Non-Fermi liquid behavior and scaling of the low-frequency suppression in the optical conductivity spectra of CaRuO₃

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Optical conductivity spectra $\sigma_1(\omega)$ of paramagnetic CaRuO₃ are investigated at various temperatures. At $T=10$ K, it shows a non-Fermi-liquid behavior of $\sigma_1(\omega) \sim 1/\omega^{1/2}$, similar to the case of a ferromagnet $SrRuO₃$. As the temperature (T) is increased, on the other hand, $\sigma_1(\omega)$ in the low-frequency region is progressively suppressed, deviating from the $1/\omega^{1/2}$ dependence. Interestingly, the suppression of $\sigma_1(\omega)$ is found to scale with ω/T at all temperatures. The origin of the ω/T scaling behavior coupled with the non-Fermiliquid behavior is discussed.

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The Fermi-liquid model has provided a fundamental concept in understanding metals.¹ However, in some strongly correlated systems, non-Fermi-liquid (NFL) behaviors have been often observed, where the Fermi-liquid picture fails. In the normal state of high T_c superconductors (HTS), evidences of NFL behaviors were reported in many experiments involving photoemission, transport, and optical measurements.² In particular, their optical conductivity spectra $\sigma_1(\omega)$ show $1/\omega$ dependence in contrast to the usual Drude form of $\sim 1/\omega^2$, and their scattering rates show linear temperature (T) and ω dependences up to the mid-IR region. Such unusual behaviors have been explained in terms of the marginal Fermi liquid. 3

Recently, perovskite ruthenates have attracted much attention as another class of materials exhibiting NFL behavior. The ruthenates belong to 4*d* transition-metal oxides, and the electron correlation effects are believed to play a crucial role in determining their physical properties. 4 Together with their intriguing transport properties, 5.6 the optical spectra show a distinct NFL behavior.^{7,8} For an itinerant ferromagnet $SrRuO₃$ (a ferromagnetic transition temperature T_c =165 K), Kostic *et al.*⁷ reported that its $\sigma_1(\omega)$ at low *T* follow a $1/\omega^{1/2}$ dependence, indicating a NFL behavior stronger than that of HTS. Recently, Dodge *et al*. ⁸ fitted the $\sigma_1(\omega)$ of SrRuO₃ with $\sigma_{\alpha}(\omega) \sim (\tau^{-1} - i\omega)^{-\alpha}$ with $\alpha \sim 0.4$ down to a very low-energy region of ~ 0.001 eV. Although the NFL behavior in the ruthenate has been widely accepted, its origin is not clearly understood. In addition, an unusual suppression of $\sigma_1(\omega)$ in the low-energy region occurs in the paramagnetic (PM) state, but is absent in the ferromagnetic (FM) state.⁸ However, this intriguing phenomenon, which might be coupled with a NFL behavior, has not been addressed properly.

While $CaRuO₃$ has the electronic structure similar to that of $SrRuO₃$, this material does not show any magnetic ordering down to a very low T .⁹ CaRuO₃ can provide a relatively wide *T* window for investigating the interesting PM state as well as another example for understanding the NFL behavior. In this paper, we investigated the electrodynamic responses of CaRuO₃. It was found that $\sigma_1(\omega)$ at 10 K follows $\sim 1/\omega^{1/2}$, indicating a NFL behavior. With increasing *T*, the suppression of $\sigma_1(\omega)$ near $\omega \approx 0$ develops below the characteristic energy ω_c , which corresponds to a peak structure in $\sigma_1(\omega)$ and shifts to higher frequencies as *T* increases. It is remarkable that the low-frequency optical spectra in a function of $\sigma_1(\omega)/\omega^{-1/2}$ show a ω/T scaling behavior in a very wide *T* range. While there have been similar scaling behavior reported in some physical properties of other NFL systems,^{10,11} the ω/T scaling behavior in ruthenates is an observation in optical spectra. This scaling indicates that the only characteristic energy scale should be set by *T* in the PM state of the perovskite ruthenates.

