Phase diagram of the relaxor ferroelectric $(1-x)Pb(Zn_{1/3}Nb_{2/3})O_3-xPbTiO_3$

D. La-Orauttapong,¹ B. Noheda,² Z.-G. Ye,³ P. M. Gehring,⁴ J. Toulouse,¹ D. E. Cox,² and G. Shirane²

Department of Physics, Lehigh University, Bethlehem, Pennsylvania 18015

²Brookhaven National Laboratory, Upton, New York 11973

³Department of Chemistry, Simon Fraser University, Burnaby, British Columbia, Canada V5A 1S6

⁴NIST Center for Neutron Research, NIST, Gaithersburg, Maryland 20899

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Recently, a new orthorhombic phase has been discovered in the ferroelectric system $(1 - x)Pb(Zn_{1/3}Nb_{2/3})O_3-xPbTiO_3$ (PZN-*x*PT) for x=9%, and for x=8% after the application of an electric field. In the present work, synchrotron x-ray measurements have been extended to higher concentrations $10\% \le x \le 15\%$. The orthorhombic phase was observed for x=10%, but, surprisingly, for $x \ge 11\%$ only a tetragonal phase was found down to 20 K. The orthorhombic phase thus exists only in a narrow concentration range with near-vertical phase boundaries on both sides. This orthorhombic symmetry (M_C type) is in contrast to the monoclinic M_A -type symmetry recently identified at low temperatures in the Pb($Zr_{1-x}Ti_x$)O₃ (PZT) system over a triangle-shaped region of the phase diagram in the range x=0.46-0.52. To further characterize this relaxor-type system, neutron inelastic scattering measurements have also been performed on a crystal of PZN-*x*PT with x=15%. The anomalous soft-phonon behavior ("waterfall" effect) previously observed for x = 0% and 8% is clearly observed for the 15% crystal, which indicates that the presence of polar nanoregions extends to large values of x.

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I. INTRODUCTION

Recently, a number of studies have attempted to understand the origin of the very large piezoelectric coefficients measured in perovskite oxides such as $Pb(Zr_{1-r}Ti_r)O_3$ (PZT) and $(1-x)Pb(Zn_{1/3}Nb_{2/3})O_3-xPbTiO_3$ (PZN-xPT) near the morphotropic phase boundary (MPB). The MPB is an almost vertical phase boundary that separates the rhombohedral (R) and the tetragonal (T) regions of the phase diagram of these systems (temperature versus x). In a study of PZN-8%PT, Park and Shrout found the piezoelectric coefficient d₃₃ to exceed 2500 pC/N and strain levels reaching 1.7% induced by a field applied along [001].¹ These ultrahigh values are an order of magnitude greater than those previously attainable in conventional piezoelectric and electrostrictive ceramics including PZT, currently the material of choice for high-performance actuators. Several experimental and theoretical studies now indicate that these very high values are related to the presence of a particular phase.

X-ray investigations by Noheda et al.² and Cox et al.³ have shown that, in addition to the known rhombohedral and tetragonal phases, a sliver of a new phase exists in the phase diagram near the MPB as shown in Fig. 1 for PZT (Ref. 2) and PZN-xPT (Ref. 3), respectively. In the PZT system, the newly identified lower-symmetry phase is of monoclinic M_A type (space group Cm) for $0.46 \le x \le 0.52^{2}$, while in PZN-*x*PT an orthorhombic (*O*) phase (space group *Bmm*2) has been irreversibly induced by a field in an 8%PT crystal^{4,5} and has also been observed in a polycrystalline sample prepared from a previously poled crystal of 9% PT.³ This O phase is the limiting case of a monoclinic M_C -type phase (space group Pm) when the lattice parameters a and c become equal. A true M_c phase (with $a \neq c$) is observed in PZN-8%PT during the application of an electric field.⁴ Very recently, Uesu *et al.*⁶ have also observed a true M_C phase in 9% PT following an examination of several unpoled (asgrown) as well as poled crystals with nominally the same 9% concentration. Most of these were orthorhombic O but one of the unpoled crystals showed a definite monoclinic M_C distortion. This raises the very interesting possibility that, for slightly higher concentrations (e.g., 10%-12% PT), the ground state is actually M_C , so that the orthorhombic 9% PT phase might logically be regarded as the end member of the M_C region. However, as described below, the 10% PT phase has been found to be unequivocally orthorhombic (a=c), while unexpectedly a tetragonal phase is realized at 11% PT, yielding a narrow "chimneylike" shape for the intermediate orthorhombic region.

