

# Photoelectron energy-loss functions of SrTiO<sub>3</sub>, BaTiO<sub>3</sub>, and TiO<sub>2</sub>: Theory and experiment

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(Received 9 July 2001; published 4 February 2002)

We compare experimental O 1s electron energy-loss structures below 30 eV of single crystalline SrTiO<sub>3</sub>, BaTiO<sub>3</sub>, and TiO<sub>2</sub> with their theoretical electron energy-loss functions. The photoelectron energy-loss structures of *in situ* fractured surface in ultrahigh vacuum can be approximated by a sum of four components for SrTiO<sub>3</sub> and BaTiO<sub>3</sub>, and of three components for TiO<sub>2</sub>. Electronic structures were calculated from first principles using the full-potential linearized augmented plane-wave method in the local-density approximation. The momentum matrix elements between Bloch functions were evaluated to determine the electron energy-loss functions. The theoretical electron energy-loss functions agree well with experimental spectra except a structure at around 20 eV of SrTiO<sub>3</sub> and that at around 18 eV of BaTiO<sub>3</sub>. The difference of high binding energy peaks is explained from the positions of semicore states.

DOI: 10.1103/PhysRevB.65.085101

PACS number(s): 79.60.-i, 71.20.-b, 79.20.Uv

## I. INTRODUCTION

Perovskite-type oxides have been a great interest in both the field of basic research and thin-film applications for superconductivity and ferroelectricity. The electronic structure of SrTiO<sub>3</sub> is of interest since stoichiometric SrTiO<sub>3</sub> is highly insulating, but slightly reduced one shows the superconductivity. SrTiO<sub>3</sub> crystallizes in the simple cubic perovskite structure  $Pm\bar{3}m$  ( $O_h^1$ ) at room temperature ( $a = 3.9051 \text{ \AA}$ ).<sup>1</sup> Above the ferroelectric Curie point BaTiO<sub>3</sub> has the same structure while below the temperature a slight tetragonal distortion  $C_{4v}^1$  modifies the perovskite structure. For tetragonal phase BaTiO<sub>3</sub> the difference between the lattice constants of the  $c$  and  $a$  axes is 1% ( $a = 3.9920$ ,  $b/a = 1.000$ , and  $c = 4.0361 \text{ \AA}$ ).<sup>2</sup> The difference in electronic structure between the ferroelectric and paraelectric BaTiO<sub>3</sub> is also interesting since the deviation of crystal structure below and above the Curie point is so small, though the dielectric property changes largely. In these materials a titanium atom is surrounded by six oxygen atoms. In spite of difference from the cubic crystal structure, TiO<sub>2</sub> of rutile structure  $P4_2/mnm$  ( $D_{4h}^{14}$ ) has the same Ti-O coordination as SrTiO<sub>3</sub> and BaTiO<sub>3</sub>. The lattice constants are  $a = 4.5936$  and  $c = 2.9587 \text{ \AA}$ , and the internal coordinate  $u$  is 0.3048.<sup>3</sup> In the unit cell of rutile including two TiO<sub>2</sub> molecules, Ti atoms are positioning at the sites of (0,0,0) and (1/2,1/2,1/2), and four coordinated O atoms occupy at the sites of  $\pm(u, u, 0)$  and  $\pm(u + 1/2, 1/2 - u, 1/2)$ .

Reported fundamental absorption edges of SrTiO<sub>3</sub>,<sup>4</sup> BaTiO<sub>3</sub>,<sup>5</sup> and TiO<sub>2</sub> (Ref. 6) at room temperature are 3.22, 3.15, and 4.0 eV, respectively. The closeness of the absorption edge of SrTiO<sub>3</sub>, BaTiO<sub>3</sub>, and TiO<sub>2</sub> suggests that the edge is predominantly due to transitions between the O 2p to Ti 3d states with admixture of Sr or Ba wave functions. Although the similarity in the crystal field among these materials, there are great discrepancies in superconducting and ferroelectric characteristics. For these materials the differences in detail of electronic structure and dielectric functions are still of fundamental interest. Simple cubic SrTiO<sub>3</sub> offers a natural starting point for the study of the electronic structure and dielectric functions. The crystal-field splitting of the O 2p states occurs because the oxygen resides at a site of tetragonal  $D_{4h}$  ( $4/mmm$ ) point symmetry in SrTiO<sub>3</sub>. The structure of the empty conduction band (CB) could play a decisive role as well as that of the filled valence band (VB) in the electronic properties of SrTiO<sub>3</sub>.

