

EuMn₂Ge₂ and EuMn₂Si₂: Magnetic structures and valence transitionsM. Hofmann,^{1,*} S. J. Campbell,^{2,1} and A. V. J. Edge²¹*Technische Universität München, FRM II, Lichtenbergerstr 1, D-85747 Garching, Germany*²*School of Physical, Environmental and Mathematical Sciences, The University of New South Wales, Australian Defence Force Academy, Canberra, ACT 2600, Australia*

(Received 28 January 2004; published 28 May 2004)

The magnetic structures of ¹⁵³EuMn₂Ge₂ and ¹⁵³EuMn₂Si₂ have been determined by neutron diffraction measurements (~ 1.8 – 723 K). The Mn sublattices of both EuMn₂Ge₂ and EuMn₂Si₂ order antiferromagnetically [$T_N=667(9)$ K; space group $I4'/m'm'm$ and $T_N=391(5)$ K; space group $I_p4/m'm'm'$, respectively] with no evidence for ordering of the Eu⁺² ions in EuMn₂Ge₂ down to 1.5 K. EuMn₂Si₂ exhibits a thermally driven valence transition around $T_v\sim 527$ K with a pronounced increase in the unit cell volume of $\sim 7\%$ from the Eu³⁺ state at low temperatures ($T<\sim 150$ K) to an average valence state of ~ 2.5 at high temperatures ($T>\sim 600$ K). The valence-induced volume changes have been analyzed for the first time in terms of the interconfigurational fluctuation model with occupation probabilities for the Eu²⁺ state in EuMn₂Si₂ and the average Eu^{val} values found to agree well with our reanalysis of earlier ¹⁵¹EuMn₂Si₂ isomer shift data. The strength of the magnetic interaction for antiferromagnetic ordering of the Mn sublattice is decreased by $\sim 10\%$ – 15% as a result of the change in the electronic configuration of EuMn₂Si₂.

DOI: 10.1103/PhysRevB.69.174432

PACS number(s): 75.25.+z, 87.64.Bx, 75.20.Hr

I. INTRODUCTION

Interest in characterizing and understanding the behavior of intermediate valence systems of the $4f$ electron series has continued unabated for several decades (e.g., Refs. 1–3). Rare-earth (R) intermetallic compounds containing europium are of special interest—they exhibit a wide range of unusual physical and magnetic properties as well as intermediate valences associated with the transition from the Eu²⁺ ($4f^6$) configuration to the Eu³⁺ ($4f^7$) configuration (e.g., Ref. 4). Ternary EuT₂M₂ compounds (T=transition metal; M=Si, Ge, P) with the tetragonal ThCr₂Si₂-type structure have attracted particular attention as the pure 1-2-2 compounds form readily and solid solutions can also be formed across wide concentration ranges of the T and M elements. This enables aspects of valence transitions linked with substitutional effects in pseudoternary systems to be investigated (e.g., Refs. 5–8), in addition to the intrinsic behavior of the valence transitions in the pure 1-2-2 compounds themselves. An additional feature is the influence of the transition metal to the overall magnetism of the compounds. For example, the Ni sublattice in EuNi₂Si_{2-x}Ge_x is nonmagnetic,^{5,8} whereas the Mn sublattice exhibits magnetic order in EuMn₂Si_{2-x}Ge_x⁶ as indeed it does in all RMn₂Si_{2-x}Ge₂ compounds (e.g., Refs. 4, 9).

The temperature-induced valence transitions in EuT₂M₂ systems have been investigated by a variety of techniques, including ⁵⁷Fe⁶ and ¹⁵¹Eu Mössbauer spectroscopy,^{5,6} x-ray absorption spectroscopy,^{5,8} as well as x-ray diffraction, magnetic susceptibility, magnetization, and resistivity measurements.^{5,6,8,10} Changes in the valence state induced by applied pressure^{11,12} and magnetic field⁸ have also been investigated in Eu-based compounds. While the main factors governing the magnetic ordering and structures of most RMn₂M₂ compounds are well documented (e.g., Refs. 4, 9, 13), the magnetic structures of EuMn₂M₂ compounds are

less well understood; this is due mainly to the large neutron absorption of natural Eu (e.g., 4530 b at a neutron energy of 25.3 meV). In the case of EuMn₂Si_{2-x}Ge_x, Nowik *et al.*⁶ have recently reported that EuMn₂Ge₂ contains divalent Eu and that large changes in the Eu valence and the magnetism of the Mn sublattice are caused on replacing Ge with Si, while EuMn₂Si₂ reveals features consistent with a transformation from Eu³⁺ to Eu²⁺ above ~ 500 K. They report that the Mn sublattice orders antiferromagnetically for both EuMn₂Ge₂ and EuMn₂Si₂—the former as a canted antiferromagnet and the latter with spin reorientations also occurring.

Given the range of valence and magnetic effects taking place in this system, we have carried out neutron diffraction measurements on ¹⁵³EuMn₂Si₂ and ¹⁵³EuMn₂Ge₂ in order to clarify the unresolved issues concerning the magnetic and valence behavior of those compounds. We have determined the hitherto unknown magnetic structures of EuMn₂Ge₂ and EuMn₂Si₂ and analyzed the anomalous volume changes observed in EuMn₂Si₂ above ambient temperature by an extension of the interconfigurational fluctuation model in which the rare earth ions can be described as fluctuating in time between two configurations and in which the effect of cooperative phenomena in concentrated Eu compounds are taken into account.^{14,15} Good agreement is found between the occupation probability determined for the Eu²⁺ state of ¹⁵³EuMn₂Si₂ from the present analysis of volume change data and our reanalysis of earlier ¹⁵¹EuMn₂Si₂ isomer shift data.

II. EXPERIMENTAL

The neutron diffraction measurements were carried out on the time-of-flight diffractometer GEM (~ 7 – 723 K) at the ISIS spallation neutron source, UK. Additional measurements were carried out on the EuMn₂Ge₂ sample on the E6 diffractometer (~ 1.8 – 300 K; wavelength $\lambda = 2.444$ Å) at the Hahn–Meitner Institut, Germany. An important feature of these experiments was the investigation of compounds using

the low neutron absorption isotope ^{153}Eu (of natural abundance $\sim 52.2\%$) as the large absorption cross section of the ^{151}Eu isotope prohibited the use of samples prepared with natural Eu. The ^{153}Eu was purchased in the form of a ~ 0.5 g metallic sheet of purity $\sim 99.9\%$ and of enrichment 98.77% in the ^{153}Eu isotope (Oak Ridge National Laboratory) with the 99.999% Si, 99.999% Ge, and 99.99% Mn purchased from Aldrich Chemicals, RIC Corporation, and Goodfellow, respectively. While standard preparation techniques were used, in view of the high cost of the ^{153}Eu isotope, particular care was taken in the preparation of the ~ 0.5 g $^{153}\text{EuMn}_2\text{Ge}_2$ and $^{153}\text{EuMn}_2\text{Si}_2$ samples. Samples of equivalent mass were initially prepared using natural Eu to refine the preparation technique. In view of the highly pyrophoric reactivity of Eu, the starting materials were handled in an argon gas chamber. Ultimately, samples were prepared in a standard argon arc furnace with each sample remelted up to seven times. The ingot was weighed after each separate melt and the melting process completed when the target mass—corresponding to the stoichiometry of the 1-2-2 compounds—was reached. Before the initial melt, 17.5% excess ^{153}Eu and 3.5% excess Mn were added to compensate for evaporative losses during the argon arc melts.

