## Electronic structure of one-dimensional indium chains on Si(111)

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The driving force for the phase transition of quasi-one-dimensional (1D) indium chains on the Si(111)-4  $\times$  1 surface has been controversial. Using first-principles density-functional calculations we investigate the surface band structure of the low-temperature phase including a periodic lattice distortion. We find that the surface states  $m_2$  and  $m_3$  hybridize to yield a band-gap opening, while the surface state  $m_1$  crosses the Fermi level. The simulated scanning tunneling microscopy (STM) images reproduce the features observed in the STM measurements, such as a double periodicity and an out-of-phase distribution in the filled- and empty-state images. The present results agree in many respects with recent photoelectron spectroscopy and STM experiments but do not support a 1D charge-density-wave mechanism accompanying a metal-insulator transition.

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Low-dimensional systems provide many interesting physical phenomena such as charge-density waves (CDWs), Jahn-Teller distortions, or the formation of non-Fermi-liquid ground states.<sup>1</sup> Recently, self-organized one-dimensional (1D) metallic chains on silicon surfaces have attracted much attention because of technological applications for the formation of atomic-scale structures.<sup>2,3</sup> As a consequence of a rapid development in lithography, the size of electronic devices is expected to be reduced down to the atomic limit where quasi-1D systems can be utilized as atomic-scale interconnects.

An important example of quasi-1D systems is the selforganized indium chains on the Si(111) surface.<sup>3–11</sup> Each 1D indium chain is composed of the two zigzag rows (see Fig. 1).<sup>11</sup> Using angle-resolved photoemission (ARP), scanning tunneling microscopy (STM), and reflection high-energy electron diffraction (RHEED), Yeom et al.<sup>3</sup> found that this system undergoes a reversible phase transition from a hightemperature  $4 \times 1$  structure to a low-temperature  $4 \times "2"$ structure at about 100 K. Here, "2" means the presence of half-order streaks (along the chain direction) rather than peaks in a RHEED pattern, indicating little correlation between the chains which contain a periodic lattice distortion. The ARP study<sup>3</sup> of Yeom *et al.* found a dramatic change in the surface-state bands (denoted as  $m_1, m_2$ , and  $m_3$ ) between the  $4 \times 1$  and  $4 \times "2"$  structures, indicating that the former is metallic whereas the latter is almost semiconducting without any electronic states crossing the Fermi level. However, according to later low-temperature ARP data<sup>7</sup> of Yeom et al., the two surface states  $m_2$  and  $m_3$  exhibited pseudolike band gaps with their remaining spectral weights at the Fermi level. Mainly from the presence of a half-filled metallic band  $(m_3)$ which has a nearly flat Fermi surface, Yeom et al.<sup>3,7</sup> interpreted the observed phase transition in terms of a 1D CDW mechanism or, equivalently, a Peierls instability along the indium chain. On the other hand, an x-ray diffraction (XRD) experiment<sup>4</sup> observed a low-temperature  $8 \times "2"$  structure which is not fully developed even at 20 K, implying that the phase transition is not driven by a CDW. Moreover, our previous<sup>5</sup> first-principles density-functional calculations showed that both the  $4 \times 1$  and  $4 \times 2$  structures have three metallic bands crossing the Fermi level. Recently, other ARP, scanning tunneling spectroscopy (STS), and STM experiments of Yeom and his co-workers<sup>8,9</sup> obtained more information on the temperature-dependent electronic structures of the In/Si(111) system. This recent ARP experiment<sup>8</sup> observed that the three surface-state bands  $m_1$ ,  $m_2$ , and  $m_3$ clearly exhibit a band-gap opening below the transition temperature  $T_c$ , indicating a metal-insulator transition. The STS experiment<sup>9</sup> estimated this energy gap as  $\sim 0.16$  eV. Using a temperature-variable microscopic four-point probe method, Tanikawa et al.<sup>10</sup> found a dramatic change of electrical conductivity around 130 K and estimated an energy gap of  $\sim 0.3$  eV, which is two times larger than that estimated by the STS. It is noticeable that the recent STM experiment<sup>9</sup> also observed that at low temperatures below  $T_c$  the chargedensity maxima (i.e., bright protrusions) in both the filledand empty-state STM images not only doubled along the indium chain but were also completely out of phase with each other, thereby demonstrating occurrence of charge ordering in the low-temperature phase. Based on their ARP, STS, and STM data, Yeom and his co-workers<sup>8,9</sup> proposed a gap-opening mechanism in a multiband system where only



