

## High-resolution vacuum ultraviolet spectroscopy of $5d-4f$ transitions in Gd and Lu fluorides

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Observation, investigation, and characterization of vacuum ultraviolet (VUV) ( $\sim 10$  eV) luminescence due to interconfigurational  $4f^{n-1}5d-4f^n$  transitions in  $\text{Gd}^{3+}$  and  $\text{Lu}^{3+}$  are reported. High-resolution ( $\sim 0.5$  Å) VUV emission and excitation spectra as well as decay kinetics of VUV luminescence have been measured for  $\text{LiGdF}_4$ ,  $\text{GdF}_3$ ,  $\text{LiLuF}_4$ , and  $\text{LuF}_3$  crystals using synchrotron radiation. The obtained results are the direct proof that the VUV luminescence observed from  $\text{LiGdF}_4$  or  $\text{GdF}_3$  crystals and  $\text{LiLuF}_4$  or  $\text{LuF}_3$  originates from  $4f^65d-4f^7$  transitions in  $\text{Gd}^{3+}$  and  $4f^{13}5d-4f^{14}$  transitions in  $\text{Lu}^{3+}$ , respectively. The fine structure due to zero-phonon and vibronic lines was well resolved in VUV emission and excitation spectra of  $\text{LiGdF}_4$ , whereas the spectra of  $\text{GdF}_3$  and  $\text{LuF}_3$  have a smooth shape because of stronger electron-lattice coupling between the  $4f^{n-1}5d$  electronic configuration of the  $\text{Gd}^{3+}$  and  $\text{Lu}^{3+}$  ions and the lattice vibrations.

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Spectroscopy of parity-allowed interconfigurational  $4f^n \rightarrow 4f^{n-1}5d$  transitions of trivalent rare earth ( $\text{RE}^{3+}$ ) ions in a wide band-gap matrix requires a tuneable light source in the vacuum ultraviolet (VUV). In the pioneering work of Yen *et al.*,<sup>1</sup> the potential of synchrotron radiation as an excitation source for luminescence spectroscopy was demonstrated. It was first applied to  $4f^n \rightarrow 4f^{n-1}5d$  excitations of  $\text{RE}^{3+}$  ions by Elias *et al.*<sup>2</sup> and Heaps *et al.*<sup>3</sup> The pioneering work, dealing with the  $4f^{n-1}5d \rightarrow 4f^n$  VUV luminescence of  $\text{Nd}^{3+}$ ,  $\text{Er}^{3+}$ , and  $\text{Tm}^{3+}$ , was published by Yang and DeLuca.<sup>4</sup> For the first half of the lanthanide series, transitions from the lowest level of the  $4f^{n-1}5d$  electronic configuration into the  $4f^n$  ground state are spin allowed with short lifetimes (a few ns to  $\approx 50$  ns). For ions in the second half of the lanthanide series, such transitions are spin forbidden (lifetimes in the  $\mu\text{s}$  range). Depending on the ion and the host, spin-forbidden, slow emission from the lowest high-spin  $4f^{n-1}5d$  state, and fast spin-allowed emission from the lowest low-spin state coexist.<sup>5,6</sup> Up to now, VUV  $\text{RE}^{3+}$  luminescence has been detected only from  $\text{Nd}^{3+}$ ,  $\text{Er}^{3+}$ , and  $\text{Tm}^{3+}$ .<sup>4-8</sup>

To the best of our knowledge,  $\text{Gd}^{3+}$  and  $\text{Lu}^{3+}$  VUV  $d \rightarrow f$  emission has never been observed before. This may be partly due to experimental difficulties in luminescence spectroscopy in the VUV, in particular for photon energies  $\geq 10$  eV ( $80\,000\text{ cm}^{-1}$ ) where the emission was expected.<sup>9</sup> On the other hand, for  $\text{Gd}^{3+}$  with its large number of  $4f$  levels extending up to  $150\,000\text{ cm}^{-1}$ ,<sup>10</sup> it was generally accepted that the  $d \rightarrow f$  luminescence would be quenched by energy transfer to  $4f$  levels with subsequent non-radiative relaxation, populating the lower emitting  $4f$  levels. Two photon spectroscopy has been applied in experimental studies for the lower  $4f$  levels of  $\text{Gd}^{3+}$  by Dagenais *et al.*<sup>11</sup> and more recently up to  $61\,400\text{ cm}^{-1}$ .<sup>12</sup> But the onset of  $\text{Gd}^{3+}$   $4f^n \rightarrow 4f^{n-1}5d$  excitations in  $\text{CaF}_2$  was found around  $78\,000\text{ cm}^{-1}$ .<sup>13</sup> The respective  $\text{Lu}^{3+}$  excitations have been identified only recently in experiments on the  $\text{Ce}^{3+}$  luminescence in  $\text{LiLuF}_4:\text{Ce}^{3+}$ .<sup>14</sup>

