# **Doping-dependent evolution of the electronic structure of**  $\text{La}_{2-x}\text{Sr}_r\text{CuO}_4$ **in the superconducting and metallic phases**

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The electronic structure of the  $La_{2-x}Sr_xCuO_4$  (LSCO) system has been studied by angle-resolved photoemission spectroscopy (ARPES). We report on the evolution of the Fermi surface, the superconducting gap, and the band dispersion around the extended saddle point  $\mathbf{k}=(\pi,0)$  with hole doping in the superconducting and metallic phases. As hole concentration *x* decreases, the flat band at  $(\pi,0)$  moves from above the Fermi level ( $E_F$ ) for  $x > 0.2$  to below  $E_F$  for  $x < 0.2$ , and is further lowered down to  $x = 0.05$ . From the leading-edge shift of ARPES spectra, the magnitude of the superconducting gap around  $(\pi,0)$  is found to monotonically increase as *x* decreases from  $x=0.30$  down to  $x=0.05$  even though  $T_c$  decreases in the underdoped region, and the superconducting gap appears to smoothly evolve into the normal-state gap at  $x=0.05$ . It is shown that the energy scales characterizing these low-energy structures have similar doping dependences. For the heavily overdoped sample  $(x=0.30)$ , the band dispersion and the ARPES spectral line shape are analyzed using a simple phenomenological self-energy form, and the electronic effective mass enhancement factor  $m^*/m_b \approx 2$ has been found. As the hole concentration decreases, an incoherent component that cannot be described within the simple self-energy analysis grows intense in the high-energy tail of the ARPES peak. Some unusual features of the electronic structure observed for the underdoped region ( $x \le 0.10$ ) are consistent with numerical works on the stripe model.

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### **I. INTRODUCTION**

For the detailed understanding of a high- $T_c$  cuprate system, the determination of the low-energy electronic structure, i.e., the Fermi surface, the band dispersion, and the superconducting- and normal-state gaps, is required as the ground for studies of the superconducting mechanism and for the interpretation of thermodynamic and transport properties. Indeed, such information has been directly observed by angle-resolved photoemission spectroscopy (ARPES) for  $Bi_2Sr_2CaCu_2O_{8+v}$   $(Bi2212),^{1-9}$  $Bi<sub>2</sub>Sr<sub>2</sub>CuO<sub>6+y</sub>$  $(Bi2201)$ ,<sup>10,11</sup> and YBa<sub>2</sub>Cu<sub>3</sub>O<sub>7-y</sub> (YBCO).<sup>12</sup> Since the electronic properties of the high- $T_c$  cuprates are strongly dependent on the hole concentration, it is necessary to investigate the doping dependence of ARPES spectra systematically over a wide hole concentration range in order to extract key features relevant to the high- $T_c$  superconductivity.

Among the high- $T_c$  cuprate systems, we have recently focused on the  $La_{2-x}Sr_xCuO_4$  (LSCO) system<sup>13,14</sup> because the hole concentration is well controlled over an exceptionally wide range and uniquely determined by the Sr concentration  $x$  (and small oxygen nonstoichiometry). In addition, an instability towards spin-charge ordering in a stripe form has been extensively discussed from the incommensurate inelastic neutron peaks.<sup>15–17</sup> The suppression of  $T_c$  at  $x \sim 1/8$  $(Refs. 18 and 19)$  indicates that the stripe fluctuation has more static tendency in LSCO than in Bi2212.

In this paper, we address the evolution of the Fermi sur-

face, the superconducting gap, and the band dispersions with hole doping throughout the superconducting and metallic phases ( $0.05 \le x \le 0.30$ ) of LSCO, focusing on the features around the extended saddle point at  $\mathbf{k}=(\pi,0)$ , which are crucial to the determination of the Fermi-surface topology and the behaviors of superconducting- and normal-state gaps. The discussion leads to the issue of the doping dependence common to three characteristic energies of the electronic structure, and the self-energy and the electron effective mass are deduced. In the previous paper, ARPES spectra for  $x=0.10$  and 0.30 have been reported and the formation of a Fermi surface centered at  $(0,0)$  for an overdoped sample has been addressed.<sup>13</sup> On the other hand, the evolution of the ARPES spectra around the superconductor-insulator transition  $(x \approx 0.05)$  has been addressed in Ref. 14, where the suppression of quasiparticle weight around  $(\pi/2,\pi/2)$  has been also discussed for underdoped superconducting  $LSCO.<sup>14</sup>$ 

### **II. EXPERIMENT**

Single crystals of  $La_{2-x}Sr_xCuO_4$  were grown by the traveling-solvent floating-zone method and were annealed so that the oxygen content became stoichiometric. The accuracy of the hole concentration was  $\pm 0.01$ . The samples were insulating for  $x=0.05$ , superconducting for  $x=0.10$ , 0.15, and 0.22, and metallic without superconductivity for  $x=0.30$ . Details of the growth conditions and characterization of the crystals are described elsewhere.<sup>20-22</sup>

