

## Magnetic-field-induced density of states in MgB<sub>2</sub>: Spin susceptibility measured by conduction-electron spin resonance

F. Simon,<sup>1,2</sup> A. Jánossy,<sup>1</sup> T. Fehér,<sup>1,2</sup> F. Murányi,<sup>1</sup> S. Garaj,<sup>2</sup> L. Forró,<sup>2</sup> C. Petrovic,<sup>3,\*</sup> S. Bud'ko,<sup>3</sup> R. A. Ribeiro,<sup>3</sup> and P. C. Canfield<sup>3</sup>

<sup>1</sup>*Budapest University of Technology and Economics, Institute of Physics and Solids in Magnetic Fields Research Group of the Hungarian Academy of Sciences, H-1521 Budapest, P.O. Box 91, Hungary*

<sup>2</sup>*Institute of Physics of Complex Matter, EPFL, CH-1015 Lausanne, Switzerland*

<sup>3</sup>*Ames Laboratory, U.S. Department of Energy and Department of Physics and Astronomy, Iowa State University, Ames, Iowa 50011, USA*

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The magnetic-field dependence of the electron spin susceptibility  $\chi_s$  was measured in the superconducting state of high-purity MgB<sub>2</sub> fine powders from the intensity of the conduction-electron spin resonance at 3.8, 9.4, and 35 GHz. The measurements confirm that a large part of the density of states is restored at low temperatures at fields below 1 T in qualitative agreement with the closing of the  $\pi$  band gaps in the two-band model. However, the increase of  $\chi_s$  with field and temperature is larger than expected from current superconductor models of MgB<sub>2</sub>.

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It is now generally accepted that MgB<sub>2</sub> is a phonon-mediated superconductor<sup>1-3</sup> which owes its unusual properties to the strong differences in the electron-phonon coupling of its disconnected Fermi surface sheets.<sup>4</sup> The two-gap model assigns a large superconductor gap to the cylindrical Fermi surface sheets originating from B-B  $\sigma$  bonds and a much smaller gap to the sheets of  $\pi$  electrons. The model successfully describes the temperature dependence of several properties like the specific heat<sup>5</sup> or the electron tunneling spectra<sup>6</sup> in zero magnetic field while predictions for finite magnetic fields are less tested. The strong electron-phonon coupling on the  $\sigma$  sheets maintains superconductivity to about  $H_{c2}^c \approx 2.5$  T for fields perpendicular to and  $H_{c2}^{ab} \approx 16$  T for fields lying in the crystalline ( $a, b$ ) boron planes.<sup>7</sup> It has been suggested that the weaker  $\pi$  gap is closed by much smaller fields  $H_{c2}^\pi$  without destroying superconductivity. The actual value of  $H_{c2}^\pi$  is rather uncertain: from single-crystal specific heat experiments<sup>8</sup> an isotropic  $H_{c2}^\pi = 0.3-0.4$  T, from vortex imaging<sup>9</sup> 0.13 T has been estimated, while point contact tunneling experiments<sup>10-13</sup> suggest values between 1 and 2 T.

In this paper, we report on the magnetic-field dependence of the electron spin susceptibility  $\chi_s$  in the superconducting state of high-purity MgB<sub>2</sub> powders measured by conduction-electron spin resonance (CESR). We observe an unusually strong increase of  $\chi_s$  with magnetic field.  $\chi_s$  at low temperatures measures the density of states (DOS) at the Fermi level restored in the superconductor by the magnetic field. Apart from the weak electron-electron interactions,  $\chi_s$  is proportional to the DOS in MgB<sub>2</sub> and may be compared to band structure calculations directly or to the electronic specific heat after a correction for electron-phonon coupling.  $\chi_s(H, T)$  is not proportional to the electronic specific heat coefficient  $\gamma(H, T)$  if the electron-phonon coupling is different for the  $\sigma$  and  $\pi$  bands. We find, however, a larger increase of  $\chi_s$  with field and temperature than expected from calculations of the DOS and a simple two-band model.