In the present Communication, high-resolution spectro-

scopic studies of VUV emissions from  $\text{LiGdF}_4$ ,  $\text{GdF}_3$ ,  $\text{LiLuF}_4$ , and  $\text{LuF}_3$ , nominally pure and doped with  $\text{Ce}^{3+}$  are reported for the spectral range around the edge of  $4f^7-4f^65d$  transitions in  $\text{Gd}^{3+}$  and  $4f^{14}-4f^{13}5d$  transitions in  $\text{Lu}^{3+}$ .

The VUV spectroscopy was performed at the SUPER-LUMI station of HASYLAB at DESY.<sup>15</sup> High-resolution VUV emission was recorded using an open position sensitive microchannel-plate (MCP) detector coated with CsI in combination with a 1 m VUV monochromator, at resolutions up to  $0.5$  Å in second order.<sup>8</sup> The excitation spectra of VUV emission and decay curves were recorded using a Pouey type monochromator ( $\Delta\lambda = 25$  Å) equipped with a CsI sensitized microsphere plate detector. A SpectraPro 308i spectrograph with a R6358P (Hamamatsu) photomultiplier tube (PMT) was applied for measuring excitation spectra of UV/visible emission. Due to the extremely weak luminescence intensity, the VUV emission from  $\text{LiLuF}_4:\text{Ce}$  was investigated at the BW3 beamline of HASYLAB providing high-intensity excitation by XUV photons. In these measurements a high throughput  $0.4$  m VUV monochromator was used together with a MCP-PMT (Hamamatsu 1645 U-09) at a resolution of  $\sim 6$  Å.

Single crystals of nominally pure  $\text{LiGdF}_4$ ,  $\text{LiGdF}_4$  doped with  $0.05$  at. %  $\text{Ce}^{3+}$ ,  $\text{LiLuF}_4$ , and  $\text{LuF}_3$ , both doped with  $0.1$  at. %  $\text{Ce}^{3+}$ , were grown by the Czochralski method.<sup>16</sup> Powder samples of  $\text{GdF}_3$  and  $\text{LuF}_3$  were high-purity chemicals with a concentration of unwanted RE and other metals of  $0.0005$ – $0.001$  %, and an oxygen concentration of  $0.02$ – $0.05$  %.

The  $d \rightarrow f$  emission spectrum from the  $\text{LiGdF}_4$  crystal has a well-resolved fine structure which shows at least seven lines spread over  $\sim 500\text{ cm}^{-1}$  extending into a wide sideband centered at  $\sim 78900\text{ cm}^{-1}$  [Fig. 1(b)]. A striking similarity was observed between the VUV emission spectrum from  $\text{LiGdF}_4$  [which is essentially the same for the  $\text{LiGdF}_4:\text{Ce}(0.05\%)$  crystal] in the range of  $78\,500$ – $79\,500\text{ cm}^{-1}$  and the excitation spectrum of the

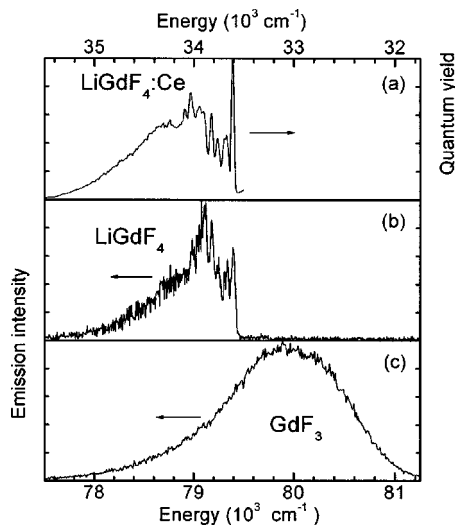


FIG. 1. (a) High-resolution excitation spectrum of  $\text{LiGdF}_4:\text{Ce}^{3+}(0.05\%)$  monitoring 311 nm emission (upper energy scale). High-resolution emission spectra ( $\Delta\lambda=0.8\text{ \AA}$ ) of (b)  $\text{LiGdF}_4$  and (c)  $\text{GdF}_3$  excited by 119 ( $84\,033\text{ cm}^{-1}$ ) and 117 nm ( $85\,470\text{ cm}^{-1}$ ) photons, respectively (lower energy scale).  $T=10\text{ K}$ .

