High-field ordered and superconducting phases in the heavy-fermion compound $PrOs_4Sb_{12}$

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The filled-skutterudite compound $PrOs_4Sb_{12}$, the first example of a Pr-based heavy-fermion superconductor, displays superconductivity with $T_c \sim 1.85$ K and has an effective mass $m^* \sim 50m_e$, where m_e is the freeelectron mass. For magnetic fields above 4.5 T, sharp features in the normal-state electrical resistivity, magnetization, specific-heat, and thermal-expansion data suggest the occurrence of a phase transition at high fields. This high-field ordered phase in the normal state may be associated with a combination of crystalline electric fields, Zeeman splitting, and quadrupolar ordering. We present an investigation of the electrical resistivity and magnetization of $PrOs_4Sb_{12}$ as a function of temperature between 350 mK and 3.5 K and magnetic field up to 18 T. The data reveal a detailed phase boundary of the high-field ordered phase as well as the lower critical field H_{c1} and the onset field of the peak effect in the superconducting state of $PrOs_4Sb_{12}$.

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I. INTRODUCTION

The filled-skutterudite compound PrOs₄Sb₁₂ displays superconductivity with $T_c \approx 1.85$ K and has an effective mass $m^* \sim 50m_e$.¹ This compound is the first example of a Prbased heavy-fermion superconductor; all other known heavy-fermion superconductors are intermetallic compounds of the rare-earth element Ce or the actinide element U. Inelastic neutron-scattering experiments, along with an analysis of magnetic-susceptibility $\chi(T)$ and specific-heat C(T)data^{2,3} for a cubic crystalline electric field (CEF), are consistent with a Pr³⁺ energy scheme consisting of a nonmagnetic Γ_3 doublet ground state (0 K), a Γ_5 triplet first exited state (~8 K), and higher energy Γ_4 triplet (~133 K) and Γ_1 singlet (~320 K) excited states. The heavy-fermion properties of the Pr-based compounds PrInAg2 and PrFe4P12 have been attributed to the interaction of the charges of the conduction electrons with the electric quadrupole moments of the $Pr^{3+}\Gamma_3$ nonmagnetic doublet ground state in the CEF.^{4,5} The evidence for a $Pr^{3+}\Gamma_3$ ground state in $PrOs_4Sb_{12}$ indicates that the electric quadrupolar fluctuations may be responsible for the heavy-fermion state in this compound and could also be involved in the superconductivity.^{1–3}

For magnetic fields *H* above ~4.5 T, sharp features in measurements of the normal-state electrical resistivity^{2,6} $\rho(T)$, magnetization^{3,7} M(H), specific heat⁸ C(T), thermal expansion⁹ $\alpha(T)$, and magnetostriction¹⁰ $\lambda(T)$ of PrOs₄Sb₁₂ indicate that a phase transition is induced at high fields. The origin of the high-field ordered phase (HFOP) is still under investigation but may be related to the crossing of the Zeeman levels of the Γ_3 and Γ_5 CEF states and a corresponding change of the ground state at high fields.⁸ In this paper, we present further results of our investigation of PrOs₄Sb₁₂, utilizing electrical-resistivity measurements up to 18 T and magnetization measurements with magnetic field $H \parallel [111]$ and [001] crystallographic directions up to 5.5 T.

II. EXPERIMENTAL DETAILS

The PrOs₄Sb₁₂ samples studied were single crystals grown in Sb flux.¹¹ X-ray-diffraction measurements confirmed the cubic LaFe₄P₁₂-type structure.¹² The $\rho(H,T)$ measurements were made with a Linear Research LR 700 4-wire ac bridge operating at 16 Hz with constant current amplitudes of 100 μ A(0 T \leq H \leq 10 T) and 300 μ A(10 T \leq H \leq 18 T), and in a transverse geometry in a ³He-⁴He dilution refrigerator⁶ (0 T \leq H \leq 10 T) and a ³He cryostat (10 T \leq H \leq 18 T). The *M*(*H*,*T*) measurements were performed in a ³He Faraday magnetometer with a gradient field of 1 kOe/cm in fields up to 5.5 T and at temperatures between 0.4 K and 2 K.

