# Magnetic phase diagram of the stage-1 CoCl<sub>2</sub> graphite intercalation compound: Existence of metamagnetic transition and spin-flop transitions

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The *H*-*T* phase diagram of a stage-1 CoCl<sub>2</sub> graphite intercalation compound has been determined from measurements of the ac magnetic susceptibility, dc magnetization, and in-plane resistivity in the presence of an external magnetic field along the *c* plane perpendicular to the *c* axis. This compound undergoes two magnetic phase transitions at  $T_{cu}$  (= $T_N$ =9.9 K) and  $T_{cl}$  (=7.7 K) at *H*=0. A metamagnetic transition occurs at a critical point ( $T_3 \approx 8.77$  K,  $H_3 \approx 270$  Oe). A spin-flop transition occurs at the critical point ( $T_2 \approx 6.8$  K,  $H_2 \approx 80$  Oe) due to a competition between weak antiferromagnetic interplanar interactions and in-plane anisotropic interactions. Two lines  $H_+$  and  $H_-$  above  $T_N$  are due to ferromagnetic short-range fluctuations.

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# I. INTRODUCTION

A stage-1 CoCl<sub>2</sub> graphite intercalation compound (GIC) magnetically behaves like a quasi-two-dimensional (2D) ferromagnet with a weak antiferromagnetic interplanar exchange interaction. The spin easy direction of Co<sup>2+</sup> lies in the c plane, showing an easy-plane (XY) type anisotropy. The magnetic phase transition of a stage-1 CoCl<sub>2</sub> GIC has been extensively studied using magnetic neutron scattering, dc and ac magnetic susceptibility, magnetization, and inplane and *c*-axis resistivity. 1-7 It has been revealed through these studies that this compound undergoes an antiferromagnetic phase transition at a Néel temperature  $T_N$  (=9.9 K). Below  $T_N$  the 2D ferromagnetic CoCl<sub>2</sub> layers are antiferromagnetically stacked along the c axis, forming a 3D antiferromagnetic long-range order. In fact, Ikeda et al.<sup>5</sup> measured magnetic neutron-scattering intensities of a stage-1 CoCl<sub>2</sub> GIC, and showed that relatively sharp antiferromagnetic Bragg reflections appear at wave numbers  $Q_c = (2\pi/I_c)L$ , with  $L=\frac{1}{2}, \frac{3}{2}$ , and so on, where  $I_c$  is the *c*-axis repeat distance. The Bragg intensity at  $(00\frac{1}{2})$  decreases as the temperature (T) increases, and tends to reduce to zero, indicating a 3D antiferromagnetic ordered below  $T_N$ . The transition is somewhat smeared probably because of the islandlike nature of this compound. The spin correlation length along the caxis,  $\xi_c$ , is limited to be over about 20 CoCl<sub>2</sub> layers ( $\approx 200$ Å). Note that in a stage-1  $CoCl_2$  GIC, the  $CoCl_2$  layers are formed of small islands, which is common to acceptor-type GIC's. The peripheries of islands provide acceptor sites for electrons transferred from the graphite layer to the CoCl<sub>2</sub> layer.3

The magnetic phase diagram of a stage-1 CoCl<sub>2</sub> GIC was studied by Nicholls and Dresselhaus.<sup>3</sup> They measured the field dependence of the dispersion  $\chi'$  of ac magnetic susceptibility when an external magnetic field (*H*) is applied along the *c* plane (perpendicular to the *c* axis). They showed that the *H* dependence of  $\chi'$  exhibits a peak at a characteristic magnetic field ( $H_i \approx 380$  Oe) at low temperatures. As *T* is raised, this peak becomes sharper and stronger in magnitude and then disappears around 10 K just above  $T_N$ . They suggested two possible interpretations for the behavior. In the first interpretation,  $H_t$  is a spin-flop transition field. This possibility is ruled out because the spin flop to paramagnetic transition at higher H has not been detected up to a field of 10 kOe. In the second interpretation,  $H_t$  is a metamagnetic transition field. They concluded that the metamagnetic transition is more likely in a stage-1 CoCl<sub>2</sub> GIC. The nature of the field-induced transition was also examined from magnetic neutron scattering by Chouteau *et al.*<sup>6</sup> The intensity of antiferromagnetic Bragg reflection at  $(00\frac{1}{2})$  starts to decrease at ~400 Oe, and seems to disappear at ~800 Oe at 1.7 K.

In spite of such success, so far the complicated *T* dependence of ac magnetic susceptibility near  $T_N$  is not fully understood in terms of the above simple model. In fact, Nicholls and Dresselhaus<sup>3</sup> showed that  $\chi'$  has two peaks at 9.7 and 8.6 K, and that the absorption  $\chi''$  has a single peak at 9.7 K. Yazami and Chouteau<sup>4</sup> showed that  $\chi'$  has a peak at 9.77 K and a shoulder at 8.22 K, and that  $\chi''$  has two peaks at 9.77 and 8.22 K. These results suggest that an ordered phase may exist below  $T_N$ .

