# **Magnetic and electric hyperfine interactions in the rare-earth indium compounds** *R***2In studied by 111Cd perturbed angular correlations**

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The magnetic and electric hyperfine interactions of the probe nucleus <sup>111</sup>Cd on the In site of the ferromagnetic rare-earth  $(R)$  indium compounds  $R_2$ In  $(R=Pr, Nd, Sm, Gd, Dy, Ho, Er, and Tm)$  have been investigated by perturbed angular correlation (PAC) spectroscopy. In the paramagnetic phase, the axially symmetric quadrupole interaction (QI) decreases by more than a factor of 20 from  $R=Pr$  to  $R=Er$  indicating a significant influence of the 4*f* electrons on the charge distribution at the In site. In the ferromagnetic phase, the spin and temperature dependence of the magnetic hyperfine field  $B<sub>hf</sub>$  and its orientation relative to the *c* axis of hexagonal *R*<sub>2</sub>In have been determined by measuring the combined magnetic and electric hyperfine interaction as a function of temperature for all *R* constituents. The sign of *Bhf*, determined by applying an external field of 4 T, is positive for light and negative for heavy *R*2In. The comparison of the 111Cd hyperfine fields in *R*2In and in *R* metals suggests that the indirect 4*f* −4*f* coupling is mediated by intra-atomic 4*f* −5*d* exchange and 5*d*−5*d* interaction of neighboring *R* atoms rather than by 4*f* exchange with the *s*-conduction electrons. The spin dependence of the saturation value of  $B<sub>hf</sub>(0)$  and of the Curie temperature in  $R<sub>2</sub>$ In reflect a substantial difference of the *f* −*d* exchange parameter  $\Gamma$  between the light (LR=Pr, Nd, Sm) and the heavy (HR=Gd, Tb, ...)  $R_2$ In compounds:  $\Gamma_{LR}/\Gamma_{HR} = 1.5(1)$ . The deviation of the magnetic hyperfine field from its saturation value at low temperatures can be explained by the excitation of spin waves. In Gd<sub>2</sub>In, the low temperature decrease of *Bhf* follows Bloch's *T*3/2 relation. In the other *R*2In compounds with nonzero angular momentum of the *R* constituent, the temperature dependence of  $B_{hf}$  is best described by the modified power law  $T^{3/2}$  $\exp(-\Delta/k_B T)$  which suggests the existence of an energy gap of about  $\Delta/k_B \approx 15-20$  K in the spin wave spectrum of these anisotropic ferromagnets. With the exception of  $Pr_2In$  and  $Nd_2In$ , where the hyperfine field vanishes discontinuously at the Curie temperature, the magnetic phase transitions of  $R_2$ In are of second order. A critical increase of the linewidth of the magnetic interaction close to the phase transition indicates a spatial variation of the exchange interaction with a spread of the Curie temperature of about 2–5 K. The temperatureinduced changes of the orientation of the  $4f$  spins relative to the *c* axis of  $R_2$ In have been deduced from the angle between  $B<sub>hf</sub>$  and the symmetry axis of the electric field gradient.

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### **I. INTRODUCTION**

Measurements of magnetic and electric hyperfine interactions (hfi) are a useful tool for the investigation of magnetically ordered compounds. Electron spin polarizations, unquenched orbital angular moments, and magnetic dipole moments can give rise to magnetic hyperfine fields  $B<sub>hf</sub>$  at nuclei in magnetic compounds. These hyperfine fields provide information on the exchange interactions leading to spontaneous magnetic order, on the order of magnetic phase transitions, on spin wave excitations, on relaxation processes, and on other parameters characterizing a magnetic system. They can be determined by measuring their interaction with known nuclear magnetic moments using techniques such as NMR, Mössbauer spectroscopy, perturbed angular correlations (PAC), and  $\mu$ SR. Additional information, *e.g.*, on the orientation of the magnetic moments or on magnetoelastic distortions, can frequently be obtained from the nuclear electric quadrupole interaction (QI) between the quadrupole moment of the nuclear probe and an electric field gradient (EFG) which arises if the charge distribution surrounding the probe site has noncubic symmetry.

The magnetic systems investigated by hyperfine spectroscopic techniques range from the pure 3*d* and 4*f* elemental ferromagnets to ordered and disordered intermetallics, inorganic compounds, amorphous alloys, nanocrystalline materials, etc. Much of the experimental and theoretical hyperfine interaction work has been focused on magnetic systems involving the rare earth  $(R)$  elements Ce to Tm.<sup>1</sup> Because these elements differ in the number of well-shielded 4*f* electrons, they have rather similar chemical properties. The 4*f* spins, which play a decisive role in the exchange interactions, and the orbital contributions to the 4*f* magnetic moments, however, vary strongly with the number of 4*f* electrons. Consequently, one finds a large number of isostructural series of *R* compounds that—for different *R* constituents—differ only

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slightly in the crystallographic properties, but strongly in the magnetic properties and thus offer very favorable conditions for the separation of the magnetic from other solid-state parameters.

There are numerous hyperfine interaction studies of intermetallic compounds of rare earths with other elements.<sup>2</sup> In most of these studies, the hyperfine interaction is observed at impurity nuclei or the nuclei of the non-rare-earth constituents. At the  $R$  nuclei (except Gd) one has huge magnetic fields and electric field gradients, caused by the unquenched orbital angular momentum of the 4*f* shell and a precise determination of the much smaller contributions to the hyperfine interaction produced by the magnetic host may become difficult. Intermetallic compounds of the rare earths with 3*d* transition elements have attracted much interest because of the coexistence and interaction of highly localized  $(4f)$  and itinerant (3*d*) electrons. Hyperfine interaction studies of intermetallic compounds of rare earth and *sp* elements have frequently been aiming at information on the mechanism of the indirect exchange, which couples the spins of the localized nonoverlapping 4*f* electrons.

In the present work, we have used the probe nucleus <sup>111</sup>Cd for a PAC investigation of the magnetic and electric hyperfine interactions in the rare-earth indium compound  $R<sub>2</sub>$ In that is part of a systematic study of intermetallic compounds of rare earth and  $sp$  elements. Apart from  $R_2$ In, the *R*-In phase diagram presents several other intermetallic compounds, $3$  offering not only the possibility to vary the magnetic constituent in a given structure, but also to study the magnetic properties of different structures with the same *R* element.

The particular choice of In rather than another *sp* constituent for such a systematic investigation is related to the experimental technique employed: In most PAC and some Mössbauer studies, the probe nucleus is an impurity in the investigated compound, which raises the question of the lattice site occupied by the probe atom. Sometimes the hyperfine parameters provide an answer to this question, but frequently the probe site and the site preference (in cases of several nonequivalent lattice sites) cannot be determined from the hyperfine parameters alone, which leads to obvious difficulties for the interpretation of the experimental data. This problem does not arise in  $<sup>111</sup>$ Cd PAC studies of In com-</sup> pounds. The excited states of <sup>111</sup>Cd, one of the most favorable nuclei for PAC measurements, are populated by the electron capture decay of the radioisotope  $111$ <sub>In</sub>. Although the decay makes the daughter isotope  $111$ Cd an impurity in In compounds, the probe site is well known because the recoil caused by the electron capture decay is far too small to dislocate the isotope from its lattice position.

In the following, we report a series of PAC measurements of the magnetic and electric hyperfine interactions of <sup>111</sup>Cd on In sites of  $R_2$ In, carried out for  $R=Pr$ , Nd, Sm, Gd, Dy, Ho, Er, and Tm as a function of temperature in the range 10 K $\leq$  T $\leq$  300 K. Results for Tb<sub>2</sub>In have been published previously.4 The questions addressed in this study are the spin dependence of the magnetic hyperfine field, the influence of the *R* constituent on the temperature dependence of  $B<sub>hf</sub>$ , the order of the magnetic phase transitions, the spin orientation and its changes with temperature, and the variation of the EFG at the In site across the  $R_2$ In series.

# **II. CRYSTAL STRUCTURE AND MAGNETIC PROPERTIES** OF  $R_2$ In

The crystal structure of  $R_2$ In reported by Palenzona<sup>5</sup> and Franceschi<sup>6</sup> is isomorphous with the hexagonal Ni<sub>2</sub>In lattice. The unit cell contains two structurally different *R* sites and one In site which has 11 *R* atoms at different distances  $d_n$  as nearest neighbors (NN). There are 6 NN *R* atoms at  $d_1$  $=(c^2/16+a^2/3)^{1/2}$ , 2 NN *R* atoms at  $d_2=c/2$ , and 3 NN *R* atoms at  $d_3 = a/\sqrt{3}$ . Both lattice parameters *a* and *c* (*a*  $=0.5534$  nm,  $c=0.6893$  nm for  $R=Pr$ ) decrease linearly with increasing *R* atomic number, *a* slightly stronger than *c*. The ratio  $c/a$  therefore increases from  $c/a = 1.246$  for  $R = Pr$  to  $c/a = 1.255$  for  $R = Tm$ <sup>5</sup>

The magnetic properties of  $R_2$ In have been investigated by magnetization and resistivity measurements, $7-9$  by neutron diffraction,<sup>10</sup> and by <sup>119</sup>Sn Mössbauer spectroscopy.<sup>11,12</sup> In the paramagnetic phase, all  $R_2$ In (except Sm<sub>2</sub>In) show Curie-Weiss behavior of the susceptibility with effective moments close to the free-ion values and positive paramagnetic Curie temperatures  $(\theta_p \le 197 \text{ K})$ .<sup>9</sup> In the magnetically ordered phase the susceptibility of *R*=Sm, Gd, Tb, and Dy indicates a transition from ferromagnetic to antiferromagnetic order as temperature is decreased.  $Gd<sub>2</sub>$ In presents a metamagnetic transition at *T*=99.5 K. For *R*=Ho, Er, and Tm the susceptibility shows a maximum at intermediate temperatures without giving an indication of the type of magnetic order.

The neutron diffraction studies of  $R_2$ In carried out for  $R$  $=$  Gd, Tb, Er (Ref. 10) indicate a ferromagnetic structure below  $T_c$  with the 4*f* moments on both *R* sites close to the free-ion value. In the antiferromagnetic structure of  $Gd<sub>2</sub>$ In below 100 K, the spins are perpendicular to the hexagonal *c* axis.  $Gd<sub>2</sub>$ In presents a helicoidal structure with all spins in a given basal plane parallel to each other and a spiral angle between subsequent planes of about  $60^{\circ}$  at 20 K. Tb<sub>2</sub>In is ferromagnetic down to 45 K with the 4*f* moments in the basal plane. At lower temperatures, a small helicoidal component is observed. Er<sub>2</sub>In also presents a ferromagnetic structure with the magnetic moments tilted out of the basal plane by an angle of  $13(5)^\circ$  independent of temperature. At 1.6 K, indications of a helicoidal component have been found.