FIG. 1. Optimized structure of In/Si(111): (a) the side view of the  $4 \times 1$  structure, (b) the top view of the  $4 \times 1$  structure, and (c) the top view of the  $4 \times 2$  structure. The dark and gray circles represent In and Si atoms, respectively. Two different choices for the  $4 \times 1$  and  $4 \times 2$  unit cells are indicated by the solid and dashed lines. The arrows in (c) show pairing patterns of the outer indium atoms. The **x** and **y** directions are  $\lceil \overline{110} \rceil$  and  $\lceil 11\overline{2} \rceil$ , respectively.

one  $(m_3)$  band among the three surface bands has a Fermisurface nesting with  $2k_F = \pi/a_x$  ( $a_x$  is the lattice constant along the x direction: see Fig. 1).

In this paper, using first-principles density-functional calculations we reinvestigate the electronic structure of the In/Si(111) system within the  $4 \times 2$  structure. We find that the  $m_2$  and  $m_3$  states hybridize to yield a band-gap opening. The size of this band gap is 0.19 (0.24) eV along the symmetry line  $\Gamma K(K'X')$ , in accordance with that (~0.16 eV) measured by a recent STS experiment.9 However, the present calculations show that the  $m_1$  state still crosses the Fermi level along the  $\Gamma K$  and  $\Gamma X'$  symmetry lines. In addition, we find that the patterns of simulated STM images are strongly sensitive to the position of the Fermi level. If the Fermi level moves up toward the middle of the pseudogaps, the observed double periodicity and out-of-phase patterns in the filled- and empty-state STM images are well reproduced. Our results for the surface-state energy bands and the simulated STM images agree well with the recent ARP, STS, and STM experiments,<sup>8,9</sup> but are not compatible with a 1D CDW formation accompanying a metal-insulator transition.

Our first-principles calculations are performed using norm-conserving pseudopotentials<sup>12</sup> and the generized gradient approximation (GGA).<sup>13</sup> We used the same calculational parameters<sup>14</sup> as employed in our previous<sup>5</sup> calculations, except the number of **k** points for the **k**-space integrations. The present k-space integration was done with meshes of 224 (112) **k** points in the surface Brillouin zone (SBZ) of the  $4 \times 1$  (4×2) unit cell, which is more than the 64 (32) k points used in our previous<sup>5</sup> calculations. Despite the present greater k-point samplings, there is little change in the atomic positions of the  $4 \times 1$  and  $4 \times 2$  structures, as well as in the energy difference between the two structures, compared with those of our previous calculations. The calculated surface band structure of  $In/Si(111)-4 \times 2$  is displayed in Fig. 2. Unlike our previous<sup>5</sup> surface band structure, where the  $m_2$ and  $m_3$  states cross each other along the  $\Gamma K$  and K'X' symmetry lines just above the Fermi level, the present one shows that band gaps open along the the  $\Gamma K$  and K'X' lines by 0.19 and 0.24 eV, respectively (see Fig. 2). In our previous calculations, the mapping of the surface bands was in error because of the choice of sparse meshes along the symmetry lines, but here we obtain the energy levels at dense meshes as shown in Figs. 2(b) and 2(c). Remarkably, the magnitudes of the present pseudogaps are close to the measured band gap  $(\sim 0.16 \text{ eV})$  from the STS experiment.<sup>9</sup> However, as shown in Fig. 2(a), the  $m_1$  state still crosses the Fermi level along the  $\Gamma K$  and  $\Gamma X'$  symmetry lines, indicating that the 4×2 structure is metallic. Therefore, our band-structure calculations of In/Si(001)-4×2 do not support a metal-insulator transition claimed by Yeom and his co-workers.<sup>3,7–9</sup>

