfirmed later by not only  $\mu$ <sup>+</sup>SR (Ref. 19) but also neutron diffraction experiments.<sup>20</sup> This leads the question of magnetism of  $Li<sub>x</sub>CoO<sub>2</sub>$ , in particular for Li-deficient phases. Nevertheless, magnetism of  $Li<sub>x</sub>CoO<sub>2</sub>$  is, to the authors' knowledge, not fully investigated, in particular, there are no systematic studies of microscopic magnetism for Li-deficient phases at low temperatures.

Muon spin spectroscopy, as it is very sensitive to the local magnetic environment, yields crucial data in frustrated 2D layered cobaltites.<sup>16–18,21,22</sup> That is, only  $\mu$ <sup>+</sup>SR detected the appearance of a short-range magnetic order (IC-SDW state) in  $\left[\text{Ca}_2\text{CoO}_3\right]_{0.62}\left[\text{CoO}_2\right]$  below  $\sim$  100 K,<sup>21,22</sup> at which the  $\rho(T)$  curve exhibited a broad minimum, whereas susceptibility<sup>23</sup> and neutron diffraction experiments did not. This is because the  $\mu^+$  only feels the magnetic fields due to its nearest neighbors and is specially sensitive to short-range magnetic order which sometimes appears in low-dimensional systems, while both neutron scattering and  $\chi$  measurements mainly detect long-range magnetic order; if the correlation length is very short, neutron-diffraction peaks broaden and eventually disappear.

Here, we report on both weak (relative to the spontaneous internal fields in the ordered state) transverse-field (wTF)  $\mu$ <sup>+</sup>SR and zero field (ZF)  $\mu$ <sup>+</sup>SR, for polycrystalline Li<sub>x</sub>CoO<sub>2</sub> samples with  $x=1.0$ , 0.95 and 0.7 at temperatures between 1.8 and 300 K. The former method is sensitive to local magnetic order via the shift of the  $\mu^+$  spin precession frequency in the applied field and the enhanced  $\mu^+$  spin relaxation, while  $ZF-\mu^+SR$  is uniquely sensitive to weak local magnetic [dis] order in samples exhibiting quasistatic paramagnetic moments.

# **II. EXPERIMENT**

Polycrystalline  $LiCoO<sub>2</sub>$  was synthesized by a conventional solid state reaction technique using reagent grade  $Li<sub>2</sub>CO<sub>3</sub>$  and  $Co<sub>3</sub>O<sub>4</sub>$  powders as starting materials. The powders were thoroughly mixed in a ball mill using ethanol as solvent. After drying, the mixtures were calcined at 450 °C for 12 h in an air flow. After grinding, the calcined powder was pressed into a disk with 18 mm in diameter and 2 mm thick. The disk was sintered at 900 °C for 24 h in an  $O<sub>2</sub>$  gas flow and then furnace cooled to room temperature at a rate of 1 °C/min.

The Li-deficient samples of Li<sub>x</sub>CoO<sub>2</sub> with  $x=0.95$  and 0.7 were prepared by an electrochemical reaction at the University of Bordeaux using  $Li|LiClO<sub>4</sub>$ -ethylene carbonatedimethyl carbonate  $Li<sub>x</sub>CoO<sub>2</sub>$  cells. Powder x-ray diffraction  $(XRD)$  studies indicated that the samples of  $Li<sub>x</sub>CoO<sub>2</sub>$  with  $x=1.0$ , 0.95, and 0.7 were single phase with a rhombohedral system of space group  $R\overline{3}m$ . The preparation and characterization of the Li-deficient samples were reported in detail elsewhere.<sup>15</sup> An induction coupled plasma (ICP) analysis showed that the compositions (Li/Co ratio) of the samples were 1.034, 0.955, and 0.671, respectively.

Susceptibility  $(y)$  was measured using a superconducting quantum interference device (SQUID) magnetometer (mpms, Quantum Design) in the temperature range between 400 and 5 K under magnetic field  $H \le 55$  kOe. The  $\mu$ <sup>+</sup>SR experiments were performed on the M20 surface muon beam line at TRIUMF. The experimental setup and techniques were described elsewhere.<sup>24</sup>

# **III. RESULTS**

#### **A. Susceptibility**

Figure 1 shows the susceptibility  $\chi$  and inverse susceptibility  $\chi^{-1}$  of the present Li<sub>x</sub>CoO<sub>2</sub> powders as a function of temperature, measured in field-cooling (FC) mode with  $H = 10$  kOe. The  $\chi(T)$  curve in LiCoO<sub>2</sub> indicates a paramagnetic behavior down to 5 K, while the rapid increase in  $\chi$ below  $\sim$  50 K suggests the existence of localized moments, usually explained due to an undetected magnetic impurity (such as  $Co<sub>3</sub>O<sub>4</sub>$ ) and/or an imperfection of the crystal lattice.