#### **III. EXPERIMENTAL DETAILS**

#### **A. Sample preparation and equipment**

The PAC measurements were carried out with the  $171-245$  keV cascade of  $111$ Cd, which is populated by the electron capture decay of the 2.8  $d$  isotope<sup>111</sup>In. In the first step of the source preparation, In metal was doped with radioactive <sup>111</sup>In (concentration  $\sim 10^{-8}$ ). For this purpose, trace amounts of  $111$ In were solute extracted with ethylic ether from a commercially available aqueous solution of  $\frac{111}{10}$ Cl<sub>3</sub> and deposited on a thin In foil. It was found that the radioactivity could be reduced to the metallic state either by melting the foil in a hydrogen atmosphere or by diffusion, heating the In foil to 400 K for 1 h. The metallic state was confirmed by taking a PAC spectrum of the doped foil. Both procedures lead to the well-known PAC spectrum of <sup>111</sup>Cd in In metal. Most of the investigated samples were produced using the simpler diffusion process. In the second step of the sample preparation, the doped In was arc-melted in an argon atmosphere with the rare-earth metals in the stoichiometric ratio.

 $R_2$ In compounds are known to rapidly oxidize in air.<sup>5</sup> To avoid degradation, the samples (metallic spheres of about 30 mg) were not ground to a powder, but immediately after production transferred to the vacuum of a closed-cycle He refrigerator which was used to cool them to  $10 K \leq T$  $\leq$  300 K. The temperature was stabilized to about 0.1 K. The PAC measurements were carried out with a standard 4-detector  $BaF<sub>2</sub>$  setup.

Inactive samples of  $R_2$ In with  $R=Pr$ , Nd, Sm, Gd, Dy, Ho, Er, and Tm were characterized by x-ray diffraction measurements. The compounds were ground to a powder in an argon atmosphere and mixed with water-free silicon grease. In all cases except  $Pr<sub>2</sub>In$ , the diffraction pattern of the Ni<sub>2</sub>In structure reported by Palenzona<sup>5</sup> was observed. Contaminations by foreign phases were not detected. Pr<sub>2</sub>In was found to oxidize very rapidly even under the silicon grease cover and only slight indications of the diffraction peaks were observed.

#### **B. Data analysis**

The angular correlation of two successive  $\gamma$  rays of a  $\gamma$ - $\gamma$  cascade, expressed by angular correlation coefficients  $A_{kk}$  ( $k=2,4$ ) may be modulated in time by hyperfine interactions in the intermediate state of the cascade. For polycrystalline samples, this modulation can be described by the perturbation factor  $G_{kk}(t)$  which depends on the multipole order, the symmetry and time dependence of the interaction, and on the spin of the intermediate state (for details see, e.g., Frauenfelder and Steffen<sup>13</sup>). For a static hyperfine interaction, the perturbation factor can be written as a sum of oscillatory terms:

$$
G_{kk}(t) = s_{k0} + \sum_{n} s_{kn} \cos(\omega_n t) \exp\left(-\frac{1}{2}\delta\omega_n t\right). \tag{1}
$$

The frequencies  $\omega_n$  are associated with the energy differences between the hyperfine levels into which the nuclear state is split by the hyperfine interaction. Except for a few simple cases where analytical expressions for the perturbation factor are available, the frequencies  $\omega_n$  and the amplitudes  $s_{kn}$  have to be determined by diagonalization of the interaction Hamiltonian. The number of terms in Eq.  $(1)$  depends on the spin *I* of the intermediate state. The exponential factor accounts for possible distributions of the static hyperfine interaction caused by structural, chemical, and other defects, which lead to an attenuation of the oscillatory PAC pattern. The parameter  $\delta$  is the relative width of a Lorentzian distribution.

Frequently, several fractions of nuclei subject to different hyperfine interactions are found in the same sample. The effective perturbation factor is then given by

$$
G_{kk}(t) = \sum_{i} f_i G_{kk}^i(t). \tag{2}
$$

 $f_i$  (with  $\Sigma_i f_i = 1$ ) is the relative intensity of the *i*th fraction.

In magnetically ordered  $R_2$ In the probe nuclei  $\frac{111}{\text{In}}/111\text{Cd}$ are subject to a magnetic hyperfine field and an EFG related to the noncubic point symmetry of the In site. The hyperfine field interacts with the nuclear magnetic moment and the EFG with the nuclear electric quadrupole moment *Q* of the intermediate state of the cascade. In the most general case, the theoretical perturbation function for a combined magnetic and electric hyperfine interaction depends on five interaction parameters and on the nuclear spin *I*. The interaction parameters are the magnetic frequency  $\nu_M = g \mu_N B_{hf}/h$  (*g* represents the nuclear *g* factor,  $\mu_N$  the nuclear magneton), the quadrupole frequency  $v_q = eQV_{zz}/h$ , the asymmetry parameter  $\eta=(V_{xx}-V_{yy})/V_{zz}$ , and the Euler angles  $\theta$  and  $\varphi$ which describe the relative orientation of the magnetic hyperfine field and the EFG tensor.  $V_{ii} = \frac{\partial^2 V}{\partial i^2} (i = x, y, z)$  are the principal-axis components of the EFG tensor with  $|V_{xx}|$  $\leq |V_{yy}| \leq |V_{zz}|.$ 

As expected from the crystal structure and confirmed by the PAC spectra of the paramagnetic phase (see below), the EFG at the In site of the  $R_2$ In is axially symmetric  $(\eta=0)$ with respect to the *c* axis. In this case, the energy eigenvalues of the combined interaction are independent of the Euler angle  $\varphi$ , and for a given nuclear spin *I* the perturbation factor depends on only three parameters:  $\nu_M$ ,  $\nu_q$ , and the angle  $\theta$ between  $B_{hf}$  and the symmetry axis of the EFG.

The number of independent parameters, which can be extracted from the PAC spectra of  $^{111}Cd:R_2In$  is further reduced by the fact that in most  $R_2$ In compounds the magnetic interaction is much stronger than the quadrupole interaction. (See below.) For  $\nu_M \gg \nu_q$  the eigenvalues of the Hamiltonian are to first order given by  $E_M = h\nu_M + C_{l,m}h\nu_q(3\cos^2\theta - 1)$  and consequently the quadrupole frequency  $v_q$  and the angle  $\theta$ cannot be determined independently by a measurement of the interaction energies. In most cases, the experimental results are therefore expressed in terms of the magnetic interaction frequency  $\nu_M$ , the quadrupole parameter  $\nu_q^{\theta}$  $=(3 \cos^2 \theta - 1)v_q$ , and the relative width  $\delta$  of the hfi distribution.

#### **IV. MEASUREMENTS AND RESULTS**

PAC spectra  $A_{22}G_{22}(t)$  of <sup>111</sup>Cd in  $R_2$ In spectra were recorded for the constituents *R*=Pr, Nd, Sm, Gd, Dy, Ho, Er, and Tm as a function of temperature between 10 K and 300 K. The hyperfine parameters of  $^{111}Cd$ : Tb<sub>2</sub>In are given in Ref. 4.

The Curie temperatures derived from the present PAC data differ considerably from those found in the <sup>119</sup>Sn Mössbauer study of  $R_2$ In (Refs. 11 and 12) (see below) in which the samples had a Sn content of about 0.5%. To investigate to which extent this relatively high concentration of Sn impurities (compared to the In concentration of  $\sim 10^{-8}$ ) affects the order temperature, the <sup>111</sup>Cd PAC measurements were extended to  $Gd_2In_{0.95}Sn_{0.05}$ .

The sign of the magnetic hyperfine field was determined for *R*=Nd, Sm, Gd, Dy, and Tm by applying an external



FIG. 1. PAC spectra of <sup>111</sup>Cd in the paramagnetic phase of some  $R_2$ In at 290 K.

magnetic field of 4 T at 4.2 K and observing the rotation of the integral angular correlation in a time-window of 3 ns. In the light  $R_2$ In,  $R = Nd$ , Sm the hyperfine field was found to be positive, i.e., parallel, in the heavy  $R_2$ In,  $R = Gd$ , Dy, Tm negative, i.e., antiparallel to the external field. For a comparison with  $R_2$ In, the measurements were extended to some rare-earth metals (Sm, Gd, Dy). As in  $R_2$ In, the sign of the  $111$ Cd hyperfine field is positive in light (Sm) and negative in heavy (Gd, Dy) *R* metals.

# A. The quadrupole interaction of  $\frac{111}{C}$ Cd in paramagnetic  $R_2$ In

Some of the <sup>111</sup>Cd PAC spectra  $A_{22}G_{22}(t)$  observed in the paramagnetic phase of  $R_2$ In at 290 K are shown in Fig. 1. For the light constituents  $R = Pr$ , Nd the spectra show the periodic modulation of the anisotropy typical for a perturbation by a well-defined axially symmetric QI ( $\eta \le 0.1$ ). As one moves from the light to the heavy  $R_2$ In, the strength of QI decreases drastically: The precession period in  $Gd<sub>2</sub>$ In is more than 3 times larger than in  $Pr_2In$  and at the end of the  $R<sub>2</sub>$ In series it has increased to the point that only the initial decrease of the anisotropy fits into the 600-ns-time window of <sup>111</sup>Cd. The values of the quadrupole frequency derived from these spectra are listed in Table I. In the analysis  $\nu_q$ ,  $\eta$ and  $\delta$  were treated as free fit parameters. As a measure of the temperature dependence of the QI, Table I also gives the quadrupole frequency  $v_q$  at  $T \sim 1.05$   $T_c$  in the paramagnetic phase close to the transition. In most cases, the asymmetry parameter was  $\eta \le 0.15$ , with the exception of Pr<sub>2</sub>In. In this compound, the asymmetry parameter increased substantially with decreasing temperature. Close to magnetic phase transition, one has  $\eta=0.45$ . The relative linewidth  $\delta$  of the QI distribution was found to increase across the  $R_2$ In series from  $\delta \approx 0.07$  for Pr<sub>2</sub>In to  $\delta \approx 0.3$  at the end of the series. In the case of  $Er<sub>2</sub>In the QI is too weak—compared to the time$ range available—for a determination of  $\eta$  and  $\delta$ . The quadrupole frequency of  $Er<sub>2</sub>In$  is therefore subject to a systematic uncertainty of the order of 100%. Some of the  $R_2$ In spectra showed a second component  $\left[v_q \approx 100 \text{ MHz}, \eta \approx 0\right]$ , relative intensity less than 10%] indicating a slight contamination by a nonidentified phase.

### **B. Combined magnetic and electric hyperfine interactions of**  $111$ Cd in the magnetically ordered phases of  $R_2$ In

The PAC spectra observed in the magnetically ordered phase of  $R_2$ In at 10 K are collected in Figs. 2 and 3. There are noticeable differences between the spectra of the heavy (Fig. 2) and the light (Fig. 3)  $R_2$ In. Typically, the spectra of the heavy constituents  $R = Gd$ , Dy, Ho, Er, and Tm show a large number of periodic oscillations (with the corresponding frequency decreasing from  $R = Gd$  to Tm), with the oscillation amplitudes slowly modulated in time. The periodic oscillations are caused by the magnetic interaction; the amplitude modulations reflect the much weaker QI ( $\nu_M \gg \nu_q$ ). For the light constituents  $R = Pr$ , Nd, Sm one observes nonperiodic modulation patterns, indicating that the ratio between the electric quadrupole and the magnetic dipole interaction in the light  $R_2$ In is larger than in the heavy  $R_2$ In. This is consistent with the increase of the QI observed in the paramag-

TABLE I. Experimental hyperfine interaction parameters of  $\frac{111}{Cd}$  in  $R_2$  In: The magnetic interaction frequency  $v_M(0)$ , the coefficient *B*, and the energy gap  $\Delta/k_B$  [see Eq. (8)] derived from the low temperature variation of the magnetic frequency  $\nu_M(T)$ , the Curie temperature  $T_C$ , the quadrupole parameter  $\nu_q^{\theta}$  $=(3 \cos^2 \theta - 1)\nu_q$  at 10 K, the quadrupole frequency  $\nu_q$  in the paramagnetic phase at 290 K and close to the magnetic phase transition ( $T \approx 1.05$   $T_C$ ).

