Theoretical study of angle-resolved two-photon photoemission in two-dimensional insulating cuprates

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We propose angle-resolved two-photon photoemission spectroscopy (AR-2PPES) as a technique to detect the location of the bottom of the upper Hubbard band (UHB) in two-dimensional insulating cuprates. The AR-2PPES spectra are numerically calculated for small Hubbard clusters. When the pump photon excites an electron from the lower Hubbard band, the bottom of the UHB is less clear, but when an electron in the nonbonding oxygen band is excited, the bottom of the UHB can be identified clearly, accompanied with additional spectra originated from the spin-wave excitation at half filling.

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The charge gap in Mott insulators is a consequence of strong electron correlation. The nature of excitations across the gap is controlled by both the lower Hubbard band (LHB) and the upper Hubbard band (UHB). Therefore, the clarification of the momentum dependence of the two bands will be very crucial for understanding the nature of the Mott-gap excitation.

Parent compounds of high- T_c superconductors such as La_2CuO_4 and $Ca_2CuO_2Cl_2$ are a good example of the Mott insulator in two dimensions (2D). It was theoretically proposed that the top of the LHB [more precisely the Zhang-Rice singlet band (ZRB) (Ref. 1)] is located at k $=(\pm \pi/2, \pm \pi/2)$, while the bottom of the UHB is at $(\pi, 0)$ and $(0, \pi)$ ² The location of the top of the LHB has clearly observed by angle-resolved been photoemission experiments.³ On the other hand, the bottom of the UHB has not been directly observed yet, but only indirectly confirmed by resonant inelastic x-ray scattering that reveals momentum-dependent Mott gap excitations.⁴

In this Brief Report, we propose angle-resolved twophoton photoemission spectroscopy (AR-2PPES) as a new technique to detect the location of the bottom of the UHB in the 2D insulating cuprates. The two-photon photoemission spectroscopy has been widely used for the studies of the electronic excitations at metal surfaces and their decay in the time domain.^{5,6} On the other hand, for strongly correlated systems such as high- T_c cuprates there are a few studies only in the metallic and superconducting regions of Bi₂Sr₂CaCu₂O_{8+ δ}^{7,8} but no report on insulating materials. Therefore, the application of AR-2PPES to the insulating cuprates will open a new way of spectroscopic study for strongly correlated electron systems.

The AR-2PPES spectrum is numerically calculated for small clusters described by the Hubbard model with realistic parameters. We consider two types of pump-photon excitation: One corresponds to the case where the pump photon induces an excitation from LHB to UHB, while the other is an excitation from the nonbonding (NB) oxygen band in which the oxygen $2p_{\sigma}$ orbitals form an asymmetric state with respect to the Cu $3d_{x^2-y^2}$ orbital. In the former, we find two kinds of AR-2PPES spectra that reflect information on either the UHB or LHB. However, the location of the bottom of UHB is not clearly identified because of diffusive features in the spectra. In the latter case, we clearly find the location of the bottom of the UHB. In addition to this, new spectral weights that are not seen in inverse photoemission spectra emerge in AR-2PPES. The origin of the additional spectra is attributed to the spin-wave excitation expected at half filling. These theoretical results will be useful for the analysis of AR-2PPES experimental data in the near future.

We employ a single-band Hubbard model with long-range hoppings to describe the electronic states in the 2D insulating cuprates. The Hamiltonian reads

$$H_{\text{Hub}} = -\sum_{\langle \mathbf{i}, \mathbf{j} \rangle, \sigma} t_{ij} (c_{\mathbf{i}, \sigma}^{\dagger} c_{\mathbf{j}, \sigma} + \mathbf{h} \cdot \mathbf{c} \cdot) + U \sum_{\mathbf{i}} n_{\mathbf{i}, \uparrow} n_{\mathbf{i}, \downarrow} - \mu \sum_{\mathbf{i}, \sigma} n_{\mathbf{i}, \sigma},$$
(1)