FIG. 1. Temperature dependences of (a) magnetic susceptivility  $\chi$  and (b)  $\chi^{-1}$  for Li<sub>x</sub>CoO<sub>2</sub> with *x*=1, 0.95, and 0.7.  $\chi$  was measured in field-cooling FC mode with *H*= 10 kOe. In order to know the nature of the anomaly around 175 K, the  $\chi(T)$  curve in  $Li_{0.7}CoO_2$ measured in zero field cooling ZFC mode is also plotted in Fig.  $1(a)$ .

The origin of localized moments is discussed later.

On the other hand, for  $Li_{0.7}CoO_2$ , as *T* decreases from 300 K,  $\chi$  increases monotonically down to  $\sim$ 175 K and suddenly drops; then  $\chi$  decreases with decreasing the slope  $\left(\frac{d\chi}{dT}\right)$ down to  $\sim$ 100 K, and then  $\chi$  increases rapidly with further decreasing *T*. This behavior clearly indicates the existence of a magnetic transition around 175 K $(=T_m)$ . Since there is no marked difference between the data obtained in zero fieldcooling (ZFC) and FC mode, this is unlikely due to a transition to a ferromagnetic, ferrimagnetic or spin-glass state.

The  $\chi(T)$  curve in Li<sub>0.95</sub>CoO<sub>2</sub> is located between those in  $LiCoO<sub>2</sub>$  and  $Li<sub>0.7</sub>CoO<sub>2</sub>$ . It should be noted that the value of  $T_m$  in Li<sub>0.95</sub>CoO<sub>2</sub> is almost the same as for Li<sub>0.7</sub>CoO<sub>2</sub>, although the change in  $\chi$  at  $T_m$  of  $Li_{0.95}CoO_2$  is rather small compared with that of  $Li_{0.7}CoO_2$ . According to XRD and electrochemical analyses at room temperature, both  $Li_{0.95}CoO_2$  and  $Li_{0.7}CoO_2$  are a single phase. The present  $\chi$ measurement therefore may suggest a magnetic phase separation below  $T_m$  in the Li deficient samples.

Assuming that only  $Co<sup>3+</sup>$  and  $Co<sup>4+</sup>$  moments are responsible for the paramagnetic behavior of  $\chi$  at temperatures above  $T_m$ , the Curie-Weiss law in the general form is written as

$$
\chi = \frac{N\mu_{\text{eff}}^2}{3k_{\text{B}}(T - \Theta_p)} + \chi_0,\tag{1}
$$

where  $N$  is the number density of Co ions (per unit gram),  $\mu_{\text{eff}}$  is the effective magnetic moment of Co ions,  $k_B$  is the Boltzmann's constant, *T* is the absolute temperature,  $\Theta_p$ is the paramagnetic Curie temperature, and  $\chi_0$  is the temperature-independent susceptibility. Using Eq. (1) over the temperature range above 70 K for  $LiCoO<sub>2</sub>$  and above 180 K for  $Li_{0.95}CoO_2$  and  $Li_{0.7}CoO_2$ , we obtain the values for  $\mu_{eff}$ and  $\Theta_p$  for the Li<sub>x</sub>CoO<sub>2</sub> samples given in Fig. 2.



FIG. 2. (a) Effective magnetic moment of Co ions  $(\mu_{eff})$  and (b) paramagnetic Curie temperature  $(\Theta_p)$  as a function of Li content *x* in  $Li_xCoQ_2$ . Three solid lines in Fig. 2(a) represent the change in  $\mu_{\text{eff}}$  =g $\sqrt{S(S+1)}\mu_B$  and g=2] caused by the increase in Co<sup>4+</sup> ions with  $S = 5/2$ ,  $3/2$ , and  $1/2$ , respectively.

The values of  $\mu_{\text{eff}}$  and  $\Theta_p$  are found to be approximately 0 for LiCoO2. This is in good agreement with the results of several studies on  $LiCoO<sub>2</sub>$ ; that is,  $Co<sup>3+</sup>$  ions in  $LiCoO<sub>2</sub>$  are in a low spin state  $(t_{2g}^6, S=0)$ . For the Li deficient samples, as *x* decreases from 1,  $\mu_{\text{eff}}$  increases almost linearly, while  $\Theta_p$ decreases. If we assume  $S=0$  for  $Co^{3+}$  in  $Li<sub>x</sub>CoO<sub>2</sub>$ , the slope of the  $\mu_{\text{eff}}$  vs *x* curve is well explained by the increase in Co<sup>4+</sup> ions in a high spin state  $(t_{2g}^3 e_g^2, S=5/2)$ , and is difficult to fit by Co<sup>4+</sup> ions in an intermediate  $(t_{2g}^4 e_g^1, S=3/2)$  and/or low spin state  $(t_{2g}^5, S=1/2)$ . The transition at  $T_m$  is therefore likely due to a spin state transition of  $Co<sup>4+</sup>$  ions in the Li deficient samples. This could indicate the possibility that the  $Co<sup>4+</sup>O<sub>6</sub>$  octahedra are locally distorted into prisms, as in the case of the one-dimensional  $CoO_3$  chains in  $Ca_3Co_2O_6$ .<sup>25</sup> On the other hand, the magnitude of  $\Theta_p$  for the  $Li_{0.7}CoO_2$ sample indicates a strong AF interaction between Co spins in 2DTL, suggesting large geometrical frustration in  $Li_{0.7}CoO_2$ at low *T*.