ARPES measurements were carried out at the undulator beamline 5-3 of Stanford Synchrotron Radiation Laboratory (SSRL). Incident photons had energies of  $h\nu=29$  or 22.4 eV and were linearly polarized. The electric vector and the wave vector of the incident photons and the sample surface normal were kept in the horizontal plane. The samples were fixed with respect to the incident light with an incident angle of 45° and ARPES spectra were collected using a hemispherical analyzer of 50 mm radius. The total instrumental resolution including the analyzer and the monochromator was approximately 45 meV and the angular acceptance was  $\sim \pm 1^{\circ}$ . In the case of LSCO,  $1^\circ$  corresponds to  $1/19$  and  $1/23$  of the  $(0,0)$ - $(\pi,0)$  distance in the Brillouin zone (BZ) of the CuO<sub>2</sub> plane for incident photon energies of  $h\nu=29$  and 22.4 eV, respectively. The samples were cleaved *in situ* at the plane parallel to the  $CuO<sub>2</sub>$  planes by knocking a top post glued on the sample under an ultrahigh vacuum better than 5  $\times 10^{-11}$  Torr. The orientation of the sample surface normal was finely readjusted using the reflection of a laser beam. The directions of the *a* and *b* axes were finely corrected using band folding in the ARPES spectra with respect to the  $k_y = 0$  line. Since the sample surface degraded rapidly at high temperatures, the samples were kept at low temperatures  $(T \approx 11)$  K) during the measurements. The cleanliness of the surface was checked by the absence of a hump at energy  $\sim$  -9.5 eV and of a shoulder of the valence band at  $\sim$  -5 eV. All the spectra presented here were taken within 12 h after cleaving. The position of the Fermi level  $(E_F)$  was repeatedly calibrated with gold spectra during the measurement, and the experimental uncertainty in the energy calibration was about  $\pm 2$  meV. The intensities of the spectra at different angles have been normalized to the intensity of the incident light. In the present paper, the measured crystal momenta  $\mathbf{k}=(k_x,k_y)$  are referred to in units of  $1/a$ , where *a* is twice the Cu-O bond length within the  $CuO<sub>2</sub>$  plane, and the extended zone notation is adopted; that is, a  $k_x$  value larger than  $\pi$  means that the momentum is in the second BZ.

#### **III. RESULTS**

#### **A. ARPES spectra**

ARPES spectra of overdoped LSCO  $(x=0.22)$  in the superconducting state are shown in Fig. 1. Here, the spectra are the raw data recorded on the spectrometer except for the fact that the energies have been calibrated to the Fermi edge of gold. It seems that the intensity of the dispersive component relative to the angle-independent background is weaker for LSCO than that for Bi2212. Probably, since the cleaved surface of LSCO is not so flat as that of Bi2212, some photoelectrons lose momentum information at the surface of LSCO and thus detected as an angle-independent background. In addition, the peak intensity is also strongly affected by the transition matrix element, which is different among various cuprate materials. The relative weakness of the dispersive component due to the high background may induce some uncertainty of the spectral line shape, compared to Bi2212. However, the peak energy is less affected by it, and the peak width of LSCO is practically similar to that of



FIG. 1. ARPES spectra of overdoped  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$  (*x*  $=0.22$ ) without any data manipulations except for the energy calibration. Insets show the measured momenta (circles) in the Brillouin zone and the in-plane component of the polarization of the incident photons (arrows). In going along  $(0,0) \rightarrow (\pi,0)$ , the band crosses  $E_F$  near  $(\pi,0)$ , although part of spectral weight remains below  $E_F$  at  $(\pi,0)$ .

Bi2212 under a similar doping level and the same instrumental resolution. $^{23}$  Indeed, the energy position and width of the peak were well reproduced by several experiments, indicating the validity of the analysis of the ARPES peak performed in Sec. III E.

Usually the band dispersion is obtained by tracing the ARPES spectral peak. As one goes from  $(0,0)$  to  $(\pi,0)$  or from  $(2\pi,0)$  to  $(\pi,0)$ , the peak energy increases towards  $E_F$ as shown in Fig. 1(a). Around  $\sim(0.8\pi,0)$  and  $\sim(1.2\pi,0)$ , the peak reaches the vicinity of the Fermi level  $(E_F)$  and the peak intensity decreases between these points. However, part of the spectral weight remains below  $E_F$  even at  $(\pi,0)$ , and the weight completely disappears only in going from  $(\pi,0)$ to  $(\pi,\pi)$  [Fig. 1(b)]. The remnant weight at  $(\pi,0)$  is larger for  $x=0.22$  than for  $x=0.3$ ,<sup>13</sup> indicating that a band of flat dispersion around  $(\pi,0)$  lies quite close to the Fermi level for  $x=0.22$ .<sup>11,24</sup> Since even for  $x=0.3$  a small weight remains below  $E_F$  at  $(\pi,0)$ ,<sup>13</sup> the band around  $(\pi,0)$  is not a single peak but has a broad energy distribution, implying a complicated spectral weight distribution around ( $\pi$ ,0) as dis-



FIG. 2. ARPES spectra of optimally doped  $\text{La}_{2-x}\text{Sr}_{x}\text{CuO}_{4}$  (*x*  $=0.15$ ) (Refs. 13 and 14), displayed in a similar way to Fig. 1. Along (0,0) $\rightarrow (\pi,0)$ , the peak clearly remains below  $E_F$ , indicating a Fermi surface centered at  $(\pi,\pi)$ . The band around  $(\pi,0)$  shows a very flat dispersion and is located slightly below  $E_F$ .

cussed recently.<sup>25,26</sup> Along the  $(0,0) \rightarrow (\pi,\pi)$  cut, although the dispersive feature is weak, the increase of the intensity at  $E_F$  compared to the background around  $(0.4\pi,0.4\pi)$  suggests a Fermi-surface crossing as in  $x=0.3$  and  $0.15^{13,14}$ Overall, the electronic structure for  $x=0.22$  is in transition between the electronic structures characterized by the Fermi surfaces centered at  $(0,0)$   $(x=0.30)$  and at  $(\pi,\pi)$   $(x)$  $= 0.15$ .<sup>13</sup>