The formation of the pseudogaps in Figs. 2(b) and 2(c) is caused by the hybridization of the  $m_2$  and  $m_3$  states. Noting that the  $m_2$  and  $m_3$  states have similar charge distributions [see Fig. 2(c) in Ref. 5], such a hybridization easily takes place when the surface states around the X(M) point in the  $4 \times 1$  SBZ are folded back around the  $\Gamma(X')$  point in the  $4 \times 2$  SBZ [see the inset of Fig. 2(a)]. The band-gap opening in the  $4 \times 2$  structure results in the energy lowering of the the



FIG. 2. Surface band structure of  $In/Si(111)-(4 \times 2)$ . The inset in (a) shows the surface Brillouin zone for the  $4 \times 1$  and  $4 \times 2$  unit cells with that for the  $1 \times 1$  unit cell as a reference. The shaded areas are the projected bulk-band structure. (b) and (c) magnify the calculated energy levels around A, A', B, and B', equivalent to the two boxes in (a). Three different choices for the Fermi level (i.e.,  $E_{F0}, E_{F1}$ , and  $E_{F2}$ ) are given in (b) and (c): see the text.

 $m_2$  and  $m_3$  states near the K and K' points [i.e., at the points A and B in Fig. 2(a)], consistent with low-temperature ARP data<sup>7</sup> where the edges of the  $m_2$  and  $m_3$  states around the K point shift away from the Fermi level. Despite the significantly reduced spectral wights of the  $m_2$  and  $m_3$  states near the Fermi level, the ARP data of Ref. 7 showed some remaining spectral weights representing the *pseudogap* nature. It is notable that this low-temperature ARP data showed the presence of the  $m_1$  state, though its intensity is very weak. In this sense, the earlier<sup>7</sup> ARP experiment finding the presence of  $m_1$  near the Fermi level seems to differ somewhat from the recent<sup>8</sup> ARP experiment where the  $m_1$  band disappears at low temperatures below  $T_c$  (see below).

Recently, Yeom and his co-workers performed another<sup>8</sup> ARP experiment to determine the dispersions of the surface states over more extended regions in the SBZ. At low temperatures they observed a clear gap opening of the  $m_2$  and  $m_3$ bands with the disappearance of the  $m_1$  band. Here, the dispersions of the  $m_2$  and  $m_3$  bands along the XK (equivalently  $\Gamma K$ ) and MK' (equivalently X'K') lines are nearly parabolic with energy minima at the X point and around a half point between the M and K' points, respectively. In Ref. 8, it is difficult to find the energy minimum along the latter symmetry line because the intensity around the M point was very