The experiments on GEM were carried out over the temperature ranges $\sim 7\text{--}723$ K for EuMn_2Si_2 and $\sim 7\text{--}650$ K for EuMn_2Ge_2 using a standard cryofurnace. The samples were mounted in thin-walled vanadium cans of diameter 3 mm in order to further reduce the neutron absorption effects. The E6 experiments on EuMn_2Ge_2 covered the temperature range $\sim 1.8\text{--}300$ K and the sample was mounted in a thin Al cylinder (diameter 2 mm). In this form the final samples had an absorption cross section of ~ 342 b at a neutron energy of 25.3 meV compared with a cross section of ~ 4380 b for the equivalent samples prepared with natural Eu. The crystal and magnetic structures were determined from the diffraction patterns by Rietveld refinements using the computer program GSAS.¹⁶ This allowed the data from the four available detector banks of GEM¹⁷—each covering a different d -spacing range—to be refined simultaneously. X-ray diffraction patterns confirmed that both samples crystallize in the ThCr_2Si_2 -type structure, as expected. In conjunction with the neutron diffraction measurements, it is estimated that small-level impurity phases are present in both samples. For example, $\sim 2\%$ – 3% EuO is present in $^{153}\text{EuMn}_2\text{Si}_2$ with $\sim 2\%$ – 3% EuO present in $^{153}\text{EuMn}_2\text{Ge}_2$. Given the low level of these impurity phases and the need to simultaneously refine the crystal and magnetic structures, these phases were not included in the Rietveld refinements.

III. RESULTS AND DISCUSSION

As described below, $^{153}\text{EuMn}_2\text{Ge}_2$ was found to exhibit more straightforward structural and magnetic behavior compared with $^{153}\text{EuMn}_2\text{Si}_2$. We therefore consider the results and analysis of the $^{153}\text{EuMn}_2\text{Ge}_2$ sample first in the discussion.

A. $^{153}\text{EuMn}_2\text{Ge}_2$: Magnetic structure

Figure 1 shows the neutron diffraction patterns of $^{153}\text{EuMn}_2\text{Ge}_2$ from two different detector banks of GEM at 398 K along with Rietveld refinements to the data. The refinements in Figs. 1(a) and 1(b) represent the fit obtained solely on the basis of the ThCr_2Si_2 -type structure appropriate to this class of 1-2-2 compound. The misfit to the data is evident, indicating the presence of significant magnetic scattering in $^{153}\text{EuMn}_2\text{Ge}_2$ at 398 K. By comparison, the refinements in Figs. 1(c) and 1(d) represent the high quality fit ($\chi^2 \sim 2.4$) obtained based on the antiferromagnetic structure for $^{153}\text{EuMn}_2\text{Ge}_2$ described below.

As outlined previously,¹⁸ for the RMn_2X_2 series with the ThCr_2Si_2 -type structure, a ferromagnetic order of the Mn sublattice would lead to an increase in the intensity of peaks obeying the reflection conditions $h+k=2n$. However, as indicated by Fig. 1, for $^{153}\text{EuMn}_2\text{Ge}_2$, we find that the intensities of several reflections [e.g., (101), (103), (105)] are enhanced compared with the nuclear scattering expected from the 1-2-2 lattice. The occurrence of magnetic intensity in such peaks with $h+k=2n+1$ satisfies the reflection conditions for an anti- c -lattice translation mode. This leads to the result that Mn atoms at the (0, 1/2, 1/4) and (1/2, 0, 1/4) positions have magnetic moments pointing in the opposite direction to each other. Further, as discussed fully elsewhere e.g., Refs. 18, 19, the intensity ratio for the (101) and (103) peaks indicates that the moment direction is along the c axis rather than in the (110) plane. The variation of the intensity of the (101) magnetic peak with temperature is shown in Fig. 2(a) with the variations of the nuclear (200) and (110) reflections shown for comparison. The magnetic structure of EuMn_2Ge_2 , space group $I4'/m'm'm$, is depicted in Fig. 2(b).

The lattice parameters of EuMn_2Ge_2 at ambient temperature [$a=4.24972(3)$ Å; $c=10.9084(2)$ Å from the present investigation] correspond well with the values for SrMn_2Ge_2 ($a=4.30$ Å; $c=10.91$ Å).²⁰ Given the further similarity in the ionic radii of Sr^{2+} ($r=1.32$ Å) and Eu^{2+} ($r=1.31$ Å),²¹ this equivalence in structural parameters between SrMn_2Ge_2 and EuMn_2Ge_2 provides clear evidence that Eu ions are in the Eu^{2+} valence state in EuMn_2Ge_2 , in agreement with earlier findings (e.g., Ref. 6). The arrangement of magnetic moments on the Mn sublattice shown in Fig. 2(b) is similar to the magnetic structure found in the earth alkaline intermetallic compounds CaMn_2Ge_2 and BaMn_2Ge_2 .¹⁹ In light of the common 2+ valence state for the CaMn_2Ge_2 , BaMn_2Ge_2 , and EuMn_2Ge_2 compounds and given the small magnetization for EuMn_2Ge_2 ,²² Malaman *et al.*¹⁹ noted the possibility of antiferromagnetic (001) Mn layers in EuMn_2Ge_2 , as established in the present experiments.