In Fig. 2, ARPES spectra for optimally doped LSCO (*x*  $=0.15$ ) are displayed again<sup>13,14</sup> in a similar way to Fig. 1. Even though the spectra were taken at a temperature ( $\sim$ 11 K) well below  $T_c$  ( $\approx$ 39 K), the condensation peak is absent or unresolved for LSCO as in Bi2201, $^{10}$  while the line shape with a peak, dip, and hump has been observed around  $(\pi,0)$  for Bi2212.<sup>1,27,28</sup> As one goes from  $(0,0)$  to  $(\pi,0)$  or from  $(2\pi,0)$  to  $(\pi,0)$ , the peak approaches  $E_F$  but clearly remains below  $E_F$  at  $(\pi,0)$ , indicating a Fermi surface centered at  $(\pi,\pi)$ . In going from  $(\pi,0)$  to  $(\pi,\pi)$ , the peak intensity decreases, while the midpoint of a leading edge is always below  $E_F$  (-3 meV at the closest to  $E_F$ , i.e., the minimum-gap locus), implying that the band goes above  $E_F$ 



FIG. 3. ARPES spectra near the Fermi level  $(E_F)$  for  $La_{2-x}Sr_xCuO_4$  ( $x=0.05$ ) near the superconductor-insulator transition, displayed in a similar way to Fig. 1. Along ( $\pi,0$ ) $\rightarrow$ ( $\pi,\pi$ ), the peak disperses towards  $E_F$  and loses its intensity before reaching  $E_F$ around  $(\pi,0.25\pi)$ , indicating a "normal-state gap" opened on the underlying Fermi surface.

through the superconducting gap. The band around  $(\pi,0)$ shows a very flat dispersion and is located slightly below  $E_F$ .<sup>11,24</sup> The spectra along  $(0,0) \rightarrow (\pi,\pi)$  for *x*=0.15 are similar to those for  $x=0.3$  (Ref. 13) and 0.22: one can identify the dispersion of the weak feature crossing  $E_F$  at  $\sim(0.4\pi,0.4\pi)$ . Thus, the electronic structure for  $x=0.15$  is similar to those for other optimally doped Bi2212 (Ref. 2) and  $Bi2201$  (Ref. 11), except for that the dispersive spectral peak along  $(0,0) \rightarrow (\pi,\pi)$  is weak for LSCO.

ARPES spectra of the heavily underdoped LSCO (*x*  $=0.05$ ) in the normal state are shown in Fig. 3. As the hole concentration *x* decreases, the peak near  $E_F$  around  $(\pi,0)$ becomes broader and weaker. This is consistent with the spectra of other underdoped cuprates, where the dispersive feature is so broad that it is merely a shoulder rather than a spectral peak.<sup>3,5</sup> When the hole concentration *x* decreases down to  $x \le 0.03$  for LSCO, the feature near  $E_F$  becomes too weak to discuss the dispersion because of the spectral weight transfer into a band around  $-0.5$  eV (see Fig. 6).<sup>14</sup> As shown in Fig. 3, while the band for  $x=0.05$  stays below  $E_F$ with very weak dispersion along  $(0.8\pi,0) \rightarrow (\pi,0)$ , the band disperses rather strongly towards  $E_F$  along  $(\pi,0)$ 



FIG. 4. (a) Dispersive component of ARPES spectra taken along  $(0,0) \rightarrow (\pi,\pi)$  for  $x=0.15$ . The angle-independent background has been subtracted from the original spectra shown in Fig.  $2(c)$ . (b) and  $~c)$  Second derivatives of the ARPES spectra taken along  $(0,0)$  $\rightarrow (\pi,\pi)$  and  $(0,0) \rightarrow (\pi,0) \rightarrow (2\pi,0)$ , respectively, for  $x=0.15$ . The positive and negative peaks in the second derivatives are colored with light and dark gray, respectively, in the figure. Original ARPES spectra are shown in Fig. 2. The dispersive component of the ARPES spectra has been smoothed by convoluting with the Gaussian and then differentiated twice (see the text). The results are displayed in Figs. 5 and 6 in order to visualize the dispersion relation.

 $\rightarrow (\pi,0.2\pi)$  and the feature disappears around  $(\pi,0.25\pi)$ before the leading-edge midpoint reaches  $E_F$ , indicating that a gap is opened around  $(\pi,0.25\pi)$  for  $x=0.05$ . Presumably, the gap is opened on the underlying Fermi surface as in the superconducting samples although  $T_c \approx 0$  and may be regarded as a "normal-state gap." $5-9$  Remarkably, in the  $(0,0) \rightarrow (\pi,\pi)$  cut, no dispersive feature nor intensity modulation could be identified at  $\sim E_F$  for  $x \le 0.12$ ,<sup>14</sup> in contrast to the spectra for  $x \ge 0.15$ . Therefore, the electronic structure near  $E_F$  for  $x=0.05$  is similar to that for  $x=0.1$  reported in the previous paper:<sup>13</sup> the Fermi surface centered at  $(\pi,\pi)$  is observed around  $(\pi,0.25\pi)$ , but it is invisible around  $(\pi/2,\pi/2)$ .

