Thermodynamic and magnetic properties of the layered triangular magnet NaNiO₂

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We report muon-spin rotation, heat capacity, magnetization, and ac magnetic susceptibility measurements of the magnetic properties of the layered spin-1/2 antiferromagnet NaNiO₂. These show the onset of long-range magnetic order below $T_N = 19.5$ K. Rapid muon depolarization, persisting from T_N to about 5 K above T_N , is consistent with the presence of short-range magnetic order. The temperature and frequency dependence of the ac susceptibility suggests that magnetic clusters persist above 25 K and that their volume fraction decreases with increasing temperature. A frequency dependent peak in the ac magnetic susceptibility at $T_{\text{sf}}=3$ K is observed, consistent with a slowing of spin fluctuations at this temperature. A partial magnetic phase diagram is deduced.

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I. INTRODUCTION

Triangular lattice antiferromagnets exhibit a rich variety of ordering phenomena related to geometrical frustration.¹ When the triangles forming the lattice are distorted from equilateral to isosceles there is a partial release of the geometrical frustration, which can lead to more unusual forms of magnetic order exemplified in the fractional spin liquid in Cs_2CuCl_4 ² the spin-density wave in $Na_{0.75}CoO_2$ ³ and the rich B -*T* phase diagram of $CoNb₂O₆$.⁴ The series of triangular lattice magnets $LiNiO₂$, AgNiO₂, and NaNiO₂, seems to offer the possibility of tuning the release of the geometrical frustration by changing the exchange parameters, allowing models describing these systems⁵⁻⁷ to be tested experimentally. However, the difficulty of producing stoichiometric LiNiO₂ has led to a variety of sample-dependent results.⁸ $AgNiO₂$ can be produced in stoichiometric form but no magnetic Bragg peaks have so far been reported.⁹ Recently neutron powder diffraction studies have determined the low temperature magnetic structure of NaNiO_2 .^{10,11} A peak in the magnetic susceptibility interpreted as the Néel temperature, T_N , has been observed around 20 K.^{12–14} These disagree with the value of $T_N \sim 23$ K recently deduced from neutron powder diffraction data¹¹ (see below). In this paper, we report a detailed study of polycrystalline $NaNiO₂$ establishing the value of $T_N = 19.5$ K from both bulk and microscopic techniques (zero-field muon spin rotation (μSR) , heat capacity, and magnetic susceptibility measurements). Our work demonstrates the presence of magnetic clusters forming above T_N . We also investigate the low-temperature anomaly in the magnetic susceptibility observed previously.¹¹

II. CRYSTAL AND MAGNETIC STRUCTURE

Above 480 K the space group of $NaNiO₂$ is rhombohedral $(R\overline{3}m)$ and there is a cooperative Jahn-Teller transition to a low temperature monoclinic $(C2/m)$ phase below this temperature.15 The low-temperature structure can be considered to be layers of $NiO₆$ octahedra in the *ab* plane, with a trigonal distortion lengthening the Ni-O bonds in the *ac*

plane along an axis at 41° to the *c* axis of the crystal. The $\text{Ni}^{3+}(3d^7)$ ion is in the low spin state $(t_{2g}^6e_g^1, S=1/2)$, so the ground state is a singly occupied $|3z^2-r^2\rangle$ orbital with *z* along the axis of the Jahn-Teller induced trigonal distortion.¹⁵

Darie *et al.*¹⁰ find the ordering of the magnetic moments at 4 K to be a slight modification of the A-type antiferromagnetic ordering previously proposed.¹² The magnetic moments were found to be aligned at an angle of $100(2)^\circ$ to the *a* axis in the *ac* plane with no moment along the *b* axis. The Curie-Weiss constant, θ_{CW} = +36 K,¹⁴ shows the presence of ferromagnetic interactions above T_N .