#### $B. wTF- $\mu$ <sup>+</sup>SR$

The wTF- $\mu$ <sup>+</sup>SR spectra in a magnetic field of  $H \sim 90$  Oe in the three  $Li<sub>x</sub>CoO<sub>2</sub>$  samples exhibit a clear reduction of the  $\mu^+$  precession paramagnetic amplitude below  $\sim$  50 K. The wTF- $\mu$ <sup>+</sup>SR spectra below  $\sim$  50 K were well fitted in the time domain with a combination of a slowly relaxing precessing signal due to the external field and a fast nonoscillatory signal inferring either a fluctuating field or a static random field, as in the case of the other layered cobaltites:  $16,18,21,22$ 

$$
A_0 P(t) = A_{\text{TF}} \exp(-(\lambda_{\text{TF}} t)^{\beta_{\text{TF}}}) \cos(\omega_{\mu} t + \phi)
$$
  
+  $A_{\text{fast}} \exp(-\lambda_{\text{fast}} t),$  (2)

where  $A_0$  is the initial asymmetry,  $P(t)$  is the muon spin polarization function,  $\omega_{\mu}$  is the muon Larmor frequency,  $\phi$  is the initial phase of the precession,  $A_n$  and  $\lambda_n$  (*n*=TF and fast)



FIG. 3. Temperature dependences of (a)  $A_{\text{TF}}$  and  $A_{\text{fast}}$ , (b)  $\lambda_{\text{TF}}$ and  $\lambda_{\text{fast}}$ , and (c) the power of the exponential relaxation  $\beta_{\text{TF}}$ , (d) the shift of the muon precession frequency  $\Delta\omega_{\mu}$ , and (e) the inverse susceptibility  $\chi^{-1}$  in a polycrystalline LiCoO<sub>2</sub> sample. The data were obtained by fitting the wTF- $\mu$ <sup>+</sup>SR spectra with Eq. (2).

are the asymmetries and exponential relaxation rates of the two signals, and  $\beta_{\text{TF}}$  is the power of the exponential relaxation. The power exponential (or stretched exponential) function suggests wide distribution of the relaxation rate, if  $\beta_{\text{TF}} \neq 1$ . The nonoscillatory signal (*n*=fast) has finite amplitudes below  $\sim$  50 K.

Figures 3, 4, and 5 show the temperature dependences of  $A_n$ ,  $\lambda_n$  (*n*=TF and fast),  $\beta_{TF}$ , the shift of  $\omega_\mu(\Delta \omega_\mu)$  and  $\chi^{-1}$  in the polycrystalline LiCoO<sub>2</sub>, Li<sub>0.95</sub>CoO<sub>2</sub>, and  $Li_{0.7}CoO_2$  samples. Here,  $\Delta \omega_{\mu}$  is defined as  $[\omega_{\mu}(T)]$  $-\omega_{\mu}$ (300 K)]/ $\omega_{\mu}$ (300 K); but since a reference sample was not measured,  $\Delta \omega_{\mu}$  is not equivalent to the muonic Knight shift.

For LiCoO<sub>2</sub>, as *T* decreases from 300 K,  $A_{TF}$  is constant at its maximum value  $(\sim 0.24)$  down to 50 K, indicating that the sample volume is 100% paramagnetic. Then,  $A_{TF}$  drops at 50 K with further decreasing  $T$ , and  $A_{TF}$  seems to level off to  $\sim$ 0.19 below 20 K. On the other hand,  $A<sub>fast</sub>$  increases monotonically with decreasing *T* below 50 K up to  $\sim$  0.05 at 1.8 K. This indicates the existence of a magnetic transition with an onset temperature  $T_c^{\text{on}} \sim 50 \text{ K}$  and a transition width  $\Delta T \sim 30$  K in LiCoO<sub>2</sub> with volume fraction of the magnetic phase  $(V_F)$  roughly estimated as  $\sim$  20% even at 1.8 K. Interestingly, the transition around 50 K is not detected by  $\chi$  and NMR experiments.<sup>13</sup> Here, it should be noted that all components of the muon spin signal are observed even at 1.8 K,



FIG. 4. Temperature dependences of (a)  $A_{\text{TF}}$  and  $A_{\text{fast}}$ , (b)  $\lambda_{\text{TF}}$ and  $\lambda_{\text{fast}}$ , and (c) the power of the exponential relaxation  $\beta_{\text{TF}}$ , (d) the shift of the muon precession frequency  $\Delta\omega_{\mu}$ , and (e) the inverse susceptibility  $\chi^{-1}$  in a polycrystalline Li<sub>0.95</sub>CoO<sub>2</sub> sample. The data were obtained by fitting the wTF- $\mu$ <sup>+</sup>SR spectra with Eq. (2).