#### **B. Band dispersions**

Overall band dispersions near  $E_F$  are visualized in Fig. 5, below, by use of the second derivatives, which are shown in Fig. 4 for example. First, the step at  $E_F$  seen in the spectrum at  $(0,0)$  seems to be present at all the angles with almost constant intensity, as shown in Figs. 1, 2, and 3. Hence, we assigned the spectrum at  $(0,0)$  to the angle-integrated signals likely due to the surface imperfection, because no emissions are allowed at  $(0,0)$  from the  $d_{x^2-y^2}$  symmetry of Cu 3*d* 



FIG. 5. Band dispersion near the Fermi level for  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ , measured by ARPES. The second derivatives of the ARPES spectra, which are shown in Fig. 4, for example, are displayed as a density plot on the gray scale, where white regions denote the negative peak of the second derivatives. Note that, because of the finite instrumental resolution  $\Delta E \sim 45$  meV, the structures near  $E_F$  are pushed down below the resolution limit  $\sim -\Delta E/2$  (dashed lines).

orbitals due to the photoemission matrix-element effect. In order just to remove this extrinsic step, the spectra at  $(0,0)$ were subtracted from all the spectra at the other angles under simple normalization to the intensity of the incident light. The validity of this subtraction may be understood by a typical result shown in Fig. 4(a). Indeed, the spectrum at  $(0,0)$  is so featureless that its subtraction makes essentially no effect on the second derivatives except for the extrinsic step at  $E_F$ . All the resulting spectra were then smoothed by convoluting with the Gaussian whose energy width is the order of the energy resolution (typically  $\sim 50$  meV), since the collected signals were of the order of  $\sim 10^3$  counts for the peak component and thus the signal-to-noise ratio is the order of  $\sim$  1/30. Along the momentum direction, no smoothing or interpolation is applied to the data and thus each horizontal pixel in Fig. 5 corresponds to each ARPES spectrum. Finally, the spectra are differentiated two times and displayed by the gray scale plot in Fig. 5, where white regions denote the negative peak of the second derivatives. In the differentiation, the energy step of the data was smaller enough  $(5 \text{ or } 10)$  meV) compared to the energy resolution. Indeed, taking the second derivatives would be an appropriate way to visualize the band dispersion of this system, because for  $x \leq 0.1$  the dispersive feature does not show a clear peak but a shoulder. Practically, the second derivative method has been widely used and outlined the band dispersions excellently from the ARPES spectra.<sup>29–35</sup> The validity of the above data manipulations is assured by comparing the second derivatives in Fig.  $4(c)$  with the original raw spectra in Fig. 2(a), and comparing Fig. 5 with the gray scale plot of the original data shown in the top panels of Fig. 10, below, for  $x=0.30$  and 0.15. In Fig. 5, thin black curves following the negative peaks in the second derivatives are also drawn. Thus their error bars were represented by the half width of the white gradation. Note that, because of the Fermi cutoff and the finite instrumental resolution  $\Delta E \sim 45$  meV, spectral features near  $E_F$  are pushed down below  $\sim -\Delta E/2$  (dashed lines).<sup>36</sup> The obtained band dispersion for  $x=0.15$  is similar to the ARPES results of other optimally doped cuprates such as Bi2212 (Ref. 2) and Bi2201 (Ref. 11).

Figure 5 shows that the so-called " $(\pi,0)$  flatband" is clearly observed for  $x=0.15, 0.10$ , and 0.05 in the sense that the flat region around the saddle point at  $(\pi,0)$  is extended up to  $\sim$ (0.7 $\pi$ ,0).<sup>11,24</sup> The flatband, which is  $\sim$ 120 meV below  $E_F$  for  $x=0.05$ , moves upwards monotonically with hole doping, crosses the Fermi level around  $x \approx 0.2$ , causing the increase of the density of states  $(DOS)$  at  $E_F$  as observed by angle-integrated photoemission<sup>37</sup> (AIPES) and the quasiparticle density reflected in the electronic specific heat,<sup>38</sup> and finally goes above the Fermi level. Since the chemical potential shift with hole doping is small  $(\leq 100 \text{ meV})$  in the region  $0 \le x \le 0.15$ ,<sup>39</sup> the energy shift of the flatband in this composition range is due to the deformation of the band structure itself. Probably the lowering of the flatband at  $(\pi,0)$  is due to the influence of short-range antiferromagnetic correlations. Under the antiferromagnetic correlations, the spectral function of magnetic excitations  $\chi''(\mathbf{q},\omega)$  is peaked near  $\mathbf{q}=(\pi,\pi)$ . Then, the photohole at  $(\pi,0)$  is particularly dressed strongly in the collective magnetic excitations, because the photohole at  $(\pi,0)$  can enter into a state of similar energy around  $(0,\pi)$  by producing a collective excitation **q**  $= (\pi,\pi)$ , as proposed by Shen and Schrieffer.<sup>40,41</sup> Since the emissions from the dressed photoholes are predominant among the spectral intensity in the underdoped region, the kinetic energies of photoelectrons from  $(\pi,0)$  are lowered by the stronger dressing of photoholes with decreasing hole concentration.

