Correlation effects in Sr_2RuO_4 and Ca_2RuO_4 : Valence-band photoemission spectra **and self-energy calculations**

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We have studied the electronic structure of Sr_2RuO_4 and Ca_2RuO_4 using x-ray photoemission spectroscopy (XPS) and subsequent model calculations. While the t_{2g} band of Sr_2RuO_4 has substantial spectral weight at the Fermi level, that of Ca₂RuO₄ has no spectral weight at E_F and shows a peak at −1.8 eV. In the valence-band XPS spectrum of Sr_2RuO_4 , a satellite structure of the t_{2g} band is observed. In order to explain the spectral features, we have carried out band-structure calculations using the unrestricted Hartree-Fock (HF) approximation and found good agreement with the experimental result for Ca_2RuO_4 . In order to explain the satellite structure of $Sr₂RuO₄$, we have performed second-order perturbation calculations of the self-energy corrections around the unrestricted HF solution of $Sr₂RuO₄$.

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Transition-metal oxides have been attracting considerable interest due to their rich physical properties such as metalinsulator transition, exotic superconductivity, and spincharge-orbital ordering.1,2 Among them is the newly discovered Mott transition system Ca_{2−x}Sr_xRuO₄, which shows a rich phase diagram including superconductor, paramagnetic metal, antiferromagnetic insulator, and paramagnetic insulator phases.³ In order to understand the origin of this rich and complicated phase diagram, it is highly important to study the electronic structure of Ca2−*x*Sr*x*RuO4 using spectroscopic methods. Although photoemission spectroscopy is a powerful technique to study the electronic structure of solids, one should pay attention to the surface sensitivity of photoemission spectroscopy in order to interpret the spectrum properly. In particular, the electronic structure of complicated transition-metal oxides may be considerably affected by the surface effect. The first ultraviolet photoemission studies of $Sr₂RuO₄$ (Refs. 4,5) have reported Fermi surfaces that were apparently different from the prediction of the band-structure calculations^{6,7} and have raised serious controversy. Recently, Damascelli *et al.* have shown that the $Sr₂RuO₄$ surface prepared in suitable conditions gives the Fermi surface consistent with the band-structure calculation.⁸ In addition, the theoretical study by Liebsch⁹ has shown that the correlation effect is enhanced at the surface layer and that, in strongly correlated systems, the electronic structure of the surface can be very different from that of the bulk even without the surface reconstruction. Therefore, it is very important to study the electronic structure of the Ru oxides using x-ray photoemission spectroscopy that is more bulk sensitive than ultraviolet photoemission spectroscopy.

In the present work, we have examined the electronic structure of the end members $Sr₂RuO₄$ and $Ca₂RuO₄$ using x-ray photoemission spectroscopy (XPS) measurements that are rather bulk sensitive. Subsequently, we have analyzed the obtained valence-band photoemission spectra using model Hartree-Fock (HF) calculations and self-energy calculations. The comparison between the theoretical and experimental results indicates that the correlation effect beyond the Hartree-Fock treatment is much stronger in metallic $Sr₂RuO₄$ than in insulating $Ca₂RuO₄$.

Our XPS measurements were carried out at room temperature using a JPS9200 spectrometer. Monochromatic Al $K\alpha$ (1486.6 eV) radiation was used as an x-ray source. The pass energy of the electron analyzer was set to 10 eV. The total energy resolution including the x-ray source and the electron analyzer was about 0.6 eV. The binding energy was calibrated using the Fermi edge and the Au 4*f* core level (84.0 eV) of the gold reference sample. Single crystals of $Sr₂RuO₄$ and $Ca₂RuO₄$ grown using a floating zone method were cleaved *in situ*. The base pressure of the chamber was 7×10^{-8} Pa. The photoemission data were corrected at room temperature within 24 h after the cleavage. The angle θ between the surface normal and the outgoing photoelectron was set to be 20°.