X-ray photoelectron spectroscopy (XPS) is suitable to examine the electronic structure of the filled levels and dielectric response of a solid. The XPS satellite structures are generated by intrinsic and extrinsic processes. The intrinsic satellites are caused by several mechanisms under the influence of a core hole. On the other hand, the extrinsic satellites are caused by the dielectric response to the photoexcited electrons. During the approach of an excited electron to the solid surface, the Coulomb field accompanied with the moving electron interacts with the electrons of the solid via long-range dipole fields. The long-range Coulomb interactions

bring about interband transitions and plasma excitations. Thus the electron energy-loss structure observed in high-resolution XPS can probe unoccupied electronic states of insulators.<sup>7</sup>

In the previous paper,<sup>8</sup> we examined the XPS satellites for SrTiO<sub>3</sub> by comparing with theoretical electron energy-loss functions and experimental electron energy-loss spectroscopy (EELS) spectra. It was found that the O 1s, Sr 3d, and Ti 2p satellites have common features which can be ascribed to extrinsic energy-loss structures. The O 1s and Sr 3d spectra agree well with theoretical energy-loss functions while the Ti 2p spectra show more complicated structure due to intrinsic satellites.

In this paper, we extend the analysis to the experimental O 1s photoelectron energy-loss functions of SrTiO<sub>3</sub>, BaTiO<sub>3</sub>, and TiO<sub>2</sub>. We discuss their similarities and differences from the viewpoint of the electronic structures. We show that all compounds have similar peaks in the electron energy-loss functions because they have a common Ti-O coordination as a local structure unit. We also show that the energy-loss functions have differences which are attributed to the positions of semicore states in A-site cation atoms.

In Sec. II and III, we present the experimental and theoretical results. The experimental spectra are discussed by using the theoretical ones in Sec. IV. Section V is a summary.

## II. EXPERIMENT

For XPS at room temperature we used a Surface Science Laboratories Model SSX-100 spectrometer with monochromatized Al K $\alpha$  source having a diameter of 300  $\mu$ m spot on the sample surface. The pass energy of the spectrometer was set to 50 eV. The solid angle of the input lens of the energy analyzer was 30°. The spectrometer was calibrated utilizing the Au 4f<sub>7/2</sub> electrons (83.79 eV) and the full width at half maximum (FWHM) of the Au 4f<sub>7/2</sub> peak was 1.03 eV.

Fracturing of single crystals *in situ* in ultrahigh vacuum (UHV) is the only reliable way to prepare almost perfect and stoichiometric surfaces indispensable for studying intrinsic surface properties of oxides. The gross electronic structure of the fractured surfaces reflects that of perfect surfaces. At first, single crystals of SrTiO<sub>3</sub>, BaTiO<sub>3</sub>, and TiO<sub>2</sub> from K&R Creation Inc. (Japan) have been cut to smaller pieces ( $\approx 0.5 \times 0.5 \times 3$  mm<sup>3</sup>) for the measurements. Then, the bar of crystals were attached to Cu sample holders and introduced into a measurement chamber. The samples were fractured in a vacuum of  $5 \times 10^{-10}$  Torr at the analyzing position of the measurement chamber, and then we immediately started the measurement of as-fractured spectra. No contamination signals could be detected for 20 min after the fracturing. The binding energies of the measured spectra were corrected with C 1s of 284.7 eV of the contaminated carbon on the surfaces after a long exposure to the vacuum. Since the samples are nonconductive, conditions for a neutralizer were optimized to obtain XPS spectra. Although the peak positions changed from sample to sample, the O 1s spectra had symmetrical single Gaussian profile and excellent reproducibility.

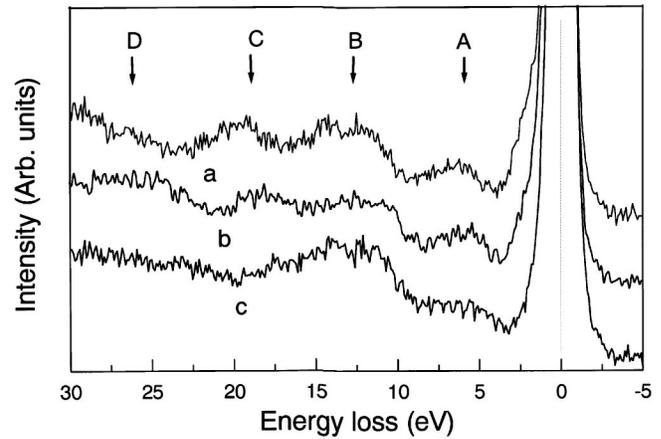


FIG. 1. Experimental electron energy-loss spectra for the O 1s electrons of (a) SrTiO<sub>3</sub>, (b) BaTiO<sub>3</sub>, and (c) TiO<sub>2</sub> *in situ* fractured in UHV.