where $c_{\mathbf{i},\sigma}^{\dagger}$ is the creation operator of an electron with spin σ at site **i**, and $n_{\mathbf{i},\sigma} = c_{\mathbf{i},\sigma}^{\dagger} c_{\mathbf{i},\sigma}$. The summations $\langle \mathbf{i}, \mathbf{j} \rangle$ run over neighboring pairs up to the third-nearest neighbors. The hopping parameter t_{ij} then contains three terms: t, t', and t'' for the first, second, and third neighbors. U is the on-site Coulomb interaction, and μ is the chemical potential. We take the parameter values of the t-t'-t''-U model to be t'/t= -0.34, t''/t=0.23, and U/t=10, which are realistic ones for the 2D cuprates.²

In AR-2PPES examined in the present work, we consider the situation that the pump photon induces a dipole transition from occupied states to UHB and the probe photon kicks an electron in UHB out of sample. Generally there are two kinds of contributions for the electron energy distribution of AR-2PPES:^{9,10} One is due to simultaneous excitations that is given, at zero temperature, by

$$I_{s}(E_{\rm kin},\omega_{1},\omega_{2},\mathbf{k}) = \frac{2\pi}{N} \sum_{f,\sigma} \left| \sum_{m} \frac{\langle f|c_{\mathbf{k},\sigma}|m\rangle\langle m|j_{x}|i\rangle}{E_{m} - E_{i} - \omega_{1} - i\Gamma_{im}} \right|^{2} \times \delta(E_{\rm kin} + E_{f} - E_{i} - \omega_{1} - \omega_{2}), \quad (2)$$

and the other is due to two sequential (cascade) excitations, expressed as



FIG. 1. Schematic picture of two-photon photoemission processes in insulating cuprates. Two processes are shown: The pump photon with energy ω_1 excites an electron from (a) the lower Hubbard band (LHB) [more precisely the Zhang-Rice singlet band (ZRB)] or (b) the nonbonding (NB) oxygen band to the upper Hubbard band (UHB). The excited electron is emitted outside with the kinetic energy $E_{\rm kin}$ by the probe photon with energy ω_2 .

$$I_{c}(E_{\rm kin},\omega_{1},\omega_{2},\mathbf{k}) = \frac{(2\pi)^{2}}{N} \sum_{f,\sigma} \sum_{m} \frac{|\langle f|c_{\mathbf{k},\sigma}|m\rangle\langle m|j_{x}|i\rangle|^{2}}{\Gamma_{mm}} \times \delta(E_{m}-E_{i}-\omega_{1})\,\delta(E_{\rm kin}+E_{f}-E_{m}-\omega_{2}),$$
(3)

where N is the number of sites, E_{kin} is the kinetic energy of photoelectron, and $\omega_1(\omega_2)$ is the pump-photon (probephoton) energy. The state $|i\rangle$ is the ground state of a halffilled system with energy of E_i , and $|m\rangle(|f\rangle)$ is the intermediate (final) state with energy of E_m (E_f), which is the eigenstate of H_{Hub} . The current operator j_x connects $|i\rangle$ with $|m\rangle$, where an electric field is assumed to have a polarization along the x direction in the square lattice. We choose the energy relaxation constant Γ_{mm} to be twice as large as the phase relaxation constant Γ_{im} neglecting the pure dephasing.¹¹ The relaxation constants are also assumed to be independent of $|m\rangle$: $\Gamma_{mm} = 2\Gamma_{im} = 2\Gamma$. We choose $\Gamma = 0.2t$.

In order to calculate I_s and I_c , we use numerically exact diagonalization techniques for small clusters with periodic boundary conditions. For I_s in Eq. (2), a standard technique combining the conjugate gradient and Lanczos methods is employed. For I_c in Eq. (3), we select some dozens of $|m\rangle$ that have large values of $|\langle m|j_x|i\rangle|^2$. The delta functions are broadened by a Lorentzian with a width of 0.2*t*.