because  $A_{\text{TF}}(1.8 \text{ K}) + A_{\text{fast}}(1.8 \text{ K}) \sim A_{\text{TF}}(300 \text{ K}).$ 

As *T* decreases from 300 K,  $\lambda_{TF}$  is almost constant  $(\sim 0.15$  MHz) down to 80 K, then increases with further decreasing *T*. At temperatures below 300 K,  $\beta_{\text{TF}}$  decreases monotonically with decreasing *T* down to 50 K, and then increases and levels off to a constant value below 20 K. The magnitude of  $\lambda_{\text{fast}}$  increases with decreasing *T* below 50 K (where it is first detected), and reaches  $\sim$  41 MHz at 1.8 K, which is  $\sim$ 150 times larger than  $\lambda_{TF}$ (1.8 K).

For the Li deficient sample  $Li_{0.7}CoO_2$ , the  $\lambda_{TF}(T)$ ,  $\beta_{TF}(T)$ , and  $\Delta \omega_{\mu}(T)$  curves exhibit a clear change in their slope at 170 K, where the magnetic transition was found by the  $\chi(T)$ measurement, while  $A_{TF}$  remains at 0.24 down to 25 K (see Fig. 5). This indicates that  $Li_{0.7}CoO_2$  is still paramagnetic below 170 K. The transition is therefore attributed to the spin state transition of the  $Co<sup>4+</sup>$  ions from the low-temperature low-spin (or mixture of low- and intermediate-spin) state to the high-temperature high-spin state, as in the case of the related cobaltites  $\left[Ca_2CoO_3\right]_{0.62}^{RS}\left[CoO_2\right]_{0.2}^{21,22}$  This is consistent with the result of the present  $\chi$  measurement above described.

Furthermore, the decrease in  $A_{TF}$  below 25 K (and the accompanying increase in  $\lambda_{\text{TF}}$ ) indicate the existence of a magnetic transition with  $T_c^{\text{on}} \sim 25 \text{ K}$  in Li<sub>0.7</sub>CoO<sub>2</sub>. This also suggests that the magnetic transition at low-*T* is a common behavior in the layered cobaltites and  $T_c^{\text{on}}$  is strongly dependent on the valence of Co ions.



FIG. 5. Temperature dependences of (a)  $A_{\text{TF}}$  and  $A_{\text{fast}}$ , (b)  $\lambda_{\text{TF}}$ and  $\lambda_{\text{fast}}$ , (c) the power of the exponential relaxation  $\beta_{\text{TF}}$ , (d) the shift of the muon precession frequency  $\Delta \omega_{\mu}$ , and (e) the inverse susceptibility  $\chi^{-1}$  in a polycrystalline Li<sub>0.7</sub>CoO<sub>2</sub> sample. The data were obtained by fitting the wTF- $\mu$ <sup>+</sup>SR spectra with Eq. (2).

In order to understand the effect of  $x$  on the wTF- $\mu$ SR results, Fig. 6 shows the normalized  $A_{\text{TF}}(N_{A_{\text{TF}}})$  and  $\lambda_{\text{TF}}$  as a function of *T* below 150 K for the three samples. Here,  $N_{A_{\text{TF}}}$ is defined as  $A_{TF}(T)/A_{TF}(300 \text{ K})$  and roughly measures the volume fraction of paramagnetic phases in the sample. As *x*



FIG. 6. Comparison of (a) normalized  $A_{\text{TF}}[=A_{\text{TF}}(T)/$  $A_{\text{TF}}(300 \text{ K})$ ] and (b)  $\lambda_{\text{TF}}$  as a function of *T* for the three  $\text{Li}_x\text{CoO}_2$ samples with *x*= 1.0, 0.95, and 0.7.



FIG. 7. ZF- $\mu$ <sup>+</sup>SR time spectra at 1.8 K for the three Li<sub>x</sub>CoO<sub>2</sub> samples with  $x=1$ , 0.95, and 0.7 in the time domain below 1  $\mu$ s. Only in the top spectrum for  $LiCoO<sub>2</sub>$ , a first minimum around 70 ns and a first maximum around 130 ns are clearly seen. The top two spectra are each shifted upwards by 0.1 for clarity of the display.

decreases from 1.0 to 0.7, the onset transition temperature  $T_c^{\text{on}}$  decreases  $\sim$  65, 50, and 25 K with decreasing *x*, while the values of  $N_{A_{\text{TF}}}$  are all around 0.8 at 1.8 K, i.e., the volume fraction of the magnetic phase is independent of *x*.

