## **Far-infrared photoconductivity of electrons in an array of nanostructured antidots**

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We present far-infrared (FIR) photoconductivity measurements for a two-dimensional electron gas in an array of nanostructured antidots. We detect, and resistively and spectrally resolve, both the magnetoplasmon and the edge-magnetoplasmon modes. Temperature-dependent measurements demonstrate that both modes contribute to the photoresistance by heating the electron gas via resonant absorption of the far-infrared radiation. Influences of the spin effect and phonon bands on the collective excitations in the antidot lattice are observed.

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There has recently been a growing interest in investigating the photoresistance related to the elementary excitations of a two-dimensional electron gas (2DEG) in semiconductor heterostructures. $1-6$  For example, under GHz radiation, the magnetoresistance of a 2DEG shows an unexpected large oscillation whose period is determined by the electron cyclotron resonance  $(CR)$ .<sup>1</sup> Using THz radiation, a plasmon of tunneling coupled bilayer 2DEGs is found to contribute to the photoresistance in a unique way.<sup>4</sup> Even the spin effects result in striking photoresistance changes.<sup>2,3</sup> Among others, the spin-orbit interaction, which was discovered about 80 years ago by atomic spectroscopy and gave birth to the very concept of *spin*, has been found rather difficult to be spectrally measured for the 2DEGs. The problem was recently solved by measuring the spin-flip excitation using photoconductivity spectroscopy.<sup>2</sup> Of particular interest is the high sensitivity of the photoconductivity technique, which has the potential to study unique elementary electronic excitations of nanostructured semiconductors with only a few units. As a first step, very recently Jager *et al.*<sup>5</sup> and Ye *et al.*<sup>6</sup> both studied the photoconductivity of a 2DEG in an antidot array. While these experiments, together with the pioneering one of Vasiliadou et al.,<sup>7</sup> have shed light on the interesting photoconductivity effect of a 2DEG in an antidot array, primary questions such as the role of the characteristic excitations of the antidot array on its photoresistance are surprisingly left open, which is the central subject of this work.

The elementary electronic excitations of a 2DEG in an antidot array subjected to a perpendicular magnetic field *B* are dominated by a characteristic two-mode behavior with collective excitations.<sup>8,9</sup> The upper mode  $\omega^+$  at large *B* field approaches the CR frequency  $\omega_c = eB/m^*$ , which is determined by the electron effective mass *m*\*. The lower one  $\omega_{FMP}$ , known as the edge-magnetoplasmon (EMP) mode, is associated with the electrons skipping around the depleted area with a radius *R* formed by the antidot potential. Using the modified-dipole and effective-medium approximations, the dispersion of these modes can be described by<sup>8</sup>

$$
1 - \frac{(1-f)\omega_0^2}{\omega(\omega + \omega_c)} - \frac{f\omega_0^2}{\omega(\omega - \omega_c)} = 0.
$$
 (1)

Here  $\omega_0$  is the frequency of the  $\omega^+$  mode at  $B=0$ , depending on the antidot lattice period *a*, the 2DEG's carrier density  $N<sub>s</sub>$ , and its dielectric surrounding. The geometrical filling factor  $f = \pi R^2/a^2$  indicates the portion of the 2D area where the electrons are depleted. These modes have been well studied by far-infrared  $(FIR)$  transmission spectroscopy,<sup>9</sup> but have not been clearly identified in photoconductivity experiments,<sup>5–7</sup> leaving the question open of whether and how they might influence the photo resistance of the 2DEG in an antidot array.

In this paper, we report FIR photoconductivity experimental results obtained for a 2DEG in an antidot array. We find clearly that both  $\omega^+$  and  $\omega_{EMP}$  modes contribute to the photoresistance by heating the electron gas via resonant absorption of the FIR radiation. In addition, we present interesting results indicating the influences of spin and electron-phonon interaction in the antidot lattice.