311 nm emission from  $\text{LiGdF}_4:\text{Ce}(0.05\%)$  in the range of  $33\,500\text{--}34\,500\text{ cm}^{-1}$  [see Fig. 1(a)]. The VUV emission from  $\text{GdF}_3$  is situated at higher photon energies and shows a single structureless band centered at  $\sim 80\,000\text{ cm}^{-1}$  [Fig. 1(c)]. The excitation of VUV emission from  $\text{LiGdF}_4$  has a well-pronounced onset at  $79\,000\text{ cm}^{-1}$  which overlaps only with shortest-wavelength line of the emission spectrum [Fig. 2(a)]. The orange (590–640 nm) luminescence, which is due to  $4f^6G_{7/2}\text{--}^6P_J$  transitions in  $\text{Gd}^{3+}$ ,<sup>17</sup> is also observed from  $\text{LiGdF}_4$  under excitation to high-lying energy levels of  $\text{Gd}^{3+}$ . The most intense emission line at 311 nm is due to transitions from the lowest excited  $4f^7P_{7/2}$  level to the  $^8S_{7/2}$  ground state of  $\text{Gd}^{3+}$ . Excitation spectra of UV/visible luminescence from  $\text{LiGdF}_4$  have a well-pronounced fine structure and their onsets lie at energies slightly below that of the VUV emission [see Figs. 2(b) and 2(c)]. The structureless excitation spectrum of VUV emission from  $\text{GdF}_3$  has its threshold near  $83\,000\text{ cm}^{-1}$  [Fig. 2(d)]. The decay times of VUV emission from both Gd compounds lie in the nanosecond range: 2.8 ns for  $\text{LiGdF}_4$  and 0.97 ns for  $\text{GdF}_3$  at 10 K. The complete thermal quenching of VUV emission observed from the  $\text{LiGdF}_4$  crystal as well from the  $\text{GdF}_3$  powder takes place near 200 K.

The methodology proposed in Ref. 18 allows the estimation of the energy for the lowest  $4f^n\text{--}4f^{n-1}5d$  transition in the  $\text{RE}^{3+}$  ion doped into a particular host if the value of this energy is known for  $\text{Ce}^{3+}$ . In  $\text{LiGdF}_4$  weakly doped with  $\text{Ce}^{3+}$  the intensity of  $\text{Ce}^{3+} 5d\text{--}4f$  luminescence is practically negligible because of very efficient energy transfer from  $\text{Ce}^{3+}$  to  $\text{Gd}^{3+}$  resulting in the 311 nm emission from  $\text{Gd}^{3+}$ . However, from the excitation spectrum of the 311 nm Gd emission [Fig. 1(a)], the energy of the zero-phonon line for the lowest  $4f\text{--}5d$  transition of  $\text{Ce}^{3+}$  in  $\text{LiGdF}_4$  can be determined as  $33\,615\text{ cm}^{-1}$ . The estimated energy for the zero-phonon line of the lowest  $4f^7\text{--}4f^65d$  transition in  $\text{Gd}^{3+}$  is  $79\,415\text{ cm}^{-1}$ , that is very close to the observed threshold in