It is important to notice that AR-2PPES spectrum generally contains two kinds of energy-dependent spectral features.¹² One is the spectrum that satisfies $E_{kin} = \omega_1 + \omega_2$ $+ \epsilon_i$, ϵ_i being the energy level of an occupied state. Since E_{kin} is proportional to $\omega_1 + \omega_2$, a peak structure obeying this relation is called the 2ω peak, from which we can extract knowledge of the occupied state. The other gives $E_{kin} = \omega_2 + \epsilon_m$, ϵ_m being the energy level of an unoccupied state. A peak satisfying this relation is called the ω peak and provides knowledge of the unoccupied state.



FIG. 2. Pump-photon energy ω_1 dependence of two-photon photoemission spectra at $\mathbf{k} = (\pi, 0)$ in a 4×4 *t-t'-t"-U* cluster. (a) Simultaneous excitation, and (b) cascade excitation. The range of ω_1 is determined from the optical conductivity $\sigma(\omega)$ in (c). The dashed (dotted) line in (a) and (b) denotes a guide to the eyes for the spectrum coming from the LHB (UHB).

First, we examine the case where the pump photon induces a dipole transition from ZRB to UHB, as schematically depicted in Fig. 1(a). Since ZRB is regarded as the LHB in the single-band Hubbard model, the dipole transition is controlled by a current operator obtained from Eq. (1): $j_x=i\Sigma_{k,\sigma}\alpha_{\bf k}c_{k,\sigma}^{\dagger}c_{{\bf k},\sigma}$ with $\alpha_{\bf k}=-2t\sin k_x-4t'\sin k_x\sin k_y$ $+2t''\sin 2k_x$.

Figures 2(a) and 2(b) show the dependence of I_s and I_c , respectively, at $\mathbf{k} = (\pi, 0)$ on the pump-photon energy ω_1 , calculated by using a half-filled 4×4 cluster where $\mu = 4.55t$. We choose the range of $\omega_1(5t \le \omega_1 \le 13t)$ from the optical conductivity $\sigma(\omega)$ shown in Fig. 2(c). We note that the range examined corresponds to 1.7 eV $\leq \omega_1 \leq 4.6$ eV, taking t =0.35 eV. Since I_s and I_c are plotted as a function of (E_{kin}) $-\omega_2)/t$, the 2 ω peak containing information on the LHB appears as a structure whose position increases linearly with ω_1 . Such a peak is seen along the dashed lines. We find that the 2ω peak in I_s is clearer than that in I_c . This is due to the fact that I_s includes a virtual excitation via $|m\rangle$ but not in I_c . As for a structure whose position is independent of ω_1 , we can find a broad peak at around $E_{kin} - \omega_2 = 2.5t$ in both I_s and I_c . The weight is enhanced at around $E_{kin} - \omega_2 = 8.5t$, where $\sigma(\omega)$ shows a peak. For the ω peak, I_s and I_c show qualitatively similar ω_1 dependence.

Figures 3(a) and 3(b) show the detailed momentum dependence of the 2ω and ω peaks in I_s at $\omega_1=6t$ and 9t,



FIG. 3. Momentum dependence of two-photon photoemission spectra I_s from the simultaneous process in a $4 \times 4 t - t' - t'' - U$ cluster. The pump-photon energy is (a) $\omega_1 = 6t$ and (b) $\omega_1 = 9t$. The single-particle spectral function $A(\mathbf{k}, \omega)$ at half filling is shown in (c). $A(\mathbf{k}, \omega)$ below and above $\omega/t=0$ can be comparable to I_s in (a) and (b), respectively.