Our sample is an inverted-doped InAs step quantum well with a 40-nm  $In<sub>0.75</sub>Al<sub>0.25</sub>As cap layer. The step quantum well$ is composed of 13.5-nm  $In<sub>0.75</sub>Ga<sub>0.25</sub>As$ , an inserted 4-nm InAs channel, and a 2.5-nm-thick  $In_{0.75}Ga_{0.25}As$  layer. Underneath the quantum well is a 5-nm spacer layer of In<sub>0.75</sub>Al<sub>0.25</sub>As on top of a 7-nm-wide Si-doped In<sub>0.75</sub>Al<sub>0.25</sub>As layer. The sample is grown by molecular beam epitaxy on a buffering multilayer accommodating the lattice mismatch to the semi-insulating GaAs substrate. Figure  $1(a)$  shows the band structure calculated by solving the Schrödinger and Poisson equations self-consistently. The 2DEG is formed about 55 nm below the surface, mainly confined in the narrow InAs channel.<sup>10</sup> Figure 1(b) shows a sketch of our sample with antidots. An extreme long 2DEG Hall bar with a channel width of  $W=40 \mu m$  and a total length *L* of about 10 cm was defined by chemical wet etching, which contains the antidot array with a period of  $a = 800$  nm. The holes with a geometric diameter of about 200 nm were defined by holography and chemical wet etching. The 2DEG channel runs meandering in a square of  $4\times4$  mm<sup>2</sup>. The extremely large *L*/*W* ratio enhances the sensitivity of our measurement. With the antidots, the carrier density  $N_s$  and mobility  $\mu$  at 1.5 K were determined by Shubnikov–de Haas measurement to be  $6.01\times10^{11}$  cm<sup>-2</sup> and 62 000 cm<sup>2</sup>/Vs, respectively, reduced compared with those of the corresponding unpatterned



FIG. 1. (Color online) (a) Band structure calculated by solving the Schrödinger and Poisson equations self-consistently. The 2DEG is formed about 55 nm below the surface, mainly confined in the narrow InAs channel. (b) Schematic bias circuit and sample structure showing the long Hall bar with ohmic contacts. The zoom-in part is an atomic force micrograph of the antidot array.

sample<sup>2</sup> of  $6.66 \times 10^{11}$  cm<sup>-2</sup> and 150 000 cm<sup>2</sup>/V s. Ohmic contacts were made by depositing a AuGe alloy followed by annealing.

Our experiment was performed by applying a dc current of 9  $\mu$ A to the Hall bar and measuring the changes of the voltage drop caused by FIR radiation. At fixed magnetic fields, the broadband FIR radiation was modulated by the Michelson interferometer of a Fourier transform spectrometer. Using the sample itself as the detector, the corresponding change in the voltage drop of the sample was ac coupled to a broadband preamplifier and recorded as an interferogram, which was Fourier transformed to obtain the photoconductivity spectrum. The sample was mounted in a He cryostat with a superconducting solenoid. All data reported here were obtained in Faraday geometry.

Figure 2 shows typical FIR photoconductivity spectra measured at different *B* fields and temperatures. Different beam splitters of the spectrometer are used to optimize the measurement for resonances lying in different frequency regimes. As shown in Fig.  $2(a)$  at the low magnetic field of  $B=3.2$  T, two resonances are clearly observed. By increasing the *B* field to 6.4 T, the resonance at the lower energy has a slight redshift and gets weaker, while the higher-energy resonance shows a significant blueshift and dominates the spectrum. Two additional weak resonances are observed; one appears as a shoulder of the dominant resonance and the other lies at about  $285 \text{ cm}^{-1}$ , and these are indicated by thick and thin arrows, respectively. By further increasing the *B* field to 9.6 T, the dominant resonance splits into multipeaks, while the weak one at  $285 \text{ cm}^{-1}$  gains resonance strength. The resonance at the low energy disappears at large



FIG. 2. (Color online) FIR photoconductivity spectra measured at (a)  $T=1.5$  K for three different magnetic fields and (b) *B*  $=$  3.2 T for three different temperatures. Arrows indicate weak resonances described in the text. Spectra in (a) are vertically offset for clarity.

*B* fields. In Fig. 2(b) we plot the spectra measured at *B*  $=$  3.2 T and at different temperatures. In this case the dc current was reduced to 180 nA to avoid heating the 2DEG by the current. The observed resonances are found to be extremely temperature sensitive, with their amplitudes decreasing quickly by only slightly increasing the temperature.