The valence-band XPS spectra of Sr_2RuO_4 and Ca_2RuO_4 are shown in Fig. 1 (solid curves). At the photon energy of 1486.6 eV, the cross section of the Ru 4*d* subshell is dominant compared with that of O 2*p*. Therefore, it is expected that the experimental results show up the Ru 4*d* spectra. The Ru 4*d* t_{2g} band of Sr_2RuO_4 has substantial spectral weight at the Fermi level (E_F) , which is consistent with the metallic behavior of Sr_2RuO_4 . In addition, the t_{2g} band shows a weak satellite structure at -1.5 eV, which is consistent with the previous photoemission study and theoretical calculations.⁹ The intensity of the satellite structure is rather weak in the XPS spectrum compared to that in the ultraviolet photoemission spectrum of Sr_2RuO_4 ⁵ This is probably because the satellite formation is promoted by the enhanced correlation effect at the surface layer as pointed out by Liebsch.⁹

We have investigated the electronic structure of the layered perovskite $Ca₂RuO₄$ and $Sr₂RuO₄$ by using the multiband *d*-*p* model where full degeneracy of the Ru 4*d* and the O $2p$ are taken into account.¹⁰ The model Hamiltonian is given by

FIG. 1. Upper panel: Experimental result (solid curves) and calculated result by the model HF method (dotted curve) for $Ca₂RuO₄$. Lower panel: Those for $Sr₂RuO₄$.

$$
H = H_p + H_d + H_{pd},\tag{1}
$$

$$
H_p = \sum_{\mathbf{k},l,\sigma} \epsilon_{\mathbf{k}}^p p_{\mathbf{k},l\sigma}^\dagger p_{\mathbf{k},l\sigma} + \sum_{\mathbf{k},l>l',\sigma} V_{\mathbf{k},ll'}^{pp} p_{\mathbf{k},l\sigma}^\dagger p_{\mathbf{k},l'\sigma} + \text{H.c.,}
$$
\n(2)

$$
H_{d} = \epsilon_{d}^{0} \sum_{i,m,\sigma} d_{i,m\sigma}^{\dagger} d_{i,m\sigma} + \sum_{m,m',\sigma,\sigma'} h_{m,\sigma,m',\sigma'} d_{i,m\sigma}^{\dagger} d_{i,m'\sigma'}
$$

+ $u \sum_{i,m} d_{i,m\uparrow}^{\dagger} d_{i,m\uparrow} d_{i,m\downarrow}^{\dagger} d_{i,m\downarrow} + u' \sum_{i,m\neq m'} d_{i,m\uparrow}^{\dagger} d_{i,m'\downarrow}^{\dagger} d_{i,m'\downarrow}$
+ $(u' - j') \sum_{i,m>m',\sigma} d_{i,m\sigma}^{\dagger} d_{i,m'\sigma} d_{i,m'\sigma}$
+ $j' \sum_{i,m\neq m'} d_{i,m\uparrow}^{\dagger} d_{i,m'\uparrow} d_{i,m\downarrow}^{\dagger} d_{i,m'\downarrow}$
+ $j \sum_{i,m\neq m'} d_{i,m\uparrow}^{\dagger} d_{i,m'\uparrow} d_{i,m'\downarrow}^{\dagger} d_{i,m'\downarrow}$ (3)

TABLE I. Parameter sets for $Ca₂RuO₄$ and $Sr₂RuO₄$.

	$(pd\sigma)$ (eV)	r (\deg)	(deg)	δ_{IT}
Ca ₂ RuO ₄	-2.8	12.5	10	0.975
Sr ₂ RuO ₄	-3.4	θ	θ	1.025

$$
H_{pd} = \sum_{\mathbf{k},l,m,\sigma} V_{\mathbf{k},lm}^{pd} d_{\mathbf{k},m\sigma}^{\dagger} p_{\mathbf{k},l\sigma} + \text{H.c.}
$$
 (4)