## $C. ZF- $\mu$ <sup>+</sup>SR$

Figures 7 and 8 show ZF- $\mu$ <sup>+</sup>SR time spectrum at 1.8 K for the three samples of  $Li_xCoO_2$  ( $x=1$ , 0.95, and 0.7). The three spectra exhibit a clear fast relaxation in the time domain below  $\sim$  50 ns (Fig. 7) caused by Co 3*d* spins, although the main signal shows a slow relaxation with a minimum at around  $4-6$   $\mu$ s (Fig. 8) due to nuclear moments. In other



FIG. 8. ZF- and LF- $\mu$ <sup>+</sup>SR time spectra at 1.8 K for the three  $Li<sub>x</sub>CoO<sub>2</sub>$  samples with  $x=1$ , 0.95, and 0.7 at 1.8 K in the time domain below 10  $\mu$ s. The top LF spectrum for LiCoO<sub>2</sub> indicates the static nature of field distribution in the sample. The spectra are each shifted upwards by 0.14 for clarity of the display.

words, the ZF spectra indicate that the three samples are almost paramagnetic even at 1.8 K, while a small fraction of them enters into a magnetic phase, as well as the wTF- $\mu$ <sup>+</sup>SR measurement [see Fig. 6(a)].

In the top spectrum of Fig. 7, a first minimum around 70 ns and a first maximum around 130 ns are clearly seen as a strongly damped cosine oscillation, indicating a formation of quasistatic antiferromagnetic (AF) internal fields in  $LiCoO<sub>2</sub>$ . However, the oscillation is also well reproduced by a zerothorder Bessel function of the first kind  $J_0(\omega_\mu t)$  that describes the muon polarization evolution in an IC-SDW field distribution.<sup>24,26,27</sup> We therefore cannot refuse the possibility of an IC-SDW order in the sample.

The full spectrum was fitted using a combination of the following three signals: an exponential relaxing cosine oscillation, a dynamic Gaussian Kubo-Toyabe function  $G^{DGKT}(t,\Delta,\nu)$  (for the signal from other muon sites experiencing fluctuating disordered magnetic fields due to nuclear moments), and an exponential relaxation from fluctuations of the longitudinal components

$$
A_0 P(t) = A_{AF} \cos(\omega_{AF} t + \phi) e^{-\lambda_{AF} t} + A_{KT} G^{DGKT}(t, \Delta, \nu)
$$
  
+ 
$$
A_x e^{-\lambda_x t},
$$
 (3)

where  $A_0$  is the empirical maximum muon decay asymmetry,  $A_{AF}$ ,  $A_{KT}$ , and  $A_x$  are the asymmetries associated with the three signals,  $\lambda_{AF}$  and  $\lambda_x$  are their relaxation rate,  $\Delta$ is the static width of the local frequencies at the disordered sites, and  $\nu$  is the field fluctuation rate. When  $\nu=0$ ,  $G^{DGKT}(t,\Delta,\nu)$  is the static Gaussian Kubo-Toyabe function  $G_{zz}^{\text{KT}}(t,\Delta)$  given by

$$
G_{zz}^{\text{KT}}(t,\Delta) = \frac{1}{3} + \frac{2}{3}(1 - \Delta^2 t^2)e^{-\Delta^2 t^2/2}.
$$
 (4)

The longitudinal field  $(LF)$  spectrum with  $H=80$  Oe shows that such relaxation is mainly caused by a quasistatic but disordered weak field distribution in the sample (see the top spectrum in Fig. 8), implying that  $\nu \sim 0$ . This is because the applied LF competes with the internal random field distribution and aligns the muon spins in its original direction. As a result, if we ignore the fast relaxed component due to the AF field, the LF spectrum seems to be almost independent of time. This also suggests that the  $A<sub>x</sub>$  signal is likely to be induced by a static random field caused by Co spins. In order to further elucidate the nature of the  $A<sub>x</sub>$  signal, more precise work is needed, in particular, using a single crystal sample to eliminate the effect of randomly oriented grains.

Figures  $9(a) - 9(e)$  show the temperature dependences of (a)  $f_{AF}$ , (b)  $\lambda_{AF}$ , (c)  $\lambda_x$ , (d)  $A_{AF}$ ,  $A_{KT}$ , and  $A_x$ , and (e)  $\Delta$  and  $\nu$ for the  $(x=1.0)$ LiCoO<sub>2</sub> sample. The muon precession frequency  $(f_{AF})$  in the local magnetic field  $H_{int}$  due to the AF is given by

$$
\omega_{\mu} \equiv 2\pi f_{\text{AF}} = \gamma_{\mu} H_{\text{int}},\tag{5}
$$

where  $\gamma_{\mu}$  is muon gyromagnetic ratio. As *T* increases from 1.8 K,  $f_{AF}$  is almost independent of *T* up to  $\sim$  25 K, and then, abruptly decreases towards 0 with further increasing *T*. The change around 25 K is too steep for the prediction in order parameter of the two-dimensional Ising model for the AF