We studied samples from several batches. Sample 1 is made from a 99.99% purity natural isotopic mixture of <sup>10</sup>B and <sup>11</sup>B amorphous boron; samples 2 and 3 are made from crystalline, isotopically pure <sup>11</sup>B. Chemical analysis, the high normal-state conductivities, and the narrow CESR lines at  $T_c$  attest to the high purity of the samples. Details of sample characterization are discussed in Ref. 14. Sample 2 was made from the batch used in the CESR work of Ref. 7. Fine powders with grain sizes less than 1  $\mu\text{m}$  were selected from the starting materials to reduce the inhomogeneity of microwave excitation. The aggregates of small grains were hand crushed and then mixed in a 1:1 weight ratio with a fine SnO<sub>2</sub> powder. The mixture was suspended in isopropanol and the larger particles were eliminated by sedimentation or in a centrifuge while the small grains were extracted by filtering. Mixing with SnO<sub>2</sub> separates the MgB<sub>2</sub> particles and reduces eddy-current screening of microwaves. We checked by electron microscopy that MgB<sub>2</sub> grains were smaller than 0.5  $\mu\text{m}$ . Superconducting quantum interference device (SQUID) magnetometry confirmed that the superconducting properties are the same in the original batch and the sample of small grains. The powders were finally cast into epoxy for the ESR experiments. CESR experiments were performed at 3.8, 9.4, 35, 75, and 225 GHz corresponding to approx. 0.14, 0.34, 1.28, 2.7, and 8.1 T resonance fields, respectively. The higher-frequency experiments reproduce those of Ref. 7; the CESRs of superconducting and normal grains are resolved at 75 and 225 GHz even at temperatures much below  $T_c$ , confirming that  $H_{c2}^c$  is somewhat below 2.7 T.  $\chi_s$  of MgB<sub>2</sub> was measured directly from the CESR intensity without need for core electron corrections as in static susceptibility measurements. A fine powder of the air-stable metallic polymer *o*-KC<sub>60</sub> was mixed into the epoxy for some of the samples to serve as a temperature-independent ESR intensity standard.<sup>15</sup> Intensity measurements at 9 GHz (where instrumental factors are well controlled) with and without KC<sub>60</sub> were consistent. The absolute value of  $\chi_s$  was measured against a secondary CuSO<sub>4</sub>·5H<sub>2</sub>O standard at 9.4 GHz.

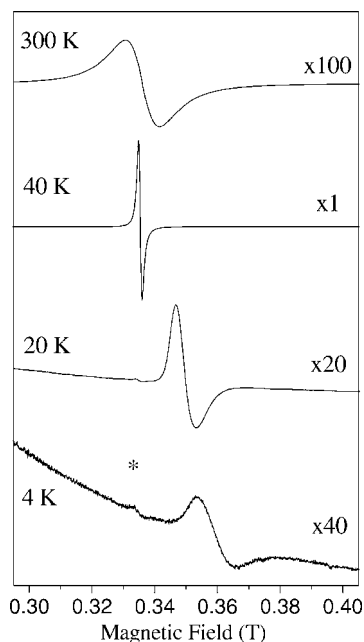


FIG. 1. Temperature dependence of the CESR signal of  $\text{MgB}_2$  fine powder sample (sample 1) at 9.4 GHz (0.34 T). \* denotes the ESR signal of a tiny amount of paramagnetic impurity phase.

Figure 1 shows the CESR spectra at 9.4 GHz for sample 1. The room-temperature peak-to-peak linewidth  $\Delta H_{pp} = 111 \pm 3$  G of the derivative absorption line is dominated by spin-lattice relaxation due to phonons. The residual linewidth at 40 K arises from static imperfections and is sample dependent. The residual linewidth is somewhat smaller for sample 1 ( $\Delta H_{pp} = 10 \pm 0.3$  G) than for samples 2 and 3 ( $11 \pm 0.3$  and  $20 \pm 0.6$  G), while the residual resistance ratio (RRR) is larger for the latter two samples.<sup>14</sup> Unlike the RRR, the CESR linewidth is insensitive to intergrain scattering and the difference may be related to the different morphology of Sample 1 and 2, 3. The small asymmetry of the line shape (the ratio of maxima of the derivative ESR line  $A/B = 1.16$  for sample 1) at 40 K shows that microwave penetration is nearly homogeneous,<sup>16</sup> the typical particle size is comparable to the microwave penetration depth,  $\delta = 0.3 \mu\text{m}$ , and the reduction of the CESR signal intensity due to eddy-current screening is less than 5%.