 $d^{\dagger}_{i,m\sigma}$ are creation operators for the 4*d* electrons at site *i*. $d^{\dagger}_{\mathbf{k},m\sigma}$ and $p_{\mathbf{k},l\sigma}^{\dagger}$ are creation operators for Bloch electrons with wave vector **k** constructed from the Ru 4*d* and O 2*p* orbitals, respectively. $h_{m,\sigma,m',\sigma'}$ represents the crystal field and spinorbit interaction of the 4*d* orbital. The magnitude of the spinorbit interaction is 0.15 eV for the Ru 4*d* orbital. The intraatomic Coulomb interactions between 4*d* electrons are given by Kanamori parameters, u, u', j , and j' . The transfer integrals between the Ru 4*d* and O 2*p* orbitals $V_{\mathbf{k},lm}^{pd}$ are given in terms of Slater-Koster parameters $(p d\pi)$ and $(p d\sigma)$. The transfer integrals between 2*p* orbitals $V_{k,l'}^{pp}$ are expressed by $(pp\sigma)$ and $(pp\pi)$. Here, the ratio $(pd\sigma)/(pd\pi)$ is −2.2. The present model takes into account the spin-orbit interaction and the lattice distortion such as Jahn-Teller distortion, tilting, and rotation of $RuO₆$ octahedron. In the present calculation, *u*, *u'* are, respectively, 2.5 eV, 1.5 eV; $j=j'=0.5$ eV. $(pp\sigma)$ and $(pp\pi)$ are fixed at 0.60 and −0.15 eV, respectively, for the undistorted lattice. The transfer integrals between Ru 4*d* and O 2*p* orbitals are adjusted to get a good agreement with the LDA results; the values of rotation angle *r*, the tilting angle *t*, and the Jahn-Teller distortion δ_{IT} are from the previous work of Friedt *et al.*¹¹ These values are listed in Table I. When the lattice is distorted, the transfer integrals are scaled using Harrison's law.

The HF mean-field treatment is applied to the two-body Hamiltonian terms in H_d by replacing, for example, $\mu \Sigma_{i,m} d_{i,m}^{\dagger} d_{i,m} d_{i,m}^{\dagger} d_{i,m}$ by its average value:¹²

$$
u \sum_{i,m} d_{i,m\uparrow}^{\dagger} d_{i,m\downarrow} d_{i,m\downarrow}^{\dagger} = u \sum_{i,m} \langle d_{i,m\uparrow}^{\dagger} d_{i,m\uparrow} \rangle d_{i,m\downarrow}^{\dagger} d_{i,m\downarrow}
$$

+
$$
u \sum_{i,m} d_{i,m\uparrow}^{\dagger} d_{i,m\uparrow}^{\dagger} \langle d_{i,m\downarrow}^{\dagger} d_{i,m\downarrow} \rangle
$$

-
$$
u \sum_{i,m} \langle d_{i,m\uparrow}^{\dagger} d_{i,m\uparrow} \rangle \langle d_{i,m\downarrow}^{\dagger} d_{i,m\downarrow} \rangle.
$$

In the Hartree-Fock calculation, we input initial values of the order parameters such as $\langle d_{i,m}^{\dagger} d_{i,m} \rangle$ and diagonalized the mean-field Hamiltonian to get a set of eigenfunctions. The new values of the order parameters were then calculated at these eigenfunctions. These self-consistency cycles were iterated until successive differences of all the order parameters converged to less than 2×10^{-4} by sampling 40 000 *k* points in the first Brillouin zone. The single-electron excitation spectrum was then calculated from the HF results by using Koopmans's theorem.

Our calculated spectra of $Ca₂RuO₄$ and $Sr₂RuO₄$ within the HF approximation are shown in Fig. 1 together with the

FIG. 2. N_k plot of Sr_2RuO_4 .

experimental results. The calculated results are further broadened considering the energy resolution of the experimental setup. We observed a good agreement between calculated and experimental results in positions and intensities of the main peaks for $Ca₂RuO₄$. From our calculation, we can conclude that the two main peaks at around −1.8 eV and −6.2 eV are of the partial Ru 4*d* contribution from, respectively, the Ru $4d_{t_{2g}}$ –O 2*p* antibonding band and the Ru $4d_{t_{2g}}$ –O 2p bonding band. The asymmetric line shape of the Ru $^{4}d_{t_{2g}}$ -O 2*p* antibonding band (Ru t_{2g} band) is also reproduced by the calculation. For Sr_2RuO_4 , our HF calculation gives a similar result of the Fermi surface to that obtained from the local density approximation (LDA) calculation by Oguchi⁶ with two electronlike surfaces around Γ and one holelike surface around *M* (see Fig. 2). However, comparing with the experimental result (Fig. 1), the calculated Ru t_{2g} band near the Fermi level is too broad, and the relative intensities of the two peaks near the Fermi level do not match the experimental result.