Using a PHI Model 500 spectrometer with LaB<sub>6</sub> electron gun EELS of the samples prepared in the same way was also carried out in a pressure of  $5 \times 10^{-10}$  Torr for comparison.

Core electrons in the orbitals shallower than Ti 2s can be excited by Al K $\alpha$  radiation. The core lines are followed by energy-loss structure ranging from 3 to 30 eV relative to the zero loss line. The most intense and best resolved line is the O 1s. The Ti 2p spectra showed similar energy-loss structure to that observed for the O 1s spectra, though they are more complicated due to p spin doublet and intrinsic satellites. Since no prominent emission from the region of bulk band gap ( $E_g$ ) was observed in the valence-band (VB) experiment, there are no clear intrinsic surface states, and then alteration to the electron energy-loss function is scarcely expected from the empty surface states. The experimental energy-loss structures of *in situ* fractured SrTiO<sub>3</sub>, BaTiO<sub>3</sub>, and TiO<sub>2</sub> are different from each other as shown in Fig. 1. The energy-loss structure of SrTiO<sub>3</sub> and BaTiO<sub>3</sub> can be approximated by a sum of four components, though that of TiO<sub>2</sub> was approximated by a sum of three components. Structures A and B at around 5.5 and 12.5 eV, respectively, were commonly observed for SrTiO<sub>3</sub>, BaTiO<sub>3</sub>, and TiO<sub>2</sub>. For SrTiO<sub>3</sub> and BaTiO<sub>3</sub> an additional structure C was positioned at around 20 and 18 eV, respectively. The center of structure D varied from at around 29 eV for SrTiO<sub>3</sub> to 26 eV for BaTiO<sub>3</sub>, and to 25 eV for TiO<sub>2</sub>. The perovskite-type crystals are accompanied with the additive electron energy-loss structure C on the three-components structure based on the TiO<sub>6</sub> octahedron crystal field of rutile. It means that A-site cations of the perovskites affect significantly to the origin of these peaks.

## III. CALCULATIONS

We calculated the bulk electronic structures of SrTiO<sub>3</sub>, BaTiO<sub>3</sub>, and TiO<sub>2</sub> within the local-density approximation (LDA),<sup>9</sup> using the WIEN97 package<sup>10</sup> which is based on the full potential linearized augmented plane-wave method. The LDA succeeded to describe the valence and conduction bands of various compounds,<sup>9</sup> however, the LDA failed to

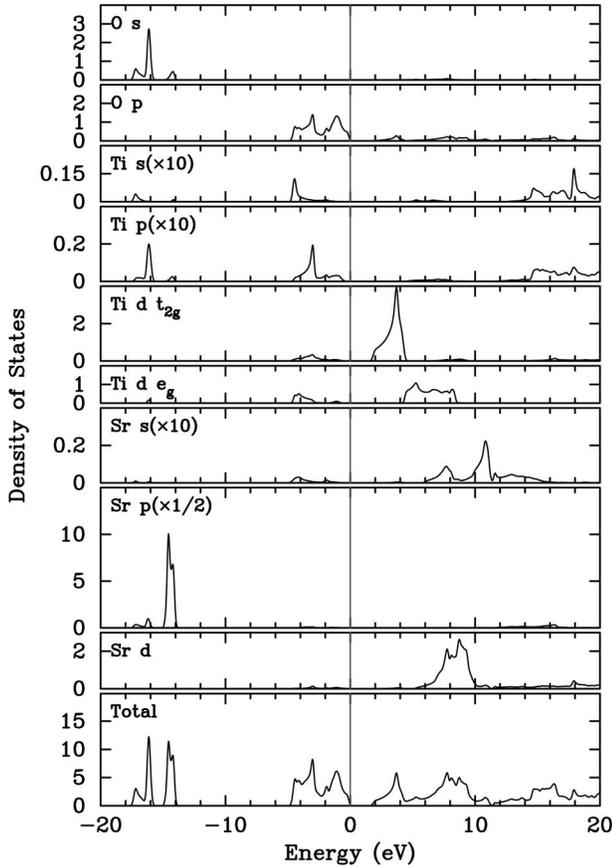


FIG. 2. Calculated density of states (DOS) for SrTiO<sub>3</sub>. The lowest panel shows total DOS in units of states/(eV cell). Other panels show orbital decomposed partial DOS (PDOS) in units of states/(eV atom). The PDOS labeled by ( $\times 10$ ) and ( $\times 1/2$ ) are plotted by scaling with corresponding values.

reproduce the band gaps of semiconductors and insulators. Typically, the band gap obtained by the LDA is only half of the experimental values. Thus the transition energies between valence and conduction bands are also underestimated more or less.