$\mathbb{R}$		$\nu_M(0)$ (MHz) $B(10^{-4} \text{ K}^{2/3}) \Delta/k_B(\text{K}) T_C(\text{K})$			$\nu_a^{\theta}(\text{MHz})$		$v_q$ (290 K)(MHz) $v_q$ (T $\approx$ 1.05 $T_c$ )(MHz)
Pr	20(1)			54	$\nu_a = 38(1)$	38.3	64.7; $\eta$ =0.45
Nd	39.6	4.3(2)	22(3)	104	$v_a = 54.5(5)$	32.5	48.6
Sm	51.0	4.0(1)	54(3)	163	68(1)	26.3	34.5
Gd	72.1	2.7(1)		191	22.0(5)	13.1	17
Tb	59.6	3.5(1)	13(4)	163	9.0(5)	11.7(2)	15.7
Dy	51.7	5.8(3)	20(5)	122	17.0(5)	10.3(1)	14.3
H <sub>o</sub>	40.6	11.4(2)	15(2)	83	16.5(5)	$7_{(+2,-5)}$	13.8
Er	26.3	29(2)	13(2)	43	10.7(5)	$1.5_{(+1,-1.5)}$	8.3
Tm	15.4	159(35)	15(3)	17	4.8(3)		



FIG. 2. PAC spectra of  $^{111}$ Cd in heavy  $R_2$ In;  $R = Gd$ , Tb, Dy, Ho, Er, Tm at 10 K.

netic phase from  $Er<sub>2</sub>In$  to  $Pr<sub>2</sub>In$ . The parameters of the magnetic and electric hyperfine interaction and the relative width  $\delta$  of the Lorentz distribution were extracted by fitting the theoretical perturbation function for a combined interaction to the measured spectra. Based on the results for the paramagnetic phase, it was assumed that the QI in the ferromagnetic phase has axial symmetry.

For *R*=Gd, Dy, Ho, Er, Tm, and Sm, one has  $\nu_M > \nu_a$  and therefore only the quadrupole parameter  $v_q^{\theta} = (3 \cos^2 \theta - 1)v_q$ could be determined unambiguously. The value of  $\nu_M(0)$ , extrapolated from the temperature dependence of the magnetic hyperfine frequency (see Sec. V B 1), and  $v_q^{\theta}$  at 10 K are listed in Table I. The Lorentz width  $\delta$ , which in the magnetically ordered phase mainly describes the distribution of the magnetic hyperfine field, was of the order of  $\delta \leq 0.03$  in



FIG. 3. PAC spectra of <sup>111</sup>Cd in light  $R_2$ In;  $R=Pr$ , Nd, Sm at 10 K.



FIG. 4. PAC spectra of  $^{111}$ Cd in Dy<sub>2</sub>In at different temperatures.

all compounds, also those with a large distribution of the QI in the paramagnetic phase.

The typical evolution with temperature of the PAC spectra in magnetically ordered heavy  $R_2$ In is illustrated in Fig. 4, using  $Dy_2In(T_C=122 \text{ K})$  as an example. One feature of these spectra merits particular attention: As one approaches the order temperature, the oscillations of the anisotropy at times  $t > 100$  nsec are increasingly attenuated and finally completely wiped out. (See the  $120 \text{ K}$  spectrum in Fig. 4,) This behavior, which has been observed in all heavy  $R_2$ In, reflects a critical increase of the Lorentzian linewidth  $\delta$  close to  $T_C$ . The linewidth  $\delta$  and the magnetic hyperfine frequency  $\nu_M$ derived from the spectra in Fig. 4 are shown in Fig. 5 as a function of temperature.

In the paramagnetic phase, the QI is expressed by the quadrupole frequency  $v_q$ , in the magnetically ordered phase by the quadrupole parameter  $v_q^{\theta} = (3 \cos^2 \theta - 1)v_q$ . The variation of these parameters with temperature for  ${}^{11}Cd$  in Dy<sub>2</sub>In is shown in the lower section of Fig. 6. The magnetic hyper-



FIG. 5. The temperature dependence of the magnetic hyperfine frequency of  $^{111}$ Cd (full triangles) in Dy<sub>2</sub>In (left-hand scale). The solid line corresponds to the molecular-field magnetization calculated for the angular momentum  $J=15/2$  of  $Dy^{3+}$ . The full circles show the relative linewidth  $\delta$  of the magnetic hyperfine field (righthand scale).



FIG. 6. The quadrupole frequency  $v_q$  and the parameters  $v_q^{\theta}$ =(3 cos<sup>2</sup> $\theta$ −1) $\nu_q$  of <sup>111</sup>Cd in the paramagnetic and the ferromagnetic phase, respectively, of  $Dy_2$ In as a function of temperature. The upper section shows the angle  $\theta$  between the direction of  $B_{hf}$  and the symmetry axis of the EFG in ferromagnetic  $Dy_2$ In, derived from the experimental values of  $\nu_q^{\theta}(T)$  (lower section), assuming that the temperature dependence  $v_q(\vec{T})$  measured in the paramagnetic phase can be extrapolated to the ferromagnetic region (dashed line in the lower section). The solid line in the upper section corresponds to the temperature dependence of the angle  $\theta$ , derived from the quadrupole interaction of the probe  $^{119}$ Sn in Dy<sub>2</sub>In. (Ref. 11).

fine frequencies  $\nu_M(T)$  of all heavy  $R_2$ In compounds investigated in this study are collected in Fig. 7.

As an example of the temperature dependence of the <sup>111</sup>Cd PAC spectra in the light  $R_2$ In, we show in Fig. 8 a series of spectra observed in Nd<sub>2</sub>In. These present several interesting aspects. One is the observation that the amplitude of the PAC pattern in the paramagnetic phase, which is a measure of the fraction of the sample in the paramagnetic state, decreases continuously as one approaches the magnetic phase transition at  $T_c$ =104 K from higher temperatures and finally gives way to the nonperiodic pattern of the ferromagnetic phase. Such behavior is evidence for a coexistence of the paramagnetic and the ferromagnetic phases in a small temperature interval around the magnetic order transition (Ref. 14 ). The spectra of <sup>111</sup>Cd:Nd<sub>2</sub>In (Fig. 8) close to  $T_c$ 





FIG. 8. PAC spectra of  $^{111}$ Cd in Nd<sub>2</sub>In at different temperatures.

were therefore analyzed assuming two fractions of probe nuclei, one with the relative intensity *f para* describing probes in the paramagnetic phase, the other one with intensity  $(1-f_{para})$  describing probes in the ferromagnetic phase. The resulting variation of the paramagnetic fraction with temperature is shown in the lower section of Fig. 9.

The second interesting aspect of  $Nd<sub>2</sub>In—and$ Pr2In—concerns the order of the magnetic phase transition.



FIG. 7. The temperature dependence of the magnetic hyperfine frequency of  $^{111}$ Cd in heavy  $R_2$ In;  $R =$ Gd, Tb, Dy, Ho, Er, Tm. The solid lines represent the molecular-field magnetizations, calculated for the respective angular moment *J* of the *R* constituents. The dotted lines are to guide the eyes.

FIG. 9. The magnetic interaction frequency  $\nu_M$ , the quadrupole frequency  $v_q$ , and the angle  $\theta$  between the magnetic hyperfine field and the symmetry axis of the EFG of  $^{111}$ Cd in Nd<sub>2</sub>In as a function of temperature. The bottom section shows the temperature dependence of the ferromagnetic fraction in the vicinity of the magnetic first-order transition at  $T_C = 104$  K.



FIG. 10. The temperature dependence of the magnetic hyperfine frequency of <sup>111</sup>Cd in light  $R_2$ In;  $R=Pr$ , Nd, Sm. The solid line represents the molecular-field magnetization of Sm, calculated with the angular moment  $J=5/2$  of Sm<sup>3+</sup>. The open triangles represent the hyperfine interaction of the probe nucleus  $^{119}Sn$  in Nd<sub>2</sub>In [normalized to  $\nu_M(0)$  of <sup>111</sup>Cd]. The dotted lines are to guide the eyes.

Figure 10 displays the temperature dependence of the magnetic hyperfine frequency of  $^{111}$ Cd in the light *R*<sub>2</sub>In, *R*=Pr, Nd, and Sm. While the transition in Sm<sub>2</sub>In is of second order—as in the heavy  $R_2$ In compounds—the hyperfine field in  $Nd<sub>2</sub>In$  and  $Pr<sub>2</sub>In$  vanishes discontinuously at the transition temperature, indicating a first-order transition (FOT). The PAC observation of a FOT in  $Nd<sub>2</sub>$ In agrees with the result of the <sup>119</sup>Sn Mössbauer study of this compound. For a comparison, the Mössbauer data extracted from Ref. 11 are included in Fig. 10.

In  $Sm<sub>2</sub>In$ , the QI is still much weaker than the magnetic interaction and therefore only the QI parameter  $\nu_q^{\theta}$  $=(3 \cos^2 \theta -1)v_a$  can be derived from the measured spectra. In the light  $Pr_2In$  and  $Nd_2In$ , however, one no longer has  $\nu_q \ll \nu_M$  and therefore the quadrupole frequency  $\nu_q$  and the angle  $\theta$  between the symmetry axis of the EFG and  $B<sub>hf</sub>$  can be separated in the analysis. The temperature dependence of the angle  $\theta$  of Nd<sub>2</sub>In is shown in the topmost section of Fig. 9. In the case of  $Pr_2In$ , the analysis with respect to the angle  $\theta$  is complicated by the fact that, as one approaches the phase transition, the QI shows a considerable asymmetry which introduces the Euler angle  $\varphi$  as an additional parameter. With the asymmetry parameter fixed to the value in the paramagnetic phase close to  $T_c$ , the spectra of the ferromagnetic phase, which are practically independent of temperature, are compatible with an angle  $\theta \le 10^{\circ}$ .