III. RESULTS AND DISCUSSION

A. Normal-state properties

The behavior of the electrical resistivity ρ below 4.2 K and 18 T is summarized in Fig. 1. Figures 1(a) [Ref. 6] and 1(b) show $\rho(T)$ data in various constant fields, while Fig. 1(c) displays isotherms of $\rho(H)$. In this temperature range, the phonon contribution to ρ is negligible.¹³ The $\rho(T,H)$ data in Figs. 1(b) and 1(c) were taken on a different PrOs₄Sb₁₂ sample and in a different cryostat. The absolute value of the resistivity is sample dependent in the present work, probably due to irregular sample shapes and the presence of microcracks in the samples. Thus, the $\rho(T,H)$ data in Figs. 1(b) and 1(c) were normalized to those in Fig. 1(a) by comparing the $\rho(T)$ data at 10 T for both samples, which differ by a factor of ~0.44. The sharp drops in $\rho(T)$ below 2.5 T are due to the superconducting transition. A kink in the $\rho(T)$ curves develops above ~4.5 T and becomes most pronounced between 7 T and 11 T, and then gradually subsides as H increases further. This kink is apparently related to the



FIG. 1. (a) (Ref. 6) and (b) Electrical resistivity ρ vs *T* in various magnetic fields *H* up to 18 T for PrOs₄Sb₁₂ single crystals. (c) ρ vs *H* at various temperatures *T* up to 4.2 K. The rapid drop in ρ to zero for *H*<2.5 T is due to the superconducting transition, while the shoulder in $\rho(T)$ at \sim 1 K above 4.5 T and sharp kinks in $\rho(H)$ (marked as H_1^* and H_2^*) below 0.7 K are due to a HFOP (Ref. 8).

occurrence of a HFOP which will be discussed later (Fig. 4). The $\rho(T)$ data between 8 T and 10 T almost overlap with each other [Fig. 1(a) and Ref. 6]. The $\rho(H)$ data below 1 K reach a maximum at ~9 T as shown in Fig. 1(c), while the dome-shaped feature becomes more pronounced as *T* decreases. Two sharp kinks (H_1^* and H_2^*) become easily identified below 0.61 K and mark the boundary of the HFOP.^{6–8}

The ρ vs H isotherms reveal that ρ is enhanced in the HFOP over a linear interpolation of ρ from outside this region [Fig.1(c)]. Due to the crystalline electric field and the Zeeman splitting of $Pr^{3+}J=4$ states, the 4-*f* electron populations in each level will change with temperature. These changes will affect the interactions between 4-f and conduction electrons that, in turn, will affect the transport properties.^{14–17} Calculations of $\rho(H,T)$ for such a case, in which an exchange interaction^{14–16} and an aspherical Cou-lomb interaction^{14,16,17} between the Zeeman split 4-*f* and conduction electrons have been added to the cubic CEF Hamiltonian with a Γ_3 ground state at H=0 T, agree qualitatively with the experimental ρ vs H isotherms (detailed calculations are described in Ref. 18). The calculated ρ vs H isotherms are plotted in Fig. 2 and can be compared with the experimental ρ vs H isotherms in Fig. 1(c). In this calculation, we found that a Γ_1 ground state will not produce the same features as we observe in the measurements of the $\rho(H)$ isotherms.¹⁸ This provides further support for a Γ_3 ground state in PrOs₄Sb₁₂.

