Raman transport and magnetization study of the RuSr₂ R_{2-x} Ce_xCu₂O_{10+ δ} (R=Gd,Eu) high-temperature superconducting cuprates

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We present the results from a Raman transport and magnetization study on $\operatorname{RuSr}_2 R_{2-x} \operatorname{Ce}_x \operatorname{Cu}_2 O_{10+\delta}$. This compound has been shown to exhibit the coexistence of superconducting and magnetic order. Unlike the other superconducting ruthenate cuprate, $\operatorname{RuSr}_2 R \operatorname{Cu}_2 O_8$, $\operatorname{RuSr}_2 R_{2-x} \operatorname{Ce}_x \operatorname{Cu}_2 O_{10+\delta}$ contains a significant ferromagnetic component. We find that the peak in the low-field zero-field-cooled magnetization data increases with increasing Ce concentration. This increase is mirrored by an increase in the saturation magnetization at 9.5 kG. However, there is no direct correlation between these increases and the superconducting transition temperature. Furthermore, there are no well-defined changes in either the resistance or the thermopower data that can be correlated with the magnetic-ordering transition. A simple explanation for the increase in the saturation magnetization at 9.5 kG is that, similar to SrRuO₃, the RuO₂ layers in RuSr₂ R_{2-x} Ce_xCu₂O_{10+ $\delta}} are itinerant ferromagnetic metals. We show that the RuSr₂<math>R_{2-x}$ Ce_xCu₂O_{10+ δ} transport data can be interpreted in terms of both the resistance and thermopower being dominated by the CuO₂ layers. In this interpretation, the RuO₂ layers only affect the resistance in the CuO₂ layers via exchange coupling and possible spin scattering. The Raman spectra is essentially the same as that found in RuSr₂RCu₂O_{δ} and there is no evidence of Raman modes that can be associated with the R_{2-x} Ce_xO₂ substructure.</sub>

DOI: 10.1103/PhysRevB.64.094515

PACS number(s): 74.72.-h, 74.25.Fy, 74.25.Ha

INTRODUCTION

It has recently been shown that both $RuSr_2R_{2-x}Ce_xCu_2O_{10+\delta}$ and $RuSr_2RCu_2O_8$ (R = Gd, Eu) display superconducting and magnetic order with the magnetic-ordering temperature being up to four times greater than the superconducting transition temperature.^{1,2} These superconductors were discovered by Bauernfeind, Widder, and Braun^{3,4} and the unit cells are assumed to be similar to $TaSr_2Nd_{2-x}Ce_xCu_2O_{10+\delta}$,⁵ NbSr₂Eu_{2-x}Ce_xCu₂O_{10+ δ}, and NbBa₂RCu₂O₈.⁶ Most research effort has been focused on $RuSr_2RCu_2O_8$ where a number of studies have reported that $RuSr_2RCu_2O_8$ is a ferromagnetic superconductor.⁷⁻¹⁴ This generated considerable interest because superconductivity cannot coexist with magnetic order without some form of accommodation, for example, via a spontaneous vortex phase or by a modulation of the respective order parameters.¹⁰ However, a neutron powder-diffraction study showed that the low-field magnetic order in RuSr₂GdCu₂O₈ is predominantly antiferromagnetic in the RuO_2 layers and that there is a magnetic reorientation with increasing applied magnetic field.¹⁵ A magnetization study on RuSr₂EuCu₂O₈ showed that the magnetization data could be interpreted in terms of predominantly low-field antiferromagnetic order $(0.05\mu_B/\text{Ru} \text{ at } 5 \text{ K})$ and a spin reorientation to ferromagnetic order with increasing magnetic field.¹⁶ In the case of RuSr₂GdCu₂O₈ the remanent magnetization is higher $[0.15\mu_B/\text{Ru} \text{ (Ref. 16) or } 0.115\mu_B/\text{Ru} \text{ (Ref. 17) at 5 K] but}$ is still within the upper estimate of a ferromagnetic component determined from a powder-neutron-diffraction study.¹⁵