#### **V. DISCUSSION**

# A. The electric field gradient of  $^{111}$ Cd in  $R_2$ In

The electric field gradient (EFG)  $V_{zz}$  of <sup>111</sup>Cd in  $R_2$ In at 290 K, calculated from the measured quadrupole frequency  $\nu_q$  (see Table I) with the quadrupole moment  $Q=0.80(10)b$ of the 245 keV state,15 decreases strongly with increasing *R* atomic number from  $V_{zz} = 2.0(2) \times 10^{17} \text{V/cm}^2$  for Pr<sub>2</sub>In to  $V_{zz}$ =0.15 × 10<sup>17</sup> V/cm<sup>2</sup> for Er<sub>2</sub>In. This decrease cannot be explained by the variation of the lattice parameters *a* and *c* across the  $R_2$ In series. Because of the lanthanide contraction



FIG. 11. The variation of the electric field gradient (EFG)  $V_{zz}$  of <sup>111</sup>Cd in *R*<sub>2</sub>In at 290 K (full circles in the lower section), calculated from the measured quadrupole frequency  $v_q$ . The dotted line in the lower section shows the lattice contribution to the EFG for the In charge state  $Z=+2$ . The full circles in the upper section represent the electronic contribution  $V_{zz}^{el}$  to the EFG, estimated from the measured values and the calculated lattice contribution. The open triangles in the upper section correspond to the root mean square radius  $\langle r_{4f}^2 \rangle^{1/2}$  of the 4*f*-wave function.

both *a* and *c* decrease slightly from Pr to Tm. The resulting variation of the EFG has been estimated by calculating the lattice contribution  $V_{zz}^{lat}$  in a point-charge model. The contributions of the  $R$  and the In sublattice to the total EFG can be expressed in terms of  $(1-\gamma_{\infty})V_{zz}^{lat}/Z$ , where  $(1-\gamma_{\infty})=30$  is the Sternheimer correction<sup>16</sup> for  $\ddot{C}d^{2+}$  and *Z* the charge state of the *R* and In ions, respectively. Between  $Pr_2In$  and  $Er_2In$ the contributions  $(1-\gamma_{\infty})V_{zz}^{lat}/Z$  of the *R* and In sublattices vary from  $-1.28$  to  $-1.52$  and from  $+0.44$  to  $+0.49$  (in units of  $10^{17}$ V/cm<sup>2</sup>), respectively. While it appears safe to use  $Z_R$ = +3 for the *R* ions, the charge state of the In ions is less obvious. Since the electronegativity of In is slightly larger than that of the *R* elements, one would expect that the In charge state in  $R_2$ In has a smaller value than in In metal  $(Z_{1n}=+3)$ . <sup>155</sup>Gd Mössbauer studies of the isomer shift in  $Gd_2$ In (Ref. 17) suggest a charge transfer of 0.25 *s*-electrons/Gd from Gd to In. To explain the trend of the EFG of  $^{111}$ Cd in *RIn<sub>3</sub>*, Mishra *et al.*<sup>18</sup> had to assume  $Z_{In}$  $= +1$ . In Fig. 11 we compare the measured EFG  $V_{zz}$  to the lattice EFG  $(1 - \gamma_{\infty})V_{zz}^{lat}$  calculated for the In charge state *Z*  $=+2$  (dotted line in the lower section of Fig. 11). The comparison shows that the lanthanide contraction produces a slight increase of  $(1 - \gamma_{\infty}) V_{zz}^{lat}$  across the *R*<sub>2</sub>In series. Other In charge states lead to the same trend, but different absolute values of  $(1 - \gamma_0)V_{zz}^{lat}$ . The strong decrease of the measured EFG with increasing *R* atomic number must therefore be attributed to changes of the valence and conduction electron contribution to the EFG. As *ab initio* calculations of the EFG in  $R_2$ In are not available, we write the total EFG—for a qualitative discussion—as a sum of a lattice and an electronic contribution,

$$
V_{zz} = (1 - \gamma_{\infty}) V_{zz}^{lat} + V_{zz}^{el}.
$$
 (3)

Assuming that the two contributions have opposite signs, as suggested by the systematic of impurity EFG's in noncubic

metals, $19$  the trends of the experimental EFG and of  $(1)$  $-\gamma_{\infty}$ ) $V_{zz}^{lat}$  in Fig. 11 imply that the electronic part  $V_{zz}^{el}$  decreases strongly with increasing  $R$  atomic number. The variation of  $V_{zz}^{el}$ , derived from the experimental EFG for the In charge  $Z_{In} = +2$ , is shown in the upper section of Fig. 11. As the number of 4*f* electrons is the main parameter changing between Pr and Er, this variation is likely to be related to changes in the properties of the 4*f* electrons. Remarkably, the *Z* dependence of the electronic EFG contribution is very similar to that of the root mean square 4*f* radius, which characterizes the radial extension of the 4*f* wave function. (See open triangles connected by the dashed line in the upper section of Fig. 11, values of  $\langle r_{4f}^2 \rangle^{1/2}$  taken from Ref. 20.) Both quantities show a strong decrease in the group of the light *R* and a much weaker variation in the group of the heavy *R*. This similarity between the radial extension of the 4*f* wave function and the contribution  $V_{zz}^{el}$  to the EFG suggests that the EFG at the In site of  $R_2$ In is sensitive to the 4*f* charge distribution, possibly by overlap of the probe valence electrons with the 5*d* and 6*s* electrons of the rare earths which are hybridized by the interaction with the 4*f* shell.

The QI of  $^{119}$ Sn in  $R_2$ In (Ref. 11) shows a completely different behavior. The EFG values scatter between  $V_{zz} \sim 0$ for Er<sub>2</sub>In and  $V_{77} \sim 7.3 \times 10^{17} \text{ V/cm}^2$  for Gd<sub>2</sub>In [calculated with *Q*=−0.061(3)*b* (Ref. 21)] without a pronounced difference between light and heavy  $R_2$ In or any other systematic trend. This is remarkable since the data available on the EFG's of the probe nuclei  $\frac{111}{11}$ Cd and  $\frac{119}{5}$ Sn in the same noncubic metal<sup>22</sup> show that the  $119$ Sn EFG is systematically larger than the  $<sup>111</sup>Cd EFG$  by about a factor of 3. The reason</sup> for the drastically different EFG trends of <sup>111</sup>Cd and <sup>119</sup>Sn in  $R<sub>2</sub>$ In is presently not clear. Although the site occupied by the probes has not been identified experimentally, there is no reason to assume that  $^{119}$ Sn and  $^{111}$ Cd are on different positions in  $R_2$ In.

Precise data on the temperature dependence of the  $\rm ^{111}Cd$ QI in the paramagnetic phase of  $R_2$ In could be obtained only for *R*=Nd, Sm, Gd, Tb, and Dy. The values of  $\left(\partial \ln v_q / \partial T\right)_{|300 \text{ K}}$  cover a small range, extending from  $-31(1)10^{-4}$  K<sup>-1</sup> for *R*=Gd, Tb to  $\sim$  -25 10<sup>-4</sup> K<sup>-1</sup> for *R* =Nd, Sm, Dy. A quite different behavior has been reported for <sup>111</sup>Cd in the rare-earth metals.<sup>23</sup> Here ( $\partial \ln v_q / \partial T$ )<sub>1300 K</sub> is about a factor of 2 smaller and shows a strong linear decrease with increasing *R* atomic number.

#### **B. The magnetic hyperfine interaction**

#### *1. The spin dependence and sign of the saturation field*  $B_{hf}(0)$

The magnetic hyperfine field at the nuclei of non-rareearth atoms in magnetically ordered compounds is caused by the Fermi contact term in the nucleus-electron interaction and reflects the spin polarization of the *s* electrons  $\Delta \rho$  $=[\rho \uparrow(0)-\rho \downarrow(0)]$  at the probe nucleus. A finite *s*-electron spin density may arise from the spin polarization of the host conduction electrons, the polarization of the electron core of the probe by a localized spin, and the overlap of the valence electrons of the probe with spin polarized valence electrons of the magnetic ions.

Because of the small spatial extension of the 4*f* electrons, magnetic order in rare-earth compounds requires a mechanism of indirect exchange between the 4*f* electrons. Mainly two mechanisms of indirect 4*f* −4*f* coupling have been proposed: In the Ruderman-Kittel-Kasuya-Yosida (RKKY) theory the coupling is mediated by the *s*-conduction electrons, which are spin polarized by exchange with the 4*f* electrons. In an alternative concept, which was proposed by Campbell, $^{24}$  the indirect coupling is provided by intra-atomic 4*f* −5*d* exchange and interatomic 5*d*−5*d* interaction between the spin polarized 5*d* electrons of neighboring *R* atoms. In spite of considerable experimental and theoretical effort, a clear picture of the indirect coupling in intermetallic compound *RM*<sup>x</sup> of rare earths and *sp* elements has not yet emerged. There is experimental evidence that, e.g., in *RM*  $(M = Cu, Ag, Mg)$  and  $RIn<sub>3</sub>$  the indirect coupling is mainly mediated by  $sp$  electrons,<sup>25</sup> but in a number of cases the experimental data are partially in conflict with the RKKY formalism and suggest that the 5*d*-electrons play an important role in the indirect exchange interaction.<sup>2</sup>

In the RKKY theory, a spin located at position  $R_n$  induces a spatially nonuniform spin polarization in a sea of free conduction electrons,

$$
P(r) = -\frac{9n^2\pi\Gamma}{2E_F}\langle S_z\rangle F(2k_F|r - R_n|). \tag{4}
$$

 $E_F$  and  $k_F$  are the free-electron Fermi energy and wave vector, respectively.  $\Gamma$  is an effective *s*-*f* exchange constant (assumed to be independent of the electron wave vector), and  $F(x) = [x\cos(x) - \sin(x)]/x^4$  is the oscillating RKKY function. The spin polarization induced by spin  $\vec{S}_n$  interacts with a second spin  $S_m$  localized at  $R_m$ . The resulting indirect coupling can be described by the Hamiltonian  $H_{nm} = -j_{nm}\vec{S}_n \cdot \vec{S}_m$ . As the total angular momentum *J* rather than the spin *S* is the constant of motion, the spin has to be substituted by its pro*jection*  $(g-1)J$  on the total angular momentum *J* (Ref. 26), leading to  $H_{nm} = -j_{nm}(g-1)^2 J(J+1)$ . In the RKKY theory, the interaction constant  $j_{nm}$  is proportional to the square of the *s*-*f* exchange parameter  $\Gamma$  and the RKKY function  $j_{nm}$  $\propto \Gamma^2 F(2k_F R_{nm})$ , so that the Curie temperature is proportional  $to^{27}$ 

$$
T_C \propto \Gamma^2 (g-1)^2 J(J+1). \tag{5}
$$

The indirect coupling via intra-atomic 4*f* −5*d* exchange and 5*d*−5*d* interaction can be described phenomenologically by the same Hamiltonian. In this coupling scheme,  $\Gamma$  would be a measure of the 4*f* −5*d* exchange and the long-range RKKY function has to be replaced by a function which adequately accounts for the radial dependence of the 5*d*−5*d* interaction.