Several CaRuO₃ epitaxial films on (100) SrTiO₃ substrates were fabricated using 90° off-axis sputtering techniques.12 Their thicknesses were about 5000 Å. To obtain high crystalline quality films with little strain effect, we used vicinal substrates with large miscut angles $(4 \text{ and } 7^{\circ})$. The dc resistivity $\rho(T)$ was measured up to 500 K using the standard four-probe method. Figure 1 shows the $\rho(T)$ curve of a film, which is nearly the same as that of a bulk single crystal, including a crossover near around 50 K below which the *T* dependence changes from $T^{1/2}$ to $T^{3/2}$.⁹ The 300-K resistivity value of the film is \sim 270 $\mu\Omega$ cm, comparable to that of the bulk single-crystal value of resistivity ~200 $\mu\Omega$ cm.⁹ The resistivity ratio $\rho(300 \text{ K})/\rho(10 \text{ K})$ is about 9, indicating the high quality of our film. It is interest-

FIG. 1. *T*-dependent $\rho(T)$ curves of a CaRuO₃ film (open circle) and a SrRuO₃ single crystal (open triangle). The data of SrRuO₃ are quoted from Ref. 5.

ing that the $\rho(T)$ in the PM state of the perovskite ruthenates follows a $T^{1/2}$ dependence. The $\rho(T)$ of CaRuO₃ increases continuously up to 500 K with no saturation, and $\rho(T)$ $\sim T^{1/2}$ above 50 K.⁶ Note that, as displayed in Fig. 1, the reported ρ values of a single crystal SrRuO₃ in the PM state also show the $T^{1/2}$ dependence.⁵ The $T^{1/2}$ dependence of $\rho(T)$ in the perovskite ruthenates is another anomalous feature, distinguished from the linear *T* dependence of $\rho(T)$ in the normal state of HTS.

Near normal incident reflectivity spectra $R(\omega)$ were measured in a wide photon energy region of 5 meV–30 eV. The Kramers-Kronig (KK) analysis was used to calculate $\sigma_1(\omega)$ from the measured $R(\omega)$. For KK transformation, $R(\omega)$ in the low-frequency region were extrapolated with the Hagen-Rubens relation. *T*-dependent $R(\omega)$ were measured in a photon energy region below 6 eV. Above 6 eV, the room temperature $R(\omega)$ was used for high-frequency extrapolation. The overall features of the measured $R(\omega)$ were similar to those in $SrRuO₃$ reported by Kostic *et al.*⁷ The calculated $\sigma_1(\omega)$ from the KK analysis agreed with the experimental $\sigma_1(\omega)$ independently obtained by spectroscopic ellipsometry in the visible region, which demonstrates the validity of our KK analysis.¹³ A high-frequency region of $\sigma_1(\omega)$ in CaRuO₃ were described in our published paper. 4 In the paper, we focus on the far-IR region.

Figure 2 shows the *T*-dependent $\sigma_1(\omega)$ in the far-IR region. The peak at \sim 570 cm⁻¹ is due to a transverse opticphonon mode, whose *T* dependence is rather weak. Interestingly, $\sigma_1(\omega)$ at 10 K shows a clear NFL behavior, deviating from that of conventional metals. As shown in the inset of Fig. 2, $\sigma_1(\omega)$ at 10 K is proportional to $1/\omega^{1/2}$,¹⁴ which is much slower than the frequency dependence of a Fermi liquid of $1/\omega^2$. Even at a higher *T*, the $1/\omega^{1/2}$ dependence in $\sigma_1(\omega)$ is retained in the high-frequency region, which might be correlated with the $T^{1/2}$ dependence of $\rho(T)$ at high temperatures. A similar NFL behavior was also observed in $SFRuO₃$.⁷ It is interesting that the $1/\omega^{1/2}$ dependence in $\sigma_1(\omega)$ can be observed in perovskite ruthenates with different magnetic ground states.