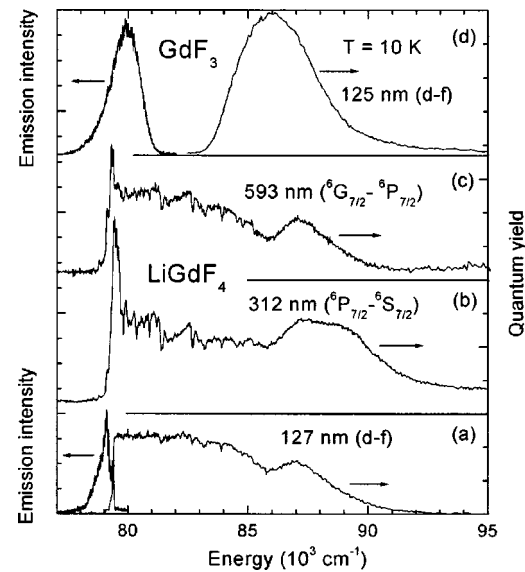


FIG. 2. (a) High-resolution excitation spectrum of  $4f^65d\text{--}4f^7\text{ Gd}^{3+}$  emission at 127 nm from  $\text{LiGdF}_4$  crystal together with high-resolution emission spectrum from  $\text{LiGdF}_4$  crystal excited by 119 nm ( $84\,033\text{ cm}^{-1}$ ) photons. High-resolution excitation spectra ( $\Delta\lambda=0.8\text{ \AA}$ ) of  $4f^7\text{--}4f^7\text{ Gd}^{3+}$  emissions monitoring (b) 312 nm ( $^6P_{7/2}\text{--}^6S_{7/2}$ ) and (c) 593 nm ( $^6G_{7/2}\text{--}^6P_{7/2}$ ) emission. (d) Excitation spectrum ( $\Delta\lambda=2.9\text{ \AA}$ ) of  $4f^65d\text{--}4f^7\text{ Gd}^{3+}$  emission at 125 nm from  $\text{GdF}_3$  together with high-resolution emission spectrum from  $\text{GdF}_3$  excited by 117 nm ( $85\,470\text{ cm}^{-1}$ ) photons.  $T=10\text{ K}$ .

excitation for VUV emission from  $\text{LiGdF}_4$  as well as to the energy of the shortest-wavelength emission line from this crystal ( $79\,377\text{ cm}^{-1}$ ).

The above consideration allows us to ascribe the observed VUV luminescence from  $\text{LiGdF}_4$  (and from  $\text{GdF}_3$ ) to inter-configurational radiative transitions in  $\text{Gd}^{3+}$  from the lowest  $4f^65d$  level to the  $4f^7\text{ }^8S_{7/2}$  ground state. This conclusion is also confirmed by the following arguments. The decay time is expected to scale down to a few nanoseconds with increasing emission energy for the parity-allowed  $4f^65d\text{--}4f^7$  radiative transitions in  $\text{Gd}^{3+}$ , which are also spin allowed because the lowest  $4f^65d$  level of  $\text{Gd}^{3+}$  has the same spin as the  $4f^7\text{ }^8S_{7/2}$  ground state, as for all  $\text{RE}^{3+}$  ions in the first half of lanthanide series. Only a single band of the fast emission, which is due to transitions from the lowest  $4f^65d$  level to the  $4f^7\text{ }^8S_{7/2}$  ground state is observed in the spectrum because of the absence of spin-orbit splitting for the  $^8S$  ground term of  $\text{Gd}^{3+}$ . The  $\text{Gd}^{3+} 5d$  crystal-field splitting in  $\text{GdF}_3$  is expected to be smaller than in  $\text{LiGdF}_4$  because of the higher coordination number for  $\text{Gd}^{3+}$  (9 instead of 8), and accordingly the  $\text{Gd}^{3+} 4f^65d\text{--}4f^7$  luminescence is observed at higher energy in  $\text{GdF}_3$ .

As was mentioned before, the observation of VUV emission due to the  $4f^65d\text{--}4f^7$  transitions in  $\text{Gd}^{3+}$  is a rather unexpected result because of the considerable number of closely spaced  $4f^7$  levels in the same energy region as the  $4f^65d$  states, enabling nonradiative relaxation from the lowest  $\text{Gd}^{3+} 4f^65d$  level. However the branching between radiative and nonradiative transitions favors the radiative decay at low temperatures. Most probably, the reason for this effect is

that the respective non-radiative energy transfer is heavily spin forbidden, because the multiplicity of the lowest  $4f^65d$  level of  $Gd^{3+}$  is eight, whereas the  $4f^7$  levels of  $Gd^{3+}$  closest to this  $4f^65d$  level are doublet or quartet.<sup>19</sup>

The crystal-field splitting of the ground state of  $Gd^{3+}$  is extremely small,<sup>20</sup> i.e., only a single zero-phonon line can be expected in the VUV emission spectrum of  $Gd^{3+}$ . Thus, the fine structure of VUV emission from  $LiGdF_4$  should be due to one zero-phonon line corresponding to the electronic origin of the  $4f^65d-4f^7$   $^8S_{7/2}$  transition plus vibronic lines. The shape of the spectra with a zero-phonon line, a few narrow vibronic lines corresponding to different modes of lattice vibrations, and a wide lower-energy vibronic side band is typical for the case of intermediate electron-lattice coupling which is confirmed by the estimation of the Huang-Rhys parameter  $S \sim 1$  from the energy difference between the zero-phonon line and the maximum of the wide side band, taking into account the phonon spectrum of scheelite crystals.<sup>21</sup>