FIG. 9. (Color online) Temperature dependences of (a)  $f_{AF}$ , (b)  $\lambda_{AF}$  (c)  $\lambda_x$ , (d)  $A_{AF}$ ,  $A_{KT}$ , and  $A_x$ , and (e)  $\Delta$  and  $\nu$  for the LiCoO<sub>2</sub> sample. The data were obtained by fitting the  $ZF-\mu$ <sup>+</sup>SR spectra with Eq. (3). The solid line in (a) represents the temperature dependence of order parameter of the two-dimensional Ising model and broken line the BCS gap energy. Small solid circles in (a) and (b) were obtained from the ZF spectra measured in the time domain below  $3 \mu s$ , to know the change in  $f_{AF}$  in detail. Small open circles in (a) and (b) are the data obtained for the samples from the other source.

state<sup>28</sup> or the BCS gap energy for the SDW state,<sup>29</sup> in contrast to the  $f_{SDW}(T)$  curve for  $Na_{x}CoO_{2}$ , which is well explained by BCS.17,18 Such abrupt change in the order parameter indicates a transition at  $\sim$ 30 K (= $T_N$ ). Considering a



FIG. 10. Temperature dependences of  $\Delta$  for the three  $Li<sub>x</sub>CoO<sub>2</sub>$ samples. The data were obtained by fitting the  $ZF-\mu$ <sup>+</sup>SR spectra with Eq.  $(3)$ .



FIG. 11. (Color online) Crystal structures of  $LiCoO<sub>2</sub>$  and  $A_x \text{CoO}_2$  ( $A = \text{Na}$ , K, Rb, and Cs) in hexagonal unit cell.

small volume fraction of the magnetic phase, it is not surprising that the past measurements failed to detect the AF transition.

In order to confirm the existence of the ordered state in  $LiCoO<sub>2</sub>$ , a powder sample from the other source (Kusaka Rare Metal Labs.) was also checked by  $ZF-\mu^+SR$ . The result, shown by small open circles in Figs.  $9(a)$  and  $9(b)$ , clarifies that the AF ordered state is an intrinsic behavior for  $LiCoO<sub>2</sub>$ .

The  $\lambda_{AF}(T)$  curve exhibits a sharp maximum at  $T_N$  and decreases with decreasing *T* showing a critical behavior at the transition. Although the AF signal appears below  $T_N$ , a slow exponential relaxation signal is observed even at 120 K; that is,  $\lambda_x$  is ~0.1×10<sup>6</sup> s<sup>-1</sup>, which is consistent with the wTF measurement. The value of  $\lambda_x$  increases with decreasing *T* down to 30 K, and then decreases with further lowering *T*. In other words, the  $\lambda_x(T)$  curve is similar to the  $\lambda_{AF}(T)$ curve below  $T_N$ .

The volume fraction  $(V_F)$  of the AF phase is estimated as 9% at 1.8 K  $\left[=A_{AF}/(A_{AF}+A_{KT}+A_{x})\right]$ , and  $V_F$  for the phase showing the exponential relaxation signal  $(A_x)$  as 8%. The total  $V_F$  for the magnetic phases is thus 17% and is in good agreement with the rough estimation from the wTF measurement [see Fig.  $6(a)$ ].

For the dynamic Kubo-Toyabe signal,  $\Delta$  is almost independent of *T* below 120 K, while the  $\nu(T)$  curve shows a critical change between 30 and 60 K. That is,  $\nu$  is very small (below  $0.1 \times 10^6$  s<sup>-1</sup>) below 30 K, as expected from the LF- $\mu$ SR spectrum, while  $\nu \sim 0.5 \times 10^6$  s<sup>-1</sup> above 60 K, indicating that the internal random field is fluctuating above 60 K. This is consistent with the past  $\mu$ SR work on LiCoO<sub>2</sub> measured in the  $T$  range between 460 and 100 K by Dalmas *et al.*;<sup>30</sup> i.e., the ZF spectrum was well fitted by a dynamic Kubo-Toyabe function and  $\Delta$  was almost constant  $(0.4 \text{ mT} = 0.36 \times 10^6 \text{ s}^{-1})$  between 100 and 260 K. Above 260 K,  $\Delta$  decreased linearly with increasing *T* up to 460 K  $(\Delta = 0.28 \text{ mT} = 0.25 \times 10^6 \text{ s}^{-1}$  at 460 K). Finally, Fig. 10 shows the  $\Delta(T)$  curve for the Li<sub>x</sub>CoO<sub>2</sub> samples with *x*=1.0, 0.95, and 0.70. It is found that Li deficiency reduces  $\Delta$  in the whole *T* range measured, suggesting that Li nuclear magnetic moments play a significant role for determining  $\Delta$ .

