Rounding of a first-order magnetic phase transition in Ga-doped $\text{La}_{0.67}\text{Ca}_{0.33}\text{MnO}_3$

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The effect of disorder on the critical properties of the ferromagnetic phase transition in colossal magnetoresistive manganite $La_{0.67}Ca_{0.33}MnO_3$ has been studied by substituting Ga for Mn. It is found that, upon 10% Ga substitution, the peak in the specific heat at the Curie point T_C changes drastically and appears as a small anomaly. Static magnetization data analyzed in the asymptotic critical region using modified Arrott plots and the Kouvel-Fisher method give values for the critical exponents $\beta=0.387(6)$, $\gamma=1.362(2)$, and $\delta=4.60(3)$. The results show that the first-order transition in $La_{0.67}Ca_{0.33}MnO_3$ becomes continuous by Ga substitution. The critical properties of the rounded transition in $La_{0.67}Ca_{0.33}Mn_{0.9}Ga_{0.1}O_3$ suggest that the magnetic subsystem in this mixed-valent perovskite is close to that of a conventional isotropic ferromagnet belonging to the Heisenberg universality class with short-range interactions. It is concluded that the first-order magnetic transition in pure $La_{0.67}Ca_{0.33}MnO_3$ is induced by fluctuations from a competing mode, which couples to the magnetic subsystem.

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INTRODUCTION

Colossal magnetoresistive (CMR) manganites of the type $R_{1-x}A_xMnO_3$, where R is a trivalent rare-earth ion and A is a divalent alkaline earth ion, has been a subject of intensive research in recent times due to their intricate magnetic and electrical properties.¹ For these compounds various electronic, magnetic, and structural orders compete leading to very rich phase diagrams. Recently, the importance of multicritical points for their unconventional "colossal" behavior has been emphasized. $2-4$

For a certain range of compositions $(0.2 \le x \le 0.4)$, the $R_{1-x}A_xMnO_3$ may show interdependent paramagneticferromagnetic (pm-fm) and insulator-metal transitions. An explanation of this phenomenon has been given by a doubleexchange model,⁵ where electron hopping between Mn- e_g levels align the $Mn-t_{2g}$ spins due to a strong intra-atomic Hund's coupling. For a quantitative explanation of CMR, additional mechanisms such as magnetoelastic couplings due to Jahn-Teller (JT) effects have been invoked.⁶ Several experimental and theoretical works have demonstrated a close connection between JT distortions and localization of charge carriers or in other words, formation of polarons, in the insulating phase.^{7,8} As a result, some of the theories associate CMR with a first-order pm-fm transition triggered by a discontinuous transition between polaronic and extended itinerant states of charge carriers.⁹

For the archetypical CMR material $La_{0.67}Ca_{0.33}MnO_3$ clear evidence of a first-order pm-fm transition has been found, such as strong volume anomaly at the Curie point (T_c) ,⁸ thermal hysteresis,¹⁰ and negative slopes observed in magnetic isotherm plots H/M versus M^2 .¹¹ The existence of a first-order pm-fm transition in the La_{1−*x*}Ca_{*x*}MnO₃ system is also corroborated by a tricritical point at the Curie temperature T_c for $x=0.4$.¹² On the other hand, recently it has been shown that another low temperature material, metallic $Nd_{0.6}Pb_{0.4}MnO_3$ with T_C =156 K and a sizeable CMR, has a continuous phase transition.¹³ A continuous phase transition has also been observed in $La_{0.7}Sr_{0.3}MnO_3$.¹⁴ Some of the insulating manganites such as $La_{0.67}Mg_{0.33}MnO_3$ (Ref. 15) and $La_{0.875}Sr_{0.125}MnO_3$ (Ref. 16) also show a continuous pm-fm transition with critical properties resembling those predicted for Heisenberg ferromagnets with short-range interactions. This can be expected although the double exchange is driven by the motion of conduction electrons $(Mn-e_o)$, the effective magnetic interaction near the transition is renormalized to isotropic short-range interactions that couple the core-like $Mn-t_{2g}$ -spins. Thus, the first-order and the continuous pm-fm transitions observed in different manganites indicate that the nature of the pm-fm transition seems to depend on the A-site doping.