As for the underdoped samples  $(x=0.05$  and 0.10), the band dispersion around  $(\pi,0)$  is not symmetric between the  $(\pi,0)\rightarrow(0,0)$  and  $(\pi,0)\rightarrow(\pi,\pi)$  directions. While the band is very flat, showing almost no dispersion along  $(\pi,0)$  $\rightarrow$ (0.7 $\pi$ ,0), the dispersion along  $(\pi,0) \rightarrow (\pi,0.3\pi)$  is substantial and consistent with a simple parabolic dispersion (with a gap at  $E_F$ ). The asymmetric dispersion and the unclear Fermi surface around  $(\pi/2, \pi/2)$  for underdoped LSCO are consistent with the electronic structures calculated by numerical exact diagonalization on small clusters with stripes<sup>42</sup> and calculated within the Hubbard model with the stripes using the Hartree-Fock approximation<sup>43</sup> and dynamical mean-field theory.<sup>44</sup>

The band around  $(\pi,0)$  is thought to primarily contribute to the formation of the superconducting condensate in a *d*-wave superconductor, because the quasiparticle weight near  $E_F$  around ( $\pi/2, \pi/2$ ) is virtually absent in underdoped LSCO  $(x \le 0.12)$ . As shown in Fig. 5, when LSCO is optimally doped, the flatband around  $(\pi,0)$  is located slightly below  $E_F$  as in the other cuprate systems. This is the case for all the hole-doped high- $T_c$  cuprates studied by ARPES so far,<sup>2</sup> suggesting that the energy position of the  $(\pi,0)$  flatband has a universal doping dependence among high- $T_c$  cuprates and that the optimum  $T_c$  requires the  $(\pi,0)$  flatband to be near  $E_F$ .<sup>45</sup> As for the relevance of the flatband energy to the high  $T_c$ , the presence of the flatband near  $E_F$  enhances the density of low-energy single-particle excitations which are involved in the formation of the superconducting condensate through a large portion of the **k** space.<sup>24</sup>

In Fig. 6, we summarize the doping dependences of the dispersions around  $(\pi,0)$  and  $(\pi/2,\pi/2)$ . It is clearly seen that the flatband around  $(\pi,0)$  is lowered as *x* decreases and loses its intensity in the insulating phase. As reported previously, $^{14}$  the spectral weight is transferred from the band near  $E_F$  ( $\sim$  -0.1 eV) to the lower Hubbard band at  $\sim$  -0.5 eV in the vicinity of the superconductor-insulator transition ( $x \approx 0.05$ ). The evolution of the band near  $E_F$  is different between  $(\pi,0)$  and  $(\pi/2,\pi/2)$ : with decreasing *x*, the spectral weight is largely lost already at  $x=0.12$  for  $\sim(\pi/2,\pi/2)$ , whereas it remains substantial down to *x*  $=0.05$  for  $\sim (\pi,0)$ . On the other hand, the evolution of the insulating band at  $\sim$  -0.5 eV is similar between ( $\pi$ ,0) and  $(\pi/2,\pi/2)$ .

### **C. Fermi surface**

From the ARPES spectra taken at various doping levels, the doping dependence of the Fermi surface has been deduced as shown in Fig. 7. Here the Fermi-surface crossings have been determined to be the momenta where the leadingedge energy reaches a local maximum and the spectral peak intensity (quasiparticle weight) changes most strongly. They correspond to the minimum-gap loci, when a gap is opened on the Fermi surface. As for the superconducting gap, it has been confirmed that the minimum-gap locus coincides with the Fermi surface in the normal state. $46$  In Fig. 7, thick error bars denote the actually measured positions of Fermi surface and the width of the error bars indicate two momenta where the most weight of dispersive features is clearly below  $E_F$ and has almost gone above  $E_F$ . The area enclosed by the Fermi surface is  $71\pm3$  %,  $79\pm8$  %, and  $85\pm5$  % of the half BZ area for  $x=0.3$ , 0.22, and 0.15, respectively, consistent with the Luttinger sum rule for the electron density  $1-x$  $(570\%, 78\%, \text{ and } 85\%, \text{ respectively})$ . As for  $x=0.1$  and 0.05, since the Fermi surface around  $(\pi/2, \pi/2)$  was invisible, dotted curves are tentatively drawn in Fig. 7 so that the area enclosed by the Fermi surface is  $\sim 0.9$  and  $\sim 0.95$ , respectively, $2^{2}$  of the half BZ area, supposing that the Luttinger sum rule is still satisfied. As the hole concentration



FIG. 6. Doping dependence of the band dispersion around ( $\pi$ ,0) (upper panels) and ( $\pi/2$ , $\pi/2$ ) (lower panels) for La<sub>2-x</sub>Sr<sub>x</sub>CuO<sub>4</sub>. From left to right, the samples are an antiferromagnetic insulator (AFI) for  $x=0$ , an insulator for  $x=0.03$ , near the superconductor-insulator transition (SIT) for  $x = 0.05$ , superconductors (SC) for  $x = 0.07$ , 0.10, 0.12, 0.15, and 0.22, and a normal metal (NM) for  $x = 0.30$ . Data in the wide energy range were taken from Ref. 14. The features at  $\sim -0.5$  eV in the underdoped samples are the lower Hubbard band.

decreases, the Fermi surface near  $(\pi,0)$  smoothly moves through  $(\pi,0)$  so that the topological center of the Fermi surface is turned over from  $(0,0)$  to  $(\pi,\pi)$  at  $x \sim 0.2$ . On the other hand, the position of the Fermi surface near  $(\pi/2, \pi/2)$ is less sensitively dependent on the hole concentration and the weak spectral intensity near  $(\pi/2, \pi/2)$  at  $E_F$  becomes invisibly weak for  $x \le 0.12$ .<sup>14</sup> The Fermi surface of LSCO is thus strongly doping dependent, while the Fermi surface of optimally doped LSCO is basically similar to that of  $Bi2212.<sup>2,3</sup>$ 

Figure 7 indicates that "small hole pocket" around  $(\pi/2, \pi/2)$  is absent even in the underdoped LSCO. Hence the decrease in the carrier density proportional to  $x$ , which has been observed in the Hall coefficient measurement as  $1/R_H \propto x^{47}$  should be attributed to the fact that the quasiparticle weight around  $E_F$  decreases as  $\alpha x$  due to the spectral weight transfer to higher binding energies. $14,37$ 