In this paper we have determined the H-T phase diagram of a stage-1 CoCl<sub>2</sub> GIC precisely using superconducting quantum interference device (SQUID) ac magnetic susceptibility and SQUID dc magnetization, and in-plane resistivity in the presence of an external magnetic field H along the cplane. The H-T diagram thus obtained is much more complicated than we expected. The antiferromagnetic phase transition occurs at an upper critical temperature  $T_{cu}$  (= $T_N$ =9.9 K). A metamagnetic transition is observed at a critical point ( $T_3 \approx 8.77$  K and  $H_3 \approx 270$  Oe). Spin-flop transitions are newly observed at points ( $T_1 \approx 7.6$  K,  $H_1 \approx 8$  Oe) and  $(T_2 \approx 6.8 \text{ K}, H_2 \approx 80 \text{ Oe})$  below a lower critical temperature  $T_{cl}$  (=7.7 K). These results indicate that the ordered phases below  $T_N$  have several different spin structures depending on T and H. The H-T diagram of a stage-1 CoCl<sub>2</sub> GIC will be discussed in comparison with those of Ising antiferromagnets  $FeCl_2$  (Refs. 8 and 9) and  $FeBr_2$ , <sup>10–14</sup> showing metamagnetic transitions. In FeCl<sub>2</sub> and FeBr<sub>2</sub>, the 2D ferromagnetic layers are antiferromagnetically stacked along the c axis, forming a 3D antiferromagnetic phase below the Néel temperature. In spite of such similarities, the magnetic phase diagram of FeBr<sub>2</sub> is much more complicated than that of FeCl<sub>2</sub>. The present study is motivated by a series of works on  $\text{FeBr}_2$ .<sup>10-14</sup>

## **II. PRELIMINARY DETAILS**

In a stage-1 CoCl<sub>2</sub> GIC, there is a single graphite layer between adjacent CoCl<sub>2</sub> layers. The *c*-axis repeat distance is 9.38 Å. The structure of the CoCl<sub>2</sub> layer consists of Co<sup>2+</sup> layers which are sandwiched between two Cl<sup>-</sup> layers along the *c* axis. The Co layers are formed of a triangular lattice with an in-plane lattice constant a=3.572 Å.<sup>15</sup> The spin Hamiltonian of stage-1 and stage-2 CoCl<sub>2</sub> GIC's is written as

$$H = -2J \sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j + 2J_A \sum_{\langle i,j \rangle} S_i^z \cdot S_j^z + 2J' \sum_{\langle i,k \rangle} \mathbf{S}_i \cdot \mathbf{S}_k, \quad (1)$$

with a fictitious spin S = 1/2, where *J* is the ferromagnetic intraplanar exchange interaction between the nearestneighbor Co<sup>2+</sup> pairs (i,j) in the same Co layer,  $J_A$  is the anisotropic exchange interaction favoring *XY* anisotropy, and (-J') is the antiferromagnetic interplanar exchange interaction between the nearest-neighbor Co<sup>2+</sup> pairs (i,k) in the adjacent Co layers. The values of *J* and  $J_A$  are assumed to be the same for stage-1 and stage-2 CoCl<sub>2</sub> GIC's  $(J = 7.75 \text{ K and } J_A = 3.72 \text{ K})$ , while the value of *J'* for stage-1 CoCl<sub>2</sub> is much larger than that for a stage-2 CoCl<sub>2</sub> GIC.<sup>1,16</sup> For convenience, we introduce the equivalent fields (intraplanar exchange field, interplanar exchange field, and *XY* anisotropy field) defined by

$$H_{E} = \frac{2zJS}{g_{a}\mu_{B}}, \quad H'_{E} = \frac{2z'J'S}{g_{a}\mu_{B}}, \quad H^{out}_{A} = \frac{2zJ_{A}S}{g_{c}\mu_{B}}, \quad (2)$$

respectively, where  $g_a$  (=6.40) and  $g_c$  (=4.75) are the Landé g factors along the c plane and along the c axis, respectively, z (=6) is the number of in-plane nearest-neighbor Co atoms, and z' (= 6) is the number of in-plane nearest-neighbor Co atoms. The values of  $H_E$  and  $H_A^{out}$  are estimated as 108.3 and 70 kOe, respectively. The value of  $H'_E$  is on the order of 380 Oe for a stage-1 CoCl<sub>2</sub> GIC (see Sec. VI). Note that an in-plane sixfold symmetry-breaking field  $H_A^{in}$  is not included in the above spin Hamiltonian. The value of  $H_A^{in}$  is on the order of 10 Oe (see Sec. VI). Because of  $H_A^{in}$ , the direction of spin in the c plane is limited to the angle given by  $\phi$ =  $(\pi/6)n$  (n = 0,1,...,5), where  $\phi$  is the angle between the spin and an in-plane crystalline axis.<sup>2,17</sup> The competitions between  $H_A^{in}$  and  $H_E'$  and between  $H_E'$  and  $H_A^{out}$  lead to the occurrence of the spin-flop transition and the metamagnetic transition, respectively.

# **III. MOLECULAR FIELD THEORY**

Here we present a simple model of the molecular field theory for the spin-flop transition and metamagnetic transition.<sup>18,19</sup> For simplicity, we consider an antiferromagnetic system where the sublattice magnetizations ( $\mathbf{M}_1$  and  $\mathbf{M}_2$ ) are collinear with the easy axis (z axis) at H=0. When **H** is applied along the z axis, the direction of the sublattice magnetizations may rotate in the (x, z) plane. When the sublattice magnetizations are parallel to the *z* axis, the free energy of the system is given by  $F_{\parallel} = -\chi_{\parallel} H^2/2 - K$ , where  $\chi_{\parallel}$  is the susceptibility along the *z* axis and *K* is the anisotropy energy. On the other hand, when the sublattice magnetizations lie in the (x,z) plane, the free energy is given by  $F_{\perp} = -\chi'_{\perp} H^2/2$ , where  $\chi'_{\perp}$  is the susceptibility along the *z* axis. The susceptibility  $\chi'_{\perp}$  is not the same as  $\chi_{\perp}$  which is the susceptibility along the *x* axis when **H** is applied along the *x* axis. At a critical field  $H_{SF}$  defined by