We used cubic structures for SrTiO<sub>3</sub> and BaTiO<sub>3</sub>. The TiO<sub>2</sub> has a tetragonal structure. The Muffin-tin sphere radii  $R$  were chosen as (in a.u.): Sr and Ba, 2.5; Ti, 1.9; O, 1.5. The cutoff  $K_{\max}$  for basis functions is set to  $RK_{\max}=7.0$  where  $R$  is minimum sphere radius, i.e., 1.5 for oxygen. The self-consistent calculations were performed by using  $20 \times 20 \times 20$   $k$ -point sampling for SrTiO<sub>3</sub> and BaTiO<sub>3</sub>, and  $13 \times 13 \times 21$  for TiO<sub>2</sub>.

The calculated densities of states (DOS) shown in Figs. 2–4 are consistent with the previous calculations.<sup>11–18</sup> As common characteristics to all compounds, the band gaps appear between the O  $2p$  valence bands and the Ti  $3d$  conduction bands. As shown in the partial densities of states, the O  $2p$  orbitals and Ti  $3d$  orbitals are hybridized. Below the O  $2p$  bands, the semicore states by O  $2s$  orbitals appear from  $-16$  to  $-18$  eV. For SrTiO<sub>3</sub> and BaTiO<sub>3</sub>, additional semicore states originate from  $A$ -site cation orbitals: Sr  $4p$  from  $-14$  to  $-15$  eV and Ba  $5p$  from  $-9$  to  $-10$  eV.

The states at the bottom of the empty conduction bands

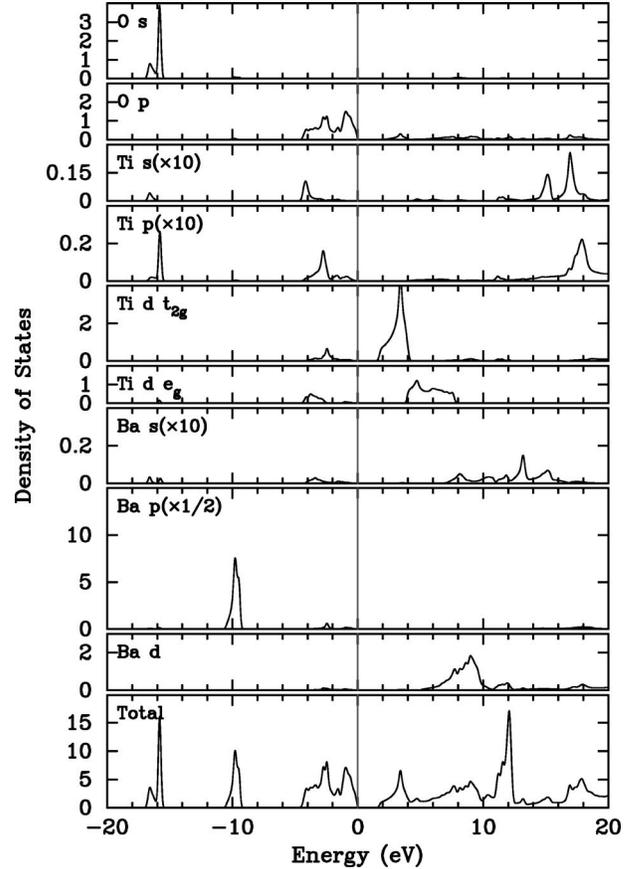


FIG. 3. Calculated density of states (DOS) for BaTiO<sub>3</sub>. The lowest panel shows total DOS in unit of states/(eV cell). Other panels show orbital decomposed partial DOS (PDOS) in unit of states/(eV atom). The PDOS labeled by ( $\times 10$ ) and ( $\times 1/2$ ) are plotted by scaling with corresponding values.