respectively. The former, plotted as functions of $E_{\rm kin} - \omega_1$ $-\omega_2$, can be compared to the occupied side of the singleparticle spectral function $A(\mathbf{k}, \omega)$ at half filling² in Fig. 3(c), while the latter can be compared to the unoccupied side. As expected, I_s at $\omega_1 = 6t$ shows momentum dependence globally similar to that of $A(\mathbf{k}, \omega)$ in the energy region of $-8 < \omega/t$ <0, although the details of spectral shape, for example, at $\mathbf{k} = (0,0)$ are different. We note that the spectral weight below $E_{\rm kin} - \omega_1 - \omega_2 = -8t$ is due to one-photon photoemission keeping an electron in the UHB. In I_s at $\omega_1 = 9t$, despite the broad spectral-weight distributions and additional weights at around $E_{kin} - \omega_2 = 3t$ in the **k**=(0,0), ($\pi/2$,0), and (0, $\pi/2$) spectra, the momentum dependence shows a similarity to that of $A(\mathbf{k}, \omega)$ for $\omega > 0$: From (π, π) to $(\pi, 0)$ and $(0, \pi)$, the spectra show a dispersive feature qualitatively consistent with the dispersion in the UHB. However, because of diffusive features in the spectra, it seems to be difficult to identify the location of the bottom of the UHB exactly from the ω -peak analysis.

Next we consider the case where the energy of the pump photon is tuned to an excitation from the NB oxygen band to UHB [see Fig. 1(b)]. In order to simplify the problem, we



FIG. 4. (a) Angle-resolved two-photon photoemission spectra I_s from the simultaneous process in the case that the pump photon excites an electron from the NB band, obtained by using a $\sqrt{20} \times \sqrt{20} t - t' - t'' - J$ cluster. The energy of the pump photon is tuned to the energy difference between the NB band and the bottom of the UHB with momentum $(\pi, 0)$ and $(0, \pi)$ as shown in the electron-addition spectral function $A(\mathbf{k}, \omega)$ in (b).

construct the Wannier orbitals centered at the copper and oxygen sites according to Ref. 1, and rewrite a current operator between copper and oxygen sites by using the Wannier orbitals. After all, we obtain an expression of the current operator between the occupied NB band and unoccupied UHB: $j_x = \sum_{\mathbf{k},\sigma} \beta_{\mathbf{k}} c_{\mathbf{k},\sigma}^{\dagger} b_{\mathbf{k},\sigma}$, where $b_{\mathbf{k},\sigma}$ is the annihilation operator NB of the state, and $\beta_{\mathbf{k}} = C \cos(k_x/2) \sin(k_y/2) / \sqrt{1 - (\cos k_x + \cos k_y)/2}$ with $C=2d_{Cu-O}T_{pd}$, d_{Cu-O} and T_{pd} being the distance and hopping amplitude between neighboring Cu and O, respectively. In the present work, we assume that (i) the dispersion of the NB band is negligible¹³ and (ii) there is no interaction between the hole left in the NB band and electrons in both LHB and UHB. Under these assumptions, we can neglect $b_{\mathbf{k},\sigma}$ in j_x . Thus, the dipole transition process results in an electronaddition process with the momentum-dependent factor β_k . We also take the coefficient C to be unity for simplicity. In addition to these simplifications, we use the t-t'-t''-J model instead of Eq. (1), since only UHB is necessary in this process. We note that the t-t'-t''-J model gives almost the same results as those of the t-t'-t''-U model when U is large enough to satisfy $J=4t^2/U$. The chemical potential of the half-filled t'-t'-t''-J model is determined in order for LHB and UHB to be separated by U^{14} .