$$H_{SF} = [2K/(\chi'_{\parallel} - \chi_{\parallel})]^{1/2}, \qquad (3)$$

the free energy of the two states are equal  $(F_{\parallel} = F_{\perp})$ . Hence, for  $H < H_{SF}$ , the sublattice magnetizations are parallel to the *z* axis, whereas for  $H > H_{SF}$  the sublattice magnetizations lie in the (x,z) plane. The change for the parallel to the perpendicular orientation is called spin flopping. At T=0 K, we have  $\chi_{\parallel}=0$  from the definition. The susceptibility  $\chi'_{\perp}$  can be derived as follows. To this end we define the exchange fields  $\mathbf{H}_{E}^{(1)} = -A\mathbf{M}_{2}$  and  $\mathbf{H}_{E}^{(2)} = -A\mathbf{M}_{1}$  where  $|\mathbf{M}_{1}| = |\mathbf{M}_{2}| = M$ , Ais constant, and  $|\mathbf{H}_{E}^{(i)}| = H_{E}^{0} = AM$ . We also define the anisotropic field  $\mathbf{H}_{A}^{(i)} = (KM_{iz}/M^{2})\hat{z}$  (i=1,2) which is directed along the *z* axis. When  $\theta$  is the angle between  $\mathbf{M}_{1}$  and the *x* axis, the anisotropic field is expressed by  $\mathbf{H}_{A}^{(i)} = H_{A}^{0} \sin \theta \hat{z}$ with  $H_{A}^{0} = K/M$ . The condition that the resultant magnetic field  $(\mathbf{H} + \mathbf{H}_{A}^{(i)} + \mathbf{H}_{E}^{(i)})$  should be parallel to  $\mathbf{M}_{i}$  leads to a relation

$$\tan \theta = \frac{H + H_A^0 \sin \theta - H_E^0 \sin \theta}{H_E^0 \cos \theta} \quad \text{or } \sin \theta = \frac{H}{2H_E^0 - H_A^0}.$$
 (4)

Then  $\chi'_{\perp}$  can be obtained as  $\chi'_{\perp} = (M_{1z} + M_{2z})/H$ =  $2M \sin \theta/H = 2M/(2H_E^0 - H_A^0) = 1/[A - K/(2M^2)]$ . Using this relation for  $\chi'_{\perp}$  in Eq. (3), the spin flop field  $H_{SF}$  can be expressed by  $H_{SF} = [H_A^0(2H_E^0 - H_A^0)]^{1/2}$ . The magnetic field  $H_s$  at which the net magnetization saturates is defined by Eq. (4) with  $\theta = \pi/2$ :  $H_s = 2H_E^0 - H_A^0$ . Since  $H_S^2 - H_{SF}^2 = 2(2H_E^0 - H_A^0)(H_E^0 - H_A^0)$ , the inequality  $H_{SF} < H_S$  holds valid only for  $H_E^0 > H_A^0$ . For  $H_E^0 < H_A^0$ , the metamagnetic transition occurs from the antiferromagnetic state to the ferromagnetic state at  $H = H_E^0$ , where  $F_{AF} = F_F$ . The free energy of the system is described by  $F_{AF} = -AM^2$  for the antiferromagnetic state and by  $F_F = AM^2 - 2HM$  for the ferromagnetic state.

For the spin-flop transition, the H-T diagram consists of an antiferromagnetic (AF) phase, a spin-flop (SF) phase, and a paramagnetic (P) phase [see Fig. 1(a)]. The boundary between the AF and SF phases is a first-order transition line, while the boundaries between the SF and P phases and between the AF and P phases are second-order transition lines. These three boundaries meet a critical point. For the metamagnetic transition, the H-T diagram consists of an AF phase and a P phase [see Fig. 1(b)]. The boundary between the AF and P phases is perfectly smooth at a critical point. The boundary at the high-T side above the critical point is a second-order transition line, while the boundary at the low-Tside below the critical point is a first-order transition line.



FIG. 1. (a) Schematic *H*-*T* diagram for the spin-flop transition  $(H_E^0 > H_A^0)$ . The second-order critical lines (P-AF, P-SF) (solid lines) meet the first-order spin-flop line (the dotted line) tangentially at a multicritical point.  $H_s = 2H_E^0 - H_A^0$  and  $H_{SF} = [H_A^0(2H_E^0 - H_A^0)]^{1/2}$ . (b) Schematic *H*-*T* diagram for metamagnetic transition  $(H_E^0 < H_A^0)$ . The second-order critical line (the solid line) meets the first-order line (the dotted line) at a critical point. (c) Experimental observation of a metamgnetic transition. *H* is an external magnetic field and  $H_i$  is an internal field defined by Eq. (5). The demagnetizing effect opens the coexistence line (P-AF) into a coexistence area of the AF phase and P phase [(AF+P) phase]. See the details in Sec. VI B.

Figure 1(c) shows the schematic H-T diagram for the metamagnetic transition experimentally observed. The applied field H is different from the internal field  $H_i$  by

$$H_i = H - NM(H_i), \tag{5}$$

where N is the demagnetizing factor of the system and  $M(H_i)$  is the magnetization as a function of  $H_i$ . See the detail of the *H*-*T* diagram in Sec. VI B. Typical examples of a spin-flop transition and a metamagnetic transition were reported for MnF<sub>2</sub> (Ref. 20) and FeCl<sub>2</sub>,<sup>8,9</sup> respectively.

## **IV. EXPERIMENTAL PROCEDURE**

We used a sample of a stage-1 CoCl<sub>2</sub> GIC with a stoichiometry of C<sub>5.63</sub>CoCl<sub>2</sub>. The density of this system is calculated as  $\rho_m = 2.06 \text{ g/cm}^3$ . The dimension of the sample used for the magnetic measurements was  $3 \times 4 \text{ mm}^2$  in the *c* plane and 0.2 mm in thickness along the *c* axis. The ac magnetic susceptibility and DC magnetization were measured using a SQUID magnetometer (Quantum Design, MPMS XL-5) with an ultra-low-field capability as an option. A field-cooled magnetization ( $M_{FC}$ ) was measured with decreasing *T* from 25 to 1.9 K with *H*, where the sample was annealed for 10 min at 30 K in the presence of *H* along the *c* plane before measurement. The *H* dependence of zero-field-cooled magnetization ( $M_{ZFC}$ ) at fixed *T* was measured with increasing *H* from 0 to 1 kOe, where the sample was cooled from 298 K to *T* at *H*=0 before the measurement. The dispersion ( $\chi'$ )



FIG. 2. *T* dependence of (a)  $\chi'$  and (b)  $\chi''$  for a stage-1 CoCl<sub>2</sub> GIC ( $0 \le H \le 70$  Oe). h = 50 mOe. f = 1 Hz.  $H \perp c$  (*c* is the *c* axis).  $h \perp c$ .

and absorption  $(\chi'')$  were measured with increasing *T* from 1.9 to 18 K in the presence of  $H (0 \le H \le 10 \text{ kOe})$ , where the frequency of the ac field was f=1 Hz and the amplitude of the ac field was h=50 mOe.