# **IV. DISCUSSION**

#### **A. Origin of magnetism in LiCoO2**

The past  $\chi$  measurements, XPS analysis and bandstructural calculations indicate that  $Co<sup>3+</sup>$  ions are in a low spin state  $(t_{2g}^6)$  with *S*=0 at ambient temperature.<sup>11–13</sup> We therefore propose the following two hypothesis, in order to explain the experimental results, in particular, the appearance of magnetism below 60 K in  $LiCoO<sub>2</sub>$ .

(1) Charge disproportionation. Although Co ions are surrounded by six  $O^{2-}$  ions to form CoO<sub>6</sub> octahedra, the valence state of Co ions would still be strongly affected by the nearest neighboring Li ions. The Co valence is therefore considered to be partially fluctuating as  $2Co^{3+} \rightarrow Co^{2+} + Co^{4+}$  according to thermal vibration and/or self diffusion of Li ions. Past works on rocksalt-type CoO (Refs. 31 and 32) suggest that Co<sup>2+</sup> ions are in a high spin state with  $S=3/2$  ( $t_{2g}^5e_g^2$ ), whereas  $\text{Co}^{4+}$  in a low spin state with  $S=1/2(t_{2g}^5)$  at  $\lim_{x \to 0} T$ . Both the different spin state and orbital symmetry  $(t_{2g}$  and  $e_g$ ) and coexisting Co<sup>3+</sup> ions with *S*=0 naturally induces wide distribution of the magnetic field at the  $\mu^+$  sites, which would be a reason for strong damping of the cosine oscillation (see Fig.  $7$ ).

For Li-deficient samples, such deficiency itself stabilize both  $Co<sup>3+</sup>$  and  $Co<sup>4+</sup>$  states in order to maintain charge neutrality. Since the Li deficiency also increases the average valence of Co ions,  $Co<sup>2+</sup>$  ions are unlikely to exist in the sample.

(2) Spin state transition. Czyżyk et al. reported that the gap energy, which corresponds to the splitting between  $t_{2g}$ and  $e_g$  Co *d* states  $(10D_q)$ , was calculated to be 1.2 eV by LDA,<sup>13</sup> whereas it was measured as  $2.7 \pm 0.3$  eV by XPS at ambient *T*. <sup>12</sup> In spite of the relatively large gap energy reported, the present work suggests that the spin state of  $Co<sup>4+</sup>$ ions changes around 170 K. The existence of spin state transitions were also reported for the other thermoelectric layered cobaltites; such as,  $\text{Na}_x\text{CoO}_2$ ,<sup>33</sup> (Na, Ca)<sub>x</sub>CoO<sub>2</sub>,<sup>34</sup> and  $\text{[Ca}_2\text{CoO}_3\text{]}_{0.62}\text{[CoO}_2\text{]}^{0.6,21,22}$ 

On the contrary, the small  $10D_q$ , which induces the spin state transition at finite *T*, is considered to be an essential factor for explaining large thermopowers  $(II)$  in layered cobaltites.<sup>35</sup> Actually, the threefold degenerate  $t<sub>2</sub>$ , Co *d* states are further split in the rhombohedral crystal field (due to a rhombohedral distortion of  $CoO<sub>6</sub>$  octahedra in the  $CoO<sub>2</sub>$ plane) into a nondegenerate  $a_{1g}$  and doubly degenerate  $e'_{g}$ states. As a result, the spin state transition is thought to be favored in the layered cobaltites. Since the split between  $a_{1g}$ and  $e'_{g}$  depends on the rhombohedral distortion of  $CoO_{6}^{36}$  a spin state of  $Co^{3+}$  in LiCoO<sub>2</sub> would vary from a low-spin state  $(t_{2g}^6)$  to an intermediate-spin state  $(t_{2g}^5 e_g^1 = e_g'^4 a_g^1 e_g^1)$  at low *T* without a structural phase transition.

(3) Surface magnetism. Since we used polycrystalline samples,  $\mu$ <sup>+</sup>SR provides information concerning not only inside but also surface of particles. There is therefore the possibility that only the surface layer would be magnetic, while the rest (inside) nonmagnetic. This is because the change (decrease) in oxygen-coordination number at surface  $Co<sup>3+</sup>$ ions could stabilize higher spin states  $(S=1 \text{ or } S=2)$ , as recently proposed for  $LaCoO<sub>3</sub>$ .<sup>37</sup> Also, charge disproportionation mentioned above would be favored at surface, to minimize surface energy.

In order to elucidate the effect of surface on magnetism,  $\mu$ <sup>+</sup>SR experiments on single crystals are desirable, although large single crystals are currently unavailable; i.e., the maximum size of crystals grown by a flux technique is about  $0.15 \times 0.15 \times 0.01$  mm<sup>3</sup>.<sup>38</sup> It is thus not impossible but very difficult to measure  $\mu$ <sup>+</sup>SR spectra for LiCoO<sub>2</sub> crystals, at present.