A low-symmetry phase discovered in both PZT and PZN*x*PT in the vicinity of the MPB appears to be a common feature of the highly piezoelectric perovskite systems. Recently, Vanderbilt and Cohen⁷ (VC) have provided a natural explanation for these recently discovered new phases in both PZT and PZN-*x*PT systems by extending the Devonshire theory to eighth order. This study yields a new phase diagram for ferroelectric perovskites that includes three different types of monoclinic phases M_A , M_B , and M_C (named after this work).

The effect of an applied electric field on the polarization has also been studied theoretically and experimentally. A polarization rotation mechanism has been proposed by Fu and Cohen⁸ to explain the ultrahigh electromechanical response found in PZN-*x*PT using BaTiO₃ as a model. According to their model, the application of an electric field along the [001] direction in rhombohedral PZN-*x*PT induces a rotation of the polarization vector in a (110) plane, from the rhombohedral to the tetragonal axis (i.e., $R-M_A-T$). However, an experimental x-ray study by Noheda *et al.* on as-grown PZN-*x*PT crystals has suggested that, as the applied electric field is increased, the polarization vector first follows this



FIG. 1. Phase diagrams for PZT (bottom) and PZN-*x*PT (top) in the vicinity of their respective MPB's, as shown in Ref. 3.

 $R-M_A-T$ path, but then abruptly jumps to a new path, in a plane containing the orthorhombic and tetragonal polar axes (i.e., $R-M_A-M_C-T$).⁴ As the field is decreased the polarization rotates from the tetragonal [001] to the orthorhombic [101] polar directions, via the M_C phase, and the initial rhombohedral state is not recovered upon removal of the field. Recently this irreversible $R-M_A-M_C-T$ polarization path has been confirmed by neutron diffraction.⁹ First-principles calculations by Bellaiche *et al.* for the rhombohedral PZT system under a [001] field also predict the $R-M_A-M_C-T$ transformation, although in this case the transformation is found to be reversible.¹⁰

With ample experimental and theoretical evidence^{11,12} for a link between the very high values of the piezoelectric and electrostrictive coefficients and the presence of a new phase, it has become essential to determine its extent in the phase diagram of PZN-*x*PT. As mentioned above, PZN-8%PT shows the expected rhombohedral symmetry and becomes orthorhombic only after a high field has been applied, whereas PZN-9%PT clearly shows the orthorhombic symmetry (M_C with a=c) even with no external field.^{3,6} In the present paper, we have studied higher PT concentrations ($10\% \le x \le 15\%$), using high-resolution synchrotron x-ray powder diffraction. For further characterization of these relaxor systems, neutron inelastic scattering measurements have also been performed on the 15% PT crystal. The specific goal of the inelastic measurements was to investigate the possible existence, at higher PT concentrations, of the "waterfall" shape previously observed in the soft optic mode phonon branch at lower PT concentrations.^{13,14}

II. EXPERIMENT

Single crystals of a $(1-x)Pb(Zn_{1/3}Nb_{2/3})O_3-xPbTiO_3$ solid solution system with x = 10%, 11%, 12%, and 15% were grown by a top-seeded solution growth (TSSG) technique using a PbO flux with an optimum flux ratio of 50 wt %.¹⁵ Platelets of about 1 mm thick and 7–15 mm² in area were cut parallel to the reference $(001)_{cub}$ plane and polished with fine diamond paste (down to 1 μ m). The (001)_{cub} faces were covered with sputtered gold layers and Au wires were attached by means of Ag paste. The poling was performed under a field of 20 kV/cm that was applied along $[001]_{cub}$ at 210 °C (above T_C) and maintained while cooling down to room temperature. The samples were then short-circuited for 30 min before the electrodes were removed. For neutron inelastic scattering studies, a bigger PZN-15%PT crystal of 2.17 g in weight and 0.27 cc in volume was cut from an as-grown crystal boule with natural $(100)_{cub}$ faces as a reference orientation.