The in-plane resistivity  $\rho$  was measured by a conventional four-probe method using an external device control option of the SQUID magnetometer. Two pairs of gold wires as the current and voltage probes were attached to the sample by silver paste (4922N, du Pont). The current was supplied through the current probes by a Keithley type 224, programmable dc current source. The voltage generated across the voltage probes was measured by a Keithley 182 nanovoltmeter. The measurements of  $\rho$  were made with increasing *T* from 1.9 to 20 K and then with decreasing *T* from 20 to 1.9 K in the presence of H ( $0 \le H \le 10$  kOe) along the *c* plane.

# V. RESULT

We have measured the *T* dependence of  $\chi'$  and  $\chi''$  at *H* = 0 for a stage-1 CoCl<sub>2</sub> GIC, where h=50 mOe and frequency *f* is varied between 0.01 and 1000 Hz. The dispersion  $\chi'$  has a peak at 9.85 K independent of *f*, and a shoulder around 8 K. The absorption  $\chi''$  has a sharp peak at 9.9 K independent of *f*, and a broad peak at 7.59 K at *f* = 0.01 Hz. This broad peak in  $\chi''$  shifts to the high *T* side with increasing *f*: 8.0 K at f=1 kHz. Figures 2–4 show the *T* dependence of  $\chi'$  and  $\chi'''$  for a stage-1 CoCl<sub>2</sub> GIC in the presence of *H* along the *c* plane, where h=50 mOe and *f* 





FIG. 3. *T* dependence of (a)  $\chi'$  and (b)  $\chi''$  for a stage-1 CoCl<sub>2</sub> GIC (100 $\leq$   $H \leq$  500 Oe). h = 50 mOe. f = 1 Hz.  $H \perp c$ .  $h \perp c$ .

=1 Hz. The absorption  $\chi''$  has two peaks at 9.9 and 7.7 K at H=0. For convenience hereafter these peak temperatures of  $\chi''$  are defined as an upper critical temperature  $T_{cu}$  (= $T_N$  = 9.9 K) and a lower critical temperature  $T_{cl}$  (=7.7 K), respectively. Note that the peak temperature ( $T_N=9.9$  K) at H=0 shifts to 9.7 K even at H=1 Oe. Such a drastic shift of  $T_{cu}$  with H may be related to the symmetry breaking of XY anisotropy, but is not well understood at present. The peak height of  $\chi''$  at H=0 drastically decreases with increasing H. This peak becomes a shoulder above 6 Oe and disappears above 40 Oe. The peak at  $T_{cl}$  becomes broader with increasing H and disappears above 100 Oe, shifting to the high-T side with further increasing H.

In contrast, the dispersion  $\chi'$  has a peak at 9.85 K close to  $T_N$  and a broad shoulder around 8.5 K at H=0. The peak at 9.85 K shifts to the low-*T* side with increasing *H* (down to 3.1 K at H=2 kOe). The shoulder around 8.5 K changes into a peak only for  $5 \le H \le 20$  Oe. Another peak appears at *T* higher than 10.15 K above 700 Oe, shifting to the high-*T* side with further increasing *H*.

Figure 5(a) shows the *T* dependence of the field-cooled (FC) magnetization  $M_{FC}$  along the *c* plane. The magnetization  $M_{FC}$  was measured with decreasing *T* from 20 to 1.9 K in the presence of *H* along the *c* plane. The magnetization  $M_{FC}$  shows a peak around  $T_N$  for  $H \leq 300$  Oe, but it increases with decreasing *T* for  $H \geq 400$  Oe. Figure 5(b) shows the *T* dependence of  $dM_{FC}/dT$  for various *H*'s. At H = 5 Oe,  $dM_{FC}/dT$  has two local minima at 8.48 and 10.01

FIG. 4. *T* dependence of (a)  $\chi'$  and (b)  $\chi''$  for a stage-1 CoCl<sub>2</sub> GIC (1 $\leq$ *H* $\leq$ 5 kOe). *h*=50 mOe. *f*=1 Hz. *H* $\perp$ *c*. *h* $\perp$ *c*.

K, and a local maximum at 9.20 K. This local maximum shifts to the low T side with increasing H and disappears above 300 Oe.

Figure 6(a) shows the *H* dependence of the zero-fieldcooled (ZFC) magnetization  $M_{ZFC}$  along the *c* plane at fixed *T*. First the sample was cooled from 298 K to *T* at H=0. Then  $M_{ZFC}$  at *T* was measured with increasing *H* from 0 to 1 kOe. In Fig. 6(b) we show the *H* dependence of  $dM_{ZFC}/dH$  at each *T*, which is obtained from Fig. 6(a). The derivative  $dM_{ZFC}/dH$  for T=4.5 K shows a sharp peak at a low field  $H_l=15$  Oe and a broad peak at a high field  $H_u$ = 375 Oe. The value of  $H_u$  is almost the same as that of the peak field of  $\chi'(H)$  reported by Nicholls and Dresselhaus.<sup>3</sup> The lower field  $H_l$  decreases with increasing *T* and reduces to zero around  $T_{cl}$ . In contrast, the higher field  $H_u$  decreases with increasing *T* and reaches 300 Oe at 8.5 K. It tends to reduce to zero around  $T_N$ .