In Fig. 4, we show I_s obtained by tuning ω_1 to an excitation energy from the localized NB band to the bottom of UHB located at $(\pi, 0)$ and $(0, \pi)$. We note that only the $(0, \pi)$ state is occupied by the excitation according to the momentum-dependent coefficient $\beta_{\mathbf{k}}$. Here $\omega_1 = \varepsilon_p + 2.4t$ with the level of the NB oxygen band ε_p . The highest-energy structure in I_s is located at $(0, \pi)$ and its energy is the same as that in $A(\mathbf{k}, \omega)$. This means that, by tuning the pumpphoton energy to the bottom of the UHB, we can observe its position in the momentum and energy spaces. If we increase ω_1 to be tuned to a quasiparticle-peak position at **k** = $(4\pi/5, 2\pi/5)$ with $\omega=3.7t$ in Fig. 4(b), the high-energy edge of the 2P-APRES spectra appears at $(4\pi/5, 2\pi/5)$ with $E_{\rm kin}-\omega_2=3.7t$ (not shown). Therefore, the dispersion of the UHB near $(\pi, 0)$ and $(0, \pi)$ would be detectable by changing ω_1 , provided the dispersion of the NB band is negligible.¹³ We note that I_c shows the same behaviors as those of I_s (not shown).

In addition to the $(0,\pi)$ structure, there are spectral weights at smaller momentum region with lower kinetic energies. For example, a peak appears at (0, 0), separated from the $(0, \pi)$ peak by $\sim t$, which is not present in $A(\mathbf{k}, \omega)$. Such additional structures come from the following reason. In the process where the NB state is excited, the final state $|f\rangle$ belongs to the half-filled system whose low-lying excitations are of the spin wave. Actually the (0, 0) peak exists at the eigenstate of the spin-wave excitation. Since the peak at $(0, \pi)$ comes from the ground state of the half-filled system, the energy separation between the $(0, \pi)$ and (0, 0) peaks is the same as the spin-wave width between the momentum transfers $\mathbf{q} = (0,0)$ and $(0,\pi)$. Accordingly the $\mathbf{q} = (\pi,\pi)$ spin-wave state contributes to the $(\pi, 0)$ peak in Fig. 4(a), which is thus expected to be degenerate with the $(0, \pi)$ peak in the thermodynamic limit. After all, we can say that the additional states in AR-2PPES contain knowledge of the spin excitation at half filling.

Finally we comment on experimental conditions that would confirm the present theoretical results. The most crucial point is whether one can get $E_{\rm kin}$ enough to reach to the momentum $(\pi, 0)$ and $(0, \pi)$. Here we note that the maximum of $E_{\rm kin}$ is given by $E_{\rm kin}^{\rm max} = E_{\rm gap}/2 + \omega_2$, $E_{\rm gap}$ being the Mott-gap magnitude with approximately 4t according to Fig.

3(c). In the case of the excitation from LHB to UHB, ω_1 should be around 9t from Figs. 2 and 3. If $\omega_2 = \omega_1$, $E_{kin}^{max} = 11t \sim 4 \text{ eV}$. In the case from the NB band, ω_1 would be 9t+E_B, where E_B is the binding energy of ZRB and approximately 2 eV. Thus, by assuming $\omega_2 = \omega_1$, $E_{kin}^{max} \sim 6 \text{ eV}$ in this case. On the other hand, the minimum value of E_{kin} necessary to reach (π ,0) can be estimated to be $\sim 6 \text{ eV}$, by taking the lattice constant ($\sim 3 \text{ Å}$) and the work function ($\sim 4 \text{ eV}$) into account. This leads to the conclusion that, under the condition $\omega_2 = \omega_1$, the momentum (π ,0) cannot be reached for the excitation from the LHB but can critically for the excitation from the NB band. If we take $\omega_2 > \omega_1$, the condition is relaxed and the possibility to observe the (π ,0) state is enhanced.

In summary, we have proposed that AR-2PPES is a promising technique to observe the location of the bottom of the UHB in 2D insulating cuprates. When the pump photon is tuned to an excitation from the LHB to UHB, the bottom of the UHB is less clear because of diffusive spectral features. On the other hand, when the photon energy is tuned to an excitation from NB oxygen band, we clearly see the bottom of the UHB. In addition to this, additional spectra that are not present in inverse photoemission spectra emerge in AR-2PPES. Their origin is attributed to the spin excitation expected at half filling.

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