The Stokes shift of  $\sim 6000$   $cm^{-1}$  observed for  $4f^7-4f^65d$  transitions in  $GdF_3$  [Fig. 2(d)] is more than 10 times larger than the maximum phonon energy in RE trifluorides,<sup>22</sup> i.e., the Huang-Rhys parameter  $S$  exceeds 5 for all phonon modes of lattice vibrations, which corresponds to the case of strong electron-lattice coupling. As a result the  $Gd^{3+}$   $4f^65d-4f^7$  emission and  $4f^7-4f^65d$  excitation spectra from  $GdF_3$  have no vibronic fine structure. It should also be noted that the influence of oxygen contaminations in the powder sample on the spectrum of the VUV emission from  $GdF_3$  cannot be significant because oxygen impurity luminescence in fluorides is known to be in the visible range.<sup>23</sup>

The structure observed in the excitation spectra of the 592 and 311 nm emission from  $LiGdF_4$ , which spreads over about  $6000$   $cm^{-1}$ , should correspond to features of  $4f^7-4f^65d$  transitions in  $Gd^{3+}$ . The rectangular shape of the excitation spectrum for  $d \rightarrow f$  emission [Fig. 2(a)] above the threshold confirms that the total absorption is observed for the stoichiometric  $LiGdF_4$ . Generally the penetration depth of exciting radiation is controlled by the absorption coefficient. Taking into account very different lifetimes of  $5d$  and  $4f$  excitations, the influence of well-known surface quenching is much stronger for the long-lived  $4f$  excitations. So the dips in the excitation spectra [Figs. 2(b) and 2(c)] can be caused by absorption modulations.

Rather extensive studies have been performed earlier for  $4f^7-4f^65d$  transitions in  $Eu^{2+}$  (see Ref. 24, and references therein), which is isoelectronic to the  $Gd^{3+}$  ion. The structure observed for  $4f^7-4f^65d$  transitions in  $Eu^{2+}$  was well enough interpreted in first approximation as being due to the splitting of the  $4f^6$  core in the  $4f^65d$  state. We are not aware of any theoretical calculations describing  $4f^7-4f^65d$  transitions in  $Gd^{3+}$ , and a detailed analysis of the structure of these transitions is beyond the scope of this communication. However, it should be noted that the energy range of this structure matches well the energy spread for the ground  $^7F_1$  multiplet of  $4f^6$  configuration of  $Eu^{3+}$ .

The VUV luminescence from the  $LiLuF_4:Ce^{3+}$  crystal possesses both fast ( $\sim 82\,600$   $cm^{-1}$ ) and slow ( $\sim 80\,200$   $cm^{-1}$ ) emission bands with nanosecond and considerably longer lifetimes, respectively [Fig. 3(a)]. The VUV emission from this crystal was rather weak and the spectrum

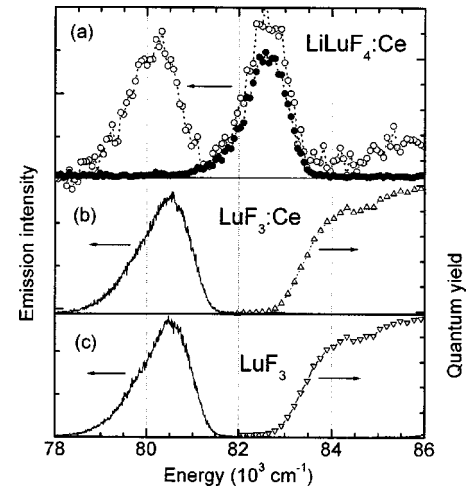


FIG. 3. (a) Emission spectra ( $\Delta\lambda=6$  Å) from  $LiLuF_4:Ce$  crystal excited by 130 eV photons at BW3. Time-resolved spectrum ( $\bullet$ ) was recorded within the time window of 0.8 ns after the excitation pulse. Time-integrated spectrum ( $\circ$ ) is also shown. High-resolution emission ( $\Delta\lambda=0.8$  Å) spectrum (solid line) excited by 116 nm photons and high-resolution excitation spectrum ( $\Delta\lambda=1$  Å) of  $4f^{13}5d-4f^{14}$  Lu emission ( $\Delta$ ) recorded at 124.5 nm from  $LuF_3:Ce$  crystal (b) and  $LuF_3$  powder (c).  $T=10$  K.