weak. Such a parabolic feature of the  $m_2$  and  $m_3$  bands along the XK (or  $\Gamma K$ ) and MK' (or X'K') lines agrees well with our calculated surface-state bands [see Fig. 2(a)] of the 4  $\times 2$  structure. According to the ARP data of Ref. 8, the bandgap positions (i.e., energy maxima) of  $m_3$  were found to be nearly at the K and K' points, while those of  $m_2$  are somewhat shifted from the K and K' point. These experimental observations are consistent with our calculated band dispersion of Fig. 2, where the point C(D) corresponding to the maximum of  $m_3$  along the  $\Gamma K(X'K')$  line is at the K(K')point while the point A(B) corresponding to the maximum of  $m_2$  is slightly shifted from the K(K') point. From their ARP data,<sup>8</sup> Yeom and his co-workers estimated that the maxima of  $m_2$  and  $m_3$  are located at 0.04 and 0.34 eV below the Fermi level, respectively. Here, the position of the experimental Fermi level does not correspond with our theoretical one, but the energy difference (0.30 eV) between the maxima of  $m_2$  and  $m_3$  is in good agreement with the present result (0.29 eV) between the A point [the maximum of  $m_2$ : see Fig. 2(a)] and the C point [the maximum of  $m_3$ : see Fig. 2(a)]. Also, the ARP data of Ref. 8 showed that the band-gap size of  $m_2$  varies over the **k** space as much as 0.05 eV; that is, the band maximum along the XK line is higher than that along the MK' line. This behavior can be seen in our calculated dispersion of  $m_2$  where the A point along the  $\Gamma K$  line is higher in energy than the B point along the X'K' line by 0.16 eV. Thus, the overall dispersions of  $m_2$  and  $m_3$  agree well between the recent<sup>8</sup> ARP experiment and the present calculations. However, unlike the recent ARP experiment our calculations show no evidence for the disappearance of the  $m_1$  band. Noting in the recent experiment that the spectrum intensity of the low-temperature phase was significantly reduced compared with that of the high-temperature phase, it seems that in the former phase the dispersion of the  $m_1$  state could not be measured because of its weak intensity.

Using a combination of STM and STS, Park et al.<sup>9</sup> observed an energy gap opening of  $\sim 0.16$  eV as the temperature is lowered below  $T_c$ , and therefore claimed that the phase transition is truly a metal-insulator transition with a clear band gap rather than a pseudogap. According to their STM data for the low-temperature phase, the filled and empty state images showed the charge-density maxima with a double periodicty  $(\times 2)$  along the indium wires, and the maxima of the two images are completely out of phase with each other. Such a charge ordering together with a band-gap opening may be related with formation of a CDW in indium wires. However, our results for the band structure of In/Si(111)-4  $\times$  2 reveal that the  $m_1$  state does not disappear but still crosses the Fermi level. This metallic feature of  $m_1$  is not compatible with a simple 1D CDW mechanism for the phase transition. For comparison with the STM measurements, we simulate the STM images for the filled and empty states of  $In/Si(111)-4 \times 2$ . We have to notice that, because the STS experiment<sup>9</sup> measured a clear band gap at low temperatures below  $T_c$ , the position of the Fermi level  $(E_F)$  was not definitely determined within the band gap. Therefore, we choose the three different locations of the Fermi level to simulate the STM images: i.e., at (i)  $E_{F0}$  being the real Fermi level, (ii)  $E_{F1}$  located 0.10-eV above  $E_{F0}$ , and (iii)  $E_{F2}$  lo-



FIG. 3. Simulated STM images of In/Si(111)-(4×2): (a) the filled-state image with  $E_F = E_{F0}$ , (b) the empty-state image with  $E_F = E_{F0}$ , (c) the filled-state image with  $E_F = E_{F1}$ , (d) the empty-state image with  $E_F = E_{F1}$ , (e) the filled-state image with  $E_F = E_{F2}$ , and (f) the empty-state image with  $E_F = E_{F2}$ . For the definition of  $E_{F0}$ ,  $E_{F1}$ , and  $E_{F2}$ , see Fig. 2. The filled (empty)-state images are obtained by integrating the charge from  $E_F$  to  $E_F - 0.3$  (+0.3) eV. The images are taken at 3.8 Å above the outermost indium atom. The open circles mark bright spots in the empty-state images.