### **D. Energy gap**

The doping dependence of the energy gap at  $E_F$  may be estimated from the leading-edge shift on the Fermi surface. $4-10,12$  Figure 8(a) shows the ARPES spectra at the momenta where the leading edge reaches the maximum energy (minimum-gap locus) around  $(\pi,0)$  as shown by open circles in the inset. Here, the spectrum at  $(0,0)$  has been subtracted as the angle-independent background for each composition. For the nonsuperconducting  $(x=0.3)$  sample, the leading-edge midpoint is apparently pushed above  $E_F$  $(\sim 6 \text{ meV})$  due to the finite instrumental resolution  $(\sim 45 \text{ meV})$ .<sup>7</sup> As the hole concentration decreases, the energy of the peak and the leading edge are shifted downwards as a result of the opening of the superconducting gap.

In Fig. 8(b), the energy shift  $\Delta$  of the leading-edge midpoint relative to that for  $x=0.3$  ( $\sim$  +6 meV) is plotted and compared with the results of other experiments on LSCO, i.e., Raman scattering,  $48$  tunneling,  $49$  and neutron scattering  $50$ studies (left axis). Crosses indicate the superconducting transition temperature  $T_c$  (right axis) and the prediction of the mean-field theory for the *d*-wave superconducting gap  $2\Delta_{\rm SC}^{\rm MF}=4.3k_{\rm B}T_{\rm c}$  (Ref. 51) (left axis). In fact, what are measured in these experiments are different quantities; e.g., the neutron scattering measures the gap in the spin-excitation spectrum, which is not simply connected to the singleparticle excitation gap probed by ARPES. In addition, the magnitude of the ARPES leading-edge shift tends to be smaller than the tunneling result, probably because the broadness of the peak reduces the apparent shift of the ARPES leading edge, while it hardly affects the peak position observed in tunneling spectra, which represent the momentum-integrated spectral function. Nevertheless the



FIG. 7. Fermi surfaces of  $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ , obtained from ARPES experiments. Thick and thin error bars denote the observed Fermisurface crossings and those folded by symmetry. As for  $x=0.10$  and 0.05, since no dispersive features are observed near  $E<sub>F</sub>$  around  $(\pi/2,\pi/2)$ , the dotted curves are tentatively drawn so that the area enclosed by the Fermi surface is  $\sim$  0.9 and  $\sim$  0.95, respectively, of the half Brillouin zone area, assuming that the Luttinger sum rule is satisfied.



FIG. 8. (a) ARPES spectra for momenta on the Fermi surface (minimum-gap locus) near  $(\pi,0)$  as denoted by open circles in the inset. From the ARPES spectrum for each composition  $x$ , the spectrum at  $(0,0)$  has been subtracted as the angle-independent background. (b) The shift  $\Delta$  of the leading-edge midpoint in the ARPES spectra relative to that of  $x=0.3$  ( $\sim$  +6 meV), denoted by open circles. Error bars denote the uncertainty in determining the leading-edge position of each spectrum. The leading-edge shift  $\Delta$ approximately represents the magnitude of the superconducting or normal-state gap and is compared with the gap deduced from the *d*-wave mean-field approximation  $2\Delta_{\rm SC}^{\rm MF}=4.3k_BT_c$  (crosses) (Ref. 51) and other experiments: Raman scattering (open diamonds) (Ref. 48), scanning tunnel spectroscopy (solid triangles) (Ref. 49), and inelastic neutron scattering (open boxes)  $(Ref. 50)$ . As *x* decreases, the magnitude of the energy gap keeps increasing even in the underdoped region in spite of the decreasing  $T_c$ .

doping dependence of the gap magnitude is consistent among the ARPES and other experiments.

As the hole concentration *x* decreases, the magnitude of  $\Delta$ keeps increasing even in the underdoped region, in spite of the decreasing  $T_c$ . This remarkable feature has also been reported for  $Bi2212$  (Refs. 6 and 8) and is thus likely to be a universal feature of the cuprate superconductors. The present data have ensured that this tendency is sustained down to *x*  $=0.05$ . Although the sample of  $x=0.05$  is not superconducting, still an energy gap is opened at  $\sim (\pi,0.25\pi)$  as shown in Fig.  $3(b)$ , corresponding to the "normal-state gap" observed for underdoped  $Bi2212.^{5-9}$  From the ARPES spectra [Figs.  $3(b)$  and  $8(b)$ ], it appears that the superconducting gap smoothly evolves into the normal-state gap with decreasing hole concentration *x*. This observation certainly has the same significance as the fact that the temperature dependence of the leading-edge shift is continuous at  $T_c$  for underdoped Bi2212.<sup>5–9</sup> These connections between the normal- and superconducting-state gaps suggest that these gaps have the same origin. Assuming that the magnitude of the energy gap  $\Delta$  represents the paring strength, the doping dependence of  $T_c$  may be roughly described using the product of  $\Delta$  and the quasiparticle density at  $E_F$  related to the flatband energy. When the hole concentration is further decreased to *x*  $< 0.05$ , the normal-state gap becomes difficult to be identified because the spectral weight of the band near



FIG. 9. Doping dependence of three characteristic energies: the leading-edge shift on the Fermi surface  $\Delta$  representing the superconducting and normal-state gaps, the energy of the flatband around  $(\pi,0), E_{(\pi,0)}$ , and the "large pseudogap"  $\Delta_{PG}$ , which would correspond to the high-energy bump in angle-integrated photoemission (AIPES) spectra (Refs. 37 and 53). Error bars for  $E_{(\pi,0)}$  indicate the uncertainties in determining the peak energy at  $\sim (\pi,0)$  (Ref. 52), based on variation among several different samples. The inset shows the scaling relations as  $\Delta_{\text{PG}} \approx 2.5E_{(\pi,0)}$  and  $\Delta_{\text{PG}} \approx 13\Delta$ .