The Néel temperature of EuMn_2Ge_2 is above the highest temperature, 623 K, accessible to us within the limited time available for our experiments. Nonetheless, as shown in Fig. 2(b), by fitting the refined magnetic moment values to the expression $\mu(T)=\mu(0)[1-(T/T_N)^d]^e$,²³ a value of $T_N=667(9)$ K is obtained with $\mu(0)=3.43(4)$ μ_B and fit parameters $d=2.7(3)$ and $e=0.36(3)$. This expression was chosen as a convenient empirical function to represent the

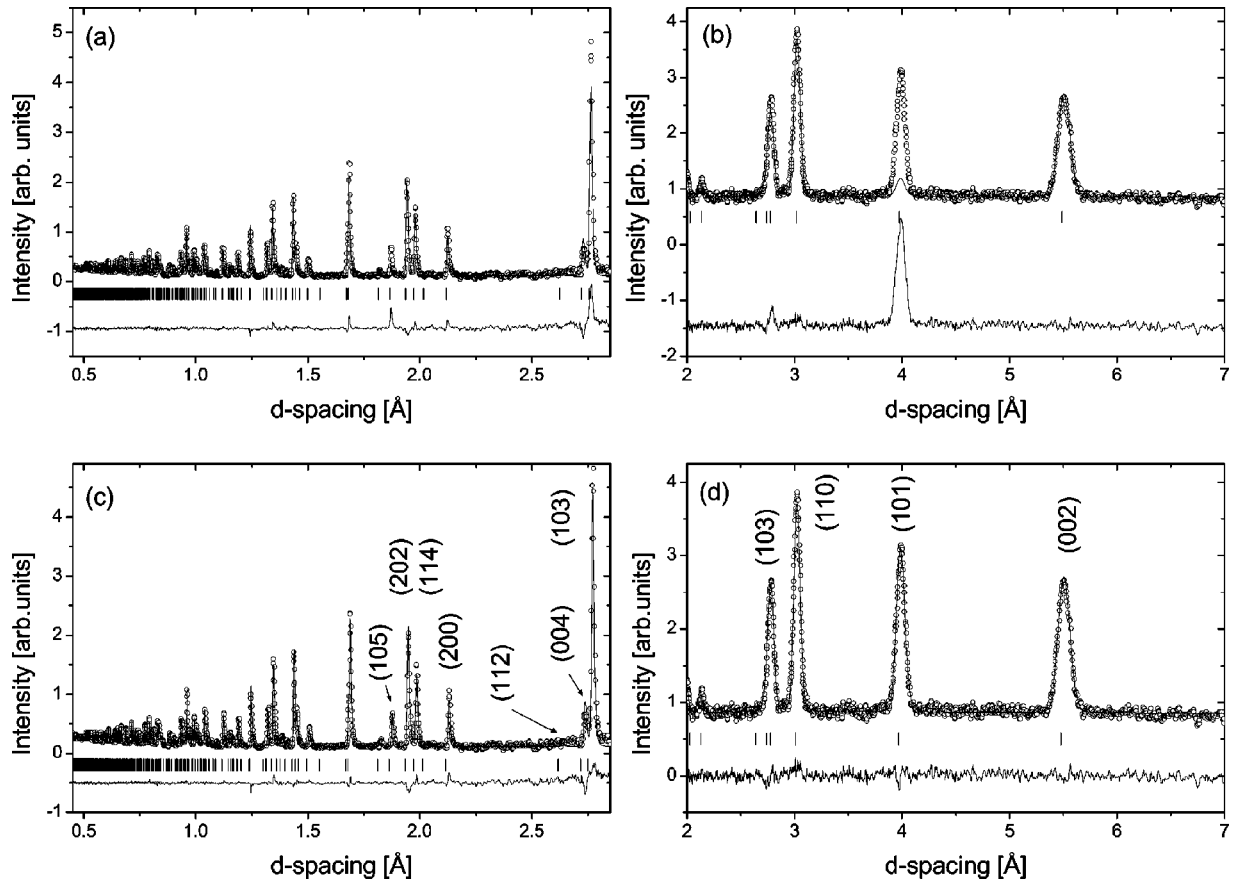


FIG. 1. Rietveld refinements to the time of flight neutron powder diffraction patterns of $^{153}\text{EuMn}_2\text{Ge}_2$ at 398 K. Diffraction patterns are shown for the 17° bank (a) and the 90° bank (b) of the diffractometer GEM, ISIS with the patterns repeated in Figs. 1(c) and 1(d). The refinement in (a) and (b) represents the fit to the ThCr_2Si_2 -type structure and is intended to draw out the magnetic scattering in $^{153}\text{EuMn}_2\text{Ge}_2$ at this temperature. The refinements in (c) and (d) represent the refinement to the axial antiferromagnetic structure for $^{153}\text{EuMn}_2\text{Ge}_2$ [Fig. 2(b)], as described in the text.

trends of the data. The refined magnetic moment on the Mn atoms was determined to be $\mu_{\text{Mn}} = 3.41(7) \mu_B$ at 1.8 K. This relatively high value for the Mn moment in EuMn_2Ge_2 compared with that typically found in such ThCr_2Si_2 -type compounds, is consistent with the values of $2.67(5) \mu_B$ and $3.66(3) \mu_B$ found for CaMn_2Ge_2 and BaMn_2Ge_2 , respectively, at 2 K.¹⁹ This behavior can be correlated with the Mn–Ge distances and the nature of this bond.²⁴

The present findings disagree with earlier magnetization and Mössbauer effect measurements that claim antiferromagnetic order for the Mn sublattice below a first-order transition temperature $T_N \sim 302$ K.⁶ As indicated above, the present results demonstrate clearly the occurrence of antiferromagnetic scattering at 398 K (Fig. 1), which persists to the continuous magnetic transition at $T_N = 667(9)$ K (Fig. 2). The possibility of observing magnetic ordering of the Eu^{2+} ions in the present neutron experiments was also of strong interest. Based on their magnetization measurements, Nowik *et al.*^{6,22} reported ferromagnetic ordering of the Eu^{2+} ions below a transition temperature of $T_C \sim 13$ K. By comparison, in the present set of eight neutron diffraction measurements from 30 to 1.8 K, no evidence, either by way of enhancement in the scattering at nuclear peak positions [see Fig. 2(b)] or by the occurrence of additional magnetic peaks, was obtained

for magnetic ordering of Eu in EuMn_2Ge_2 down to $T = 1.8$ K. The small fraction ($\sim 2\% - 3\%$) of EuO (ferromagnetic with $T_c \sim 76$ K²⁵) detected from the neutron diffraction patterns of our $^{153}\text{EuMn}_2\text{Ge}_2$ sample did not influence the crystallographic or magnetic structural refinements of the 1-2-2 phase. On the other hand, small fractions of strongly magnetic impurity phases can contribute disproportionately to the magnetization measurements of weakly magnetic systems. In summary, it is concluded that EuMn_2Ge_2 exhibits collinear antiferromagnetism below a Néel temperature of $T_N = 667(9)$ K rather than canted antiferromagnetism with a first-order transition at $T_N = 302$ K, as proposed previously.⁶

B. $^{153}\text{EuMn}_2\text{Si}_2$: Magnetic structure

Figure 3 shows the neutron diffraction patterns of $^{153}\text{EuMn}_2\text{Si}_2$ at 673 and 7 K. Several additional magnetic contributions to reflections of interplanar spacing values down to $d \sim 1$ Å can be indexed on the basis of a tetragonal cell of lattice constants $a = 3.96442(3)$ Å and $c = 10.5039(2)$ Å with the main magnetic reflections, (111), (113), and (201), marked in the low-temperature pattern of Fig. 3. These magnetic reflections indicate that $^{153}\text{EuMn}_2\text{Si}_2$ orders in a collinear antiferromagnetic arrangement of ferro-