cated just below B' [see Figs. 2(b) and 2(c)]. Our simulated STM images for the filled and empty states are displayed in Fig. 3. Here, the filled-state (empty-state) image mapping the electron density integrated at 0.3 eV downward (upward) from a given Fermi level is taken at about 3.8 Å above the outermost indium atom. (0.3 eV was the voltage at which the experimental STM data<sup>9</sup> was taken.) We find that the STM simulation [Figs. 3(a) and 3(b)] with a choice of  $E_F = E_{F0}$ does not agree with the observed<sup>9</sup> STM images. On the other hand, with  $E_F = E_{F1}$  and  $E_{F2}$  the filled- and empty-state images show bright spots with a double periodicity, which are completely out of phase with each other along the indium wires [see Figs. 3(c)–3(f). Especially, in case of  $E_F = E_{F2}$ such double periodic and out-of-phase patterns are conspicuous, in good agreement with the experimental STM data.<sup>9</sup> It is interesting to note that the location of  $E_{F2}$  is 0.05-eV above the A point [i.e., the maximum of the  $m_2$  band: see Fig. 2(b)], similar to the experimental<sup>8</sup> Fermi level which is located at 0.04 eV above the maximum of the  $m_2$  band.

Since our band structure of  $In/Si(111)-4 \times 2$  shows no evidence of being an insulator, the observed phase transition

is possibly due to an energy lowering lattice distortion with the hybridization of the surface states  $m_2$  and  $m_3$ , rather than a simple 1D CDW mechanism.<sup>3,7–9</sup> In our previous<sup>5</sup> calculations, the  $m_2$  state represents appreciable indium-p character localized between "inner" indium atoms [i.e., In<sub>2</sub>, In<sub>2</sub>, In<sub>3</sub>, and  $In_{3'}$  in Fig. 1(c)], whereas the  $m_3$  state originates mainly from the indium-Si interface bonding. Therefore, it is likely that the  $m_2$ - $m_3$  hybridization induces some attraction between  $In_2(In_{2'})$  and  $In_3(In_{3'})$  [see Figs. 1(b) and 1(c)]. As a result, the distances  $d_{In_2-In_3}$  and  $d_{In_2'-In_3'}$  become shorter, 3.06 Å, compared to 3.12 Å in the case of  $4 \times 1$  structure. Because In<sub>3</sub> and In<sub>3'</sub> are on reflection planes of the  $4 \times 1$ structure, a degenerate state would be obtained if we had chosen  $In_2$  to be attracted to  $In_{3'}$ . Including the additional possibility of the pairing directions of "outer" indium atoms [i.e.,  $In_1$ ,  $In_{1'}$ ,  $In_4$ , and  $In_{4'}$  in Fig. 1(c)], each 4  $\times$  2 unit cell has four degenerate configurations.<sup>5</sup> Thus, above  $T_c$  the atoms oscillate between their energy minima, their average positions yielding the  $4 \times 1$  structure, whereas below  $T_c$  the atoms in each  $4 \times 2$  cell are frozen randomly into one of the four degenerate ground states. This simple picture for the

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phase transition would provide an explanation for the RHEED (Ref. 3) and XRD (Ref. 4) observations that the low-temperature superstructure was not fully developed as  $4 \times 2^{\circ}$  (or  $8 \times 2^{\circ}$ ) reconstructions.

In summary, we reinvestigated the surface band structure of In/Si(111)-4×2 using first-principles density-functional theory calculations. Our results for the surface band structure showed that the 4×2 structure has a metallic feature, therefore not supporting a simple 1D CDW mechanism accompanying a metal-insulator transition. However, the dispersions of the surface bands  $m_2$  and  $m_3$  agree well with the recent ARP data.<sup>8</sup> The simulated scanning tunneling microscopy (STM) images also reproduce the features observed in the STM experiment,<sup>9</sup> such as a double periodicity and an outof-phase distribution in the filled- and empty-state images. We hope future ARP experiments will observe the presence of the  $m_1$  state crossing the Fermi level.

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- <sup>14</sup>The surface is modeled by a periodic slab geometry. Each slab contains six Si atomic layers (not including the Si surface chain) plus an In overlayer, and the bottom Si layer is passivated by one H atom per Si atom. The thickness of the vacuum region between these slabs is about 10 Å. The electronic wave functions are expanded in a plane-wave basis set with a cutoff energy of 15 Ry.