with moderate resolution was only measurable under intense XUV excitation at BW3. Due to the same reason the excitation spectrum of VUV emission from this crystal near the  $f-d$  threshold was not recorded. The VUV emission from both the  $Ce^{3+}$  doped single crystal and pure powder of  $LuF_3$  consists only of a single band ( $\sim 80\,500$   $cm^{-1}$ ) with a slow decay (longer than detectable range) [Figs. 3(b) and 3(c)]. The high-resolution measurements of both VUV emission and excitation spectra of  $LuF_3$  did not reveal any fine structure showing practically identical behavior for single crystal and powder samples. The VUV emission from  $LuF_3$  is thermally quenched near 200 K.

Following the approach of Ref. 18 for the prediction of the energy for the lowest  $4f^{13}5d$  level of  $Lu^{3+}$  in a particular host, the energy of the  $Lu^{3+}$  low-spin (singlet)  $4f^{13}5d$  level in  $LiLuF_4$  is expected at  $\sim 82\,300$   $cm^{-1}$ , which is in relatively good agreement with the energy of the high-energy band in the VUV emission spectrum of  $LiLuF_4$ . Considering the kinetic properties of VUV luminescence from  $LiLuF_4$ , the two bands observed in the VUV emission spectrum of the  $LiLuF_4$  crystal can be ascribed to spin-allowed (high-energy band, fast decay) and spin-forbidden (low-energy band, slow decay) interconfigurational  $4f^{13}5d-4f^{14}$  transitions from the lowest singlet and triplet levels of the  $4f^{13}5d$  configuration to the  $^1S_0$  ground state of the  $4f^{14}$  configuration of  $Lu^{3+}$ .

The VUV emission spectrum of  $LuF_3$  consists only of a single wide band with a slow decay, which is ascribed to spin-forbidden  $4f^{13}5d-4f^{14}$  transitions in  $Lu^{3+}$ . This is not an unusual observation since in many hosts the VUV emission of the  $4f^{n-1}5d-4f^n$  transitions in  $RE^{3+}$  ions consists only of a spin-forbidden band because of the fast nonradiative relaxation from higher-lying low-spin states to the lower-lying high-spin state.<sup>6,7</sup>

The fine structure in the VUV emission spectrum of

LiLuF<sub>4</sub> was not resolved in our moderate-resolution measurements. However, in the excitation spectrum of the Ce<sup>3+</sup> emission in LiLuF<sub>4</sub>:Ce<sup>3+</sup> from Ref. 14 both sharp zero-phonon lines and structureless side bands are observed in the energy range corresponding to Lu<sup>3+</sup> 4*f*<sup>13</sup>5*d*-4*f*<sup>14</sup> transitions, indicating intermediate coupling for the LiLuF<sub>4</sub> crystal. The Stokes shift between emission and absorption for 4*f*<sup>13</sup>5*d*-4*f*<sup>14</sup> transitions in Lu<sup>3+</sup> is larger in LuF<sub>3</sub> than in LiLuF<sub>4</sub>, which results in the absence of vibronic fine structure in both emission and excitation spectra of VUV luminescence from LuF<sub>3</sub>.

In conclusion, we observed VUV luminescence from LiGdF<sub>4</sub>, GdF<sub>3</sub>, LiLuF<sub>4</sub>, and LuF<sub>3</sub> crystals which was ascribed to radiative interconfigurational 4*f*<sup>6</sup>5*d*-4*f*<sup>7</sup> and 4*f*<sup>13</sup>5*d*-4*f*<sup>14</sup> transitions in Gd<sup>3+</sup> and Lu<sup>3+</sup>, respectively. Only fast nanosecond VUV luminescence is observed from Gd crystals, which is typical for spin-allowed 4*f*<sup>*n*-1</sup>5*d*-4*f*<sup>*n*</sup> tran-

sitions in RE ions from the first half of lanthanide series. Both fast and slow emission was detected from LiLuF<sub>4</sub>, corresponding to spin-allowed and spin-forbidden 4*f*<sup>13</sup>5*d*-4*f*<sup>14</sup> transitions in Lu<sup>3+</sup>. Fine structure due to zero-phonon lines and vibronic lines was well resolved in VUV emission and excitation spectra of LiGdF<sub>4</sub> whereas the spectra of GdF<sub>3</sub> and LuF<sub>3</sub> have a smooth shape because of stronger electron-lattice coupling between the 4*f*<sup>*n*-1</sup>5*d* electronic configuration of the Gd<sup>3+</sup> and Lu<sup>3+</sup> ions and the lattice vibrations.