The intralayer and interlayer exchange constants of NaNiO₂, *J*_|=-13.3 K and *J*_| =1.3 K, have been determined from a model assuming an A-type antiferromagnetic ordering in the presence of anisotropy;¹⁶ the layers are sufficiently strongly coupled to permit long range magnetic order below T_N . The Ni-O-Ni bond angles are $\approx 95^\circ$ at room temperature.15 An undistorted 90° geometry favours weak ferromagnetic superexchange, while a large deviation from a 90° bond angle can reverse the sign of this exchange coupling.¹⁷ In NaNiO₂ it appears that despite the distortion, in-plane ferromagnetic coupling prevails, though the precise nature of the spin and orbital ordering remains under discussion.⁵⁻⁷

III. EXPERIMENTAL RESULTS

NaNiO₂ was prepared from $Na₂O₂$ and NiO powders heated at 700 °C for 100 h under pure oxygen flow, with intermediate grinding. X-ray powder diffraction showed that the impurity concentration was below the 2% resolution limit of the apparatus. Heat capacity data measured in magnetic fields between 0 and 14 T, taken with a Quantum Design PPMS, are shown in Fig. 1(a). In zero field the transition at T_N =19.5 K is seen as a rather broad peak, and there is no evidence for other phase transitions below 30 K. With increasing magnetic field the temperature of this peak decreases to about 14 K [see Fig. $1(a)$].

FIG. 1. (Color online) The panels correspond to: (a) Heat capacity divided by temperature in fields between 0 and 14 T. (b) Real part, χ' , of the ac magnetic susceptibility. (c) Temperature dependence of the peak in χ' associated with T_{sf} with a fit to the Ogielski relation [Eq. (1)]. (d) Imaginary part, χ'' , of the ac magnetic susceptibility. (e) Inverse of magnetic susceptibility data against temperature with a linear fit showing the high-temperature Curie-Weiss behavior. The vertical dashed lines indicate temperatures referred to in the text.

Magnetic susceptibility data, taken using a Quantum Design MPMS superconducting quantum interfence device $(SQUID)$ magnetometer are shown in Figs. $1(b)$, $1(d)$, and 1(e). The high temperature dc susceptibility data, shown in Fig. 1(e), are consistent with θ_{CW} = +36 K.¹⁴ The real and imaginary parts of the ac susceptibility, χ' and χ'' , are presented in Figs. $1(b)$ and $1(d)$ (driving field 3.5 Oe). They show a frequency dependent peak in χ' located slightly above a spin-freezing temperature T_{sf} , which is determined below. Figure $1(d)$ shows the temperature variation of this peak in χ' with frequency. It was found that this could be fitted to the Ogielski scaling relation¹⁸

$$
T = T_{\rm sf} [1 + (f\tau_0)^{1/z \nu_c}], \tag{1}
$$

where *T* is the temperature of the peak in χ' , *f* is the measurement frequency, τ_0 is the relaxation time of the system, *z* is a dynamic exponent, and ν_c is a critical exponent. Fitting the data to Eq. (1) gives $T_{\text{sf}}=3\pm 0.2 \text{ K}$, $\tau_0=5.4(2)\times 10^{-3} \text{s}$ and $z\nu$ _c= 8.1 ± 0.4. This is typical of glassy behavior or the slowing of spin fluctuations. At T_N , χ' has a small maximum and rises to a larger peak near 25 K, with the frequency dependence increasing from T_N to the peak, and decreasing above it. The temperature of the peak in χ' at 25 K decreases

FIG. 2. (Color online) (a) Heat capacity divided by temperature vs field at four temperatures. (b) Partial magnetic phase diagram deduced from heat capacity (\bullet) and magnetization (\Diamond) data. AF: A-type antiferromagnetic phase. PM: Paramagnetic phase. FM: Ferromagnetic phase.

slowly with increasing frequency, which may be related to the presence of two sets of relaxation times varying differently with temperature (see below). χ'' also rises sharply near 25 K but to a plateau continuing up to \sim 35 K. Together these suggest that short-range order persists up to \sim 25 K, that slowly fluctuating clusters of spins are present within a fast fluctuating paramagnetic bulk above this temperature, and that the volume fraction of clusters decreases with increasing temperature.

Constant temperature heat capacity data with varying magnetic field are presented in Fig. 2(a). Except for the data taken at 22 K, a peak is observed which corresponds to the field labeled H_{C1} in the magnetization data reported in Ref. 16. This suggests that this marks the upper field boundary of A-type antiferromagnetic order. At 22 K the heat capacity decreases with increasing field consistent with short-range order. The partial magnetic phase diagram deduced from our heat capacity and magnetization data is shown in Fig. 2(b).