Two types of high-resolution synchrotron x-ray powder diffraction measurements were carried out on beamline X7A at the Brookhaven National Synchrotron Light Source (NSLS) with x rays from a Si(111) double-crystal monochromator. For the first set of measurements, an incident beam of wavelength ~ 0.7 Å was used and a linear position-sensitive detector was placed in the diffracted beam path. This configuration gives greatly enhanced counting rates and allows accurate data to be collected from very narrow-diameter capillary samples. The use of capillary samples helped eliminate systematic errors due to preferred orientation or texture effects. With this configuration the resulting instrumental resolution was $\sim 0.03^{\circ}$ on the 2θ scale. For the second set, incident beams of wavelengths ~ 0.69 Å and ~ 0.98 Å were used with a flat Ge (220) crystal analyzer and scintillation detector. With this type of diffraction geometry, it is not always possible to eliminate preferred orientation and texture effects, but the peak positions, on which the present results are based, are not affected. The resulting instrumental resolution is better than 0.01° on a 2θ scale, an order of magnitude better than that of a laboratory instrument.

The powder samples were prepared by chopping out small fragments from the poled crystals, crushing them, and loading them in a 0.2-mm-diameter glass capillary, as explained in Ref. 3. A closed-cycle cryostat was used for the temperature dependence measurements. The data sets were collected from 15 to 500 K and the sample was rocked $\sim 2^{\circ}-3^{\circ}$ during the data collection, in order to achieve powder averaging.

A subsequent neutron inelastic scattering study was performed on the PZN-15%PT single crystal using both the BT2 and BT9 triple-axis spectrometers at the NIST Center for Neutron Research (NCNR). The (002) reflections of highly oriented pyrolytic graphite (HOPG) crystals were used for both monochromator and analyzer. A HOPG transmission filter was used to eliminate higher-order neutron wavelengths. These measurements were made in the phonon creation



FIG. 2. Diffraction patterns of pseudocubic (111), (200), and (220) for PZN-*x*PT for x = 10% (left) at 20 K and x = 11% (right) at 15 K, showing the diffraction spectra for the orthorhombic and tetragonal phases.

mode with a fixed final energy of 14.7 meV ($\lambda_f = 2.36$ Å) while varying the incident neutron energy E_i . The horizontal beam collimation used was 40'-40'-S-40'-open and 40'-20'-S-20'-80'. The crystal was mounted on a boron nitride cylinder held in a goniometer and oriented with its [001] axis vertical, thereby giving access to the (HK0) scattering zone. It was then loaded into a vacuum furnace capable of reaching temperatures up to 670 K. Data were collected in the temperature range 200–650 K using two types of scans. First, constant-energy scans were performed by keeping the energy transfer $\hbar \omega = E_i - E_f$ fixed while varying the momentum transfer \vec{Q} . Second, constant- \vec{Q} scans were performed by holding the momentum transfer $\vec{Q} = \vec{k}_i - \vec{k}_f (k$ $= 2\pi/\lambda$) fixed and varying the energy transfer ΔE .

III. PHASE DIAGRAM FOR PZN-XPT

Based on the diffraction data reported in the previous study³ on a polycrystalline sample of PZN-*x*PT with x = 9%, a modification of the PZN-*x*PT phase diagram has been proposed which includes the new orthorhombic phase (*O*) around its MPB shown in Fig. 1. However, the proposed stability region for the new *O* phase is limited so far to only one composition. In the present work, we have determined the full extent of the *O* phase by studying higher concentrations x = 10%, 11%, 12%, and 15%. The results obtained



FIG. 3. Temperature dependence of the lattice parameters for PZN-*x*PT (x=10%) from 15 K to 375 K, for the orthorhombic (a_o , b_o , and c_o) and tetragonal (a_t and c_t) phases.

give a comprehensive picture of the new orthorhombic phase in the PZN-*x*PT phase diagram.