Although, superconducting $\operatorname{Ru}\operatorname{Sr}_2 R_{2-x}\operatorname{Ce}_x \operatorname{Cu}_2 O_{10+\delta}$ has not been studied as extensively as $\operatorname{Ru}\operatorname{Sr}_2 R \operatorname{Cu}_2 O_8$, it is apparent that it is more interesting because there is evidence that $\operatorname{Ru}\operatorname{Sr}_2 R_{2-x}\operatorname{Ce}_x \operatorname{Cu}_2 O_{10+\delta}$ is a ferromagnet.^{1,18,19} The temperature dependence of the magnetization and the saturation magnetization from $\text{RuSr}_2R_{2-x}\text{Ce}_x\text{Cu}_2\text{O}_{10+\delta}$ (*x*=0.4,0.6) have been interpreted in terms of localized Ru moments with significant spin canting.^{1,18} Furthermore, the data have been interpreted in terms of the coexistence of superconductivity and ferromagnetism where there is a spontaneous vortex phase for temperatures near the superconducting transition temperature.¹⁹

By comparison with the NbSr₂Eu_{2-x}Ce_xCu₂O_{10+ δ} and NbBa₂*R*Cu₂O₈ analogs, it is clear that there should be significant differences in the electronic and magnetic properties of RuSr₂*R*_{2-x}Ce_xCu₂O_{10+ δ} and RuSr₂*R*Cu₂O₈. This is apparent in Fig. 1 where the structures of RuSr₂*R*_{2-x}Ce_xCu₂O_{10+ δ} and RuSr₂*R*Cu₂O₈ are shown (based on the NbSr₂*R*_{2-x}Ce_xCu₂O_{10+ δ} and RuSr₂*R*Cu₂O₈ are shown



FIG. 1. Structures for (a) $RuSr_2RCu_2O_8$, (b) $RuSr_2R_{2-x}Ce_xCu_2O_{10+\delta}$, and (c) $Nd_{2-x}Ce_xCuO_4$.

analogs⁶). The only significant structural difference between NbBa₂RCu₂O₈ and RuSr₂GdCu₂O₈ is that the RuO₆ octahedra in $RuSr_2GdCu_2O_8$ are known to be rotated about the c axis by $\sim 14^{\circ}$ (Refs. 8 and 11) (one study also reported a buckling of the Ru-O-Cu bond¹¹). These rotations form coherent domains extending up to ~ 20 nm. It is not known if the RuO₆ octahedra in RuSr₂ R_{2-x} Ce_xCu₂O_{10+ δ} is also rotated. It can be seen in Fig. 1 that RuSr₂RCu₂O₈ is essenbilayer tially а CuO_2 superconductor. However, $RuSr_2R_{2-x}Ce_xCu_2O_{10+\delta}$ (based on the reported NbSr₂Eu_{2-x}Ce_xCu₂O_{10+ δ} structure) contains an R_{2-x} Ce_xO₂ structure in between the CuO₂ layers that is similar to that seen in the R_{2-x} Ce_xCuO₄ electron-doped T' structure. The comparison is more evident in Fig. 1(c) where we show the R_{2-x} Ce_xCuO₄ T' structure. Thus, the transport and superconductivity behavior in the CuO₂ layers might be expected to be similar to that of the single-CuO₂-layer superconduct-RuSr₂GdCu₂O₈, Unlike the Ru atoms ors. in $\operatorname{RuSr}_2 R_{2-x} \operatorname{Ce}_x \operatorname{Cu}_2 \operatorname{O}_{10+\delta}$ (based) the reported on NbSr₂Eu_{2-x}Ce_xCu₂O_{10+ δ} structure) are not directly above each other in the adjacent RuO₂ layers. It is therefore likely that the Ru-Ru exchange energy in the c axis direction is significantly different.

We have performed a Raman transport and magnetization study of $\text{RuSr}_2R_{2-x}\text{Ce}_x\text{Cu}_2O_{10+\delta}$ with the aim to understand the vibrational, magnetic, and superconducting behavior of $\text{RuSr}_2R_{2-x}\text{Ce}_x\text{Cu}_2O_{10+\delta}$. We show below that the saturation magnetization at 9500 G can be interpreted in terms of itinerant ferromagnetism in the RuO₂ layers. Furthermore, the transport data are dominated by the CuO₂ layers and there is possibly weak coupling between the carriers in the CuO₂ layers and the RuO₂ layers. We also show that the Raman modes are similar to those found in $\text{RuSr}_2R\text{Cu}_2\text{O}_8$.