 $E_F$  diminishes and, alternatively, the wide insulating gap  $(\sim 0.5$  eV) becomes predominant.<sup>14</sup>

Figure 9 shows the binding energy  $E_{(\pi,0)}$  of the band at  $(\pi,0)$ ,<sup>52</sup> which is confidently determined by measuring several samples for each *x*, compared with the energies of the superconducting or normal-state gap  $\Delta$  measured by the ARPES leading-edge shift and the "large pseudogap"  $\Delta_{PG}$ , which would correspond to the high-energy bump in AIPES spectra.37,53 These characteristic energies show quite similar doping dependences as shown in the inset, even though their energy scales are different:  $\Delta_{\text{PG}} \approx 2.5E_{(\pi,0)}$  and  $\Delta_{\text{PG}} \approx 13\Delta$ . Therefore, the electronic structure of the underdoped LSCO is essentially characterized by a single parameter which rapidly increases as *x* decreases for  $x \le 0.22$ . The proportionality  $\Delta_{\text{PG}} \approx 2.5E_{(\pi,0)} \approx 13\Delta$  implies that the origin of the superconducting- and normal-state gaps may be related to that of the large pseudogap and the flatband energy, indicating that the behaviors of the cuprate superconductors are strongly affected by the short-range antiferromagnetic correlations.37,40,54

#### **E. Self-energy analysis**

In order to deduce the energy position and width of the ARPES peak more precisely, a model for the spectral line shape is necessary. The actual peak is asymmetric and fairly deviated from the simple Lorentzian even for the heavily overdoped sample  $(x=0.3)$ .<sup>13</sup> Therefore, we introduce a simple but more general form of the self-energy:<sup>55</sup>

$$
\Sigma(\omega) = -\frac{\gamma}{\omega/\Gamma + i} + \frac{\gamma + \gamma_0}{\omega/G + i} \quad (G \gg \Gamma),
$$

which satisfies the Kramers-Kronig relation. The denominator of the second term is to make  $\Sigma(\omega)$  converge to zero for  $\omega \rightarrow \infty$ , a sufficiently large *G* being taken as a cutoff energy. Then, for  $\omega \ll G$ ,  $\Sigma(\omega)$  is expanded around  $E_F$  as  $\Sigma(\omega)$  $-\gamma(\omega/\Gamma) - i\gamma_0 - i\gamma(\omega/\Gamma)^2$ . Here,  $\Gamma$  is the characteristic energy which scales for the quasiparticle energy  $\omega$ ,  $\gamma_0$ =  $-\text{Im}\Sigma(0)$  represents the scattering rate of the quasiparticles at  $\omega$ =0 and should be zero for an ideal Fermi liquid, and  $\gamma$ represents the high-energy limit of the peak width since  $-\text{Im}\Sigma(\omega) \approx \gamma + \gamma_0$  for  $\Gamma \ll \omega \ll G$ . In the present analysis, the momentum dependence of the self-energy is ignored for the simplicity. Then, the spectral function  $A(\mathbf{k},\omega)$  is given by

$$
A(\mathbf{k}, \omega) = \text{Im}\left(\frac{1}{\omega - \epsilon_{\mathbf{k}} - \Sigma(\mathbf{k}, \omega)}\right),\,
$$

where  $\epsilon_{\mathbf{k}}$  is the dispersion of the single-particle band. The calculated spectra have been obtained as the product of  $A(\mathbf{k},\omega)$  and the Fermi-Dirac distribution function  $f(\omega,T)$ , and then broadened by the energy and angular resolutions  $(42 \text{ meV}$  and  $2^{\circ}$ , respectively). Finally, upon comparing with experimental spectra, the angle-independent background, i.e., the spectrum at  $(0,0)$ , is commonly added to the calculated spectra.

Parameters fixed in the analysis are the temperature and the energy and momentum resolutions, and the singleparticle dispersion  $\epsilon_k$  has been taken from the local-densityapproximation (LDA) energy band of undoped  $La_2CuO_4$ .<sup>56</sup> On the other hand, the parameters,  $\Gamma$ ,  $\gamma$ , and  $\gamma_0$ , describing the self-energy, are obtained from the present least-squaresfit analysis, and the results are shown in Table I. Here, the chemical potential shift of the LDA band due to the hole doping into  $La_2CuO_4$  is adjusted to reproduce the experiment, and the spectral intensity at each angle has also been adjusted to the experiment, because the momentum dependence of the matrix element is unknown.

TABLE I. Effective-mass enhancement factor  $m^*/m_b$  at  $E_F$  obtained from the self-energy analysis of the ARPES spectra for  $x=0.30$  (overdoped) and  $x=0.15$  (optimally doped), and parameters  $\Gamma$ ,  $\gamma$ , and  $\gamma_0$  of the model self-energy which best reproduce the experimental spectra. Here  $m^*/m_b$  obtained from the electronic specific heat coefficient  $\gamma_{el}$  (Ref. 38) is also shown for comparison.