First two hypotheses generate  $t_{2g}$  holes which play a significant role in the magnetic and transport properties of the layered cobabltites. Here we wish to comment on a domeshaped magnetic phase diagram in the layered cobaltites, proposed by us.17,18 In order to determine the diagram of  $Na<sub>x</sub>CoO<sub>2</sub>$ , we used the past result that  $LiCoO<sub>2</sub>$  is a paramagnet down to the lowest *T* measured. A magnetic transition is however observed in  $LiCoO<sub>2</sub>$  below 65 K. This suggests that similar behavior would be detected in  $NaCoO<sub>2</sub>$ . Therefore the dome-shaped phase diagram of  $\text{Na}_{x}\text{CoO}_{2}$  should be further investigated for  $0.9 \le x \le 1.0$ .

#### **B. Magnitude of internal magnetic field**

Since the AF states are induced by the competition between AF correlation and geometrical frustration in the  $CoO<sub>2</sub>$  $2DTL$ ,<sup>39–41</sup> the nature of the ordered state in  $LiCoO<sub>2</sub>$  is considered to be essentially the same as in  $Na<sub>x</sub>CoO<sub>2</sub>$ , whose internal magnetic field in the ordered state, corresponded to a frequency  $f_{\mu}$ (0 K) ~ 3 MHz. Assuming that the  $\mu$ <sup>+</sup>s in  $A_x$ CoO<sub>2</sub> (A=Li and Na) locate in the vacant sites in the *A* plane,  $f_{\mu}$ (0 K) should depend on the distance  $d_{A-C_0}$  between the Li/Na layers and CoO<sub>2</sub> planes. The ratio of *d*<sub>Li−Co</sub>/*d*<sub>Na−Co</sub> is about 0.86, although the *c*-axis length of the hexagonal unit cell for  $LiCoO<sub>2</sub>$  (=14.05 Å) (Ref. 1) is longer than that for  $\text{Na}_{0.74}\text{CoO}_2$  (=10.92 Å) (Ref. 42) due to a different crystal symmetry (see Fig. 11). Thus  $f_{\mu}$ (0 K) at the Li site would be roughly  $\ge$   $\sim$  5 MHz, because the dipolar field is proportional to *d*−3. This is roughly comparable to the experimental result  $[f_\mu(0 \text{ K}) \sim 8 \text{ MHz}].$ 

This also leads to estimates the internal fields expected in the other  $A_x$ CoO<sub>2</sub> with  $A = K$ , Rb and Cs. The *c*-axis length of  $A_x$ CoO<sub>2</sub> is reported as 12.35, 13.04, and 13.98 Å for  $A = K$ , Rb, and Cs,<sup>43,44</sup> resulting in lower  $f_{\mu}$ (0 K) ~ 2.0, 1.8, and 1.4 MHz, respectively. Actually, a preliminary  $\mu$ SR experiment on  $K_x \text{CoO}_2$  supports this prediction, because  $f_\mu$ (0 K) ~ 1.6 MHz for  $K_{0.4}CoO_2$ .<sup>45</sup>

#### **V. SUMMARY**

In order to elucidate the magnetism in layered cobaltites,  $\mu$ <sup>+</sup>SR spectroscopy and bulk susceptibility ( $\chi$ ) measurements were performed on polycrystalline samples of  $Li<sub>x</sub>CoO<sub>2</sub>$  with  $x=1.0$ , 0.95, and 0.70 in the temperature range between 300 and 1.8 K. Although all past bulk probes experiments suggested the absence of magnetic transitions at low *T*, weak transverse field (wTF-)  $\mu$ SR measurements clearly show the appearance of magnetism below  $\sim$  65 K (= $T_c^{\text{on}}$ ) even for the sample with  $x = 1.0$ . The volume fraction of the magnetic phase at 1.8 K is estimated as  $20\%$  for LiCoO<sub>2</sub>. This means that the observed magnetism is not induced by impurities but is an intrinsic behavior. The magnetism at low *T* is probably induced by either a charge disproportionation  $(2C_0^{3+} \rightarrow C_0^{2+} + C_0^{4+})$ , a spin state transition  $(t_{2g}^6 \rightarrow t_{2g}^5 e_g^1)$  of  $Co^{3+}$ , or an appearance of magnetic  $Co^{3+}$  at surface. The ZF spectra of  $LiCoO<sub>2</sub>$  consists of mainly a Kubo-Toyabe signal (for fluctuating random field) plus a small amount of rapidly relaxing signal (for fluctuating field) and an oscillating component due to an antiferromagnetic or an incommensurate spin density wave order.

For Li-deficient  $Li_xCoO_2$  samples,  $T_c^{on}$  decreases with decreasing *x*; i.e., 50 K for  $x=0.95$  and 25 K for  $x=0.7$ . The volume fraction of the magnetic phase is however almost independent of *x* and is estimated as 80% at 1.8 K, but no clear oscillations were seen in the zero field spectrum. Furthermore, Li-deficient samples are found to exhibit a spin state transition at  $\sim$ 170 K.

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