As will be seen later, one of the key features of this study is the rather unexpected finding that compositions with x \geq 11% retain tetragonal symmetry down to 20 K. This can be seen in Fig. 2, in which selected regions of the diffraction profiles are plotted for x = 10% (left) and x = 11% (right) at 20 and 15 K, respectively, showing very distinctive features for these two adjacent compositions. From the splitting and relative intensities of these profiles the symmetry of the samples can be reliably established. The x = 10% peak profiles are very well resolved and show the same general features previously described for the orthorhombic phase in x=9%,³ but with a small amount of residual tetragonal phase. The pseudocubic $(111)_c$ reflection consists of two peaks corresponding to the (012) and (210) orthorhombic reflections and a third central peak corresponding to the residual tetragonal (111) singlet. Three peaks are observed around the pseudocubic (200), reflection corresponding to the orthorhombic (202)-(020) doublet and the tetragonal (200) reflection. The pseudocubic $(220)_c$ reflection consists of a triplet and the orthorhombic (004)-(400)-(222), plus the (202)-(220) tetragonal doublet. From the intensity ratios one can estimate the fraction of tetragonal phase to be about 20% of the sample volume. This fraction is essentially constant between 20 and 300 K. For the x = 11% composition, the peak profiles are clearly those of a pure tetragonal phase with a single (111) reflection and two doublets (002)-(200) and (202)-(220). The fits of these profiles show that for x = 10% the orthorhombic unit cell has $a_o = 5.760$ Å, $b_o = 4.014$ Å, and $c_0 = 5.736$ Å and the second tetragonal phase has a_t =4.024 Å and c_t =4.091 Å. For x=11% the tetragonal



FIG. 4. Lattice parameters vs temperature for PZN-*x*PT for x = 15% (top) and 12% (bottom) over the whole temperature range from 15 K to 550 K, showing the tetragonal (a_t and c_t) to cubic (a_c) phase transition.

unit cell parameters are $a_t = 4.018$ Å and $c_t = 4.113$ Å.

The evolution of the lattice parameters with temperature for x = 10% reveals an orthorhombic-to-tetragonal phase transition, as shown in Fig. 3. At increasing temperatures, the orthorhombic lattice parameter b_{ρ} steadily increases while the c_o/a_o ratio decreases only slightly. At temperatures between 325 and 375 K, the symmetry is found to be tetragonal with lattice parameters a_t and c_t . The sudden change in a_o and c_o between 300 and 350 K suggests a first-order character to the orthorhombic-tetragonal phase transition. The residual tetragonal phase which is present between 20 and 300 K can probably be attributed to small long-range compositional fluctuations in the as-grown crystals. The overall behavior is identical to that previously reported for x = 9%.³ Similar temperature-dependence studies have been conducted for higher concentrations and the results are shown in Fig. 4. The lattice parameters as a function of temperature reveal a cubic-tetragonal phase transition for x = 15% (top) and for x = 12% (bottom). At low temperature, the system is purely tetragonal. With increasing temperature, the strain ratio c_t/a_t decreases, while approaching the transition to the cubic phase at $\simeq 490$ K and $\simeq 475$ K, for x = 15% and 12%, respectively.

The lattice parameters as a function of composition at 20 K are presented in Fig. 5, which includes the concentrations studied in this work, as well as the previous data reported in Refs. 3 and 4 for x=8% and 9%. This figure shows the structural evolution from the rhombohedral to the tetragonal phase via the orthorhombic phase. For $x \le 8\%$ the crystals exhibit the expected rhombohedral symmetry. For $x \ge 11\%$, the tetragonal symmetry is found with the strain ratio c_t/a_t increasing from 1.0237 at x = 11% to 1.0331 at x = 15%. The smooth variation in the tetragonal *a* and *c* lattice parameters



FIG. 5. Lattice parameters vs Ti concentration at 20 K for the rhombohedral $(a_r \text{ and } \alpha)$, monoclinic $(a_m, b_m, c_m, \text{ and } \beta)$ and tetragonal $(a_t \text{ and } c_t)$ phases from the results of this work, including data from Refs. 3 and 4.

with composition is consistent with fairly precise compositional control during the crystal growth process. However, at $9\% \le x \le 10\%$, the symmetry is found to be orthorhombic.