Figure 7(a) shows the *T* dependence of the normalized in-plane resistivity  $\rho/\rho_0$  for a stage-1 CoCl<sub>2</sub> GIC at various *H*'s along the *c* plane, where  $\rho_0$  is the in-plane resistivity at *H*=2 kOe and *T*=2*K*. The in-plane resistivity in the presence of *H* is measured with increasing *T* from 1.9 to 20 K  $[\rho(T\uparrow)]$  and with decreasing *T* from 20 to 1.9 K  $[\rho(T\downarrow)]$ . We note that the value of  $\rho(T\downarrow)$  is smaller than  $\rho(T\uparrow)$  below a characteristic temperature  $T_0$  for 350<*H*<700 Oe, showing an irreversible effect of in-plane resistivity. The value of  $T_0$  is dependent on *H*. Figure 7(b) shows the *T* dependence of  $d(\rho/\rho_0)/dT$ . The *T* derivative  $d(\rho/\rho_0)/dT$  shows a local minimum at 9.4 K at *H*=0. This negative peak shifts



FIG. 5. T dependence of (a)  $M_{FC}$  and (b)  $dM_{FC}/dT$  at various H's for a stage-1 CoCl<sub>2</sub> GIC.  $H \perp c$ .

to the low-T side with increasing H, and disappears above 650 Oe.

#### VI. DISCUSSION

## A. Overview of the *H*-*T* diagram

We have determined the H-T diagram of a stage-1 CoCl<sub>2</sub> GIC. Figure 8 shows the overall H-T diagram of a stage-1 CoCl<sub>2</sub> GIC. Since the antiferromagnetic interplanar exchange interaction is very weak, the entire phase diagram is accessible below 2 kOe. Figures 9(a)-9(d) show simplified H-T diagrams for several regions in the (T,H) plane. In Figs. 8 and 9 the peak temperatures for  $\chi'$  vs T and  $\chi''$  vs T with f=1 Hz and h=50 mOe are denoted by open and closed circles for each H, respectively. The peak field of  $dM_{ZFC}/dH$  vs H are denoted by open squares for each T. The local-maximum and local-minimum temperatures of  $dM_{FC}/dT$  vs T are denoted by closed triangles for each H, respectively. local-minimum The temperatures of  $d(\rho/\rho_0)/dT$  vs T are denoted by crosses. In Fig. 9(a), for comparison, we also show the H-T diagram obtained by Nicholls and Dresselhaus,<sup>3</sup> where the peak field of  $\chi'$  vs *H* is denoted by open diamonds for each T. We note that the peak field of  $\chi'(H)$  is in good agreement with that of  $dM_{ZFC}/dH$ vs H.

For convenience, the phase boundaries are denoted by the lines  $H_{ci}$  (i=1-7),  $H_c$ ,  $H_+$ ,  $H_-$ . The nature of these lines will be discussed in Secs. VI B and VI C. The features of the H-T diagram shown in Figs. 8 and 9 are summarized as



FIG. 6. *H* dependence of (a)  $M_{ZFC}$  and (b)  $dM_{ZFC}/dH$  at various *T*'s for a stage-1 CoCl<sub>2</sub> GIC.  $H \perp c$ .

follows. (i) A metamagnetic transition occurs at a critical point ( $T_3 = 8.77$  K,  $H_3 = 270$  Oe), which is the intersection of the lines  $H_{c4}$ ,  $H_{c5}$ ,  $H_{c7}$ , and  $H_c$ . The lines  $H_{c4}$  and  $H_{c5}$ denote the phase boundaries from the AF phase to the P phase via a mixed phase (AF+P). The region above the boundary  $H_{c5}$  is the P phase:  $H_{c5} \approx 1.7$  kOe at 3.3 K. (ii) The line  $H_c$  connecting between the two points  $[(T_N, H=0)]$  and  $(T_3, H_3)$ ] is a second-order line. (iii) The line  $H_{c5}$  smoothly joins to the line  $H_{c7}$  at the critical point  $(T_3, H_3)$ . The line  $H_{c7}$  intersects with the T axis at  $T'_N$  (=9.25 K) below  $T_N$ . (iv) The local minimum of  $d(\rho/\rho_0)/dT$  occurs only near the lines  $H_{c7}$  and  $H_{c5}$ . (v) At high temperatures above  $T_N$  there are two lines denoted by  $H_+$  and  $H_-$ :  $H_+=7$  kOe at 16.56 K and  $H_{-}=10$  kOe at 15.45 K. Line  $H_{-}$  seems to originate from a point  $(T_N, H=0)$ . The origin of lines  $H_+$  and  $H_-$  is due to ferromagnetic short-range fluctuations which is noncritical. Similar lines are observed in the paramagnetic region of (T,H) plane in FeBr<sub>2</sub>.<sup>10-14</sup> The discussion on these lines was given in Ref. 10. (vi) A spin-flop transition occurs at a critical point ( $T_1 \approx 7.6$  K,  $H_1 \approx 7$  Oe) [see the inset of Fig. 9(c)], which is the intersection of the lines  $H_{c1}$  and  $H_{c2}$ . (vii) A spin-flop transition occurs at a critical point  $(T_2 \approx 6.8 \text{ K}, H_2 \approx 80 \text{ Oe})$ , which is the intersection of the lines  $H_{c2}$  and  $H_{c3}$  [see Fig. 9(a)]. (viii) A spin-flop transition may occur at a critical point ( $T_4 \approx 9.3$  K,  $H_4 \approx 7$  Oe) [see Fig. 9(d).