As long as orbital angular momentum contributions to the spin polarization<sup>28,29</sup> are excluded, one therefore expects in both coupling schemes the hyperfine field to be proportional to the 4 $f$  spin and the respective exchange parameter  $\Gamma$ . In the case of RKKY coupling, all 4*f* spins contribute so that



FIG. 12. The spin dependence of the magnetic hyperfine field of  $111$ Cd in  $R_2$ In (full circles, left-hand scale) and the relative coupling constant  $\Gamma_{norm} \propto B_{hf} / (g-1)J$  (triangles, right-hand scale) with the normalization  $\Gamma_{norm}(Gd) = 1$ .

$$
B_{hf} \propto C\Gamma(g-1)J\sum_{n \neq m} F(2k_F R_{nm}).\tag{6}
$$

The parameter *C* accounts—in the case of impurity probes for the modification of the host's *s*-electron spin polarization by spin-dependent electron scattering at the impurity potential.30 In the case of intra-atomic 4*f* −5*d* exchange, the hyperfine field is produced by the overlap of the spin polarized 5*d* electrons with the valence electrons of the probe. Since the 5*d* electrons are more strongly localized than the *s* electrons, one would expect that the hyperfine field is mainly determined by the number *N* of nearest *R* neighbors and their distance  $R_i$  to the probe. Even without detailed knowledge of the radial dependence, it can be presumed that the contributions of the NN spins, symbolized by  $f(R_i)$ , increase with decreasing distance  $R_i$  Qualitatively, these factors can be summarized by the expression,

$$
B_{hf} \propto C\Gamma(g-1)J\sum_{i=1}^{N}f(R_i). \tag{7}
$$

Equations  $(6)$  and  $(7)$  show that independent of the details of the coupling mechanism, the spin dependence of the hyperfine field in a series of isostructural compounds of rare earths and *sp* elements reflects the *R* dependence of the effective exchange parameter  $\Gamma$ , provided the *R* positions vary only slightly across the series. This is the case for  $R_2$ In where the lanthanide contraction changes the lattice parameters between  $R = Pr$  and  $R = Trm$  by less than 5%. In Fig. 12 we have therefore plotted the saturation values  $B<sub>hf</sub>(0)$  of the magnetic hyperfine field of  $^{111}$ Cd in  $R_2$ In, calculated from the experimental values of  $\nu_M(0)$  (Table I) with the nuclear *g* factor *g*=0.301, versus the spin projection  $(g-1)J$ . Both for the group of the light and the heavy *R* constituents, one observes in a first approximation a linear relation between  $B<sub>hf</sub>$  and the spin projection. The slopes of these relations, which with the above assumptions are a direct measure of the exchange parameter  $\Gamma$ , however, differ considerably between both groups. A fit of linear relations to the experimental data leads to a ratio  $\Gamma_{LR}/\Gamma_{HR} = 1.5(1)$ , where  $\Gamma_{LR}$  and  $\Gamma_{HR}$  are the exchange parameters for the light  $(Pr, Nd, Sm)$  and the heavy (Gd, Tb, ..., Tm)  $R_2$ In compounds, respectively. The conclusion that the effective exchange in the light  $R_2$ In is substantially stronger than in the heavy compounds is also supported



FIG. 13. The Curie temperature  $T_C$  (full triangles, left-hand scale) and the quantity  $B^{-2/3}$  (open squares, right-hand scale) as a function of the de Gennes factor  $G = (g-1)^2 J(J+1)$ . *B* is the coefficient of the  $T^{3/2}$  term in Eq. (8). The right section shows the data of the heavy rare earths  $HR = Gd$ , Tb, Dy, Ho, Er, Tm, the left section those of the light *LR*=Sm, Nd, Pr.

by the order temperatures  $T_C$  of the  $R_2$ In series. The variation of  $T_c$  of  $R_2$ In (see column 5 in Table I) as a function of the de Gennes parameter  $G = (g-1)^2 J(J+1)$  shown in Fig. 13 is approximately linear with clearly different slopes  $\Gamma^2$  for the light and the heavy  $R_2$ In. Excluding  $T_C(\text{Gd}_2\text{In})$  which fits poorly into the linear trend, one obtains the ratio  $\Gamma_{LR}/\Gamma_{HR}$ =1.70(25), or including  $T_c(\text{Gd}_2\text{In})$  the ratio is  $\Gamma_{LR}/\Gamma_{HR}$  $=1.55(25)$ . Within the errors, both values agree with  $\Gamma_{LR}/\Gamma_{HR}$ =1.5(1) deduced from the spin dependence of *B<sub>hf</sub>*. Numerous other intermetallic compounds of rare earths and *sp* elements present similar differences. From the order temperatures of  $RAI_2$  and  $RCd$ , e.g., one estimates  $\Gamma_{LR}/\Gamma_{HR}$  $=1.7$ . The  $B_{hf}/(g-1)J$  values of <sup>119</sup>Sn in *RAl*<sub>2</sub> (Ref. 31) also differ considerably between the light and the heavy *RAl*<sub>2</sub>. One of the interpretations proposed $31$  involves an orbital angular momentum contribution to the spin polarization. When attributed to different spin exchange constants only, the spin dependence of  $B_{hf}$ <sup>(119</sup>Sn:*RAl*<sub>2</sub>) corresponds to a ratio  $\Gamma_{LR}/\Gamma_{HR}=1.45$ .

For a closer inspection of the *R* dependence of the exchange parameter  $\Gamma$  in  $R_2$ In, the upper section of Fig. 12 shows the relative coupling constant  $\Gamma_{norm}(R) \propto B_{hf} / (g-1)J$ with the normalization  $\Gamma_{norm}(Gd) = 1$ . A strong change occurs between the light and the heavy  $R_2$ In, but the variations in each group are relatively weak. For most of the heavy  $R_2$ In, the ratios  $B_{hf}/(g-1)J$  and  $(T_C/G)^{1/2}$  (see columns 4 and 5 in Table II) are constant within a few percent, decreasing only at the end of the series. At this point, it is interesting to compare the hyperfine fields of <sup>111</sup>Cd in *R*<sub>2</sub>In to those of the probe <sup>119</sup>Sn in the same series. The <sup>119</sup>Sn data taken from Ref. 11 are listed in Table III. The ratio of the hyperfine fields  $B_{hf}$ <sup>(111</sup>Cd)/ $B_{hf}$ <sup>(119</sup>Sn) (see column 4 of Table III) is within a few percent—constant across the  $R_2$ In series. This probe-independence strengthens the interpretation of the ratio  $B_{hf}/(g-1)J$  as a relative measure of the effective exchange parameter of the host compound.

Some insight into the coupling mechanism may be gained by comparing the <sup>111</sup>Cd hyperfine field in  $R_2$ In to that in the

TABLE II. The spin dependence of the saturation value of the magnetic hyperfine field of  $^{111}$ Cd in  $R_2$ In and in *R* metals.  $(g-1)J$  is the projection of the spin on the total angular momentum *J* and  $G=(g-1)^2J(J)$  $+1$ ) is the de Gennes factor.  $B_h f(R_2 \ln)/B_h f(R)$  and  $T_C (R_2 \ln)/T_C (R)$  are the ratios of the <sup>111</sup>Cd hyperfine fields and of the Curie temperatures, respectively, of  $R_2$ In and the  $R$  metals.

		$R_2$ In			R metal		
$\mathbb{R}^n$	$(g-1)J$	$B_{hf}(T)^{a,b}$	$B_{hf}/(g-1)J(T)$	$(T_C/G)^{1/2}(K)^{1/2}$	$B_{hf}(T)$	$B_{hf}(\rm R_2In)$ $B_{hf}(\mathbf{R})$	$T_C(R_2In)$ $T_C(R)$
Pr	$-0.8$	$(+)8.65$	$(-)10.8$	8.2			0.16
Nd	$-1.227$	$+17.05$	$-13.8$	7.5	$(+)7.65_{15}$ °	2.21	0.19
Sm	$-1.786$	$+21.95$	$-12.2$	6.0	$+24.26$ <sup>d,e</sup>	0.90	0.67
Gd	3.5	$-30.93$	$-8.8$	3.5	$-34.07^{f,g}$	0.91	0.65
Tb	3	$-25.63$	$-8.5$	4.1	$(-)27.55$ <sup>g</sup>	0.96	0.71
Dy	2.5	$-22.2$	$-8.9$	4.1	$-22.14^{d,h}$	1.00	0.69
Ho	2	$(-)17.4$	$(-)8.7$	4.3	$(-)14.93$ <sup>g</sup>	1.14	0.67
Er	1.5	$(-)11.3,$	$(-)7.5$	4.1	$(-)11.63$ <sup>g</sup>	0.97	0.51
Tm	1	$-6.61$	$-6.6$	3.8	$(-)6.0_{6}$ g	1.1	0.30

a This work.

b Reference 4. c Reference 47.

dSign: this work.

e Reference 48.

f Reference 49.

g Reference 50. h Reference 51.

*R* metals, if one assumes comparable coupling parameters for a given *R* element. In  $R_2$ In, the probe nucleus has 11 nearest *R* neighbors at a slightly smaller average distance  $(Pr: 0.348 \text{ nm}, \text{Tm}: 0.332 \text{ nm})$  than that of the 12 NN in the *R* metals (Pr:0.367 nm, Tm:0.354 nm). In the case  $4f - 5d$ exchange and 5*d*-robe overlap, one would therefore expect a hyperfine field ratio of  $B_{hf}(R_2In)/B_{hf}(R)=11/12=0.92$  or larger values in case of a strong radial dependence of  $f(R_i)$  in

Eq.  $(7)$ . On the other hand, the free-electron RKKY sum  $\Sigma_{n \neq m}F(2k_F R_{nm})$  of  $R_2$ In (Ref. 9) is roughly 2/3 of the RKKY sum of the  $\overline{R}$  metals,  $\frac{27}{27}$  as one would expect if in a simplifying picture  $1/3$  of the magnetic  $R$  atoms are replaced by nonmagnetic In atoms.

In the case of  $\frac{111}{Cd}$  (see column 7 of Table II) one finds a hyperfine ratio of  $B_{hf}(R_2In)/B_{hf}(R) \approx 0.9-1.1$  (except *R*  $=$ Nd) close to the ratio of the number of nearest *R* neighbors

TABLE III. The spin dependence of the saturation value of the magnetic hyperfine field of  $^{119}Sn$  in  $R_2In$ (Refs. 11 and 12) and in *R* metals. The Curie temperatures of  $R_2$  In have been derived from the temperature dependence of the magnetic hyperfine field of  $^{119}$ Sn.  $B_{hf}$ ( $^{111}$ Cd)/ $B_{hf}$ ( $^{119}$ Sn) is the ratio of the hyperfine fields of the probe nuclei  $^{111}$ Cd and  $^{119}$ Sn in  $R_2$ In,  $B_{hf}(R_2$ In)/ $B_{hf}(R)$  the ratio of the hyperfine fields of  $^{119}$ Sn in  $R_2$ In and in *R* metals.