In Fig.  $3(a)$  we plot the *B*-field dispersion of these resonances. Also shown is the magnetoresistance  $R_{xx}$  measured without FIR radiation using the standard lock-in technique, which allows us to determine the 2DEG filling factors  $\nu$  $=N_s h/eB$ . The major resonances can be nicely fit (solid curves) using Eq. (1) with three fitting parameters  $\omega_0$  $=70.2$  cm<sup>-1</sup>,  $f=0.17$ , and  $m^* = 0.039m_e$ . Within the fitting accuracy, the obtained effective mass value is equal to that directly measured from CR on the unpatterned sample from the same wafer.<sup>2</sup> We therefore identify them as the two characteristic antidot collective modes  $\omega^+$  and  $\omega_{EMP}$ . The relative strength of  $\omega^+$  over the  $\omega_{EMP}$  mode increases with increasing *B* field, in accordance with the theory.<sup>8</sup> By comparing the spectra with that obtained on the unpatterned



FIG. 3. (Color online) (a) Magnetic-field dispersions for resonances measured at  $T=1.5$  K and magnetoresistance  $R_{xx}$  measured without FIR radiation. The solid curves are fits for  $\omega^+$  (solid circles) and  $\omega_{EMP}$  (open circles) antidot modes using Eq. (1). The dotted line and dashed curve are calculated for CR and spin-flip excitation, respectively, using the effective mass of  $0.039m<sub>e</sub>$ , the spin-orbit coupling parameter of  $\alpha=2.38\times10^{-11}$  eV m and a Lande<sup> $g$ </sup> factor of  $g = -8.7$ . Dash-dotted lines indicate the optical phonon energies of InAs and GaAs. (b) Temperature dependence of the resonance strength for the  $\omega^+$  (solid circles) and  $\omega_{EMP}$  (open circles) antidot modes measured at  $B=3.2$  T. The curves in (b) are guides to the eyes.

sample, we further identify the weak resonance marked by the thick arrow in Fig.  $2(a)$  as the collective spin-flip excitation. $^{2}$  With the antidot lattice, the collective spin-flip excitation gets broader and appears as a shoulder of the  $\omega^+$ resonance. To our knowledge, spin-flip excitation in an antidot array has neither been studied experimentally nor investigated theoretically. Here we have assumed that at large *B* fields, the spin-flip excitation in the antidot array approaches that in an unpatterned 2DEG, just like the  $\omega^+$  mode approaches the CR. $8$  For comparison, in Fig. 3(a) we plot the calculated dispersion for the 2DEG spin-flip excitation neglecting both the many-body correction and the antidot potential, using the spin-orbit coupling parameter of  $\alpha$ =2.38  $\times 10^{-11}$  eV m and the Lande<sup> $g$ </sup> factor of  $g=-8.7$  determined for the unpatterened sample.<sup>2</sup> Within the *B*-field range of 6–7 T, where we can observe the spin-flip excitation, the influence of the antidot potential on its resonance frequency is found small.

Observing the spin-flip excitation in the antidot lattice demonstrates the high sensitivity advantage of the photoconductivity spectroscopy. Another advantage of the technique is that we can measure resonances within the reststrahlen bands which are prohibited for transmission spectroscopy. In our sample, both the InAs quantum well and the GaAs substrate are polar semiconductors with reststrahlen bands between their TO and LO phonon frequencies. Besides, there are two phonon bands for both  $In_{0.75}Ga_{0.25}As$  and  $In_{0.75}Al_{0.25}As$  layers, as well as the interface phonons near each interfaces. For brevity, in Fig.  $3(a)$  we plot the bulk phonon frequency of GaAs and InAs. Apparently, the splitting of the  $\omega^+$  mode at large *B* fields is caused by the influence of phonons of our sample. Experimentally, by increasing the *B* field, we find that the resonance at about 285 cm<sup>-1</sup>, indicated by the thin arrow in Fig.  $2(a)$ , stays within the reststrahlen band of GaAs substrate but gains resonance strength. While the splitting of the  $\omega^+$  mode shows anti-crossing behavior centered at about 220 and 240 cm<sup>-1</sup>, near the TO  $(218 \text{ cm}^{-1})$  and LO  $(242.5 \text{ cm}^{-1})$  phonon frequency of InAs, respectively. At the moment, we cannot explain these resonances in the reststrahlen bands regime. We note that the influence of phonons on electronic excitations of a nanostructured 2DEG in the reststrahlen band regime is a rather sophisticated problem, with the combined nature of the optical effect, $11$  band nonparabolicity, and electron-electron and electron-phonon interaction.<sup>12,13</sup> It remains a controversial subject.<sup>14</sup> However, the rich spectral features observed in our experiment provide systematic data that is essential to establish a clear theoretical picture.