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- <sup>1</sup>W. M. Yen, L. R. Elias, and D. L. Huber, *Phys. Rev. Lett.* **24**, 1011 (1970).
- <sup>2</sup>L. R. Elias, W. S. Heaps, and W. M. Yen, *Phys. Rev. B* **8**, 4989 (1973).
- <sup>3</sup>W. S. Heaps, L. R. Elias, and W. M. Yen, *Phys. Rev. B* **13**, 94 (1976).
- <sup>4</sup>K. H. Yang and J. A. DeLuca, *Appl. Phys. Lett.* **29**, 499 (1976).
- <sup>5</sup>R. T. Wegh, H. Donker, and A. Meijerink, *Phys. Rev. B* **57**, R2025 (1998).
- <sup>6</sup>R. T. Wegh and A. Meijerink, *Phys. Rev. B* **60**, 10 820 (1999).
- <sup>7</sup>J. Becker, J. Y. Gesland, N. Yu. Kirikova, J. C. Krupa, V. N. Makhov, M. Runne, M. Queffelec, T. Y. Uvarova, and G. Zimmerer, *J. Lumin.* **78**, 91 (1998).
- <sup>8</sup>Y. Chen, M. Kirm, E. Negodin, M. True, S. Vielhauer, and G. Zimmerer, *Phys. Status Solidi B* **240**, R1 (2003).
- <sup>9</sup>E. Loh, *Phys. Rev.* **147**, 332 (1966).
- <sup>10</sup>G. H. Dieke and H. M. Crosswhite, *Appl. Opt.* **2**, 675 (1963).
- <sup>11</sup>M. Dagenais, M. Downer, R. Neumann, and N. Bloembergen, *Phys. Rev. Lett.* **46**, 561 (1981).
- <sup>12</sup>P. Peijzel, Ph.D. thesis, University of Utrecht, Utrecht, 2004.

- <sup>13</sup>M. Schlesinger, T. Szczurek, and G. W. F. Drake, *Solid State Commun.* **28**, 165 (1978).
- <sup>14</sup>N. Yu. Kirikova, M. Kirm, J. C. Krupa, V. N. Makhov, E. Negodine, and J. Y. Gesland, *J. Lumin.* **110**, 135 (2004).
- <sup>15</sup>G. Zimmerer, *Nucl. Instrum. Methods Phys. Res. A* **308**, 178 (1991).
- <sup>16</sup>M. Louis, E. Simoni, S. Hubert, and J. Y. Gesland, *Opt. Mater. (Amsterdam, Neth.)* **4**, 657 (1995).
- <sup>17</sup>R. T. Wegh, H. Donker, A. Meijerink, R. J. Lamminmäki, and J. Hölsä, *Phys. Rev. B* **56**, 13 841 (1997).
- <sup>18</sup>P. Dorenbos, *J. Lumin.* **91**, 91 (2000).
- <sup>19</sup>A. Meijerink (private communication).
- <sup>20</sup>W. T. Carnall, P. R. Fields, and R. Sarup, *J. Chem. Phys.* **57**, 43 (1972).
- <sup>21</sup>S. Salaün, M. T. Fornoni, A. Bulou, M. Rousseau, P. Simon, and J. Y. Gesland, *J. Phys.: Condens. Matter* **9**, 6941 (1997).
- <sup>22</sup>M. M. Lage, A. Righi, F. M. Matinaga, J. Y. Gesland, and R. L. Moreira, *J. Phys.: Condens. Matter* **16**, 3207 (2004).
- <sup>23</sup>U. Rogulis, S. Schweizer, and J. M. Spaeth, *J. Phys.: Condens. Matter* **14**, 6949 (2002).
- <sup>24</sup>A. Ellens, A. Meijerink, and G. Blasse, *J. Lumin.* **59**, 293 (1994).