$\boldsymbol{R}$	$T_C(K)$	$R_2$ In $B_{hf}(T)$	$B_{hf}({}^{111}Cd)$ $B_{hf}({}^{119}\text{Sn})$	$R$ metal $B_{hf}(T)$	$B_{hf}(R_2In)$ $B_{hf}(\mathbf{R})$
Nd	111	$+21.9(1)$	0.77		
Sm	160	$(+)27.3(1)$	0.79		
Gd	$198^a$ , $236^b$	$-37.3(1)$	0.84	$-32.34(4)^c$	1.16
Tb	172	$-32.8(1)$	0.81	$(-)24.1(6)d$	1.37
Dy	131	$-27.1(1)$	0.82	$(-)18.5(5)d$	1.47
Ho	91,5	$(-)22.3(1)$	0.76	$(-)12(1)d$	1.85
Er	50	$(-)15.2(1)$	0.74	$-12.4(4)^e$	1.23
Tm	23, 5	$-8.4(1)$	0.79	$(-)7.2(12)^d$	1.20

a Reference 11.

b Reference 12.

c Reference 52.

d Reference 53.

e Reference 54.

 $N(R_2In)/N(R) = 0.92$ . For <sup>119</sup>Sn (see column 6 of Table III) the ratio is even larger:  $B_{hf}(R_2In)/B_{hf}(R) \approx 1.2-1.8$ . Thus, for both probes  $B_{hf}(R_2In)B_{hf}(R)$  is much larger than the ratio of the RKKY sums  $(\sim 0.60)$ . This implies that the 4*f* spins beyond the NN shell of the probe contribute little to the hyperfine field and favors 4*f* −5*d* exchange and 5*d*-probe interaction rather than long-range RKKY interaction as coupling mechanism. NMR measurements<sup>32</sup> of  $B<sub>hf</sub>$  of <sup>67</sup>Zn in pseudobinary  $R_{1-x}A_xZn$  (*A*=La, Y, Sc) have led to a similar conclusion. In these compounds, about 80% of the hyperfine field comes from the NN  $4f$  spins. The fact that for  $119$ Sn the ratio  $B_{hf}(R_2In)/B_{hf}(R)$  is substantially larger than for <sup>111</sup>Cd is possibly related to the difference of the probe volumes. The atomic volume of Sn  $(27 \text{ Å}^3)$  which is comparable to the volume of the Wigner Seitz cell of the In site of  $R_2$ In  $(\text{Pr}: 29 \text{ Å}^3; \text{ Er}: 26 \text{ Å}^3)$  is larger than the atomic volume of  $Cd(22 \text{ Å}^3)$  which could lead to a stronger overlap of the Sn valence electrons with the spin polarized 5*d* electrons.

The Curie temperatures of  $R_2$ In and  $R$  metals are related as  $T_c(R_2In) \approx 2/3$   $T_c(R)$  (at least for heavy *R*—see column 8 in Table II). This supports the picture of  $R_2$ In as a magnetically diluted *R* metal with a comparable exchange parameter, since in diluted ferromagnets above the percolation limit  $T_c$ scales with the concentration of the magnetic atoms, independent of the coupling mechanism.

The larger exchange parameter in the light  $R_2$ In deduced from the hyperfine field measurements reflects a higher degree of 4*f* −5*d* overlap which can be understood qualitatively by comparing the radial extensions of the 4*f* and 5*d* electrons in the first and the second half of the *R* series. According to Delyagin *et al.*,<sup>11,33</sup> the degree of overlap can be expressed by the ratio  $R_{4f}/R_{NN}$ . Here the root mean square 4*f* radius  $R_{4f} = (r_{4f}^2)^{1/2}$  and the NN distance  $R_{NN}$  are measures of the radial extensions of the 4*f*- and the 5*d*-wave functions, respectively. In an isostructural series, both parameters decrease with increasing *Z*. The decrease of  $R_{NN}$  (lanthanide contraction) between Pr and Tm usually amounts to only a few percent ( $\sim$ 5% in *R*<sub>2</sub>In). The 4*f* radius, however, shows a strong *Z* dependence, in particular in the first half of the rare-earth group where it decreases by about 20%. In the second half, the decrease is about 10%. (See the dotted line in the upper section of Fig.  $11$ .) Consequently, the degree of overlap decreases from Pr to Tm, leading to weaker exchange in the second half of the *R* series.

The sign of the magnetic hyperfine field  $B<sub>hf</sub>$  of <sup>111</sup>Cd on the In site of  $R_2$ In has been determined for  $R = Nd$ , Sm, Gd, Tb, Dy, and Tm. As a rule, in light  $R_2$ In  $B<sub>hf</sub>$  is parallel, in heavy  $R_2$ In is antiparallel to the external field  $B_{ext}$ . An external field of 4 T is not sufficient to break the spin-orbit coupling of the *R* moments; the external field therefore aligns the total angular momentum *J*. According to Hund's rule, for light *R* elements the spin *S* is antiparallel, and for heavy *R* it is parallel to the total angular momentum. The positive and negative sign of  $B_{hf}$  in light and heavy  $R_2$ In, respectively, therefore implies that in all  $R_2$ In the spin polarization  $\Delta \rho_i$  $=[\rho \uparrow(0)-\rho \downarrow(0)]$  at the <sup>111</sup>Cd site is antiparallel to the rareearth spin *S*. The same holds for the rare-earth metals, and as shown by Delyagin *et al.*,<sup>11</sup> also for the probe nucleus <sup>119</sup>Sn in  $R_2$ In.



FIG. 14. The magnetic hyperfine field  $B<sub>hf</sub>$  of <sup>111</sup>Cd in Gd<sub>2</sub>In (full squares), in  $Gd_2In_{0.95}Sn_{0.05}$  (open squares), in Sm<sub>2</sub>In (open circles), and of  $^{119}Sn$  in  $Gd_2In_{0.995}Sn_{0.005}$  (full triangles; Ref. 12 ), as a function of temperature on a  $T^{3/2}$  scale. The full line through the  $<sup>111</sup>Cd:Sm<sub>2</sub>In data is the result of a fit of Eq. (8) to the experi-$ </sup> mental values.

# *2. The temperature dependence of the magnetic hyperfine interaction*

The variation of the magnetic interaction frequency  $\nu_M$ with temperature was determined in all  $R_2$ In between 10 K and the order temperature  $T_C$ . The main results of the measurements are illustrated in Figs. 5, 7, 10, and 14. In all heavy  $R_2$ In, the magnetic hyperfine interaction decreases continuously towards  $T_C$ . The decrease of  $\nu_M$  is accompanied by a critical increase of the linewidth of the magnetic interaction, which is evidence for a spatial variation of the exchange interaction and a corresponding distribution of the Curie temperature. (See Sec. V B 3).

In light  $R_2$ In, a second-order transition (SOT) is found only in  $Sm_2In$ . In  $Nd_2In$  and  $Pr_2In$  the hyperfine field vanishes discontinuously at the Curie temperature. The observation that the QI in the paramagnetic phase of  $Pr<sub>2</sub>$ In becomes axially asymmetric as one approaches the phase transition (see Section IV A) is an indication of lattice distortions near  $T_c$  and suggests that these first-order transitions (FOTs) are driven by magneto-elastic effects.

In Fig. 7, the temperature dependence of  $\nu_M(T)$  of <sup>111</sup>Cd in heavy  $R_2$ In compounds is compared to the prediction of a molecular field model for localized moments (solid lines). For all heavy  $R_2$ In, the experimental trend of  $\nu_M(T)$  is slightly below the molecular field curve. It is interesting to note that in spite of the phase transitions from antiferromagnetic to ferromagnetic order in  $Gd_2In$  and  $Sm_2In$  at 100 K and 145 K, respectively, the hyperfine frequencies of  $\frac{111}{Cd}$  $\frac{119}{5n}$ , Ref. 11) in these hosts vary smoothly across the phase transitions. As pointed out by Delyagin *et al.*, <sup>11</sup> the absence of a singularity of  $B<sub>hf</sub>$  suggests that the NN spin arrangements in the ferro- and antiferromagnetic phases are rather similar and calls for a small interlayer turn angle of the spin spirals of  $Gd_2In$  and  $Sm_2In$ .

At low temperatures, the excitation of spin waves causes the magnetization to deviate from its saturation value, which is frequently expressed in terms of a temperature power law  $T^k$ . The  $T^{3/2}$  temperature dependence of the magnetization predicted by Bloch's spin wave theory for a bilinear Heisenberg ferromagnet with nearest-neighbour interactions has been experimentally verified in a large number of cases, but other exponents  $\kappa$  have also been observed.<sup>34</sup>

In Fig. 14 we have plotted the magnetic hyperfine field of <sup>111</sup>Cd in Gd<sub>2</sub>In and Sm<sub>2</sub>In vs the temperature on a  $T^{3/2}$  scale. Clearly,  $B_{hf}(T)$  of <sup>111</sup>Cd in Gd<sub>2</sub>In is well described by a  $T^{3/2}$ relation, but substantial deviations from Bloch's law occur in Sm<sub>2</sub>In and the other  $R_2$ In compounds (not shown in Fig. 14) with nonzero orbital angular momentum. An analysis of the temperature dependence of the magnetic hyperfine frequency  $\nu_M(T)$  of <sup>111</sup>Cd in *R*<sub>2</sub>In in terms of a single temperature power law  $T^k$  leads to significant differences in the exponent  $\kappa$ . A fit of (1-*BT*<sup>k</sup>) to the data in Fig. 7 for  $T/T_C \le 0.5$  results in  $\kappa = 1.45(5)$  for Gd<sub>2</sub>In,  $\kappa = 1.65(5)$  for Tb<sub>2</sub>In and  $1.8 \leq \kappa$  $\leq$  2.2 for the other *R* constituents.

Similar differences between Gd and the other rare-earth elements have been observed in the thermal decrease of the magnetization of the pure  $R$  metals. In Gd metal,<sup>35</sup> the lowtemperature variation of the magnetization for  $T/T_C \ge 0.17$  is well described by a  $T^{3/2}$  relation. In Tb<sup>36</sup> and Dy,<sup>37</sup> however, larger critical exponents  $\kappa \approx 2-2.5$  are required to reproduce the decrease of the magnetization with a single temperature power law. These differences in the low-temperature trend of the magnetization have been attributed to the differences in the crystal electric field interactions (CEF) of Gd and the other rare-earth elements. In contrast to the other *R* elements, the charge distribution of the half-filled 4*f* shell of Gd is almost spherically symmetric. In Gd compounds, the anisotropic CEF interactions between the 4*f*-charge distribution and the electric field produced by the surrounding charges are therefore weak, while for the other *R* elements one finds extremely large anisotropy energies. It was pointed out by Niira<sup>37</sup> that a magnetic anisotropy caused, e.g., by a CEF interaction may produce an energy gap  $\Delta$  in the magnon spectrum of a ferromagnetic system<sup>38</sup> and that such a gap has a substantial effect on the low-temperature dependence of the magnetization.

For hcp rare-earth metals, the CEF can be expressed in terms of the anisotropy energies  $K_l^0(1=2,4,6)$  relative to the hexagonal *c* axis and the basal plane anisotropy  $K_6^6$ . In this case, the CEF leads to an energy gap  $\Delta \approx (1/J)\sqrt{K_2^0 K_6^6}$  in the spin wave spectrum and the resulting modification of Bloch's  $\overline{T}^{3/2}$  law can be written as<sup>38</sup>

$$
M(T) = M(0) \left[ 1 - BT^{3/2} \sum_{n=1}^{\infty} n^{2/3} \exp(-n \Delta / k_B T) \right].
$$
 (8)

With energy gaps of about  $\Delta/k_B \approx 20-30$  K, Eq. (8) fully accounts for the deviations of the low-temperature magnetization of Tb and Dy metal from Bloch's  $T^{3/2}$  relation.