Our zero-field μ SR experiments were carried out using the DOLLY instrument at the Paul Scherrer Institute (PSI), Villigen, Switzerland. In our μ SR experiments, spin polarized positive muons $(\mu^+$, mean lifetime 2.2 μ s, momentum 28 MeV/ c) were implanted into polycrystalline NaNiO₂. The decay positron asymmetry function, $A(t)$,¹⁹ is proportional to the average spin polarization of the muons stopped within the sample. The muon spin precesses around an internal magnetic field, B_{μ} , at a frequency $\nu_{\mu} = (\gamma_{\mu}/2\pi)|B_{\mu}|$, where $\gamma_{\mu}/2\pi = 135.5$ MHz T⁻¹.

The asymmetry data were fitted to Eq. (2) (Ref. 20) below T_N , and to Eq. (3) above T_N :

$$
A(t) = A(0)[P_1e^{-\lambda_1 t} + P_2e^{-\lambda_2 t}\cos(2\pi\nu_\mu t + \phi_0)],
$$
 (2)

$$
A(t) = A(0)(P_1e^{-\lambda_f t} + P_s e^{-\lambda_s t}),
$$
\n(3)

where $A(0)$ is the initial asymmetry. P_1 and P_2 are, respectively, the longitudinal and transverse components of the muon polarization, and $P_1 + P_2 = 1$. The exponential relaxation associated with P_1 reflects the dynamical fluctuations of the fields being probed. The P_2 term describes muon precession with a distribution of local fields dephasing the muon spins. In a fully magnetically ordered polycrystalline sample we expect $P_2/P_1 = 2$. Coherent muon precession will be observed if long range order is present within the sample. P_s and P_f describe slow and fast dynamic fluctuations, respec-

FIG. 3. Muon decay asymmetry in $NaNiO₂$ plotted at different temperatures. The solid lines are fits of the data to Eqs. (2) and (3) with the parameters shown in Fig. 4.

tively. A small initial phase offset, ϕ_0 , was observed below T_N , larger than could be attributed to errors in determining the time that the muons enter the sample. This could be produced by a small magnetic inequivalency in the position of muons stopped within the sample, consistent with an asymmetric peak seen in Fourier transforms of the data. In the fitting procedure, data were fitted in the time range $0 \le t \le 8$ μ s, where the effect of background counts could be reliably subtracted. Rapid dynamic fluctuations lead to λ_1 $\propto \gamma_{\mu}^{2} (\Delta B)^{2}/\nu$, where ΔB is the amplitude of the fluctuating local field and ν is the fluctuation rate.²⁰

Spectra measured at four temperatures are shown in Fig. 3. There are three distinct temperature regions apparent from the muon asymmetry spectra. At low temperatures $(T \leq 19.5 \text{ K})$ there are clear oscillations in the asymmetry showing that long range magnetic order exists and the observed ratio of P_2 : $P_1 \approx 2$ [see Fig. 4(b)] indicates that the sample is magnetic over its entire volume. The values of λ_2 and λ_s are much larger than those of λ_1 and λ_f [see Figs. 4(c) and 4(d)], so at short times only the effects of λ_2 and λ_s are seen in Fig. 3. An intermediate temperature range $(19.5 < T < 24 \text{ K})$ gives no oscillations, and the relaxation is modelled with the two exponential components of Eq. (3), with the amplitude of the faster relaxing component decreasing with increasing temperature. Above 24 K the relaxation is well described by a single exponential, $P_f \exp(-\lambda_f t)$, consistent with fast fluctuations of paramagnetic moments characterized by a single correlation time in the muon time window.

The temperature dependence of the parameters derived from fitting Eqs. (2) and (3) to muon asymmetry spectra are presented in Fig. 4. The muon precession frequency, v_{μ} , in the ordered phase is shown in Fig. $4(a)$. This is proportional to the sublattice magnetization at the muon site, and was fitted to a function²¹

FIG. 4. (Color online) Temperature dependence of the parameters determined from fitting data to Eqs. (2) and (3) : (a) the oscillation frequency, ν_{μ} and the internal magnetic field, B_{μ} , with a fit to Eq. (4). (b) Amplitudes of the relaxation components P_1 and P_2 , and P_f and P_s . (c) Relaxation rates λ_2 and λ_s . (d) Relaxation rates λ_1 and λ_f . The vertical dashed lines indicate temperatures referred to in the text.