arise from the threefold degenerate Ti  $3d t_{2g}$  orbitals which are lower in energy than the twofold degenerate Ti  $3d e_g$  orbitals. In higher energy region ( $6$ – $12$  eV) for SrTiO<sub>3</sub> and BaTiO<sub>3</sub>, the bands are predominantly formed by Sr  $5s, 4d$  and Ba  $6s, 5d$  orbitals partially overlapping with the Ti  $3d e_g$  bands, but for TiO<sub>2</sub> such  $A$ -site cation contribution does not exist. As a result, the Ti  $3d e_g$  bands distribute a wider energy region for BaTiO<sub>3</sub> and SrTiO<sub>3</sub> than for TiO<sub>2</sub>. The conduction bands above  $14$  eV are mainly composed of Ti  $4s$  and  $4p$  orbitals.

The extrinsic energy-loss structures are generated by the inelastic scattering of photoexcited electrons. Within the Born approximation, the cross section of the inelastic scattering is related to dielectric functions  $\epsilon$  as<sup>19</sup>

$$K(E_0, \omega) = \frac{-\text{Im}[\epsilon(\omega)^{-1}]}{\pi a_0 E_0} \ln \left\{ \frac{\sqrt{E_0 + \sqrt{E_0 - \hbar \omega}}}{\sqrt{E_0 - \sqrt{E_0 - \hbar \omega}}} \right\}, \quad (1)$$

where  $E_0$  is the kinetic energy of the electron and  $a_0$  is the Bohr radius. Here the  $\text{Im}(\epsilon^{-1})$  is assumed to be independent of wave vector. Thus the electron energy-loss structure can be approximated by the  $-\text{Im}(\epsilon^{-1})$  if we ignore multiple-scattering effects. To obtain the theoretical electron energy-

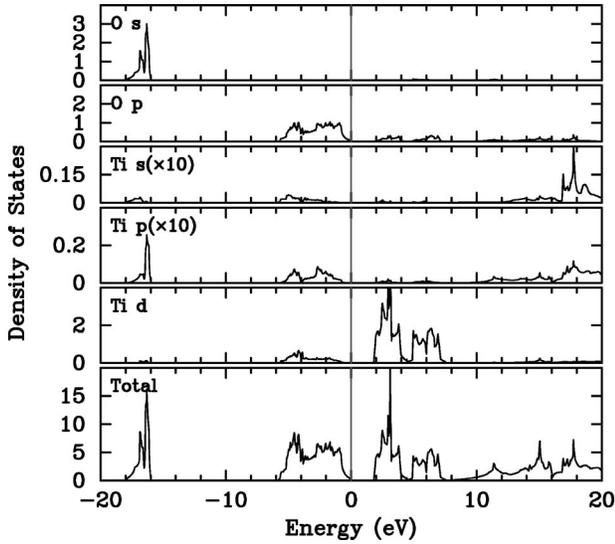


FIG. 4. Calculated density of states (DOS) for  $\text{TiO}_2$ . The lowest panel shows total DOS in units of states/(eV cell). Other panels show orbital decomposed partial DOS (PDOS) in units of states/(eV atom). The PDOS labeled by  $(\times 10)$  and  $(\times 1/2)$  are plotted by scaling with corresponding values.

loss functions, the imaginary part  $\text{Im}(\epsilon)$  of dielectric functions was calculated from the momentum matrix elements between the occupied and unoccupied wave functions.<sup>20</sup> The real part  $\text{Re}(\epsilon)$  was evaluated from the  $\text{Im}(\epsilon)$  by the Kramers-Kronig (K-K) transformation. The electron energy-loss functions of bulk  $-\text{Im}(\epsilon^{-1})$  and surface<sup>21</sup>  $-\text{Im}[(\epsilon + 1)^{-1}]$  were derived from the  $\text{Re}(\epsilon)$  and  $\text{Im}(\epsilon)$  of the calculated dielectric functions. The  $\text{Im}(\epsilon)$ ,  $-\text{Im}(\epsilon^{-1})$ , and  $-\text{Im}[(\epsilon + 1)^{-1}]$  are shown in Fig. 5–7. Since  $\text{TiO}_2$  has tetragonal symmetry, the dielectric functions depend on polarization directions. We present the direction averaged functions in Figs. 5–7. The peaks in the  $-\text{Im}[(\epsilon + 1)^{-1}]$  tend to shift to the lower energy side than in the  $-\text{Im}(\epsilon^{-1})$ .