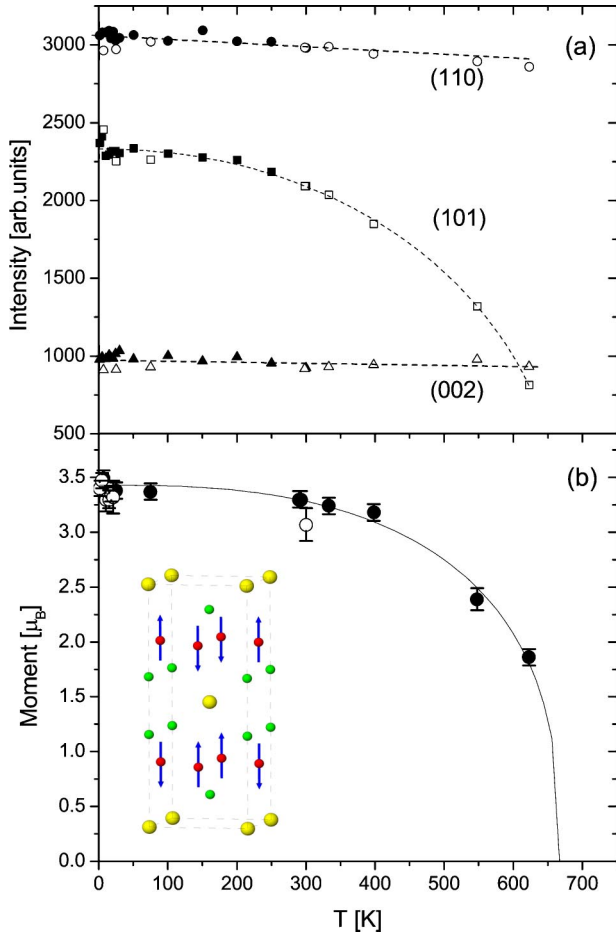


FIG. 2. (a) Graph of the intensity of the (101) superlattice reflection associated with the antiferromagnetic ordering of the Mn sublattice as a function of temperature. Graphs of the variations of the intensities of the nuclear (200) and (110) reflections with temperature are shown for comparison. (b) The variation of the Mn magnetic moment value of EuMn_2Ge_2 with temperature. As discussed in the text, the data were fitted to the expression $\mu(T) = \mu(0)[1 - (T/T_N)^d]^e$ leading to $T_N = 667(9)$ K and $\mu(0) = 3.43(4)\mu_B$. The full line represents the fit to the data with extrapolation to T_N . The open circles represent the E6 data and the filled circles the GEM data. The axial antiferromagnetic structure of EuMn_2Ge_2 below $T_N = 667$ K is also depicted (space group $I4'/m'm'm$).

magnetic (001) Mn layers coupled antiferromagnetically along the c axis with the Mn moments directed parallel and antiparallel to the c axis, as shown in Fig. 4. The magnetic space group of $^{153}\text{EuMn}_2\text{Si}_2$ is $I_p4/m'm'm'$ and refinement of the pattern at $T \sim 7$ K leads to a moment value of $\mu_{\text{Mn}} = 1.97(2)\mu_B$. As indicated in Fig. 3, the quality of the fit is good with a χ^2 value of ~ 2.0 . Figure 4 also shows the variation of the Mn magnetic moment values of EuMn_2Si_2 (closed symbols) with temperature. An analysis of the moment data to the expression $\mu(T) = \mu(0)[1 - (T/T_N)^d]^e$ leads to a Néel temperature $T_N = 391(5)$ K for $^{153}\text{EuMn}_2\text{Si}_2$. This value is in good agreement with the Néel temperature $T_N = 395$ K, determined by Nowik *et al.*⁶ from their magnetization and Mössbauer effect studies of EuMn_2Si_2 . The

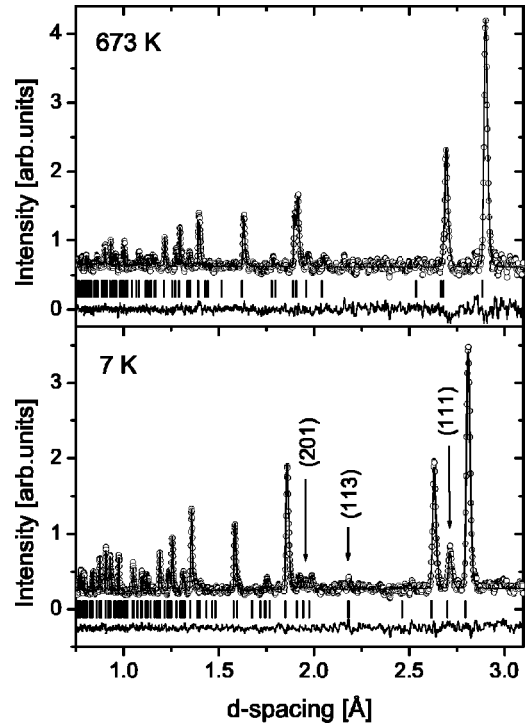


FIG. 3. Rietveld refinements to the time of flight neutron powder diffraction patterns of $^{153}\text{EuMn}_2\text{Si}_2$ at 673 and 7 K, above and below $T_N = 391(5)$ K, respectively. The (hkl) values of the most prominent magnetic reflections are marked in the 7 K pattern, as discussed in the text.

present results also show good agreement with the magnetic hyperfine field values determined from their ^{57}Fe Mössbauer studies of EuMn_2Si_2 doped with ^{57}Fe . The hyperfine field values were normalized to the moment on the Mn atoms at the common measuring temperature of 150 K [$B_{\text{hf}} \sim 12$ T, $\mu_{\text{Mn}}(150) = 1.90(2)\mu_B$], corresponding to a conversion factor of $6.3 \text{ T } \mu_B^{-1}$. On the other hand, no evidence was found in the present experiments for reorientation transitions in EuMn_2Si_2 at 107, 65, and 32 K, as reported previously.⁶ Based on their magnetization measurements, Nowik *et al.*⁶ reported a canting angle with respect to the c axis of only 6° at 5 K; should such canting occur, it would correspond to an additional Mn component in the (110) plane of around $\sim 0.2\mu_B$, below the detection limit of our neutron diffraction experiments. In summary, EuMn_2Si_2 exhibits the collinear antiferromagnetic shown in Fig. 4 below $T_N = 391(5)$ K, with no evidence for reorientation effects on the Mn sublattice, as proposed previously.⁶