The magnetization M(H) measurements were performed with the applied magnetic field oriented along the [111] and [001] crystallographic directions of a single crystal of PrOs₄Sb₁₂for 0 T $\leq H \leq 5.5$ T. Only the isothermal M(H)data for $H \parallel [111]$ are shown in Fig. 3. A kink (at H_1^*) ap-

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FIG. 2. Calculated ρ vs *H* isotherms based on a CEF Hamiltonian including equal amounts of the magnetic exchange and aspherical Coulomb interactions assuming a Γ_3 ground state (Ref. 18). The dome-shaped structure is qualitatively comparable to Fig. 1(c).

pears in M(H) curves above 4.5 T and cannot be resolved above 0.8 K for $H \le 5.5$ T. This feature is apparently associated with the onset of the HFOP. We found that the fields where the M(H) kinks occur are the same for $H \parallel [111]$ and [001] (i.e., no anisotropy). In contrast, Tenya *et al.* reported small but noticeable anisotropy in the location of the boundary of the HFOP.⁷

In previous work, a HFOP was identified from the kinks in magnetoresistivity $\rho(H,T)$ data,^{2,6} kinks in magnetization M(H,T) data,^{3,7} peaks in specific heat C(T,H) data,⁸ and peaks in thermal-expansion $\alpha(T,H)$ data.⁹ From our new set of $\rho(H,T)$ measurements, shown in Figs. 1(b) and 1(c), the



FIG. 3. M vs H ($\|$ [111]) at various temperatures. The M(H) kink occurs at H_1^* , the boundary of the high-field ordered phase. Inset: Fields at which the PE appears and disappears, deduced from M(H) data of a PrOs₄Sb₁₂ single crystal with $H\|$ [111]. H_{c2} is derived from the superconducting transition observed in the $\rho(T)$ data (Refs. 1 and 6).

upper boundary of the HFOP can be determined. The H-Tphase diagram, depicting the superconducting and the HFOP regions, is constructed in Fig. 4. Recent magnetostriction and additional thermal-expansion measurements by Oeschler et al. also indicate a similar phase boundary for the HFOP.¹⁰ Since an increase in the magnetic field would induce mixing of the ground state and the low-lying first excited state, the HFOP may be driven by the crossing of the upper level of the Γ_3 doublet and the lowest level of the Γ_5 triplet states at \sim 4.5 T and another crossing between the lowest levels of the Γ_{3} and Γ_{5} states at ~10 T, which changes the ground state.⁸ In Fig. 4, the dashed line below 4.5 T and 2 K that connects the peaks in $d\rho/dT$ (Ref. 6) and intersects the HFOP is a measure of the Zeeman splitting between the Pr^{3+} ground state and the first excited state. The nearly temperature-independent boundary of the HFOP at \sim 14.5 T resembles the antiferroquadrupolar ordered phase observed in $\text{PrPb}_3,^{19}$ which also has a Γ_3 ground state. It is plausible that the HFOP in PrOs₄Sb₁₂ has the same origin. However, the antiferroquadrupolar ordered phase observed in PrPb₃ exhibits strong anisotropy above 1 T. We did not observe such an anisotropy in the HFOP from the magnetization data of PrOs₄Sb₁₂ along [001] and [111] between 4.5 and 5.5 T, although the anisotropy at these fields may not be large enough to resolve. Neutron-scattering experiments²⁰ on our powdered single crystals of PrOs₄Sb₁₂ did not detect any signs of a HFOP.

B. Superconducting-state properties

A peak effect (PE) in the superconducting state that had an onset at ~ 1.25 T and disappeared at ~ 0.3 T below the



FIG. 4. *H*-*T* phase diagram for $PrOs_4Sb_{12}$. The superconducting-state (SC) phase boundary is derived from the electrical-resistivity $\rho(T,H)$ data (Refs. 1 and 6). The HFOP is deduced from the features observed in $\rho(T,H)$, C(T,H) (Ref. 8) M(H,T) ($H \parallel [001]$ and [111]), and $\alpha(T,H)$ (Ref. 9). The dashed line drawn through the points where $d\rho/dT$ exhibits a peak above 1 K is a measure of the energy difference between the $Pr^{3+} \Gamma_3$ ground and Γ_5 first excited state (Refs. 8 and 3).