FIG. 2. *T*-dependenct $\sigma_1(\omega)$ of CaRuO₃ below 1500 cm⁻¹. The solid circle symbols represent ω_c . The solid triangle, the solid square, and the solid circle symbols on the *y* axis represent the dc value of $\sigma(T)$ at 100, 300, and 500 K, respectively. The dotted lines are $\sigma_1(\omega)$ obtained from the Hagen-Rubens extrapolations. In the inset, $\sigma_1(\omega)$ at 10, 200, 500 K follow $1/\omega^{1/2}$ above ω_c . For clarity, the $\sigma_1(\omega)$ at 200 K and 500 K are multiplied by a factor of 0.85 and 0.7, respectively. The dotted lines are guidelines for $1/\omega^{1/2}$ dependence.

The suppression in $\sigma_1(\omega)$ is observed near $\omega \approx 0$ at higher *T*. As ω decreases from the high-frequency side, $\sigma_1(\omega)$ increases initially but decrease below the peak frequency ω_c , approaching smoothly to the measured dc conductivity values. This feature is clear even at 100 K, where the dc conductivity value is rather high by \sim 7000 Ω ⁻¹ cm⁻¹. It is noted that in the case of SrRuO₃, the low-frequency suppression occurs only in its PM state, not in its FM state.8 Together with the *T*1/2 dependence of $\rho(T)$, the low-energy suppression in $\sigma_1(\omega)$ can be regarded as a generic feature of the PM state of the perovskite ruthenates.

Note that the low-energy suppression of $\sigma_1(\omega)$ shows an interesting *T*-dependent evolution. As *T* increases, the suppression feature becomes clear and ω_c shifts to a higher frequency linearly with *T*. It is evident that the peak structure does not arise from electronic transitions or disorder effects. The values of ω_c are comparable with a thermal energy, $k_B T$. This energy scale is too low for a typical interband transition.⁴ A similar suppression in $\sigma_1(\omega)$ near $\omega \approx 0$ has been often observed in highly disordered systems, but their characteristic energy scale is expected to decrease with increasing T ,¹⁵ which is opposite to our case. Therefore, a thermal energy scale of a pseudogap-like feature observed in $CaRuO₃$ is quite unique.

The pseudogap-like feature could be closely related to nearly ferromagnetic characteristics of $CaRuO₃$. Several experimental and theoretical evidences suggest that $CaRuO₃$ should be nearly ferromagnetic.^{16–18} A strong FM fluctuation was also observed in the PM state of $SFRuO₃$.¹⁶ Especially, local-density-functional calculations on $(Ca, Sr)RuO₃$ showed that the lattice distortions associated with different ionic sizes are crucial in determining the magnetic properties.¹⁸ Further, phonon anomalies at T_c were observed in SrRuO₃,

FIG. 3. *T*-dependent $\sigma_1(\omega)/a\omega^{-1/2}$ with ω/T as the abscissa. The open circle, open trigonal, and cross symbols are for the 185 K, 225 K, and 250 K spectra of $SrRuO₃$, respectively, quoted from Ref. 7. For $SrRuO₃$, the value of a was adopted to reproduce the 40 K $\sigma_1(\omega)$. The solid line represents $Z(\omega/T) = \tanh(1.6\omega/T)$.

indicating the strong spin-lattice interaction.¹⁹ These imply that the lattice degree of freedom is strongly coupled to the magnetic ordering so that the excitation of a relevant phonon mode can be responsible for the local magnetic fluctuation in the nearly FM system. From the spin-fluctuation theory of nearly ferromagnetic materials,²⁰ it is known that the meansquare amplitude of spin-fluctuation increases linearly in proportion to *T*. Thus, one may expect the low-energy quasiparticle excitations to be strongly renormalized by the thermally induced spin fluctuations with spin-lattice coupling, where such *T*-dependent renormalization might be relevant to the suppression of $\sigma_1(\omega)$ in the low-frequency region. It is noted that the pseudogap-like feature in $\sigma_1(\omega)$ of CaRuO₃ and its proximity to the FM instability is quite analogous to the situation in HTS, which is close to the antiferromagnetic instability. 21