The calculated Fermi surface of $Sr₂RuO₄$ is presented by mapping N_k , which is the number of occupied state at each momentum *k*:

$$
N_{\mathbf{k}} = \sum_{m,\sigma} \langle d^{\dagger}_{\mathbf{k},m\sigma} d_{\mathbf{k},m\sigma} \rangle + \sum_{l,\sigma} \langle p^{\dagger}_{\mathbf{k},l\sigma} p_{\mathbf{k},l\sigma} \rangle.
$$

The N_k plot as a function of k_x and k_y is shown in Fig. 2. As mentioned above, the calculated result agrees with the prediction of LDA calculation^{6,7} as well as the observation of angle-resolved photoemission spectroscopy.8

In an attempt to explain the band narrowing and the satellite structure observed in the Ru t_{2g} band, we have tried to take the electron-correlation effect into our calculation through perturbation calculations. The Dyson equation for the full Green's function is

$$
[\tilde{\omega} - \mathbf{H}^{HF} - \Sigma_{\mathbf{k},\sigma}(\tilde{\omega})] \mathbf{G}_{\mathbf{k},\sigma}(\tilde{\omega}) = 1, \qquad (5)
$$

where $\tilde{\omega} = \omega - \mu + i\delta$, ω denotes the energy dependence, μ is the chemical potential, and δ is a positive infinitesimal. In

FIG. 3. Experimetal (dotted) and calculated (solid) results for $Sr₂RuO₄$.

our calculation, $G_{k,\sigma}(\tilde{\omega})$ is a 34 × 34 matrix and the basis set for $G_{k,\sigma}(\tilde{\omega})$ is Ru 4*d* and O 2*p*. $\Sigma^{pp}=0$ while $\Sigma_{k,\sigma}^{dd}(\tilde{\omega})$ is constructed to second order in u , u' , j , and j' using the eigenenergy $\varepsilon_{\sigma}^{n}(\mathbf{k})$ and the weight of the *mth* 4*d* orbital $\alpha_{\sigma}^{n,m}(\mathbf{k})$ in the Bloch orbitals yielded from HF calculation:

$$
\Sigma_{\mathbf{k},\sigma}^{dd}(\tilde{\omega}) = \Sigma_{\sigma}^{(1)dd} + \Sigma_{\mathbf{k},\sigma}^{(2)dd}(\tilde{\omega}).
$$
 (6)

Here, *n* is the band index and **k** is the wave vector. The form of $\sum_{\mathbf{k},\sigma}^{dd}(\tilde{\omega})$ is similar to that used in the paper of Steiner *et al.*¹³ For metallic Sr_2RuO_4 , the self-energy must satisfy Im[$\Sigma_{\mathbf{k},\sigma}(\omega)$]=0 at the Fermi level,^{14,15} this can be overcome by calculating $\Sigma_{\mathbf{k}\sigma}(\omega)$ self-consistently.

The spectral function $A_{k,\sigma}(\tilde{\omega})$ is calculated once we get $G_{k,\sigma}(\tilde{\omega})$ from Eq. (5):

$$
\mathbf{A}_{\mathbf{k},\sigma}(\tilde{\omega}) = -\frac{1}{\pi} \text{Im}[\mathbf{G}_{\mathbf{k},\sigma}(\tilde{\omega})].
$$
 (7)

Summing $A_{k,\sigma}(\tilde{\omega})$ over **k** gives us the spectral function that should be compared with the valence-band XPS spectrum.

The calculation result for $Sr₂RuO₄$ with the self-energy correction is shown in Fig. 3. The inclusion of the selfenergy correction reduced the bandwidth of the t_{2g} band near the Fermi level, which shows an improvement comparing with the HF result. The tail of the t_{2g} band is obtained, which can be attributed to the weak satellite structure observed in the photoemission spectrum. However, the intensity of the satellite structure is not well reproduced in the present calculation. Also, the calculated result cannot reproduce the line shape of the bonding Ru-O band located around −6 eV. Probably, we need to consider the higher-order terms in the self-energy.⁹

In conclusion, we have performed the XPS measurement of Ca_2RuO_4 and Sr_2RuO_4 and observed a satellite structure in the t_{2g} band of Sr_2RuO_4 . Also, we have performed model calculations to explain the XPS spectra in the valence band. The model HF calculation results show good agreement with the experimental result for $Ca₂RuO₄$ but do not reproduce the spectrum of $Sr₂RuO₄$ well. This implies that the electron correlation in metallic $Sr₂RuO₄$ is stronger and is more complicated than in insulating $Ca₂RuO₄$ and cannot be treated within the HF theory. We take into account the electron correlations in $Sr₂RuO₄$ by performing the self-energy corrections around the HF solution of $Sr₂RuO₄$. The result showed a better agreement with valence-band XPS spectrum compared to the HF result.

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