Our data demonstrates clearly that both  $\omega^+$  and  $\omega_{EMP}$ antidot modes contribute to the photoresistance. In contrast to that studied by the transmission spectroscopy, the resonance strengths of both modes measured by photoconductivity spectroscopy are extremely temperature sensitive. As shown in Fig.  $2(b)$  the resonance strengths of both modes decrease quickly by increasing the temperature from 1.5 to 2 K, during which the half width of the resonances does not change much. In Fig.  $3(b)$ , we plot the temperature dependence of the resonance strength for both modes measured at  $B=3.2$  T. Such an extremely sensitive temperature dependence can be qualitatively explained by the bolometric effect, $3,15$  where the resonant absorption of the FIR radiation effectively heats the electron gas and hence changes its resistance. In the low temperature limit  $k_B T \ll E_F$ , the heat capacity of the 2DEG is given by  $16$ 

$$
C_e = \pi^2 k_B^2 T \mathcal{D}(\mathbf{E}_{\mathbf{F}}, \mathbf{B})/3,\tag{2}
$$

proportional to the temperature *T* and the density of states  $\mathcal{D}(E_F, B)$  of the 2DEG at the Fermi energy  $E_F$ . The bolometric effect caused by electron heating is therefore more pronounced at lower temperature where  $C_e$  is smaller.

It is intriguing to compare our results with other photoconductivity experiments on the 2DEG in an antidot array. In

the early work of Vasiliadou *et al.*<sup>7</sup> , instead of a broad band FIR source, a microwave generator was used to investigate the commensurability effects. The photoconductivity experiment was performed by fixing the microwave frequency while sweeping the magnetic field. Characteristic dispersions for the antidot collective modes were not investigated due to the limited available microwave frequencies. The temperature dependence was not easy to study because of the superimposed nonresonant background which originates from the heating of the whole sample. In an improved photoconductivity spectroscopy experiment recently performed by Jager *et al.*<sup>5</sup> , the 2DEG is at a distance of 37 nm below the sample surface and the antidots are written by *e*-beam lithography and transferred into the 2DEG by shallow (with only about 6-nm) wet etching. Therefore, instead of  $\omega^+$  and  $\omega_{EMP}$ modes, CR and a magnetoplasmon mode were simultaneously observed, which is typical for a weak modulated 2DEG instead of a 2DEG with antidot confinement. The most recent experiment was performed by Ye *et al.*<sup>6</sup> using a significantly improved microwave technique with transmission lines to study both the photoconductivity and microwave transmission of a 2DEG in an antidot array. Among other interesting results, they observed a broad peak below Landau filling one in the microwave conductivity measured by sweeping the *B* field. On the peak, unlike the dc-limit conductivity, the microwave conductivity was found to be extremely temperature sensitive, decreasing with increasing temperature. As possible origins of this, antidot edge excitations of fractional quantum Hall effect states associated with either chiral Luttinger liquids<sup>6</sup> or edge reconstruction<sup>17</sup> have been discussed. Our data provide additional insight. As shown in Fig.  $3(b)$ , we have demonstrated that the contribution of the antidot edge magnetoplasmon to the photoresistance has a similar sensitive temperature dependence due to

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its bolometric nature. In addition, based on the flat *B*-field dispersion of the edge magnetoplasmon shown in Fig.  $3(a)$ , a photoresistance caused by exciting the edge magnetoplasmon at a fixed frequency would show broad structures, superimposed by a nonresonant background due to the change of the photoconductivity sensitivity by sweeping the *B* field. However, we would like to emphasize that whether the edge magnetoplasmon indeed plays a role in the experiment of Ye *et al.*<sup>6</sup> depends on two major questions: the first is how the photoresistance influences the microwave transmission in their experiment, and the second one is how large the edgemagnetoplasmon frequency in their sample is. We note that while the first question is not easy to answer due to the complicated microwave technique, the second question can be clarified by performing a photoconductivity spectroscopy experiment such as we describe in this paper. By measuring the dispersion of the  $\omega^+$  mode in the FIR regime, the geometric filling factor *f*, that depends on the depletion area of the antidot, can be determined, which can be used to estimate the  $\omega_{EMP}$  mode frequency.<sup>18</sup> In the sample of Ye *et al.*<sup>6</sup> the latter lies in the microwave regime and is rather difficult to measure directly.

In summary, we have performed a FIR photoconductivity spectroscopy experiment on a 2DEG in an array of antidots. We find that both the magnetoplasmon ( $\omega^+$ ) and the edgemagnetoplasmon ( $\omega_{EMP}$ ) modes of the antidot contribute to the photoresistance, which is extremely temperature sensitive due to the bolometric nature. We observe the influence of phonon bands on the  $\omega^+$  mode and a spin-flip excitation mode in the antidots.

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