Above 450 K (data not shown), the CESR intensities are the same for the three samples and correspond to a susceptibility of  $\chi_s = (2.3 \pm 0.3) \times 10^{-5}$  emu/mol in agreement with the previously measured value<sup>7</sup> of  $\chi_s = (2.0 \pm 0.3) \times 10^{-5}$  emu/mol and calculations of the DOS.<sup>3</sup> In sample 1, the CESR intensity is nearly  $T$  independent in the normal state; the measured small decrease of about 20% between 600 and 40 K is of the order of experimental precision at high temperatures. In samples 2 and 3 the CESR intensity decreased by a factor of 2.5 between 450 and 40 K. The nearly symmetric Lorentzian line shape showed that this intensity decrease is not due to a limited penetration depth. Neither does the intensity decrease correspond to a change in  $\chi_s$ . We measured the  $T$  dependence of the  $^{11}\text{B}$  spin-lattice relaxation time  $T_1$  in samples 2 and 3 and found a metallic,  $T$ -independent value of  $1/(TT_1) = 167 \pm 3 \text{ s}^{-1} \text{ K}^{-1}$  in agree-

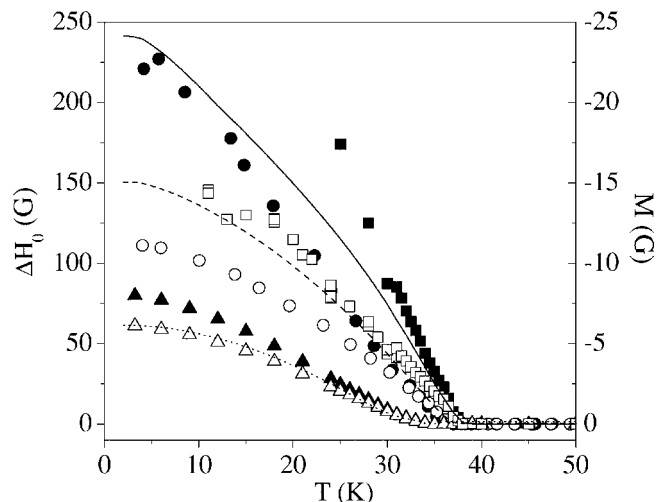


FIG. 2. Temperature dependence of the diamagnetic shift (full symbols are up sweeps, open symbols are down sweeps) of the CESR (squares, 3.8 GHz, 0.14 T; circles, 9.4 GHz, 0.34 T; triangles, 35 GHz, 1.28 T) and diamagnetic magnetization measured by SQUID (solid, dashed, and dotted curves are at 0.14, 0.34, and 1.28 T, respectively).

ment with Refs. 17 and 18. It is possible that the difference in morphology and purity at the grain surfaces explains that the CESR signal intensity is almost constant in sample 1 while it changes strongly in samples 2 and 3. We believe that the nearly constant CESR intensity in sample 1 and the constant  $1/(TT_1)$  measures correctly the metallic susceptibility of  $\text{MgB}_2$ .