IV. SOFT-PHONON ANOMALIES IN PZN-XPT

A series of neutron inelastic measurements were subsequently performed on the PZN-15%PT single crystal to study the so-called "waterfall" feature, first observed in PZN-8% PT (Ref. 13) and later in PZN (Ref. 14), at higher concentrations of PbTiO₃. Specifically, we wished to determine whether or not this waterfall feature persisted beyond the MPB. The waterfall is an anomaly of the lowest-frequency transverse optic (TO) phonon branch that is correlated with the condensation, at $T = T_d$, of local regions of randomly oriented polarization, also known as polar nanoregions (PNR's), which disrupt the propagation of long-wavelength TO polar modes. The existence of T_d , which can be hundreds of degrees higher than T_c , was first reported by Burns and Dacol for a variety of systems including both PZN and PMN.¹⁶ Because the PNR's are polar, they naturally couple to the polar TO phonon mode, which in turn can serve as a microscopic probe of the PNR's. Their presence is manifested by a drastic broadening of the TO phonon energy linewidth below a specific wave vector and gives rise to a steep ridge of scattering when plotted as a function of wave vector q as the long-wavelength phonon cross section becomes distributed in energy. The search for the waterfall feature should thus yield important information about the possible existence of PNR's beyond the MPB.

Examples of two constant-*E* scans for $\hbar \omega = 7$ meV measured along the [010] cubic direction taken in the low-



FIG. 6. Constant-*E* scans at 7 meV (phonon creation) measured at 400 K and 650 K on a PZN-15%PT crystal. Inset shows the dispersion curves for the TA and the lowest-energy TO modes, showing the anomalous behavior of PZN-*x*PT. The data from Ref. 14 are also included and shown by two vertical dotted lines.

temperature phase (400 K) and in the higher-temperature phase (650 K) are shown in Fig. 6. The solid lines are Gaussian fits that show the peak position or a ridge of scattering intensity shifted to smaller q as the temperature increases. These data, shown schematically in the inset of Fig. 6, suggest that the ridge of scattering evolves into the expected TO phonon branch behavior at higher temperature. In the inset of Fig. 6, the solid lines represent dispersions of the transverse acoustic (TA) and the lowest-frequency TO phonon branches whereas the dashed lines show the presence of the steep ridge of scattering intensity at $q \sim 0.1$ recipical lattice units (r.l.u.) for PZN-15%PT and 0.14 r.l.u. for PZN at a temperature of about 500 K (see Ref. 14). It is interesting to note that the appearance of the steep ridge of scattering is shifted towards the zone center, i.e., (2,0.14,0), (2,0.13,0), and (2,0.1,0) for x=0%, 8%, and 15%, respectively, with increasing PT concentrations. So far 15%PT is the highest concentration that we have studied, and it is possible that the higher concentrations might show a softening of a zonecenter TO phonon as observed in the conventional ferroelectric PT,¹⁷ which would established the end member of the waterfall. This indicates that the anomalous soft phonon behavior is not simply a feature of compositions near the MPB but is extended to large values of x. It must be related to the presence of polar nanoregions rather than to the newly discovered phases. Therefore, the microstructural characters of relaxor ferroelectrics are retained to some degree in the PZN-*x*PT solid solution systems up to a quite high concentration of PT beyond the MPB.

V. DISCUSSION

In common with the x = 9% sample studied previously,³ it is clear that the x=10% sample studied here has orthorhombic symmetry within the resolution limits of the powder diffraction experiment. As noted before,⁴ this orthorhombic cell can be regarded as a doubled monoclinic cell of M_C type (space group Pm) in the limit of a=c. In a recent paper,⁶ Uesu and colleagues also reported orthorhombic symmetry for several samples of x=9% with one exception; interestingly, this one sample had a monoclinic cell of M_C type. The M_C type of monoclinic distortion is not the same as the M_A type observed in the PZT system.² The M_A type has b_m directed along the pseudocubic [110] direction, while, in M_C , b_m is directed along the pseudocubic [010].

In order to understand how the symmetry of the newly discovered phases facilitates the polarization rotation, it is useful to compare PZN-*x*PT with BaTiO₃. However, there is the question whether the new PZN-*x*PT orthorhombic cell is fundamentally different from the old BaTiO₃ orthorhombic cell, both with the same space group. The difference here seems to be in the very-low-energy barrier existing in PZN-*x*PT, between the *O* and M_C states, which allows the *O* polar axis [101] to rotate easily in the monoclinic plane.