Because of the hexagonal symmetry of  $R_2$ In, substantial CEF effects should be present for all *R* constituents except *R*=Gd and one may therefore expect similar differences in the temperature dependence of the magnetization as in the *R* metals. We have analyzed the experimental temperature dependencies of  $\nu_M(T)$  in the range for  $T/T_c \le 0.5$  on the basis of Eq.  $(8)$ . This analysis, which presumes that the hyperfine coupling constant *A* relating the hyperfine field to the magnetization<sup>39</sup> [ $\nu_M(T) = AM(T)$ ] is temperature independent, leads to a finite parameter  $\Delta/k_B$  for all non-*S* state *R* constituents. The values of  $\nu_M(0)$ , *B* and  $\Delta/k_B$  derived from a fit of Eq. (8) to the  $\nu_M(T)$  data in Figs. 7 and 10 are listed in columns  $2-4$  of Table I. In the case of  $Pr<sub>2</sub>$ In, the accuracy of the data (see Sec. IV B) is insufficient for a meaningful analysis of the temperature dependence.

In the heavy  $R_2$ In, the gap energy  $\Delta/k_B \approx 15(3)$ K is practically independent of the *R* constituent and of the same order of magnitude as the magnon gap of Tb and Dy metals. In the light  $R_2$ In  $R = Nd$ , Sm, the gap energy is substantially larger, reflecting a stronger CEF interaction which is probably a consequence of the larger radial extension of the 4*f*-wave functions in first half of the 4*f* series. In contrast to the gap energy, the parameter *B* of the temperature dependence [Eq.  $(8)$ ] shows a strong variation with the *R* constituent, increasing continuously from *B*=2.7×10<sup>-4</sup> K<sup>-3/2</sup> for Gd to  $B=159\times10^{-4}$  K<sup>-3/2</sup> for Tm. In the spin wave theory of isotropic Heisenberg ferromagnets with Hamiltonian  $H$ =−J *S*1*S*<sup>2</sup> and three-dimensional dispersion relation, the relative deviation of the magnetization from its saturation value is for small wave vectors given by  $\left\{\Delta M(T)/[M(0)]\right\}$  $\propto$ {1/*S*)[( $k_BT$ )/(*J S*)]<sup>3/2</sup>}. (Note: This proportionality also holds in the presence of anisotropy energies.<sup>27</sup>) The coupling parameter  $\mathcal J$  may be replaced by the order temperature since  $\mathcal{J}\propto T_C/S(S+1)$ . This substitution leads to the relation  $B^{-2/3}$  $\propto T_c[S^{2/3}/(S+1)]$  between the coefficient *B* of the  $(1-BT^{3/2})$ temperature dependence of the magnetization and  $T_c$ . [Note: In the case of the *R* ferromagnets, *S* stands for the spin pro*jection*  $(g-1)J$ . In the range of spins of interest in this paper,  $S^{2/3}/(S+1) \approx$  const  $\approx 0.52$  and one therefore expects a practically linear relation between the Curie temperature  $T_C$ and the parameter  $B^{-2/3}$ .

To compare our experimental observations with this prediction of the spin wave theory, we have included the parameter  $B^{-2/3}$  (see Table I) in Fig. 13, where the Curie temperature  $T_c$  is plotted vs the de Gennes factor  $G = (g-1)^2 J(J)$ +1), and find that  $B^{-2/3}$  indeed follows the *G*-dependence of the order temperature very closely. The experimental *B*−2/3 values of all  $R_2$ In, except Nd<sub>2</sub>In, satisfy the linear relation  $B^{-2/3}$ =2.34(4)  $T_c S^{2/3} / (S + 1)$ . In the case of Nd<sub>2</sub>In, B<sup>-2/3</sup> is about 50% larger than expected from this relation, which is possibly related to the fact that the magnetic phase transition of Nd2In is of first order.

For  $T/T_c \le 0.5$ , the temperature-induced decrease of the magnetic hyperfine field of  $111 \text{Cd}$ : $R_2$ In can thus be consistently related to the spin wave excitations of the host. Our data also suggest that the response of the electron spin polarization to the spin wave excitations, described by the hyperfine coupling constant *A*, depends on the properties of the probe atom. In Fig. 14 we have included the  $B<sub>hf</sub>(T)$ -data of  $^{119}$ Sn in Gd<sub>2</sub>In, extracted from Fig. 3 of Ref. 12. As for <sup>111</sup>Cd,  $B_{hf}(T)$  of <sup>119</sup>Sn follows a  $T^{3/2}$  law; the coefficient  $B(^{119}Sn:Gd_2In)=2.0(1)\times10^{-4} \text{ K}^{2/3}$ , however, is considerably smaller than that of  $111$ Cd in the same host  $[B(^{111}\text{Cd}:Gd_2\text{In})=2.7 \ 10^{-4} \ \text{K}^{-3/2}].$ 

At higher temperatures, the variation of the magnetic hyperfine field may be discussed in terms of the molecular field

model. For rare-earth ferromagnets, the CEF interaction changes the equidistant molecular field splitting of the  $(2J)$  $+1$ ) *m* states, and the Boltzmann averaging of these levels then results in a different temperature dependence of the magnetization. Including the Hamiltonian of a CEF interaction with hexagonal point symmetry into the molecular field model, we have found that anisotropy coefficients  $K_2^0$  $\approx$  –(100–200) K and K<sup>0</sup>/K<sup>0</sup><sub>2</sub> $\approx$  0.1 are required to reproduce the measured  $v_M(T)$  curves of <sup>111</sup>Cd: $R_2$ In (except Gd<sub>2</sub>In). These values are comparable to the coefficients observed in the  $R$  metals. A precise determination of the coefficients is difficult because similar temperature dependences can be produced by different combinations of  $\tilde{K}_2^0$  and  $K_4^0$ . This is because the magnetization is given by the Boltzmann average over all *m* states, in contrast, e.g., to inelastic neutron scattering which directly provides the *m*-state energies. The contributions of the  $K_6^0$  and  $K_6^6$  terms to CEF energy are too small to be detected in the  $\nu_M(T)$  curves.

The Curie temperatures of most  $R_2$ In derived from the <sup>111</sup>Cd PAC measurements of  $\nu_M(T)$  (see Tables I and III) are systematically smaller—by up to 10 K—than those obtained from the  $119$ Sn Mössbauer spectra (Table III). To investigate whether this difference is related to the Sn content  $(\sim 0.5\%)$  of the Mössbauer samples, we have measured  $B_{hf}(T)$  of <sup>111</sup>Cd in Gd<sub>2</sub>In<sub>0.95</sub>Sn<sub>0.05</sub>. These data, included in Fig. 14, show that there is some increase of the saturation field and of the order temperature upon addition of this relatively large Sn concentration. The effect, however, is too small to explain the substantial difference in the order temperatures deduced from the PAC and the Mössbauer spectra.

#### *3. Evidence for Curie temperature distributions in R***2In**

As pointed out in Sec. IV B, there are two features in the PAC spectra near  $T_c$  that reflect a spatial variation of the exchange interaction and a corresponding distribution of the order temperature in  $R_2$ In. These are (i) the critical increase of the relative line width of the magnetic hyperfine field (see Figs. 4 and 5, for example) and  $(ii)$  the coexistence of the paramagnetic and the ferromagnetic phase in a small temperature interval near  $T_c$  (Figs. 8 and 9). Evidence for Curie temperature distributions has earlier been found in disordered ferromagnetic systems.  $T_C$  spreads of the order of a few K, resulting in critical line broadening and phase coexistence near  $T_c$  have been observed by Mössbauer<sup>40,41</sup> and PAC (Ref. 42) spectroscopy in concentrated and dilute, disordered alloys. The concept of spatially varying Curie  $t$ emperatures $43,44$  has also been invoked to explain the smoothness of the phase transitions in strongly disordered magnetic alloys such as Invar where the transition may extend over temperature ranges of the order of  $10^2$  K. (See, for example, Ref.  $45$ )

Recently, it was noted that distributions of the order temperature may also occur in chemically ordered intermetallic compounds.<sup>14</sup> A  $T_c$  distribution produces a critical increase of the linewidth, in particular at second-order transitions (SOT), because at low temperatures the magnetic frequency  $\nu_M$  varies little with the Curie temperature, but close to  $T_C$ ,  $\nu_M$  decreases critically with decreasing  $T_C$ :  $\nu_M \propto (1 - T/T_C)^{\beta}$  with an exponent of the order  $\beta \sim 0.3-0.4^{46}$ . At  $T \approx T_c$  small variations of the Curie temperature therefore produce broad distributions of  $\nu_M$ , while at low *T* the magnetic frequency remains sharply defined. As shown in Ref. 14, for a SOT with critical exponent  $\beta$  and a Lorentzian  $T_C$ -distribution, characterized by the center temperature  $T_c$  and the width  $\Gamma_c$ , the resulting temperature dependence of the relative line width  $\delta$  is given by

$$
\delta(T) = (\beta \ \Gamma_C/2T_C)(T/T_C)(1 - T/T_C)^{\beta - 1}.
$$
 (9)

The extraction of the parameter  $\Gamma_c$  from the critical increase of  $\delta(T)$  is discussed in detail in Ref. 14 With the critical exponent  $\beta$  fixed to  $\beta$ =0.35 and a Curie temperature of  $T_c = 122(1)K$  deduced from  $\nu_M(T)$  of Dy<sub>2</sub>In using  $\nu_M$  $\propto (1-T/T_C)^{\beta}$ , the  $\delta(T)$  data of Dy<sub>2</sub>In in Fig. 5 correspond to a  $T_C$ -distribution with a line width of  $\Gamma_C = 1.8(2)$ K. In the other  $R_2$ In compounds with SOTs,  $\Gamma_C$  is of the same order of magnitude.

A coexistence of the paramagnetic and the ferromagnetic phases near  $T_c$  becomes manifest in the PAC spectra as a superposition of two fractions. The temperature dependence of the paramagnetic fraction is given by the integral<sup>14</sup>

$$
f_{para}(T) = \int_0^T I(T'_C; T_C) dT'_C,
$$
\n(10)

where  $I(T'_C; T_C)$  represents the  $T_C$  distribution (with  $T_C$  as most frequent order temperature). In the ferromagnetic phase of  $R_2$ In, the angular correlation is perturbed by a combined magnetic and electric hyperfine interaction, in the paramagnetic phase by an axially symmetric QI. The paramagnetic component in the spectra at  $T \approx T_C$  is most easily identified in the case of  $\frac{111}{c}$ Cd:Nd<sub>2</sub>In (see Fig. 8) because of the strength and the narrow linewidth of the QI in this compound. In the heavy  $R_2$ In, the QI is much weaker, and the paramagnetic component is therefore difficult to separate from the ferromagnetic component, which because of the critical increase of the line width is strongly attenuated at  $T \approx T_C$ . A fit of Eq. (10) with a Lorentzian  $T_C$  distribution to  $f_{para}(\dot{T})$  of <sup>111</sup>Cd:Nd<sub>2</sub>In (solid line in Fig. 9) gives  $T_c$  $=104$  K and a width of the  $T_c$  distribution of about  $\Gamma_c$  $\approx$  5 K. [Note: The variations of the sample temperature of  $\sim$  0.1 K are at least one order of magnitude smaller than the  $\Gamma_c$  values required to reproduce the temperature dependences of  $\delta(T)$  and  $f_{para}(T)$  at  $T \approx T_C$ .]