The existence of a first-order pm-fm transition in $La_{0.67}Ca_{0.33}MnO_3$ is an intriguing problem in itself. It is known that thermally driven first-order transitions may be *rounded* by quenched disorder.^{17–23} This means that a firstorder transition in a pure system becomes continuous upon doping. Either a conventional critical behavior or novel types of continuous ordering transitions are observed in the disordered system. Thus, the existence of a first-order pm-fm transition in the $La_{1-x}Ca_xMnO_3$ system indicates that the inevitable mixed occupation of the A site of the perovskite lattice with La and Ca does not affect the magnetic ordering transition sufficiently to cause a continuous pm-fm transition. Interestingly, for a system with a continuous order parameter symmetry, as the magnetization in a Heisenberg-like magnet, there is a rigorous proof that, if the system undergoes a thermally driven first-order transition as a pure system, any amount of quenched disorder leads to a rounded continuous transition in spatial dimensions $d \leq 4$.^{19,24}

In general, the coupling of the magnetic subsystem to other degrees of freedom may cause a fluctuation-induced first-order transition. Such a scenario has been analyzed in terms of phenomenological Landau theory by using renormalization-group calculations for an isotropic magnetic system coupled to an Ising-like order parameter, which describes, e.g., a charge order. 3 This analysis, together with the absence of first-order transitions in disordered isotropic magnets, suggests that the first-order pm-fm transition in $La_{0.67}Ca_{0.33}MnO_3$ is most probably close to a multicritical point where an additional fluctuating order parameter transforms the pm-fm transition into a first-order transition. Such a multicritical point with two competing orders could become a triple point where three lines of first-order transitions meet and three different phases may coexist. Additional quenched disorder would round such a fluctuation-driven first-order transition in these systems. Continuous transitions will result, thereby, with certain critical properties. For some theoretical models, where a fluctuation-driven first-order transition occurs, it has been shown that the critical properties of the transition rounded by quenched disorder will be the same as those of the corresponding pure system, i.e., a system without quenched disorder and decoupled from the fluctuating competing order parameter.23 However, this need not be the case generally. In particular, the transitions near multicritical points in the presence of quenched disorder are not well understood.²¹ Therefore, it is interesting to study how strongly quenched disorder affects the pm-fm transition in La_{0.67}Ca_{0.33}MnO₃.

Here, we report how a direct substitution of nonmagnetic ions in the magnetic sublattice affects the critical properties as compared to pure $La_{0.67}Ca_{0.33}MnO_3$. Such effects of a Mn-site substitution have not been studied so far. Studies on substituting a bigger ion like Ba or Sr for Ca in the A site, i.e., $La_{0.67}(A_x Ca_{1-x})_{0.33} MnO_3$ (where A=Ba or Sr),^{11,25} have shown that a small amount of *A* ion substitution results in a crossover from a first-order transition to a continuous transition. The critical exponents obtained for the pm-fm transition in $La_{0.67}(Ba_{0.25}Ca_{0.75})_{0.33}MnO_3$ were found²⁵ in between those predicted for a three-dimensional (3D) Heisenberg model and for mean-field theory. However, such substitutions affect the lattice and modify the effective Mn-O-Mn bond angle, thereby changing the strength of the magnetic interactions. We introduce a substitutional ion Ga directly in the Mn sublattice. Ga^{3+} has an ionic radius similar to that of Mn^{3+} . Thus, this substitution avoids a static distortion of the lattice.²⁶ In addition, since Ga^{3+} has a filled shell configuration, it does not participate in the exchange interaction. Therefore, the observed change of the pm-fm transition is related only to the random impurities, viz. site-dilution, in the magnetic subsystem and suppression of dynamic JT distortion since Ga^{3+} is not a JT ion. In earlier experiments on $\text{La}_{3/2}\text{Ca}_{1/2}\text{Mn}_{1-x}\text{Ga}_x\text{O}_3$, randomly canted ferromagnetism for $x=0.1$ and features of a cluster-glass with a remaining ferromagnetically ordered component for $x=0.25$ were found.²⁶ Here, we show that the pm-fm transition becomes continuous in La_{0.67}Ca_{0.33}Mn_{0.9}Ga_{0.1}O₃, upon 10% Ga substitution for Mn in $La_{0.67}Ca_{0.33}MnO_3$. Three critical exponents associated with the static magnetization behavior at the transition are evaluated independently. The values of critical exponents are close to those expected for 3D Heisenberg model with shortrange interactions.