The high-resolution synchrotron x-ray powder diffraction study of PZN-*x*PT ($10\% \le x \le 15\%$) as a function of temperature has allowed us to define the new orthorhombic region of the phase diagram. We show that the lowtemperature orthorhombic structure of PZN-xPT is found for x = 10% but not for higher concentrations. With the results of this and earlier studies of PZN-*x*PT ($8\% \le x \le 15\%$), we have completed a revision of the PZN-xPT phase diagram around its MPB as shown in Fig. 7. The new orthorhombic phase exists in only a narrow concentration range (8% < x)<11%) between the rhombohedral and tetragonal phases with near-vertical phase boundaries on both sides. These results, shown by the solid circles in Fig. 7, are in good agreement with those of Kuwata and colleagues (shown by open circles) except for the two points indicating phase transitions at about 250 K for x = 11% and 12%. One possible reason for this discrepancy might possibly be two-phase coexistence in their ceramic samples.

To be sure that the proposed phase diagram corresponds to the ground state of these materials, the poled-unpoled problem deserves further attention. Due to the intrinsic disorder existing in these relaxor ferroelectrics, the diffraction peaks of the as-grown samples are very broad, and to solve the true underlying structure by powder diffraction is an extremely difficult task. In order to induce the ferroelectric ordered state the samples are poled by an electric field. The extremely sharp peaks of the ordered material allow us to unequivocally determine the structure. However, due to the small energy differences between the different phases around



FIG. 7. Updated phase diagram of PZN-*x*PT around its MPB. The open circles and solid lines represent the phase diagram by Kuwata *et al.* (Ref. 18). The results of this work, as well as those in Ref. 3 (x = 9%), are plotted as solid circles. The new orthorhombic phase (*O*) is represented by the shaded area.

the MPB, sometimes the poled and unpoled states of the samples do not have the same symmetry or, alternatively, the symmetry can depend on the direction of the applied electric field, as in the case of the x=8% composition.⁴ The asgrown sample is known to be rhombohedral, but an irreversible phase transition can be induced by an electric field applied along the [001] direction, and the sample poled in such a way becomes orthorhombic. However, the initial rhombohedral state can be recovered by grinding the crystals below $\sim 30 \ \mu \text{m.}^4$

In a similar way, the x=9% composition showed very sharp and well-defined diffraction peaks after poling, displaying a clear orthorhombic symmetry.³ In this case, however, the poled and unpoled samples do not have intrinsically different characteristics, as shown in Ref. 6, and the main difference is the existence of a residual tetragonal phase in the unpoled samples. Here it is worth mentioning that it is very difficult to grow a perfectly homogeneous crystal and that certain compositional variations are always present for the same nominal composition. In this work we have shown that the poled x=10% crystal behaves much like the poled x=9% (Ref. 3) and that the poled x=11%-15% samples are tetragonal, as expected for the as-grown samples.¹⁸ Therefore, we believe that the new PZN-*x*PT phase diagram contains an orthorhombic intermediate phase for 8% < x < 11% as shown in Fig. 7, where the *x* values stand for the nominal compositions.

For further characterization of PZN-xPT, we have subsequently performed a neutron inelastic scattering on the PZN-15%PT single crystal to study the "waterfall" feature. As was the case for PZN-8%PT (Ref. 13) and later for PZN (Ref. 14) measured at the same temperature, an anomalous scattering ridge in PZN-15%PT is also found, but shifted closer to the zone center. It will be interesting to study the crystals of higher values of x and then to trace the evolution of the TO modes as a function of x. Thus, the conclusion of the present study is that the waterfall phenomenon is not associated with the new low-temperature phase near the MPB, but is a more general feature of the PZN-xPT solid solution system, which retains to some degree the relaxor ferroelectric characters, which are to be associated with the presence of the polar nanoregions.

During the preparation of this manuscript two different papers by Lu *et al.*¹⁹ and Xu *et al.*²⁰ have reported the optical observation of orthorhombic and monoclinic domains, respectively, in the related ferroelectric Pb(Mg_{1/3}Nb_{2/3})O₃*x*PbTiO₃ system (PMN-*x*PT) around its MPB ($x \approx 0.33\%$ -0.35%). A third paper by Ye *et al.*²¹ reports the existence of a monoclinic phase of M_A type in PMN-35%PT, after the application of an electric field. Work is in progress to clarify which type of low-symmetry distortion occurs in the phase diagram of PMN-*x*PT. Recently, there have been several theoretical papers discussing the unique characteristics of these systems near the MPB.^{22,23} They all point to the fact that the free energy becomes flat and isotropic close to the boundary, i.e., that *R*, M_A , *O*, M_C , and *T* are all nearly degenerate.

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