Below  $T_c$ , the  $T$  and  $H$  dependence of the diamagnetic shifts, line widths, and intensities normalized at  $T_c$  are similar in all three samples. We discuss sample 1, for which the CESR signal intensity is constant in the normal state within experimental precision. For applied magnetic fields  $H < H_{c2}^c(T=0 \text{ K})$  and at  $T \ll T_c$  the CESR signal corresponds to the mixed state of the  $\text{MgB}_2$  superconductor; any nonsuperconducting fraction would be shifted to higher fields and easily detected.<sup>7</sup> The ESR of a tiny impurity phase is well outside the CESR of  $\text{MgB}_2$  (marked by \* in Fig. 1). Comparison of the diamagnetic magnetization  $M$  measured by SQUID and the diamagnetic shift of the CESR,  $\Delta H_0(T) = H_0(T) - H_0(40 \text{ K})$  ( $H_0$  is the resonance field), also verifies that below  $T_c$  we detect the CESR of the  $\text{MgB}_2$  superconductor. Figure 2 shows  $\Delta H_0(T)$  at three different ESR frequencies and  $M$  at the corresponding static magnetic fields with a scaling between  $\Delta H_0$  and  $M$  as in Ref. 7. The present diamagnetic shift data on fine-grain samples at 35 GHz and higher frequencies (not shown) agree with our previous report on large-grain samples.<sup>7</sup>  $\Delta H_0(T)$  is equal to the average reduction of the applied magnetic field in the sample and is proportional within a shape dependent constant to  $M$  of the grains.  $\Delta H_0(T)$  averaged for increasing and decreasing field sweeps is proportional to  $M$  in the field cooled sample with the same proportionality constant in a broad range of  $T$ 's for all the three magnetic fields. We used the same argument previously to identify the CESR of superconducting  $\text{MgB}_2$  particles at higher-frequency ( $> 35$  GHz) CESR experiment.<sup>7</sup>

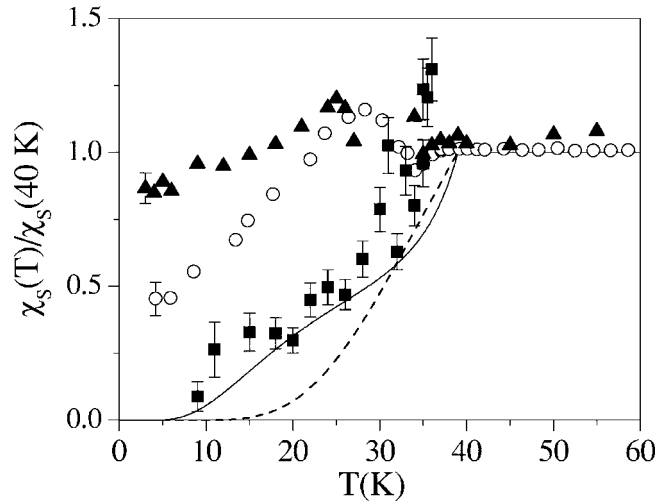


FIG. 3. The temperature- and magnetic-field-dependent spin susceptibility of  $\text{MgB}_2$  below  $T_c$  (squares, 3.8 GHz, 0.14 T; circles, 9.4 GHz, 0.34 T; triangles, 35 GHz, 1.28 T). Dashed and solid curves are  $\chi_s$  in the absence of magnetic field as calculated for the isotropic BCS and two-gap models, respectively, as explained in the text.

The CESR line broadens inhomogeneously below  $T_c$  due to the macroscopic inhomogeneities of diamagnetic stray fields. Within each isolated grain, spin diffusion motionally averages all magnetic field inhomogeneities arising from screening currents and the vortex lattice,<sup>19</sup> so this itself does not broaden the CESR of the individual grains. The line is, however, broadened in the randomly oriented powder by the crystalline and shape anisotropy of the diamagnetic shift, that changes from grain to grain. As expected for this case, the observed additional line width in the superconducting state,  $\Delta H_a$ , is proportional to the shift and  $\Delta H_a/\Delta H_0(T)$  is about 0.3 at all fields and temperatures.

The main topic of the current report is the measurement of  $\chi_s$  in the superconducting state of  $\text{MgB}_2$ . Usually,  $\chi_s$  is determined from the measurements of temperature-dependent Knight shift or spin-lattice relaxation time  $T_1$ .<sup>20</sup> To our knowledge, in  $\text{MgB}_2$  there has been no successful determination of these quantities below  $T_c$ : precision of the Knight shift measurement is limited due to the diamagnetic magnetization,<sup>17,21</sup> while  $T_1$  measurements are affected by several factors like vortex motion.<sup>17</sup> In CESR, the signal intensity is proportional to  $\chi_s$  and diamagnetism affects only the shift of the resonance line.  $\chi_s$  is proportional to the DOS of low-energy quasiparticle excitations when electron correlations are small.