#### IV. DISCUSSION

In Fig. 5, calculated dielectric functions  $\text{Im}(\epsilon)$  show several broad peaks which can be ascribed to various interband transitions. At 0–15 eV, all compounds have two broad peaks which is caused by the transition from O  $2p$  valence bands to

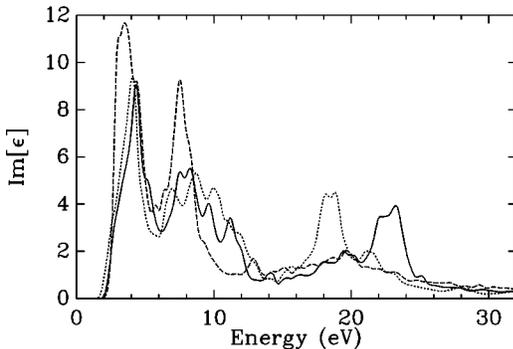


FIG. 5. Calculated dielectric functions. Solid line indicates the function for  $\text{SrTiO}_3$ , dotted line for  $\text{BaTiO}_3$ , dashed line for  $\text{TiO}_2$ .

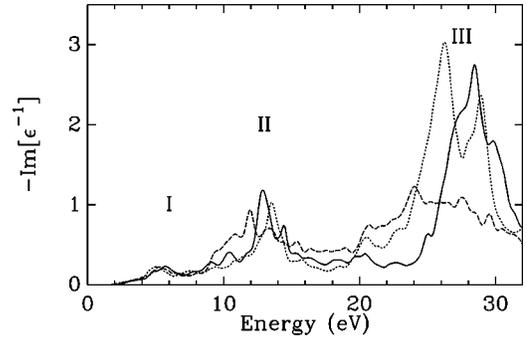


FIG. 6. Calculated electron energy-loss functions. Solid line indicates the function for  $\text{SrTiO}_3$ , dotted line for  $\text{BaTiO}_3$ , dashed line for  $\text{TiO}_2$ .

Ti  $3d$   $t_{2g}$  and  $e_g$  bands. The second peaks in  $\text{SrTiO}_3$  and  $\text{BaTiO}_3$  are broad which is in contrast with the sharp peak for  $\text{TiO}_2$ . This is because Ti  $3d$   $e_g$  bands in  $\text{TiO}_2$  is narrower than in  $\text{BaTiO}_3$  and  $\text{SrTiO}_3$ . At 15–30 eV, all compounds show broad peaks centered at 20 eV. They are ascribed to two types of transitions which are from O  $2s$  semicore states to Ti  $3d$  conduction bands and from O  $2p$  valence bands to high-energy conduction bands (Ti  $4s$  and  $4p$ ). Additional structures appear around 22–24 eV for  $\text{SrTiO}_3$  and 18–20 eV for  $\text{BaTiO}_3$ . They are caused by the transition from Sr  $4p$  (Ba  $5p$ ) semicore states to Sr  $5d$  (Ba  $6d$ ) conduction bands. Since the momentum matrix elements between  $np$  and  $(n+1)d$  orbitals can be large, these peaks are larger than those from O  $2s$  semicore states.

The theoretical energy-loss functions  $-\text{Im}(\epsilon^{-1})$  show several peaks corresponding to various features in  $\text{Im}(\epsilon)$ . It was shown that theoretical energy-loss functions for  $\text{SrTiO}_3$  have three prominent features.<sup>8</sup> These three features also appear for  $\text{BaTiO}_3$  and  $\text{TiO}_2$ . Feature I is caused by the splitting of the Ti  $3d$  bands into  $t_{2g}$  and  $e_g$  subbands. Feature II arises from the resonance of the O  $2p$  valence electrons. Feature III at 20–30 eV is most dominant and corresponds to the plasmonlike collective excitation of the valence and semicore electrons. Feature III of  $\text{BaTiO}_3$  appears to be lower energy than that of  $\text{SrTiO}_3$ . Feature III of  $\text{TiO}_2$  has lowest energy among three compounds and becomes wide. These differences can be explained by the positions of semi-

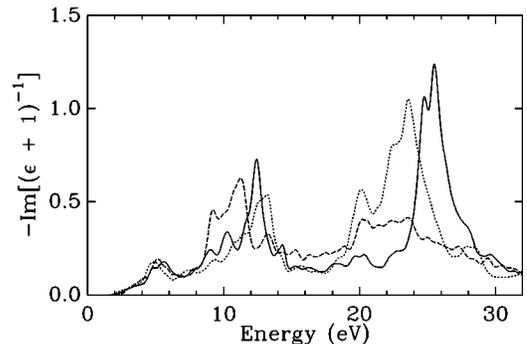


FIG. 7. Calculated surface electron energy-loss functions. Solid line indicates the function for  $\text{SrTiO}_3$ , dotted line for  $\text{BaTiO}_3$ , dashed line for  $\text{TiO}_2$ .