#### B. Spin-flop transition and metamagnetic transition

We discuss the nature of the spin-flop transition at the critical point  $(T_2, H_2)$  and the metamagnetic transition at the





FIG. 8. Overview of the *H*-*T* diagram for a stage-1 CoCl<sub>2</sub> GIC, which is determined from the *T* dependence of  $\chi'(\bigcirc), \chi''(\bigcirc)$ , and  $dM_{FC}/dT(\bigtriangleup)$ , and the *H* dependence of  $dM_{ZFC}/dH(\Box)$ .  $H(\bot_c, c$  is the *c* axis) is the value of external field. Lines  $H_c$ ,  $H_{c3}$ ,  $H_{c4}$ ,  $H_{c5}$ , and  $H_{c7}$  are the phase boundaries. The coordinates  $(T_3, H_3)$  and  $(T_2, H_2)$  are critical points. Lines  $H_-$  and  $H_+$  are due to ferromagnetic short-range fluctuations.

FIG. 7. *T* dependence of normalized in-plane resistivity  $\rho/\rho_0$  for a stage-1 CoCl<sub>2</sub> GIC for various *H*'s, which is measured with increasing *T* and decreasing *T* between 1.9 and 20 K.  $\rho_0$  is the inplane resistivity at H=2 kOe and T=2 K.  $H\perp c$ . (b) *T* dependence of  $d(\rho/\rho_0)/dT$  for various *H*'s, where  $\rho$  is obtained from the measurement with decreasing *T*.

critical point  $(T_3, H_3)$  [see Fig. 9(a)]. In a stage-1 CoCl<sub>2</sub> GIC, three competing fields  $H_A^{in}$ ,  $H'_E$ , and  $H_A^{out}$  contribute to the field-induced transitions. Since  $H \ll H_A^{out}$ , the direction of spins along the *c* axis is energetically unfavorable. In this sense the field transitions have a *XY* character. As described in Sec. III, the competition between two fields  $H_E^0 = H'_E$  and  $H_A^0 = H_A^{in}$  ( $H'_E \gg H_A^{in}$ ) leads to a spin-flop transition at the critical point ( $T_2$ ,  $H_2$ ) [see Fig. 1(a)]. The spin-flop transition between the AF and SF phases is of first order. Line  $H_{c2}$ meets line  $H_{c3}$  tangentially at the critical point ( $T_2$ ,  $H_2$ ). Note that the boundary between the SF and AF phases is not observed in the present work, partly because of the first-order transition. The spin-flop field at T=0 K can be described by

$$H_2 = [(2H'_E - H^{in}_A)H^{in}_A]^{1/2} \approx (2H'_E H^{in}_A)^{1/2}.$$
 (6)

The transition between the SF and P phases, which is of second order, occurs on the line  $H_{c3}$ :  $H_{c3}=2H'_E-H^{in}_A\approx 2H'_E$ . In Fig. 9(a) we find  $H_2=80$  Oe at  $T_2=6.8$  K and  $H_{c3}=500$  Oe at T=6.14 K.

In contrast, the competition between two fields  $H_E^0 = H_E'$ and  $H_A^0 = H_A^{out}$  ( $H_E' \ll H_A^{out}$ ) leads to the metamagnetic transition at the critical point ( $T_3$ ,  $H_3$ ). As described in Sec. III, there is a first-order transition line between the AF phase and the P phase [see Fig. 1(b)]. This line persists up to the critical point ( $T_3$ ,  $H_3$ ) from T = 0 K, and joins smoothly on to a second-order line. On the first-order transition line, the magnetization M discontinuously changes from 0 to the saturation magnetization  $M_s$  corresponding to that of the ferromagnetic phase. In real systems, because of the geometry the internal magnetic field  $H_i$  is no longer equal to the external magnetic field H<sup>8</sup> and is given by Eq. (5). The demagnetizing effects open the coexistence line into a coexistence area of AF and P phases [the (AF+P) phase] for the corresponding plot in the (T-H) plane, where the two phases coexist in varying proportions [see Fig. 1(c)]. As shown in Fig. 9(a) for a stage-1 CoCl<sub>2</sub> GIC, line  $H_{c4}$  is the boundary between the AF phase and (AF+P) phase and line  $H_{c5}$  is the boundary between the (AF+P) phase and the P phase. The values of  $H_{c4}$  and  $H_{c5}$  are described by  $H_{c4} = H'_E$  and  $H_{c5} = H'_E$  $+N\Delta M_s$ , where  $\Delta M_s = \Delta M_a \rho_m / W$ ,  $\Delta M_a$  (in units of emu/ Co mol) is the change of the measured magnetization at Tbetween lines  $H_{c4}$  and  $H_{c5}$ ,  $\rho_m$  (=2.06 g/cm<sup>3</sup>) is the density, and W (=197.46 g/Co mol) is the gram weight of the system per Co mole. Experimentally we have  $H_{c4} \approx 350$  Oe and  $H_{c5} \approx 1000$  Oe at T = 6 K. From Fig. 6(a) we have  $M_a$ =9788 (emu/Co mol) at  $H_{c5}$  and  $M_a$ =4320 (emu/Co mol) at  $H_{c4}$  for T=6 K, leading to  $\Delta M_a = 5468$  (emu/Co mol) or  $\Delta M_s = 57.0$  emu/cm<sup>3</sup>. Then the demagnetization factor can be estimated as N = 11.4 ( $N/4\pi = 0.9$ ), which is much larger than that predicted from the geometry of the sample. Such a large N is partly due to the fact that our sample is highly nonellipsoidal in shape, thus giving rise to a large distribution in internal fields.