$$
\nu_{\mu}(T) = \nu_{\mu}(0)[1 - (T/T_N)]^{\beta_m}.
$$
 (4)

The fit gives $\nu_{\mu}(0) = 64.2(2) \text{MHz}$ corresponding to a field at the muon site of \sim 0.5 T. Dipole field calculations show that this field will be experienced by muons near any of the oxygen atoms in the octahedron surrounding a nickel atom, in regions of high electron density, 22 and show that our results are consistent with the magnetic structure determined by Darie *et al.*¹⁰ Our calculations also suggest that the muon precession frequency is insensitive to small deviations from this magnetic structure. Fitting Eq. (4) to the muon precession frequencies gave $T_N = 19.51(1)K$ and $\beta_m = 0.24(1)$. This value of $\beta_{\rm m}$ suggests that the system is behaving as a twodimensional (2D) *XY* magnet.²³

IV. DISCUSSION AND CONCLUSIONS

From our muon-spin rotation, heat capacity and magnetic susceptibility data we determine $T_N = 19.5$ K, in agreement with the values determined in Refs. 12–14. We have followed the power law variation of the sublattice magnetization as a function of temperature, which shows strong twodimensionality in the magnetic ordering. The *B*-*T* phase diagram presented in Fig. 2(b) shows that the boundary of the AF ordered phase also tends smoothly to T_N .

In relation to the peak just above T_{sf} in the magnetic susceptibility, the formation of a true spin glass is excluded by the observation of muon precession down to 1.6 K. The most plausible interpretation of this feature is a slowing of spin fluctuations around T_{sf} . It is also possible that a small concentration of oxygen vacancies, each with two associated $Ni²⁺$ impurity spins for charge balance, exist within the NiO₆ layers. These would weakly couple with one another with a separate energy scale to the bulk $Ni³⁺$ spins, and given their larger spin could account for such an artifact in the magnetic susceptibility. This artifact is unlikely to be related to stacking frustration. We note that extrapolating the Ogielski scaling relation to the muon time window suggests a maximum in the dynamic relaxation rate λ_1 should be observed around 7 K, and a broad maximum of low amplitude is just detectable at this temperature [Fig. $4(d)$].

The presence of two exponential relaxation components above T_N [see Eq. (3)] suggests that short-range magnetic order persists over a small temperature range of \sim 5 K above T_N . The fluctuations in the magnetic field producing the faster relaxing component, λ_s , are two orders of magnitude slower than those producing the slowly relaxing component, λ_f . P_s decreases with increasing temperature up to 24 K, showing that the ratio of slow to fast dynamic relaxation is decreasing. Above this temperature the muon relaxation is that expected for a system in the fast-fluctuation regime. The slow spin relaxations observed in the frequency dependence of the ac susceptibility above 25 K are not within the muon time window so are not observed. The observation of two components in the muon relaxation below 24 K, together with a changing frequency dependence of the ac susceptibility, suggest a model of coalescing magnetic clusters forming well above T_N . On cooling below \sim 50 K, ferromagnetic clusters form within the $NiO₆$ layers and there will be weak coupling between layers. As the volume fraction of clusters increases with decreasing temperature, the coupling of clusters between layers becomes more significant. This is seen in the increase in the frequency dependence of the ac susceptibility until it reaches a maximum at \sim 25 K, suggesting that slowly fluctuating short-range order occurs at this temperature. Between \sim 25 K and T_N the magnetic clusters coalesce, seen in the decrease of χ' and χ'' , effectively increasing the registry between planes. The fluctuations in this temperature range are relatively slow, leading to the P_s component of the muon relaxation, and would appear static within the neutron time window. This perhaps explains the $(0,0,1/2)$ antiferromagnetic Bragg peaks persisting above T_N , as reported in Ref. 11, which would then result from the coalescing clusters of ordered spins.

In conclusion, NaNiO_2 shows the onset of long-range magnetic order at $T_N = 19.5$ K, with the dependence of the sublattice magnetization on temperature appropriate for a 2D *XY* magnet. The slowing of spin fluctuations above T_{sf} is evident in the ac magnetic susceptibily data. At temperatures just above T_N there is evidence of short-range order and of magnetic clusters persisting within a paramagnetic phase above this temperature.

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