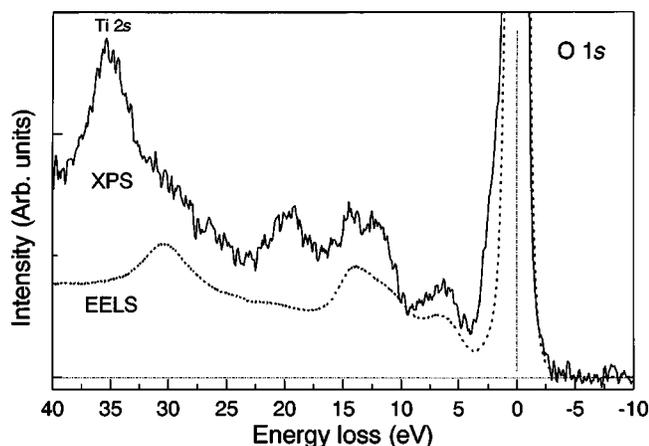


FIG. 8. O  $1s$  spectrum (solid line) with Al  $K\alpha$  radiation and EELS spectrum (dotted line) with  $E_p$  of 1000 eV for SrTiO<sub>3</sub> fractured *in situ* in UHV.

core states. For BaTiO<sub>3</sub>, the broad peaks by Ba  $5p$  states in  $\text{Im}(\epsilon)$  appear at about 5 eV lower energy than that by Sr  $4p$  in SrTiO<sub>3</sub>. Thus feature III which is resonance of valence and semicore electrons appears at lower energy for BaTiO<sub>3</sub>. The A-site cation semicore state is absent for TiO<sub>2</sub> and O  $2s$  is the only semicore state. Therefore feature III of TiO<sub>2</sub> has lowest energy. It is broad because the peak by O  $2s$  semicore state in  $\text{Im}(\epsilon)$  is weak.

The theoretical electron energy-loss functions for all compounds agree with experimental spectra except the structure C in SrTiO<sub>3</sub> and BaTiO<sub>3</sub>. The positions of structure D shift to lower energy in the order of SrTiO<sub>3</sub>, BaTiO<sub>3</sub>, and TiO<sub>2</sub>. This trend is reproduced by Feature III in theoretical spectra. It means that the positions of structure D are affected by the semicore states in A-site cation atoms. Such semicore states are ignored for the discussion of physical properties of these compounds. For low-energy phenomena, it is justified because their positions are far below the valence-band maximum and the excitation from these states are unlikely. However, they would influence the high-energy spectra as shown for electron energy-loss functions.

As described above, for the perovskites the structure of photoelectron energy-loss spectra differs from that of the calculated energy-loss functions, though for TiO<sub>2</sub> the energy-loss structures by experiment and theory agreed with each other. The O  $1s$  energy-loss and EELS spectra of SrTiO<sub>3</sub>, BaTiO<sub>3</sub>, and TiO<sub>2</sub> are shown in Figs. 8–10, respectively. The intensities of the spectra are normalized with the zero-loss peaks. In the EELS the kinetic energy of primary electrons ( $E_p$ ) was set to be 1000 eV, which was nearly equal to 950 eV for that of the O  $1s$  photoelectrons. In EELS the angle between the incident and measured electron beams is a right angle. Then the directly reflected electrons were not included in the EELS spectrum. However, the intensity ratio of inelastic scattering to elastic scattering peaks in EELS was smaller than that of the O  $1s$  photoelectrons for the perovskites. The energy-loss structures by EELS and XPS agree with each other except for the intensity of structure C at around 20 eV for SrTiO<sub>3</sub> and 18 eV for BaTiO<sub>3</sub>. In the EELS for SrTiO<sub>3</sub> and BaTiO<sub>3</sub> relative intensities at around 20 and 18 eV, re-