EXPERIMENTAL PROCEDURE

Polycrystalline La_{0.67}Ca_{0.33}Mn_{1−*x*}Ga_{*x*}O₃ (*x*=0 and *x* $=0.10$) samples were prepared by a conventional ceramic

FIG. 1. Temperature dependence of magnetization for La_{0.67}Ca_{0.33}Mn_{1−*x*}Ga_{*x*}O₃ (*x*=0 and 0.10) measured in a dc field of 3 kOe.

method. Stoichiometric amounts of La_2O_3 , $CaCO_3$, $MnC_2O_4 \cdot 2H_2O$, and Ga_2O_3 were ground well, and the homogeneous mixture was heated at 900 °C for 24 h, cooled to room temperature, reground, and heated at 1250 °C for 24 h. The black powder thus obtained was pelletized and sintered at 1500 °C for 12 h. The phase purity was investigated by x-ray diffraction. Both the compounds crystallize in orthorhombic structure with the space group *Pbnm*. Resistance measurements done by standard four-probe method showed insulator-metal transitions with resistivity peak temperatures of about 253 and 100 K for $x=0$ and $x=0.10$ compositions, respectively. The specific heat measurements were carried out in a model 6000 physical property measurement system (PPMS, Quantum Design) down to 2 K. Extensive magnetization measurements $M(T,H)$ were performed on $x=0$ and $x=0.10$ samples in external static magnetic fields *H* up to 48 kOe in the temperature range encompassing the respective critical regions $(230-260 \text{ K}$ for $x=0$ and $110-130 \text{ K}$ for $x=0.10$) near the pm-fm phase transition using a superconducting quantum interference device magnetometer. The data were collected in temperature steps of 0.5 K.

RESULTS AND DISCUSSION

The temperature dependence of magnetization measured in a field of 0.3 T of La_{0.67}Ca_{0.33}Mn_{1−*x*}Ga_{*x*}O₃ ($x=0$ and 0.10) is shown in Fig. 1. The sharp transition for $x=0$ indicates a first-order transition. The Curie temperature, defined as a point where *dM* /*dT* has a minimum, was found to be 240 and 120 K for $x=0$ and $x=0.10$, respectively. In Fig. 2, specific heat is plotted as a function of temperature. A sharp peak observed at $T \approx 236$ K in the specific heat (C_p) measurements of $x=0$ sample is also consistent with the firstorder transition. For $x=0.10$, on the other hand, no visible peak or cusp was observed in the specific heat curve. However, a small anomaly in specific heat around the Curie point can be seen when C_p/T versus *T* is plotted as shown in the inset of Fig. 2. This behavior is similar to that observed in $Nd_{0.6}Pb_{0.4}MnO_3$, which showed a continuous transition.²⁷ The ferromagnetic transition also is broadened (Fig. 1), sug-

FIG. 2. Specific heat as a function of temperature of La_{0.67}Ca_{0.33}Mn_{1−*x*}Ga_{*x*}O₃ (*x*=0 and 0.10). The arrow shows the Curie point of $x=0.10$. In the inset, C_p/T vs *T* is shown for $x=0.10$ sample around the Curie temperature.

gesting a smearing of the transition due to Ga impurities in the Mn sublattice. Since the specific heat behavior did not indicate a first-order transition for $x=0.10$ sample, we tried to analyze the static magnetization data assuming a continuous phase transition for this compound.

A continuous phase transition near the critical temperature T_c , according to the scaling hypothesis, shows a power law dependence of spontaneous magnetization $M_S(T)$, and inverse initial susceptibility $\chi_0^{-1}(T)$ on the reduced temperature $\varepsilon = (T - T_C)/T_C$ with a set of interdependent critical exponents β , γ , δ , etc.,²⁸ as given below:

$$
M_S(T) = M_0(-\varepsilon)^\beta, \quad \varepsilon < 0,\tag{1}
$$

$$
\chi_0^{-1}(T) = (h_0/M_0)\varepsilon^{\gamma}, \quad \varepsilon > 0. \tag{2}
$$

At T_c , exponent δ relates *M* and *H* by

$$
M = DH^{1/\delta}, \quad \varepsilon = 0. \tag{3}
$$

Here, M_0 , h_0/M_0 , and *D* are the critical amplitudes. Further, the scaling hypothesis predicts that $M(H, \varepsilon)$ is a universal function of *T* and *H*:

$$
M(H,\varepsilon) = \varepsilon^{\beta} f_{\pm}(H/\varepsilon^{\beta+\gamma}), \tag{4}
$$

where f_{+} for $T>T_C$ and f_{-} for $T < T_C$, are regular functions. Equation (4) implies that M/ε^{β} as a function of $H/\varepsilon^{\beta+\gamma}$ falls on two universal curves, one for temperatures above T_c and the other for temperatures below T_C .