It should be noted that the magnetic structures exhibited by EuMn_2Ge_2 and EuMn_2Si_2 are consistent with the in-plane magnetic coupling expected from their intralayer separation distances, $d_{\text{Mn-Mn}}$. As summarized by Venturini *et al.*,²⁶ RMn_2Ge_2 and RMn_2Si_2 compounds with $d_{\text{Mn-Mn}} < \sim 2.86$ Å have ferromagnetically coupled Mn planes, whereas with $d_{\text{Mn-Mn}} > \sim 2.86$ Å, antiferromagnetic or mixed Mn planes are obtained. EuMn_2Ge_2 with $d_{\text{Mn-Mn}} \sim 3.0$ Å at room temperature exhibits the expected antiferromagnetic coupling within the Mn planes [Fig. 2(b)], whereas

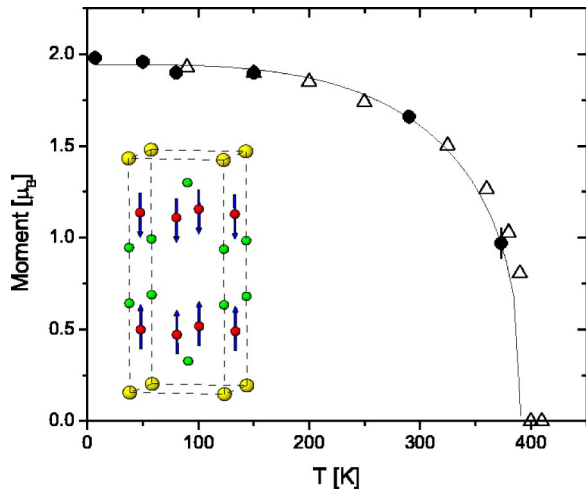


FIG. 4. The variation of the Mn magnetic moment values of EuMn₂Si₂ (closed symbols) with temperature. The full line represents the fit to $\mu(T) = \mu(0)[1 - (T/T_N)^d]^e$ leading to $T_N = 391(5)$ K and $\mu(0) = 1.95(2) \mu_B$. As discussed in the text the open symbols represent the ⁵⁷Fe magnetic hyperfine field values of EuMn₂Si₂ (Ref. 6) normalized to the value of the Mn moment at 150 K, $\mu_{Mn}(150) = 1.90(2) \mu_B$. The antiferromagnetic structure of EuMn₂Si₂ below $T_N = 391$ K with ferromagnetic (001) Mn layers coupled antiferromagnetically along the *c* axis (space group $I_{P4}/m'm'm'$) is also depicted.

EuMn₂Si₂ with $d_{Mn-Mn} \sim 2.81$ Å at room temperature exhibits ferromagnetic coupling within the Mn planes, as expected (Fig. 4).

C. Valence transition

As explained elsewhere, both the ¹⁵¹Eu and the ¹⁵³Eu isotopes are suitable for isomer shifts measurements.¹ Consequently, intermediate valence effects in several Eu systems have been investigated by ¹⁵¹Eu Mössbauer studies. In the case of EuMn₂Si₂, as shown in Fig. 5(a), the ¹⁵¹Eu isomer shift measurements reveal a valence transition from trivalent Eu for $T < \sim 90$ K to an intermediate valence state for Eu at high temperatures, $T > \sim 600$ K.⁶ As discussed below, the valence transition in this EuMn₂Si₂ sample is centered around $T_v \sim 496$ K.

Clear evidence for a thermally driven change in the valence state of EuMn₂Si₂ is also revealed by the refinements to the present neutron diffraction patterns of ¹⁵³EuMn₂Si₂. It has been pointed out that in the ThCr₂Si₂-type structure, the *a* lattice parameter is largely determined by the size of the rare earth ion, while the *c* lattice parameter depends upon the transition metal–silicon distances. However, in Eu-based compounds with the ThCr₂Si₂-type structure, it is not uncommon that both lattice parameters are determined by the Eu valence [e.g., in the EuNi₂(Si_{1-x}Ge_x)₂ series²⁷]. In the current ¹⁵³EuMn₂Si₂ studies, the *a* and *c* lattice parameters are found to show similar changes with temperature [Fig. 5(a)], with the unit cell volume of ¹⁵³EuMn₂Si₂ increasing by $\sim 7\%$ from 300 to 723 K [Fig. 5(b)]. We have applied the interconfigurational fluctuation (ICF) model^{14,15} to the analysis of the volume changes resulting from the