Critical increase of the linewidth and phase coexistence have been observed in practically all hyperfine field studies of chemically ordered magnetic compounds reported up to now. The mechanism leading to local variations of the exchange interaction in ordered systems has not yet been identified. Site disorder (atoms *A* on *B* sites of  $AB<sub>x</sub>$ ) probably plays a role.

#### *4. The spin orientation*

The relative orientation of the magnetic hyperfine field and the axially symmetric EFG reflects the local spin orientation at the probe with respect to the symmetry axis of the host lattice. With the exception of  $Nd<sub>2</sub>$ In and Pr<sub>2</sub>In, the information on the spin orientation at  $\frac{11\bar{I}}{\ln}\ln 111\text{Cd}$  in *R*<sub>2</sub>In has



FIG. 15. The angle  $\theta$  between the direction of the <sup>111</sup>Cd hyperfine field and the symmetry axis of the EFG (full squares) in some  $R_2$ In as a function of temperature. The full triangles are the  $\theta$  values deduced from  $119$ Sn Mössbauer measurements (Ref. 11), the stars corresponds to the orientation of the 4*f* moments relative to the *c* axis determined by neutron diffraction (Ref.  $10$ ).

to be extracted from the quadrupole parameter  $v_q^{\theta}$  $=(3 \cos^2 \theta - 1)\nu_q$  by extrapolating the temperature dependence of the quadrupole frequency  $\nu_q(T)$ , measured in the paramagnetic phase, to the ferromagnetic region. An example is given in Fig. 6 for the case of  $Dy_2$ In. At  $T_C$  one has  $|\nu_q^{\theta} = (3 \cos^2 \theta - 1)\nu_q| \sim 1.8 |\nu_q|$  with  $\theta \sim 16$  deg as the only solution. The decrease of  $\nu_q^{\theta}(T)$  with decreasing temperature implies an increase of the angle  $\theta$ . The variation of  $\theta(T)$ shown in upper section of Fig. 6 results from the experimental values of  $\nu_q^{\theta}(T)$  if the temperature dependence of the QI is assumed to follow the well known  $T^{3/2}$ -relation  $\nu_q(T)$  $=v<sub>a</sub>(0)(1-BT<sup>3/2</sup>)$  observed in many noncubic metals. As the variation of the QI in the paramagnetic phase is rather weak, the assumption of a linear  $v_q(T)$  relation leads to practically the same  $\theta(T)$  values. Figure 6 also shows the variation of  $\theta(T)$  for a <sup>119</sup>Sn impurity on the In site of Dy<sub>2</sub>In, measured by Mössbauer spectroscopy (full line in the upper section<sup>11</sup>).

The temperature dependencies of the spin orientation at <sup>111</sup>Cd derived in the same way from the experimental  $\nu_q^{\theta}(T)$ data of the other  $R_2$ In compounds are displayed in Fig. 15 vs the reduced temperature  $T/T_C$ . Gd<sub>2</sub>In and Tm<sub>2</sub>In are not included. In the latter case the QI in the paramagnetic phase is very small and  $v_q(T)$  too imprecise for a meaningful analysis of  $\nu_q^{\theta} = (3\cos^2\theta - 1)\nu_q$ . The decrease of quadrupole parameter with decreasing temperature, however, shows that also in  $Tm<sub>2</sub>$ In the spin orientation changes with temperature.

In the case of  $Gd<sub>2</sub>$ In, the quadrupole parameter of the ferromagnetic phase  $v_q^{\theta}(T)$  is close to the quadrupole frequency extrapolated from the paramagnetic phase:  $|v_q^{\theta}/v_q|$  $\sim$  1 at all temperatures, but in Er<sub>2</sub>In this ratio increases from  $|v_q^{\theta}/v_q| \sim 0.9$  at  $T_c$  to  $|v_q^{\theta}/v_q| \sim 1$  at  $T = 10$  K. For 0.9  $\langle \cdot | (3 \cos^2 \theta - 1) | 1 \rangle$  there are two possible solutions:  $\theta$  $\approx$  35–37° and  $\theta \ge 79$ °. Since  $\gamma$ - $\gamma$  PAC is not sensitive to the sign of the QI, one has to recur to data provided by other techniques to select the correct solution. Neutron diffraction and  $119$ Sn Mössbauer spectroscopy of R<sub>2</sub>In support the solution  $\theta \ge 79^\circ$  both for *R*=Gd and Er.

The experimental error of  $\nu_q^{\theta}(T)$  is of the order of 2%, so that qualitatively there is no doubt that the spin orientation in most  $R_2$ In—as seen by <sup>111</sup>Cd—is temperature dependent. The absolute values of  $\theta$  obtained from  $\nu_q^{\theta}(T)$ , however, depend on the  $v_q(T)$  relation assumed for the extrapolation from the paramagnetic to the ferromagnetic phase and are therefore the subject of some systematic uncertainty which we estimate to be of the order of  $\Delta \theta \le 10$  degrees.

For comparison with the  $\frac{111}{Cd}$  PAC results, the spin orientations of  $R_2$ In obtained by neutron diffraction and  $\frac{111}{2}$ Sn Mössbauer spectroscopy are included in Fig. 6  $(Dy_2In)$  and Fig. 15. In the case of  $^{119}Sn$  Mössbauer spectroscopy, the information on the spin orientation comes, as for  $111$ Cd: R<sub>2</sub>In, from the quadrupole parameter  $v_q^{\theta} = (3 \cos^2 \theta - 1)v_q$ . In contrast to  $\gamma$ - $\gamma$  PAC, however, in the case of combined interactions Mössbauer spectra are sensitive to the sign of  $\nu_q^{\theta}$ . Delyagin *et al.*<sup>11</sup> have reported that for  $R = \text{Sm}$ , Gd, Tb, Dy, and Tm  $\nu_q^{\theta(119)}$ Sn: $R_2$ In) at 4.2 K is positive, for  $R=$ Ho and Nd negative. The assumption of a positive sign of the EFG then leads to the conclusion that in the case of  $R = Sm$ , Gd, Tb, Dy, and Tm one has  $\theta \ge \theta_M$ , where  $\theta_M$  is the "magic" angle  $\theta_M = 54.7^\circ$ , i.e., the magnetic moments are in the basal plane or close to it. For *R*=Ho and Nd one has  $\theta \le \theta_M$ , i.e., the moments are parallel or close to the *c* axis of the hexagonal  $R_2$ In lattice.

A temperature dependence of  $v_q^{\theta}$  has been reported only for the case of <sup>119</sup>Sn:Dy<sub>2</sub>In where the sign of  $\nu_q^{\theta}$  was found to change from positive to negative, as temperature increased from  $40 K$  to  $80 K$  (indicated by the full line in the upper section of Fig. 6). In the case of  $^{119}Sn:Nd<sub>2</sub>In$  an anomaly in the temperature variation of the magnetic hyperfine field between  $25 K$  and  $40 K$  (see triangles connected by a dashed line in Fig. 10) has been attributed by Delyagin *et al.*<sup>11</sup> to a spin reorientation from  $\theta=0^\circ$  to  $\theta=20^\circ$ . With <sup>111</sup>Cd, a similar anomaly has not been observed.

The comparison of the  $\frac{111}{11}$ Cd PAC, the  $\frac{119}{11}$ Sn Mössbauer, and the neutron diffraction results shows that the local spin orientation is affected by the probe properties, presumably by local changes of the crystal field parameters. Pronounced differences between neutron diffraction and PAC results are found, e.g., in the case of Tb<sub>2</sub>In ( $\theta=90^\circ$  and 65°, respectively, at 10 K; see Fig. 15). The results of  $^{111}$ Cd PAC and <sup>119</sup>Sn Mössbauer spectroscopy differ in practically all  $R_2$ In compounds. A prominent example is  $Dy_2$ In (see Fig. 6): At the site of  $119$ Sn, the angle  $\theta$  increases strongly with decreasing temperature from  $\theta \sim 0^{\circ}$  to 90°. At <sup>111</sup>Cd, the spin orientation changes in the same temperature range, but only from  $\theta$  ~ 20° to ~40°. A low temperature angle of  $\theta$  ~ 90° can be definitely excluded for <sup>111</sup>Cd, because on the way from  $\theta$  $\sim$  20° to  $\theta$  ~ 90° one would pass through the magic angle  $\theta_M$  = 54.7° where the PAC pattern is that of a pure magnetic interaction. This has not been observed.

#### **VI. CONCLUSION**

The magnetic and electric hyperfine interactions of the probe nucleus <sup>111</sup>Cd on the In site of the ferromagnetic rareearth indium compound  $R_2$ In have been investigated by perturbed angular correlation measurements as a function of temperature for different *R* constituents. The main results of this study are summarized in the following paragraph.

The QI in the paramagnetic phase decreases drastically from the light to the heavy  $R$  constituents, suggesting a strong influence of the 4*f* electrons on the charge distribution at the In site. The comparison of the magnetic hyperfine field of  $111$ <sup>cd</sup> in *R*<sub>2</sub>In and in the *R* metals shows that the main contribution to  $B<sub>hf</sub>$  comes from the nearest R neighbors of the probe. This observation favors intra-atomic 4*f* −5*d* exchange and interatomic 5*d*−5*d* interaction rather than 4*f* exchange with the *s*-conduction electrons as mechanism of the indirect 4*f* −4*f* interaction. The spin dependence of the hyperfine field reflects a stronger degree of 4*f* −5*d* overlap in the first half of the *R* group. The temperature dependence of the magnetic hyperfine interaction at  $T/T_c \le 0.5$  can be explained by the excitation of spin waves. For *R* constituents with nonzero orbital angular momentum,  $B<sub>hf</sub>(T)$  follows the modified Bloch relation  $T^{3/2}$  exp $(-\Delta/k_BT)$ , suggesting an energy gap  $\Delta/k_B \approx 15-20$  K in the spin wave spectrum of  $R<sub>2</sub>$ In. The PAC spectra provide evidence for a spatial variation of the exchange interaction in chemically ordered intermetallic compounds that is probably due to some degree of site disorder. The spatially varying exchange leads to a distribution of the Curie temperature with a width of  $\sim$ 2–5 K and to the coexistence of the ferromagnetic and the paramagnetic phase in a similar temperature interval around the phase transition. The temperature-induced changes of the orientation of the 4*f* spins relative to the *c* axis of  $R_2$ In have been deduced from the angle between  $B<sub>hf</sub>$  and the symmetry axis of the EFG.

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