Now, we show that from the systematic *T*-dependent evolution of the low-frequency suppression in $\sigma_1(\omega)$, an interesting ω/T scaling behavior can occur in the perovskite ruthenates. The low-frequency suppression in $\sigma_1(\omega)$ can be expressed as a deviation from the $1/\omega^{1/2}$ dependence. As shown in the inset of Fig. 2, the deviation region of $\sigma_1(\omega)$ from $1/\omega^{1/2}$ dependence becomes wider with increasing *T*, consistent with the shift of ω_c to higher frequency. To check the possibility of scaling behavior, we plotted $\sigma_1(\omega)/a\omega^{-1/2}$ vs ω/T . With the value of the coefficient *a* adopted for the scaling, the $\sigma_1(\omega)$ at 10 K was reproduced. As shown in Fig. 3, all of the normalized conductivity spectra collapse onto a single line.²² It is noted that this scaling behavior persists up to a rather high temperature, 500 K. The ω/T scaling behavior means that the *T*-dependent suppression behavior could be determined only by *T*, indicating

$$
\sigma_1(\omega) \sim 1/\omega^{1/2} Z(\omega/T), \tag{1}
$$

or

$$
\sigma_1(\omega)T^{1/2} \sim (T/\omega)^{1/2}Z(\omega/T). \tag{2}
$$

The scaling function $Z(\omega/T)$ is fitted quite well with $Z(\omega/T)$ = tanh($\beta\omega/T$), with β =1.6. Clearly, Eqs. (1) and (2) are closely related to the characteristic properties in the PM states, such as $\rho(T) \sim T^{1/2}$ and $\sigma_1(\omega) \sim 1/\omega^{1/2}$ at high frequencies. We also plotted the SrRuO₃ $\sigma_1(\omega)$ data in the PM region (i.e., at 185 K, 225 K, and 250 K) reported by Kostic et al.⁷ Interestingly, the normalized spectra of SrRuO₃ fall on the scaling curve. This indicates that the scaling function shown in Fig. 3 could be applied to other perovskite ruthenates.

While the ω/T scaling behavior in $\sigma_1(\omega)$ of the perovskite ruthenates is quite unique, it is noted that similar scale invariance has also been observed in some physical properties of other NFL systems, such as some *f*-electron compounds¹⁰ and HTS.¹¹ The scaling behaviors in these NFL systems indicate that the only characteristic energy scale is determined by *T*, a possible origin of which was suggested to be the quantum critical fluctuation associated with the zerotemperature phase transition.²³ Similar to other NFL systems, our ω/T scaling behavior in $\sigma_1(\omega)$ may suggest a quantum critical point between the ferromagnetic and paramagnetic phases in the perovskite ruthnates: The ferromagnetic transition temperature T_c is decreased as x is increased in $Sr_{1-x}Ca_xRuO_3$ and is completely suppressed in CaRuO₃, and a quantum critical point is expected at an appropriate value of $x = x_c$.^{9,24} We note that, consistent with the magnetic quantum phase transition, the previous low *T* transport measurements hinted a phase transition from a Fermi-liquid behavior for SrRuO₃ to a NFL behavior for CaRuO₃.^{24,25} Motivated by our observation, understanding the origin of the NFL behavior associated with the ω/T scaling in $\sigma_1(\omega)$ and its possible relation with the quantum criticality is a challenging issue in the future study of perovskite ruthenates.

In summary, the optical spectra of the nearly ferromagnetic $CaRuO₃$ show non-Fermi-liquid behavior and a scaling in the low-frequency suppression. Its $\sigma_1(\omega)$ follows the $1/\omega^{1/2}$ -dependence, similar to the case of SrRuO₃. From the *T*-dependent evolution of the low-frequency suppression, it is observed that the $\sigma_1(\omega)$ normalized by the $1/\omega^{1/2}$ can be scaled with ω/T at all temperatures, indicating that only characteristic energy scale is determined by *T*. The ω/T scaling coupled with the non-Fermi-liquid behavior is expected to provide further insights into understanding the unusual electrodynamics of the ruthenates.

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