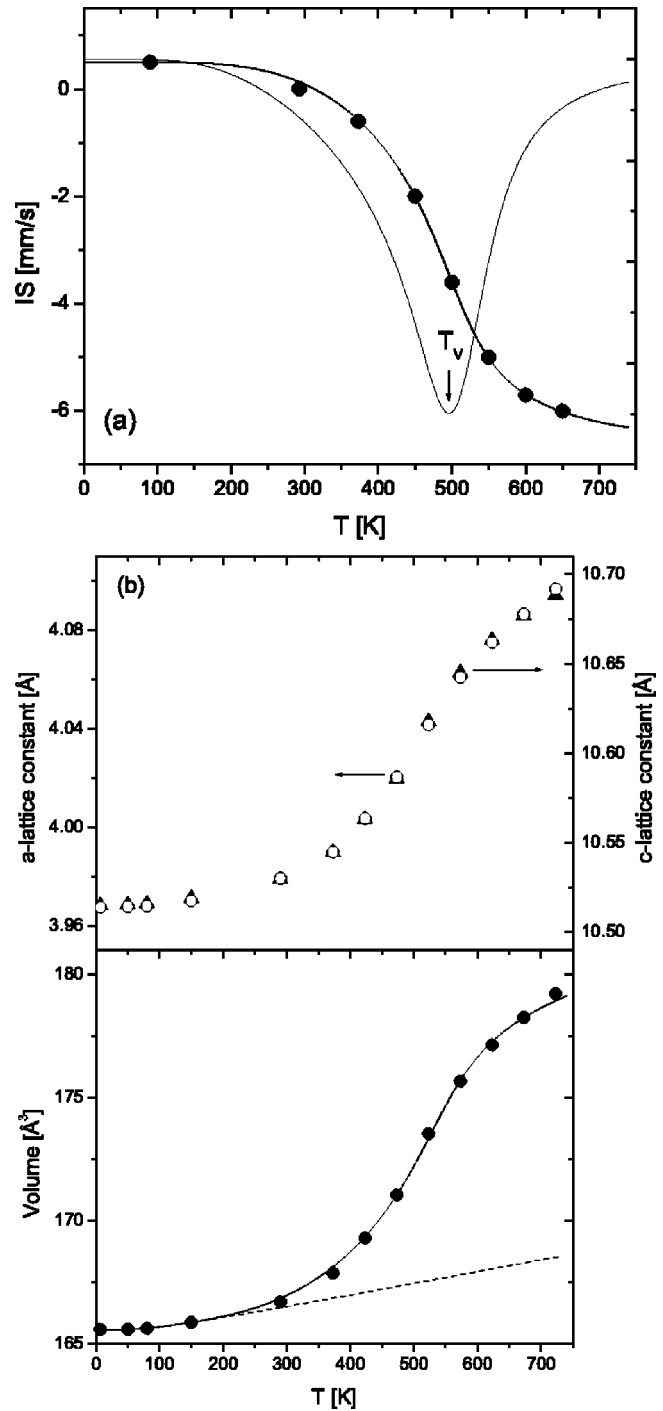


FIG. 5. (a) The ¹⁵¹Eu isomer shift of EuMn₂Si₂ (closed symbols, Ref. 6) with the full line representing our fit to the data using the ICF model (Ref. 15). Also shown is the derivative of the ICF fit to the isomer shift data, leading to a valence transition temperature of $T_v \sim 496$ K. (b) The *a* lattice parameter (O; left scale) and the *c* lattice parameter (▲; right scale) of ¹⁵³EuMn₂Si₂ along with the unit cell volume (●) as a function of temperature. The dashed line shows the lattice expansion derived from a fit to the low-temperature data ($T < 150$ K) based on the Einstein model as described in the text.

temperature-induced valence transition in a concentrated Eu compound for the first time. This extension of the ICF model to include the effects of cooperative phenomena has also been used successfully to account for the temperature-induced valence transition in EuPd_2Si_2 , as monitored by ^{151}Eu isomer shift measurements,¹⁵ and the temperature and field-induced valence transitions in $\text{Eu}(\text{Pd}_{1-x}\text{Pt}_x)_2\text{Si}_2$ ⁷ and $\text{EuNi}_2(\text{Si}_{1-x}\text{Ge}_x)_2$ as monitored by magnetic susceptibility and high field magnetization measurements.⁸

In the ICF model, the rare earth ions are described as fluctuating in time between two configurations, with each configuration being characterized by a different integral occupation of the 4*f* shell. Assuming a Eu^{3+} ground state, the ratio of the occupation probabilities of the Eu^{2+} and Eu^{3+} states, represented by p_2 and p_3 , respectively, is given by

$$\frac{p_2}{p_3} = \frac{8 \exp[-E_{\text{ex}}/kT^*]}{1 + 3 \exp[-480/T^*] + 5 \exp[-1330/T^*] + \dots}, \quad (1)$$

where $p_2 + p_3 = 1$, 480 and 1330 K are the energies of the first ($J=1$) and second ($J=2$) excited spin-orbit states of the Eu^{3+} configuration and E_{ex} is the excitation energy required to convert an Eu^{3+} configuration into an Eu^{2+} configuration. $T^* = \sqrt{T^2 + T_f^2}$ takes account of the energy level broadening (of magnitude T_f) due to hybridization.¹⁵ The relatively sharp transitions exhibited by both the isomer shift and the volume data indicate that cooperative interactions take place among the Eu charge fluctuations in this concentrated Eu compound. The data were therefore analyzed, assuming that the excitation energy, E_{ex} , depends on the probability for the valence state p_2 as $E_{\text{ex}} = E_0(1 - \alpha p_2)$, where E_0 represents the average excitation energy at $T=0$ K for all atoms and α is the average interaction parameter.¹⁵ An important aspect of our analysis is a separation of the normal lattice expansion from the measured unit cell volume in order to isolate the valence-induced changes. The dashed line in Fig. 5(b) represents the lattice expansion fit for data up to $T \sim 150$ K using an Einstein expression of the form $V(T) = V_0 + K_E/(\exp(T_E/T) - 1)$, where T is the temperature, K_E is the Einstein constant, and T_E is an effective Einstein temperature.²⁸ The Einstein model was chosen as a convenient method of describing accurately the volume expansion data and leads to the fit parameters: $V(0) = 165.578(6) \text{ \AA}^3$; $T_E = 249(35) \text{ K}$ and $K_E = 1.2(3) \text{ \AA}^3$. The net volume change, $\Delta V_{\text{val}}(T)$, due to the thermally driven valence change can be expressed in terms of $\Delta V = (V^{2+} - V^{3+})$, the difference in volume between the Eu^{2+} and Eu^{3+} configurations, as $\Delta V_{\text{val}}(T) = p_2 \Delta V$, where p_2 is defined in Eq. (1). The optimal fit to the valence-induced volume changes [Fig. 6(a)] leads to $E_0 = 1656(2) \text{ K}$, $T_f = 56(2) \text{ K}$, and $\alpha = 1.09(1)$ with a fitted value for the difference in volume between the Eu^{2+} and Eu^{3+} configurations of $\Delta V = 18.18(5) \text{ \AA}^3$. The derivative of the ICF fit to the volume data shown in Fig. 6(a) leads to a valence transition temperature of $T_v \sim 527 \text{ K}$ for the present $^{153}\text{EuMn}_2\text{Si}_2$ sample with a full width at half-maximum for the derivative curve of $\Delta T \sim 150 \text{ K}$. The asymmetry in this latter curve demonstrates that the valence transition proceeds more rapidly with in-