In the case of the $x=0$ sample, the field dependence of magnetization measured in the vicinity of the Curie point showed anomalies in the slopes similar to a metamagnetic transition. Such change in slope, according to the criterion given by Banerjee, 29 is used to distinguish a first-order transition from continuous ones by purely magnetic methods. This method is assumed by Mira *et al.*¹¹ to distinguish the nature of pm-fm phase transition in La_{0.67}(Sr_xCa_{1-*x*})_{0.33}MnO₃. They found a negative slope of isotherm plots of H/M versus M^2 for $\text{La}_{0.67}\text{Ca}_{0.33}\text{MnO}_3$ characterizing a first-order transition. We found similar results.

FIG. 3. Isotherms M^2 vs H/M of $x=0.10$ sample at different temperatures close to the Curie temperature $(T_C=116 \text{ K})$.

On the other hand, no such anomalies were found in $La_{0.67}Ca_{0.33}Mn_{0.9}Ga_{0.1}O_3$. Hence, we proceeded with the scaling analysis.

In order to extract the spontaneous magnetization and susceptibility for $x=0.10$ from the $M-H$ isotherms, we constructed the Arrott plot M^2 versus H/M in Fig. 3 after correcting the external magnetic field for the demagnetization effect. Such curves should give a series of straight lines for different temperatures and the line at $T=T_C$ should pass through the origin, according to the mean-field theory. In the present case, the curves were found to be nonlinear, suggesting that the mean-field theory is not valid. Therefore, we analyzed the data using a modified Arrott plot, 30 in which $M/\varepsilon^{\beta'}$ is plotted versus $(H/M)^{1/\gamma'}$, as shown in Fig. 4. Different values of β' and γ' were taken as trial values for the construction of the modified Arrott plot. If the system is close to a tricritical point, as in the case of $La_{0.6}Ca_{0.4}MnO_3$, then mean-field exponents for tricritical points β =0.25 and γ =1¹² are expected. In the extreme disorder limit, the exponents should reach the Fisher-renormalized tricritical exponents (β =0.5 and γ =2).^{31,32} By checking these different pos-

FIG. 4. Modified Arrott plot isotherms $M^{1/\beta'}$ vs $(H/M)^{1/\gamma'}$ for $x=0.10$ sample, with trial values $\beta' = 0.365$ and $\gamma' = 1.336$, $T \sim T_C$ \simeq 116 K is the value obtained in this study.

FIG. 5. Temperature variation of the spontaneous magnetization M_S and the inverse initial susceptibility χ_0^{-1} , along with fits obtained for power laws for $x=0.10$ sample. FIG. 6. KF plot for the spontaneous magnetization M_s and the

sibilities, we find that the best description with nearly linear behavior for fields $1 \leq H \leq 48$ kOe is obtained in the modified Arrott plots for $\beta' = 0.365$ and $\gamma' = 1.336$. From a linear extrapolation from fields above 1 kOe to the intercepts with the axes $M^{1/\beta'}$ and $(H/M)^{1/\gamma'}$, values of spontaneous magnetization $M_S(T, 0)$ and inverse susceptibility $\chi_0^{-1}(T, 0)$, respectively, can be extracted. The isothermal line that passes through the origin is the critical isotherm at $T=T_C$. These values, $M_S(T, 0)$ and $\chi_0^{-1}(T, 0)$, are then plotted as functions of temperature. The power law fits according to Eqs. (1) and (2) to $M_S(T,0)$ and $\chi_0^{-1}(T,0)$, respectively, give the values of β [Eq. (1)] and γ [Eq. (2)]. These new values of β and γ are then used to construct new modified Arrott plots. The iteration was continued until stable values of β , γ , and T_C were obtained. In Fig. 5, $M_S(T,0)$ and $\chi_0^{-1}(T,0)$ versus temperature are plotted. The continuous curves show the power law fits according to Eqs. (1) and (2) to $M_S(T,0)$ and $\chi_0^{-1}(T,0)$, respectively. This gives the values of β =0.380(2) with T_C $=116.19(2)$ K [Eq. (1)] and $\gamma=1.365(8)$ with T_c $=116.11(2)$ K [Eq. (2)]. The exponents obtained in this way are close to those expected for a short-range Heisenberg model $[\beta = 0.3680(3), \gamma = 1.3960(9)]^{33}$

In order to obtain more precise values of critical exponents, the Kouvel-Fisher (KF) method 34 has been used. In this method, plots of $M_S(dM_S/dT)^{-1}$ versus *T* and $\chi_0^{-1} (d\chi_0^{-1}/dT)^{-1}$ versus *T* (Fig. 6) should yield straight lines with slopes $1/\beta$ and $1/\gamma$, respectively. When extrapolated to the ordinate equal to zero, these straight lines should give intercepts on their *T* axes equal to the Curie temperature. The straight lines obtained from a least-squares fit to the data give the values of β =0.387(6), T_C =116.05(6) K and γ $=1.362(2)$, $T_C=115.88(6)$ K, respectively.