FIG. 5. Lower critical field H_{c1} vs *T*. Inset: *M* vs *H* (||[001]) below 100 Oe at various temperatures. H_{c1} is defined as the field where the curve departs from the initial linear region.

upper critical field $H_{c2}(T)$ was also observed in M(H) measurements (Fig. 3). The fields at which the PE appears and disappears are plotted in the inset of Fig. 3. According to recent thermal conductivity measurements on a PrOs₄Sb₁₂ single crystal in a magnetic field,²¹ there are two distinct superconducting phases in the H-T plane with twofold and fourfold rotation symmetries in the basal plane. The phase boundary between the twofold and fourfold symmetry superconducting phases is at $H \approx 0.75$ T for T ≈ 0.5 K. The onset field of our PE occurs at a higher field and for the fields below the PE region, no anomaly is observed in our M(H)curves. It is not clear whether the PE is related to the twofold and fourfold symmetry superconducting phases²¹ or to pinning from crystal defects or impurities. However, recent transverse-field muon spin rotation measurements²² with H= 200 Oe indicated that $PrOs_4Sb_{12}$ has a nearly isotropic superconducting energy gap in the superconducting state.

Figure 5 shows the lower critical field H_{c1} vs T determined for $H \parallel [001]$. $H_{c1}(0)$ is quite small, ~23 Oe. The magnetic susceptibility χ in the Meissner state was found to be $-31.5 \text{ cm}^3/\text{mol}$ (or $-1/[0.613(4\pi)]$). The demagnetization factor of the sample is estimated to be ~ 0.45 ,^{23,24} resulting in a superconducting volume fraction of \sim 74%. The Ginzburg-Landau parameter is estimated to be κ $\approx (H_{c2}/H_{c1})^{1/2} \sim 31$ with $H_{c2} \sim 2.19$ T and $H_{c1} \sim 23$ Oe. This value is a factor of 10 larger than that estimated from the relation $\kappa = \lambda / \xi_0 \sim 3$, where the penetration depth λ \sim 344 Å was taken from muon spin resonance measurements²² and the coherence length $\xi_0 \sim 113$ Å was estimated from the initial slope of H_{c2} .⁶ The discrepancy may arise from error in the estimates of H_{c1} due to the residual field in the superconducting magnet or to different qualities of samples used in the various measurements.

IV. SUMMARY

In summary, we have reported electrical-resistivity and magnetization measurements on $PrOs_4Sb_{12}$ at high magnetic fields and determined the *H*-*T* phase diagram below 18 T.

Aspherical Coulomb and magnetic exchange scattering between 4f and conduction electrons can qualitatively describe the dome-shaped features observed in the $\rho(H)$ data and provide evidence that Γ_3 is the ground state at zero magnetic field.

The high-field ordered-phase boundary is determined from kinks in $\rho(H,T)$ and M(H,T) data. The HFOP is confined to a region on the *H*-*T* plane between ~4.5 T and 14.5 T, and below ~1 K. Measurements of M(H,T) for *H* <5.5 T, parallel to the [001] and [111] directions, did not exhibit appreciable anisotropy. In analogy with the behavior of PrPb₃, the HFOP may be associated with antiferroquadrupolar order.

The M(H,T) measurements revealed a small value for the lower critical field $H_{c1}(0)$ of ~23 Oe, and a value for the upper critical field $H_{c2}(0)$ of ~2.19 T, yielding a Ginzburg-Landau parameter κ ~31. A peak effect was observed which

had an onset at ~1.3 T between 0.35 K and 0.7 K and disappeared at a field that tracked the $H_{c2}(T)$ curve which had an offset of ~0.3 T. No evidence in the M(H,T) data was found for a crossover between two superconducting phases with different order-parameter symmetry as reported by Izawa *et al.*²¹

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