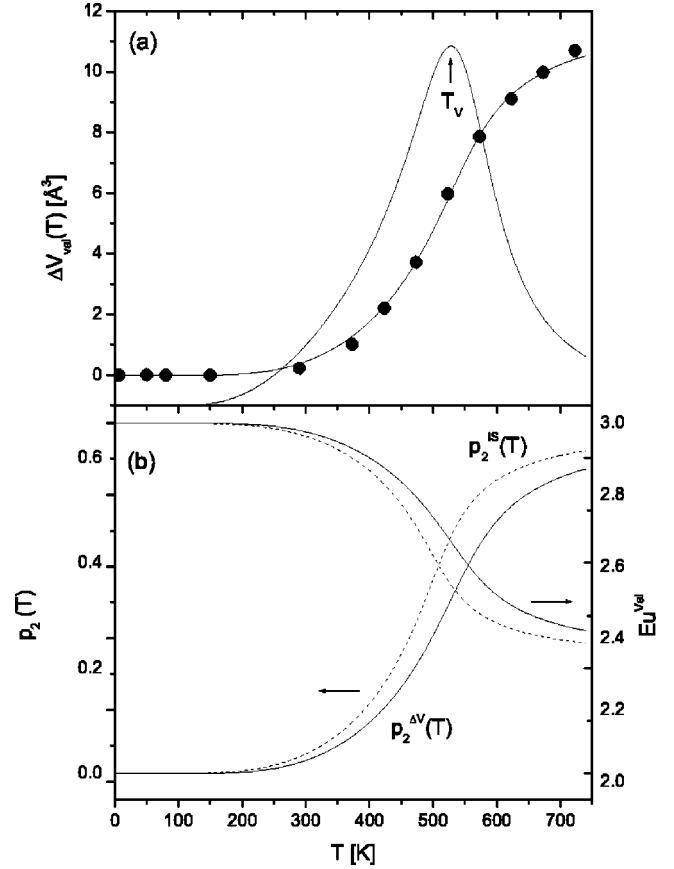


FIG. 6. (a) The valence-induced volume changes in $^{153}\text{EuMn}_2\text{Si}_2$ as a function of temperature, with the full line representing our fit to the data using the ICF model,¹⁵ as described in the text. The derivative of the ICF fit to the volume data due is also shown, leading to a valence transition temperature of $T_v \sim 527 \text{ K}$. (b) The variation of $p_2^{\Delta V}(T)$, the occupation probability of the Eu^{2+} state resulting from the volume changes (full line; left scale) along with the average valence values, Eu^{val} (full line; right scale) for the thermally driven valence transition in $^{153}\text{EuMn}_2\text{Si}_2$. The equivalent $p_2^{\text{IS}}(T)$ and Eu^{val} values (dashed lines) derived from the fit to the Mössbauer isomer shift data of Fig. 5(a) are also shown.

creasing temperature, as expected. The variation of $p_2^{\Delta V}(T)$, the occupation probability of the Eu^{2+} state resulting from these volume changes with temperature, along with the average valence values, Eu^{val} , for the thermally driven valence transition in $^{153}\text{EuMn}_2\text{Si}_2$, are shown as full lines in Fig. 6(b).

The full line through the data in Fig. 5(a) shows our analysis of the ^{151}Eu isomer shift data (the isomer shift values of $\text{Eu}^{3+} = 0.5 \text{ mm/s}$ and $\text{Eu}^{2+} = -10.1 \text{ mm/s}$ were taken from the data of $^{151}\text{EuMn}_2\text{Si}_2$ and $^{151}\text{EuMn}_2\text{Ge}_2$, respectively⁶). This leads to the fit parameters of $E_0 = 1600(10) \text{ K}$; $T_f = 104(2) \text{ K}$; $\alpha = 1.12(2)$ (by comparison, Nowik *et al.*⁶ derived the values $E_0 = 1610 \text{ K}$ and $\alpha = 1.35$, T_f value not given, in their analysis of the isomer shift data). The derivative of the present ICF fit to the isomer shift data [Fig. 5(a)] leads to $T_v \sim 496 \text{ K}$, similar to the value $T_v \sim 527 \text{ K}$ determined for the present $^{153}\text{EuMn}_2\text{Si}_2$ sample. As is evident from Fig. 6(b), the $p_2(T)$ and average Eu^{val} values

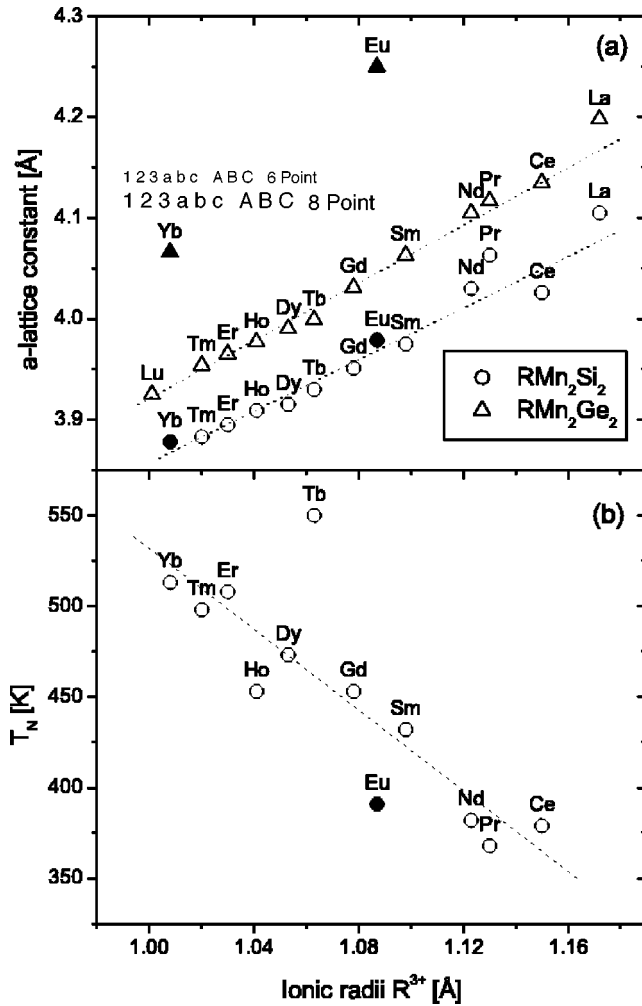


FIG. 7. (a) Values of the a lattice parameters of the RMn_2Si_2 and RMn_2Ge_2 series at room temperature as a function of the R^{3+} ionic radii.²¹ The lattice parameters values for the Eu compounds are derived from the current measurements, the Yb data from,²⁸ with the other data taken from.⁴ (b) The Néel temperatures of RMn_2Si_2 intermetallic compounds derived from the literature, e.g., Refs. 14, 19, as a function of the R^{3+} ionic radii. The dashed line shows the trend of the average Néel temperatures for the RMn_2Si_2 series, as discussed in the text.

determined from changes in the volume (full lines) and isomer shift (dashed lines) show good agreement for the thermally driven valence transition in EuMn_2Si_2 .

Figure 7(a) shows a comparison of the a lattice parameters for EuMn_2Si_2 and EuMn_2Ge_2 at room temperature with the a parameters for other compounds in the RMn_2Si_2 and RMn_2Ge_2 series as a function of the R^{3+} ionic radii given in Ref. 21. These results allow the predominant difference in the Eu valence states of EuMn_2Si_2 and EuMn_2Ge_2 to be distinguished. In particular, the trends of the RMn_2Si_2 data demonstrate that EuMn_2Si_2 is consistent with a predominantly trivalent-like behavior of the Eu ion at room temperature, whereas the significant deviation for EuMn_2Ge_2 from the trend of the lattice parameter data for RMn_2Ge_2 reflects a nontrivalent Eu state. As noted above, given that the dimensions of the basal plane in this tetragonal ThCr_2Si_2 -type