In Fig. 3, we show  $\chi_s$  below 60 K measured at three magnetic fields. The 9.4 GHz (0.34 T) and 35 GHz (1.28 T) data are normalized at 40 K while the 3.8 GHz (0.14 T) data are normalized at 100 K. At 3.8 and 35 GHz data are missing in ranges between 36 and 100 K and 27 and 34 K, respectively, where the CESR of  $\text{MgB}_2$  could not be resolved from the  $\text{KC}_{60}$  reference. Data taken at 9.4 GHz with and without reference agree well. Hysteresis in the penetration of the magnetic field into the sample below the irreversibility line does not affect the measurement of  $\chi_s$  in the studied range of  $T$

and  $H$ : line widths and shifts depend on the direction of the field sweep at low  $T$  but the intensities are the same within 5%, i.e., within the experimental precision at low  $T$ . In Fig. 3, data at 9.4 and 35 GHz are averaged for sweeps with increasing and decreasing fields while at 3.8 GHz decreasing field sweep data are shown. No correction is made for diamagnetic screening of the microwave excitation; this would increase somewhat further the measured values of  $\chi_s$ .

The remarkably fast increase of  $\chi_s$  with field and temperature is the most interesting finding of this work. As shown in Fig. 3, the data cannot be described by a superconductor with a single gap. The  $T$ -dependent  $\chi_s$  at our lowest magnetic field of 0.14 T lies well above  $\chi_s(T, H=0)$  calculated for an isotropic  $T_c=39$  K weak-coupling superconductor.<sup>22-24</sup> In a conventional superconductor a field of 0.14 T would affect the spin susceptibility little since  $H_{c2}$  varies between 2.5 and 16 T.

As we show below, the two-gap model is more successful: it explains data at the lowest field, but difficulties remain with the interpretation of data at higher fields. The solid curve in Fig. 3 shows  $\chi_s$  calculated for zero field in a model of two independent zero-temperature gaps  $\Delta_1=11$  K and  $\Delta_2=45$  K. (These values are derived from zero-field specific heat<sup>8</sup> and electron tunneling data.<sup>10</sup>) Following band structure calculations,<sup>4,26,27</sup> we assumed that  $N$ , the total DOS in the normal state, is shared in a ratio  $N_{\pi_0}/N_0=0.56$  and  $N_{\sigma_0}/N_0=0.44$  between the two types of Fermi surfaces.<sup>25</sup> Clearly,  $\chi_s$  measured at 0.14 T and above 10 K is compatible with the two-gap model using the above parameters without any important enhancement of  $\chi_s$  by the field.

The large susceptibilities at the fields of 0.34 and 1.28 T are, however, only in qualitative agreement with the two-gap model. These fields are still much below the critical field for destroying superconductivity. The explanation for the strong magnetic-field dependence observed in various experiments has been that the gap in the type- $\pi$  band is closed by fields of 1 T or less, i.e., by fields much below  $H_{c2}$ . In this picture the DOS  $N(H)=N_{\pi}+N_{\sigma}$  increases rapidly with field until  $H_{c2}^{\pi}$ , where the contribution of the  $\pi$  band to the DOS saturates at the normal-state value  $N_{\pi_0}$ . At fields above  $H_{c2}^{\pi}$ , the increase of  $N(H)$  is much slower as it arises solely from the  $\sigma$  band and  $H_{c2}$  is much larger than  $H_{c2}^{\pi}$  for all field orientations. Figure 4 shows the DOS calculated in the simplest approximation, where both  $N_{\pi}$  and  $N_{\sigma}$  increase linearly with field until they reach their normal-state value at  $H_{c2}^{\pi}$  and  $H_{c2}$ . The experimental density of states [proportional to  $\chi_s(H)$ ] follows such a nearly steplike behavior, in agreement with an  $H_{c2}^{\pi}$  equal to or less than 1 T. However, the susceptibility  $\chi_s/\chi_N=0.87(6)$  measured at 1.28 T and 4 K is much larger than expected. Extrapolating to zero field, the susceptibility predicts  $N_{\pi_0}/N_0|_{\chi}=0.8-0.9$ , a value much larger than  $N_{\pi_0}/N_0=0.56$  calculated by several groups.