$\mathcal{X}$	$m^*/m_h$ (ARPES)	$\Gamma$ (eV)	$\nu$ (eV)	$\gamma_0$ (eV)	Fermi surface	$m^*/m_h(\gamma_{el})$
0.30	2.0	0.20	0.21	0.077	Centered at $(0,0)$	2.5
0.15	2.1	0.30	0.34	0.081	Centered at $(\pi, \pi)$	2.5



FIG. 10. Results of the self-energy analysis for  $(a)$   $x=0.15$  and (b)  $x=0.30$ . Bottom panels: calculated spectra (lines) fitted to the experimental spectra (dots) along  $(0,0) \rightarrow (\pi,0)$ . Middle panels: real and imaginary parts of the self-energy used in the calculation. Top panels: dispersion  $\epsilon_k$  of the local-density-approximation energy band of  $La_2CuO_4$  whose chemical potential adjusted to experiment (dotted lines) and the peak dispersion in the calculated spectra (solid lines), overlayed with the gray scale plot of the experimental spectra, where the white region simply denotes high spectral intensity (not the second derivatives).

Figure 10 shows the results of such analysis for  $(0,0)$  $\rightarrow (\pi,0)$  cut. Both the peak line shape and the peak dispersion are successfully reproduced for the heavily overdoped sample  $(x=0.30)$ , confirming the dispersion relation and Fermi-surface crossings shown in Figs. 5 and 7. Note that the weak residual spectral weight around  $(\pi,0)$  is also present in the calculated spectra even though the band energy  $\epsilon_{\mathbf{k}}$  at  $(\pi,0)$  is above  $E_F$ , indicating that the experimental spectra are consistent with the Fermi surface centered at  $(0,0)$ . For the optimally doped sample  $(x=0.15)$ , on the other hand, the high-energy tail of the peak was difficult to reproduce after extensive trials particularly around  $(\pi,0)$ , although the peak dispersion and the peak leading edge are almost correctly reproduced by a self-energy similar to that of  $x=0.30$ . The result for  $x=0.15$  indicates that the high-energy tail around  $(\pi,0)$  contains an intense incoherent component which cannot be described by the simple model self-energy analysis. This difficulty, in addition to the limited experimental resolution, indicates that the obtained Im $\Sigma(\omega)$ , which describes the peak shape, has some uncertainties, while  $\text{Re}\Sigma(\omega)$  obtained from the peak position is reliably determined.

The effective mass  $m^*$  relative to the bare-electron mass  $m<sub>b</sub>$  is also obtained from the self-energy,

$$
\frac{m^*}{m_b} = 1 - \frac{\partial \text{Re}\Sigma(\omega)}{\partial \omega}\bigg|_{\omega=0} = 1 + \frac{\gamma}{\Gamma},
$$

and the result is shown in Table I. Namely, the electron effective mass *m*\* has been directly obtained from the band dispersion around the Fermi level. The effective-mass enhancement factor  $m^*/m_b$  deduced from ARPES spectra is approximately consistent with that from the electronic specific heat coefficients  $\gamma_{el}$ , <sup>38</sup> indicating that the self-energy used is reasonable to some extent. Furthermore, we also find the peak in the spectral function at  $E_F$  has a width of  $2\gamma_0(m_b/m^*)$  = 77 meV for both  $x=0.30$  and 0.15, in addition to the broadening due to the instrumental resolutions. The quantities of  $-\text{Im}\Sigma(0) = \gamma_0$  obtained by the present analysis are approximately consistent with the fact that the result for overdoped Bi2212 is  $\sim$ 90 meV, independent of temperature in the normal state  $T>T_c$ .<sup>57</sup> Although the spectrum of the  $x=0.15$  sample was taken in the superconducting state, our preliminary temperature-dependent measurements indicated no significant broadening of the peak above  $T_c$ except for the thermal broadening.

## **IV. CONCLUSIONS**

In summary, the systematic ARPES study of LSCO has revealed the evolution of the Fermi surface, the superconducting gap, and the band dispersion around  $(\pi,0)$  with hole doping. While the Fermi surface and the band dispersion of the optimally doped LSCO are essentially consistent with the result of Bi2212, $^2$  those low-energy electronic structures have been found to change drastically for the wide hole concentration range  $(0.05 \le x \le 0.30)$  available for LSCO. Notably, the magnitude of the superconducting-state gap  $\Delta$  keeps increasing as *x* decreases down to  $x=0.05$ , and the superconducting-state gap appears to evolve smoothly into the normal-state gap for  $x=0.05$ . It has been shown that the doping dependence of  $\Delta$  deviates from the decreasing  $T_c$  in the underdoped region but follows a doping dependence common to other two characteristic energies: the energy  $E_{(\pi,0)}$  of the extended flatband at  $\sim(\pi,0)$  and the pseudogap energy  $\Delta_{PG}$  obtained from AIPES. Therefore, the electronic structure of the underdoped cuprates may be characterized by a single parameter. For the heavily overdoped region (*x*  $=0.30$ , a simple self-energy analysis has successfully reproduced both the band dispersion and the spectral line shape and indicated the effective mass  $m^*/m_b \sim 2$ . However, as the hole concentration decreases, an incoherent component which cannot be described by a simple self-energy analysis grows intense in the high-energy tail of the ARPES peak. As the flatband at  $(\pi,0)$  is lowered with decreasing *x*, the band dispersion along ( $\pi$ ,0) $\rightarrow$ ( $\pi$ ,0.3 $\pi$ ) becomes faster, while almost no dispersion along  $(\pi,0) \rightarrow (0.7\pi,0)$  is kept. Such electronic structure is consistent with some stripe-model calculations. This picture is also supported by the earlier observation of two components in the electronic structure.<sup>14</sup>

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