From Fig. 9(a) we find  $H_{c4}=375$  Oe at T=4.5 K, indicating that  $H'_{E}\approx375$  Oe. This value of  $H'_{E}$  is in good agreement with that ( $H'_{E}=380$  Oe) reported by Nicholls and Dresselhaus.<sup>3</sup> Using Eq. (6) with  $H'_{E}=375$  Oe and  $H_{2}$ 



=80 Oe, we obtain  $J' = 2.7 \times 10^{-2}$  K and  $H_A^{in} = 8.5$  Oe. The ratio J'/J is calculated as  $3.5 \times 10^{-3}$ , which is much larger than that  $(J'/J = 1.8 \times 10^{-4})$  for a stage-2 CoCl<sub>2</sub> GIC, where J = 7.75 K and  $J' = 1.40 \times 10^{-3}$  K. In Figs. 9(a) and 9(b) we make a plot of the peak temperature of  $d(\rho/\rho_0)/dT$  vs *T* for each *H*, showing a line denoted by  $H_\rho$ . This line is located near line  $H_{c7}$  below  $H_3$  and near line  $H_{c5}$  above  $H_3$ . As shown in Fig. 7(a), the resistivity  $\rho$  for  $H < H_3$  shows no hysteresis on crossing line  $H_\rho$ . The value of  $\rho$  measured with increasing *T* is the same as that with decreasing *T*. In contrast, the resistivity  $\rho$  for  $350 \le H \le 700$  Oe shows a hysteresis that the transition in line  $H_\rho$  is of first order at least for  $350 \le H \le 700$  Oe.

In Fig. 9(b) we show the *T* dependence of lines  $H_c$  and  $H_{c7}$ . The dispersion  $\chi'$  shows a maximum on crossing line  $H_c$  and  $dM_{FC}/dT$  has a local maximum on crossing line  $H_{c7}$ . The *T* dependence of lines  $H_c$  and  $H_{c7}$  is described by<sup>20</sup>

$$H^2 = \alpha (T_c - T), \tag{7}$$

with  $\alpha = (7.87 \pm 0.02) \times 10^4$  (Oe<sup>2</sup>/K) and  $T_c = 9.71 \pm 0.05$  K ( $\approx T_N$ ) for line  $H_c$  ( $8.9 \leq T \leq 9.7$  K) and  $\alpha = (1.13 \pm 0.03) \times 10^5$  (Oe<sup>2</sup>/K) and  $T_c = 9.25 \pm 0.03$  K ( $= T'_N$ ) for line  $H_{c7}$  ( $8.4 \leq T \leq 9.3$  K). For convenience  $T'_N$  is defined as a temperature where line  $H_{c7}$  intersects with the *T* axis. Note that line  $H_{c7}$  may correspond to a line observed in FeBr<sub>2</sub> which results from a decomposition of the tricritical point into a critical end point and a bicritical end point.<sup>10–14</sup> The corresponding line in FeBr<sub>2</sub> is of first order, while line  $H_{c7}$  in a stage-1 CoCl<sub>2</sub> GIC may be of second order. At present, the nature of the phase between lines  $H_c$  and  $H_{c7}$  is not clear.

FIG. 9. (a) H-T diagram related to the metamagnetic transition at the critical point  $(T_3, H_3)$ and the spin-flop transition at the critical point  $(T_2, H_2)$ . The data denoted by open diamonds are taken from Nicholls and Dresselhaus (Ref. 3). The solid lines are guides to the eye. (b) H-Tdiagram near  $T_N$  below 400 Oe. Lines  $H_c$ ,  $H_{c5}$ , and  $H_{c7}$  are the phase boundaries. On line  $H_{\rho}$ (×),  $d(\rho/\rho_0)/dT$  shows an anomaly. The solid lines at low H are the least-squares fits of the data to Eq. (7).  $T_N = 9.9$  K and  $T'_N = 9.25$  K. (c) H-Tdiagram near  $T_{cl}$  below 20 Oe. Lines  $H_{c1}$  and  $H_{c2}$  are the phase boundaries. The coordinate  $(T_1, H_1)$  is a critical point. (d) *H*-*T* diagram near  $T_N$  below 32 Oe. The lines  $H_c$ ,  $H_{c6}$ , and  $H_{c7}$  are the phase boundaries. The coordinate  $(T_4, H_4)$  is a critical point.

We also note that the spin-flop transition at the critical point  $(T_3, H_3)$  in a stage-1 CoCl<sub>2</sub> GIC is similar to that in FeCl<sub>2</sub>  $(T_N=23.6 \text{ K})$  at the tricritical point  $(T_t=21.15 \text{ K}, H_t = 10.2 \text{ kOe})$ ,<sup>8,9</sup> where *H* is applied along the *c* axis. The ratio  $T_3/T_N$  (=0.869) for a stage-1 CoCl<sub>2</sub> GIC is nearly equal to the ratio  $T_t/T_N$  (=0.896) for FeCl<sub>2</sub>. The only difference is the spin symmetry: *XY*-like for a stage-1 CoCl<sub>2</sub> GIC, and Ising-like for FeCl<sub>2</sub>. In a layer of Fe<sup>2+</sup> ions in FeCl<sub>2</sub> all spins lie parallel to each other and normal to the layer.