To obtain the value of δ , the critical isotherm $M_S(116 K, H)$ versus *H* on a log-log scale has been plotted in Fig. 7. According to Eq. (3), this should be a straight line with slope $1/\delta$. From the linear fit we obtained $\delta=4.60(3)$, which compares well with the value $\delta=4.783(3)$ expected for a Heisenberg-like ferromagnet.³³

The scaling equation also predicts $\delta = 1 + (\gamma/\beta)^{35}$ From the values of β and γ obtained from Fig. 5, the calculated

inverse initial susceptibility χ_0^{-1} for $x=0.10$ sample.

value of δ according to this equation is 4.59 and that from the KF method is 4.52. The value of δ independently obtained from magnetization isotherm (Fig. 7) is in agreement with the scaling hypothesis within the experimental errors.

A more stringent test for scaling is to plot M/ε^{β} versus $H/\varepsilon^{\beta+\gamma}$ and to see whether the data obey the scaling equation of state [Eq. (4)]. If Eq. (4) holds, all of the data should fall on one of the two curves. By taking the values of β and γ obtained from KF method and T_c =116 K, the scaled data are plotted in Fig. 8 on a log scale. It can be clearly seen that all the data fall on two curves, one for $T>T_C$, and the other one is for $T < T_c$. Thus, our result suggests that doping in the magnetic sublattice of $La_{0.67}Ca_{0.33}MnO_3$ induces a change from a first-order to a continuous phase transition.

In the case of materials that show a continuous phase transition in the pure limit, the effect of quenched disorder is ruled by the Harris criterion,³⁶ which can be justified by renormalization group calculations.37,38 The theory predicts that quenched random impurities do not alter the static critical exponents at a continuous transition, if the specific heat

FIG. 7. *M* vs *H* on a log-log scale at 116 K, i.e., $T \sim T_c$, for *x* $=0.10$ sample. The straight line is the linear fit following Eq. (3).

FIG. 8. Normalized isotherms of *x*=0.10 sample below and above Curie temperature $(T_C \approx 116 \text{ K})$ on a log-log scale using β and γ . $|\varepsilon| = |T - T_C|/T_C$.

exponent α of the pure system is negative (α <0 as in Heisenberg-like ferromagnets), while in the opposite case, a crossover from a pure to a random fixed point with new critical exponents occurs. These predictions have been confirmed experimentally.^{32,39,40} This mechanism is closely related to the critical properties, which arise at a rounded firstorder transition.23 The critical properties found here for $La_{0.67}Ca_{0.33}Mn_{0.9}Ga_{0.1}O_3$ can be understood as those of a conventional isotropic ferromagnetic system where quenched disorder is not relevant.

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CONCLUSIONS

The effect of disorder on the critical properties of optimally doped $\text{La}_{2/3}\text{Ca}_{1/3}\text{MnO}_3$ has been studied by specific heat and static magnetic measurements in the critical region. It is shown that the substitution of nonmagnetic impurities softens the ferromagnetic transition and suppresses the phase coexistence. This disorder effect provides an important input in understanding ferromagnetism, metallicity, and the role of couplings to the lattice in the intensely studied, yet not well understood, manganite $La_{2/3}Ca_{1/3}MnO₃$. The effect of the Ga doping causes the expected rounding of the first-order transition and reveals the usual critical behavior at a ferromagnetic ordering. The estimated critical exponents indicate that the magnetic subsystem of the disordered compound likely belongs to the universality class of conventional 3D Heisenberg-like ferromagnets with short-range interactions. This would mean that, from a phenomenological point of view, the magnetic subsystem of $La_{2/3}Ca_{1/3}MnO_3$ is essentially that of a conventional isotropic ferromagnet. However, there must be a strong coupling to other modes which causes the fluctuation-driven first-order magnetic transition in the pure compound.

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