We note that the magnetic-field dependence of the electronic specific heat is not in perfect agreement with the band structure calculations, either. Specific heat experiments on  $\text{MgB}_2$  single crystals in magnetic field yield an isotropic critical field  $H_{c2}^{\pi}=0.4$  T and  $\gamma_{\sigma}/\gamma=0.45$  and  $\gamma_{\pi}/\gamma=0.55$  for the electronic specific heats of the two bands in the normal states.<sup>8</sup> While electron-phonon coupling does

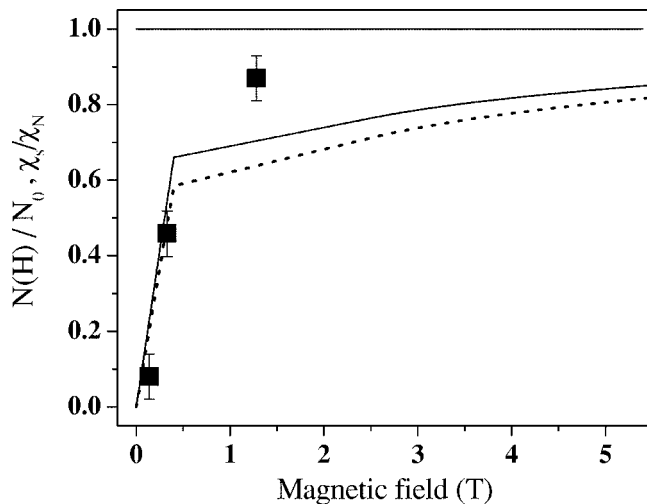


FIG. 4. Comparison of the measured field dependence of the low-temperature normalized susceptibility  $\chi_s/\chi_N$  (squares) to the predictions of the two-gap model of Ref. 26. The magnetic-field-dependent DOS (dashed line) is assumed to have independent contributions from a  $\pi$  band with  $H_{c2}^\pi=0.4$  T and a  $\sigma$  band with  $H_{c2}^\sigma=2.5$  T and  $H_{c2}^{ab}=16$  T. The solid line represents DOS calculated from single-crystal specific heat measurements (Ref. 8).

not affect the spin susceptibility, it contributes to  $\gamma$  by a factor of  $1+\lambda$ . Thus the DOS calculated from the heat capacity is  $N_{\pi 0}/N_0=[\gamma_\pi/(1+\lambda_\pi)]/[\gamma_\pi/(1+\lambda_\pi)+\gamma_\sigma/(1+\lambda_\sigma)]$  and  $N_{\sigma 0}/N_0=[\gamma_\sigma/(1+\lambda_\sigma)]/[\gamma_\pi/(1+\lambda_\pi)+\gamma_\sigma/(1+\lambda_\sigma)]$ . Using the theoretical values of the electron-phonon coupling constants,  $\lambda_\pi=0.4$  and  $\lambda_\sigma=0.9$ ,<sup>25</sup> yields  $N_{\pi 0}/N_0|_{\gamma}=0.62$ , which is less than that measured from the spin susceptibility but still significantly larger than the calculated value of 0.56.

The DOS from the band structure calculations is probably reliable; it describes the zero-field specific heat correctly. The

same calculations predict electron-phonon couplings that are in agreement with the experiments.<sup>28</sup> Thus, we conclude that a magnetic field of about 1 T does not simply close the  $\pi$  band gap but it restores also a large portion of the Fermi surface on the  $\sigma$  band. This conclusion is reinforced by the observed temperature dependence at 0.34 T. Although  $\chi_s$  measured at 0.34 T and 4 K may agree with a two-gap model with negligible perturbation of the  $\sigma$  band by small magnetic fields, there is an unexpectedly large effect of the magnetic field at higher temperatures. Most of the spin susceptibility is restored at  $T_c/2$  by a field of 0.34 T. It is evident that such a large spin susceptibility cannot be explained by a simple picture where the  $\pi$  band gap is closed at fields below 1 T and the  $\sigma$  band DOS is restored only at a rate proportional to  $H/H_{c2}$ .

In conclusion, the strong magnetic-field dependence of the spin susceptibility and specific heat poses a challenge to theory. The model where the  $\pi$  gap is closed at small fields while the  $\sigma$  gap remains mostly unaffected is inadequate.

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\*Present address: Department of Physics, Brookhaven National Laboratory, Upton, New York 11973.

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