# C. Other field-induced transitions

As shown in Figs. 9(c) and 9(d), we find two spin-flop transitions at critical points ( $T_1 \approx 7.6$  K,  $H_1 \approx 7$  Oe) and  $(T_4=9.3 \text{ K}, H_4=7 \text{ Oe})$ . The origin of the transition at  $(T_4, H_4)$  is not clear at present. Here we discuss only the nature of the spin-flop transition at the critical point  $(T_1,$  $H_1$ ). The lines  $H_{c1}$  and  $H_{c2}$  meet at the critical point. Since  $H_{c2}$  is much lower than  $2H'_E$  and  $H_1$  is lower than  $H_A^{in}$ , the fields  $H'_E$  and  $H^{in}_A$  do not contribute to this transition. One possibility is that this transition may be associated with that of a stage-2 CoCl<sub>2</sub> GIC which is contained as a minor phase. In fact, as shown in Figs. 6(b) and 8, the derivative  $dM_{ZFC}/dH$  shows a small sharp peak at low H for T  $\leq$ 7 K: typically H=15 Oe at T=4.5 K. It is believed that such a transition at low H is due to the stage-2 contribution.<sup>3</sup> We assume that the spin-flop transition may be caused by the competition between an antiferromagnetic interplanar interaction field  $H''_E$  and an in-plane anisotropic field  $(H^{in}_A)'$  for a stage-2 CoCl<sub>2</sub> GIC. Then the critical field  $H_1$  and field  $H_{c2}$ are described by  $H_1 = \{ [2H''_E - (H^{in}_A)'](H^{in}_A)' \}^{1/2}$  and  $H_{c2}$  $=2H_E''-(H_A^{in})'$ . If  $H_1=7$  Oe and  $H_{c2}\approx 20$  Oe, we obtain  $H''_E = 11.2$  Oe and  $(H^{in}_A)' = 2.45$  Oe. The characteristic field  $(H^{in}_A)'$  for the stage-2 system is relatively lower than  $H^{in}_A$  for the stage-1 system. We note that the ratio  $H''_E/H'_E$  is equal to 0.03, where  $H''_E$  is related to an antiferromagnetic interplanar interaction J" through  $H''_E = 2z'J''S/(g_a\mu_B)$ . Then the ratio J''/J can be calculated as  $1.03 \times 10^{-4}$ , which is on the same order as that for the stage-2 CoCl<sub>2</sub> GIC. As shown in Fig. 8, we find anomalies in  $\chi'$  and  $dM_{FC}/dT$  around T = 8.4 K and  $H \approx 0$  in the (T, H) plane: (i) the peak of  $\chi'$  vs T for 8.25  $\leq T \leq 8.5$  K and  $5 \leq H \leq 20$  Oe, and (ii) the local minimum of  $dM_{FC}/dT$  vs T for 8.2 < T < 8.65 K and  $5 \leq H \leq 100$  Oe. Such anomalies are also due to the contribution from a stage-2 CoCl<sub>2</sub> GIC. In fact, the dispersion  $\chi'$  of a stage-2 CoCl<sub>2</sub> GIC at f = 1 Hz has a peak at 8.40 K in the absence of  $H^{.21}$ 

## **D.** Nature of the low-temperature phase below $T_{cl}$

It is interesting to compare the critical temperatures of a stage-1 CoCl<sub>2</sub> GIC with those of a stage-2 CoCl<sub>2</sub> GIC. It is known that a stage-2 CoCl<sub>2</sub> GIC magnetically behaves like a quasi-2D XY ferromagnet with an extremely weak antiferromagnetic interplanar exchange interaction. This compound undergoes two magnetic phase transitions at  $T_{cu}$  and  $T_{cl}$ . These two critical temperatures are identified as peak temperatures of  $\chi''$  with f=1 Hz at H=0:  $T_{cu}=8.9$  K and  $T_{cl}=6.9$  K.<sup>21</sup> We find a noticeable increase in  $T_{cu}$  and  $T_{cl}$  as the stage number decreases from stage 2 to stage 1. The magnitude of antiferromagnetic interplanar interactions drastically increases as a result of the reduction of the c-axis repeat distance from 12.73 to 9.38 Å, leading to the change of dimension of the system from 2D-like to 3D-like. We note that the ratio  $T_{cu}/T_{cl}$  (=1.286) for a stage-1 CoCl<sub>2</sub> GIC is almost the same as that (=1.290) for a stage-2 CoCl<sub>2</sub> GIC, where  $T_{cu}$  (= $T_N$ =9.9 K) and  $T_{cl}$ =7.7 K for a stage-1  $\operatorname{CoCl}_2$  GIC. The ratio of  $T_{cu}$  of a stage-1 GIC to  $T_{cu}$  of a stage-2 GIC (=1.112) is almost the same as the ratio of  $T_{cl}$ of a stage-1 GIC to  $T_{cl}$  of a stage-2 GIC (=1.116). These results may suggest that the mechanism of spin ordering at H=0 is similar between stage-1 and stage-2 CoCl<sub>2</sub> GIC's.

Nevertheless, the spin order in a stage-1 CoCl<sub>2</sub> GIC is rather different from that in a stage-2 CoCl<sub>2</sub> GIC. In a stage-2 CoCl<sub>2</sub> GIC, the antiferromagnetic long-range spin order is established below  $T_{cl}$ , while in a stage-1 CoCl<sub>2</sub> GIC the 3D antiferromagnetic spin order is already established below  $T_N$ . What is the nature of the low-temperature phase below  $T_{cl}$  in stage-1 CoCl<sub>2</sub> GIC? Since  $H_A^{in}$  plays an important role for the spin-flop transition at  $(T_2, H_2)$ , it is expected that the spin structure at H=0 below  $T_{cl}$  arises from the competition between  $H'_E$  and  $H'_A$ . This problem is reduced to the 1D antiferromagnetic XY chain with in-plane sixfold anisotropy. When  $H_A^{in}$  is much smaller than  $H_E'$ , an usual AF state is energetically favorable. However, when  $H_A^{in}$ is not negligibly small compared to  $H'_E$ , the ordered phase is different from the usual AF phase. In fact, the spin structure as a function of the ratio  $H_A^{in}/H_E'$  can be determined from the minimum condition of the Landau free energy derived by Szeto and Dresselhaus.<sup>17</sup>

## VII. CONCLUSION

We have determined the H-T diagram of a stage-1 CoCl<sub>2</sub> GIC. Because of extremely weak antiferromagnetic interplanar exchange interactions the entire H-T phase diagram is accessible below 2 kOe. The H-T diagram includes a metamagnetic transition and several spin-flop transitions, which arise from competitions between antiferromagnetic interplanar interactions and in-plane anisotropic interactions. The H-T diagram at very low H is complicated by the possible existence of a stage-2 CoCl<sub>2</sub> GIC as a minority phase. In order to obtain a deeper understanding of the H-T diagram of a stage-1 CoCl<sub>2</sub> GIC, a determination of spin structures is required using neutron-scattering experiments in the presence of H along the c plane.

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