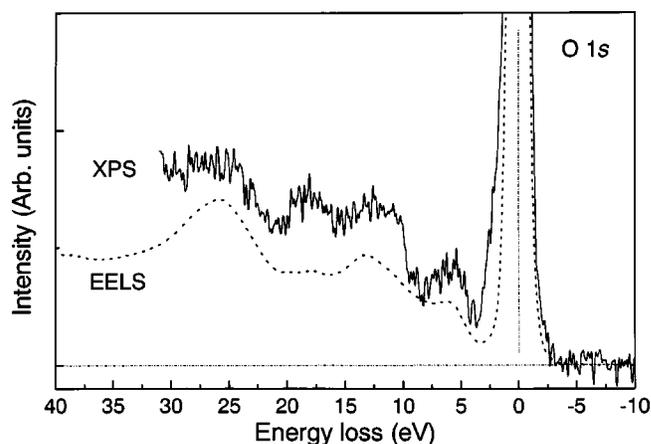


FIG. 9. O  $1s$  spectrum (solid line) with Al  $K\alpha$  radiation and EELS spectrum (dotted line) with  $E_p$  of 1000 eV for BaTiO<sub>3</sub> fractured *in situ* in UHV.

spectively, corresponding to structure C of XPS are so small and in agreement with the calculated energy-loss function in Fig. 6. At present, for SrTiO<sub>3</sub> and BaTiO<sub>3</sub> origins of the disagreement between XPS and EELS, and between XPS and theory, have not yet become clear.

Figure 10 shows the O  $1s$  energy-loss and EELS spectra of TiO<sub>2</sub> *in situ* fractured in UHV. The electrons in EELS twice travel in the sample surface but photoelectrons do once. So EELS spectrum having the same kinetic energy as photoelectrons has more information about the surface than photoelectron spectrum. The shift by  $-1$  eV of EELS spectrum reflects the effect of surface loss function. The photoelectron energy loss at around 5.5, 12.5, and 25 eV of the O  $1s$  structures coincided essentially with those of present EELS and those by theoretical calculation.

## V. SUMMARY

We have presented the experimental and theoretical results on the electron energy-loss functions of SrTiO<sub>3</sub>, BaTiO<sub>3</sub>, and TiO<sub>2</sub>. No intrinsic surface states in the energy

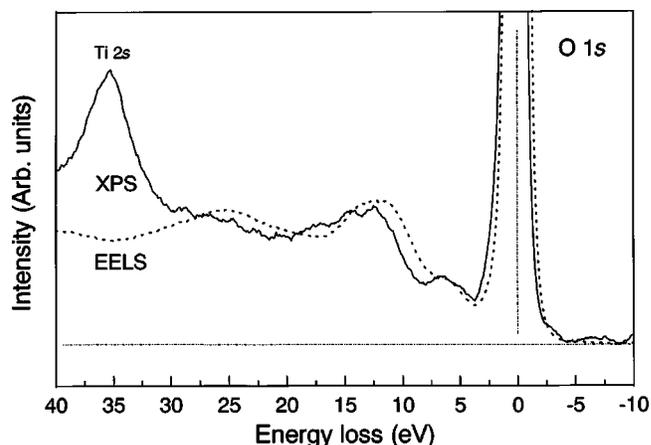


FIG. 10. O  $1s$  spectrum (solid line) with Al  $K\alpha$  radiation and EELS spectrum (dotted line) with  $E_p$  of 1000 eV for TiO<sub>2</sub> fractured *in situ* in UHV.

gaps for *in situ* fractured samples brought about an agreement between the results of a first-principles calculation and the energy-loss structure in the core-level spectra. The XPS with first-principles band calculation can reveal the DOS of unoccupied states since the energy-loss structure of the core-level spectra resulted from the single-particle excitation and collective excitations of valence electrons. For the perovskite-type structure SrTiO<sub>3</sub> and BaTiO<sub>3</sub> there remained apparent disagreement in the energy-loss structures between XPS and theory. Both theory and EELS could not predict additional structure *C* by XPS of the perovskites. The appearance and energy change of the structure *C* for the perovskites suggests that *A*-site cation affects their origins and the lower energy excitation reflects only the Ti *d*-*O p* hy-

bridization. It is found that the positions of structure *D* are affected by the semicore states in *A*-site cation atoms.

#### ACKNOWLEDGMENTS

S.K. is grateful for the support of the Izumi Foundation for Science and Technology in this work. S.K and M.O. express thanks to T. Sato of the Institute for Advanced Materials, Tohoku University, for EELS measurement. The authors thank P. Blaha, K. Schwarz, and J. Luiz for providing us their WIEN97 programs. A part of this work was performed under the interuniversity cooperate research program of Laboratory for Advanced Materials, the Institute for Materials Research, Tohoku University.

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