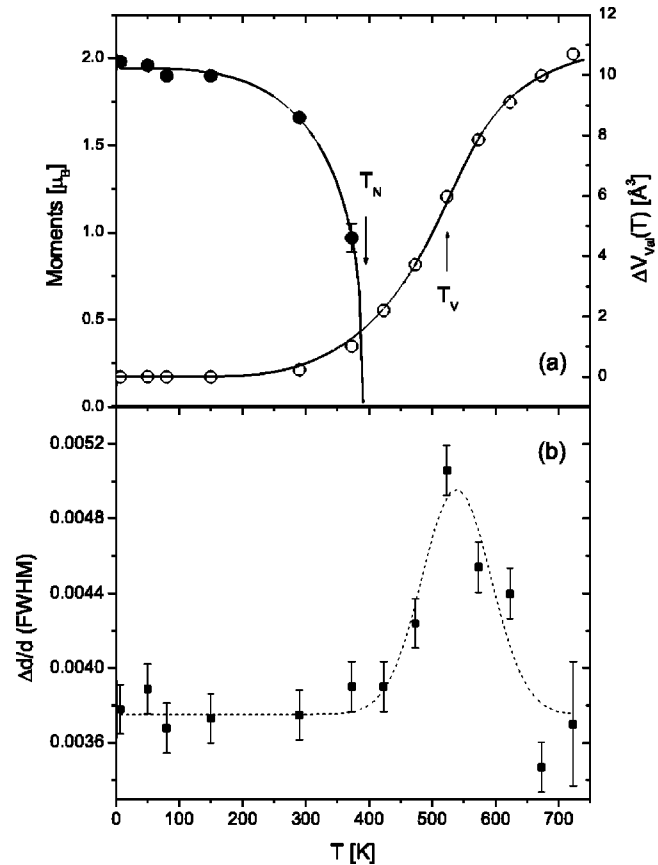


FIG. 8. (a) Graphs of the Mn magnetic moment (cf. Fig. 4) and the valence-induced volume change [Fig. 6(a)] of EuMn_2Si_2 as a function of temperature. (b) The variation of the linewidth of the (110) reflection (expressed in terms of the interplanar spacing d) of EuMn_2Si_2 as a function of temperature. The dashed line shows a Gaussian fit to the data to act as a guide for the eye.

structure are determined predominantly by the radii of the rare earth atoms, this deviation in the a lattice parameter provides strong evidence for a change in the valence state of Eu from the predominant trivalent-like behavior of EuMn_2Si_2 at room temperature to a mixed valence or even divalent state in EuMn_2Ge_2 . In a similar manner, the relatively large cell parameters of YbMn_2Ge_2 [Fig. 7(a)] indicates a larger Yb radius than that expected of a trivalent Yb ion, with an analysis leading to a Yb valence state of about 2.35 in YbMn_2Ge_2 at room temperature.²⁹

As is evident in Fig. 7(b), EuMn_2Si_2 exhibits a relatively low value for its antiferromagnetic ordering temperature, $T_N = 391$ K, compared with the Néel temperatures exhibited by the trend of neighboring RMn_2Si_2 compounds. Further support for this indication that the magnetic transition in EuMn_2Si_2 is inhibited by the valence change is provided by Fig. 8(a), which shows the temperature evolution of both the Mn magnetic moment (data reproduced from Fig. 4) and the valence-induced volume change [Fig. 6(a)]. Given the excess volume associated with the valence transition and the reduced valence state of EuMn_2Si_2 at high temperatures, as discussed above [Fig. 5(b)], this excess volume is caused by the changing electronic configuration [cf. e.g., Fig. 6(b)],

which, in turn, inhibits the magnetic ordering of the Mn sublattice. The Néel temperature of EuMn_2Si_2 appears to have been reduced by $\sim 10\%$ – 15% compared to the value of ~ 450 K derived from the extrapolation of T_N for the neighboring rare earth intermetallics. This correspondingly indicates that the exchange interaction parameter in EuMn_2Si_2 is reduced by $\sim 10\%$ – 15% as a result of the valence change. The correlation between the loss of antiferromagnetic order and the onset of the volume changes around T_N —as is evident in Fig. 8(a)—indicates that the magnetic transition is probably initiated by changes in the conduction band structure caused by the drastic changes in the Eu valence. Further evidence of the structural changes occurring in EuMn_2Si_2 as a result of the thermally driven valence transition is provided by Fig. 8(b), which shows the variation of the linewidth of the (110) reflection as a function of temperature. Here the peak in linewidth occurs around $T_v \sim 527$ K, reflecting the significant lattice strains present in EuMn_2Si_2 as the valence transition occurs.

IV. CONCLUSIONS

The magnetic structures of EuMn_2Ge_2 and EuMn_2Si_2 have been determined by neutron diffraction measurements (~ 1.8 – 723 K) on samples prepared with the low neutron absorption isotope ^{153}Eu . The Mn sublattice of EuMn_2Ge_2 has magnetic moments pointing in opposite directions along the c axis below a Néel temperature of $T_N = 667(9)$ K [Fig. 2(b); space group $I4'/m'm'm'$]. EuMn_2Si_2 also displays collinear antiferromagnetism below its ordering temperature of $T_N = 391(5)$ K with ferromagnetically coupled (001) Mn layers coupled antiferromagnetically along the c axis and the

Mn moments directed parallel and antiparallel to the c axis (Fig. 4; space group $I_p4/m'm'm'$). Contrary to the findings of magnetization measurements,⁶ there is no evidence for ordering of the Eu^{+2} ions in EuMn_2Ge_2 down to 1.5 K.

The valence-driven volume changes in EuMn_2Si_2 [Fig. 6(a)] have been analyzed for the first time in terms of the interconfigurational fluctuation model, extended in order to take the effect of cooperative phenomena into account.^{14,15} This leads to a valence transition temperature of $T_v \sim 527$ K and occupation probabilities, $p_2^{AV}(T)$, for the Eu^{2+} state, in good agreement with the $p_2^{IS}(T)$ curve determined from our reanalysis of earlier $^{151}\text{EuMn}_2\text{Si}_2$ isomer shift data [Fig. 6(b)]. The average Eu^{val} values determined from the volume and isomer shift changes are also in good agreement [Fig. 6(b)], thus demonstrating the applicability of the interconfigurational fluctuation model in enabling valence changes induced by volume changes in Eu and related compounds to be determined. The change in the electronic configuration of EuMn_2Si_2 resulting from the thermally induced valence transition reduces the magnetic interaction parameter for antiferromagnetic ordering of the Mn sublattice by $\sim 10\%$ – 15% .

ACKNOWLEDGMENTS

SJC acknowledges renewal of his Alexander von Humboldt Research Fellowship during his stay at the Technische Universität München. SJC also acknowledges support from Access to the Major Research Facilities Program, Australian Nuclear Science and Technology Organization. This project is supported in part by the award of a Discovery Grant from the Australian Research Council. We thank BENSCH, Hahn-Meitner-Institut, Berlin for access to the E6 diffractometer.

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