EXPERIMENTAL DETAILS

The RuSr₂ R_{2-x} Ce_xCu₂O_{10+ δ} samples were made from a stoichiometric mixture of RuO₂, Sr(CO₃)₂, CeO₂, CuO, and Gd₂O₃ or Eu₂O₃. The samples were first annealed in air at 960 °C for 16 h and then (i) heated at 1010 °C in flowing N₂ for 10 h, (ii) heated at 1050 °C in flowing O₂ for 10 h, (iii) heated at 1055 °C in flowing O₂ for 10 h and then (iv) heated at 1060 °C in flowing O₂ for seven days. The samples were then cooled to room temperature at a rate of 4 K/min. The sintering in N₂ gas is required to suppress the SrRuO₃ phase.⁴ This results in Sr₂*R*RuO₆, CeO₂, and CuO. A La_{1.87}Sr_{0.13}CuO₄ sample was made from a stoichiometric mix of La₂O₃, Sr(NO₃)₂, and CuO. The powder was annealed at 700 °C for 1 h and then pressed into pellets, which were heated at 990 °C, 1010 °C, and 1030 °C in air for 48 h.

The samples were characterized and the lattice parameters obtained, using x-ray diffraction (XRD) with a Co K_{α} x-ray tube. The La_{1.87}Sr_{0.13}CuO₄ sample was single phase. There was no evidence of SrRuO₃, CeO₂, CuO, RuSr₂*R*Cu₂O₈, Gd₂CuO₄, or Sr₃Ru₂O₇ in the RuSr₂ R_{2-x} Ce_xCu₂O_{10+ δ} XRD patterns after the final 1060 °C synthesis. However, samples with $x \le 0.8$ displayed a small fraction of excess Sr₂GdRuO₆ (<~7% for x=0.5) with the excess Sr₂GdRuO₆ systematically decreasing with increasing Ce concentration. There

were also extra weak peaks for $x \le 0.8$ that could not be indexed to the RuSr₂ R_{2-x} Ce_xCu₂O_{10+ δ}I4/mmm space group or other possible impurity phases. We show later that the small Sr₂GdRuO₆ impurity fraction did not effect T_c or the magnetization data.

The Raman data were obtained on ceramic-powder samples using the 514.5-nm line of a Ar-ion laser. The incident power was less than 20 mW. The incident light was vertically polarized and the scattered light was unpolarized. However, the polarization sensitivity of the double monochromator and the CCD detector meant that the detected light was predominantly vertically polarized. The resistance data was obtained using the four-terminal technique and the thermopower data was obtained using the standard differential method. The variable-temperature magnetization data were obtained using a vibrating-sample magnetometer for temperatures greater than 15 K and for magnetic fields of up to 10 000 G. One sample was also measured using a SQUID magnetometer.

A part of the RuSr₂Gd_{1.4}Ce_{0.6}Cu₂O_{10+ δ} sample was annealed at 600 °C in 0.1% O₂ and 99.9 % N₂ gas for 14 h. The decrease in δ was estimated from the change in mass to be 0.10 and there was no evidence of superconductivity. Another part of the RuSr₂Gd_{1.4}Ce_{0.6}Cu₂O_{10+ δ} sample was annealed at 100 bars in oxygen for 12 h at 600 °C, ramped to 350 °C over 24 h, and annealed at 350 °C for 72 h. We observed a mass change corresponding to an increase in δ of 0.07.

RESULTS AND ANALYSIS

The RuSr₂Gd_{2-x}Ce_xCu₂O_{10+ δ} lattice parameters were, within experimental error, independent of Ce concentration. We found that $a = (3.840 \pm 0.004)$ A and c = (28.58) ± 0.03) Å. These values are comparable to those reported by Bauernfeind, Widder, and Braun [a=3.836 Å] and c = 28.58 Å (Ref. 3)]. It is particularly interesting to note that the *a*-axis lattice parameter is within the range of that observed in RuSr₂GdCu₂O₈ [a = 3.838 Å (Ref. 3)]. In the case of RuSr₂GdCu₂O₈ it is assumed that the rotations of the RuO₆ octahedra are driven by the large Ru-O-Ru bond length when compared with the Cu-O-Cu bond length. Thus, a similar a-axis lattice parameter in both RuSr₂GdCu₂O₈ $RuSr_2Gd_{2-x}Ce_xCu_2O_{10+\delta}$ may and indicate that $RuSr_2Gd_{2-x}Ce_xCu_2O_{10+\delta}$ also has a rotation of the RuO_6 octahedra.

We find that, while the structure of $RuSr_2Gd_{2-x}Ce_xCu_2O_{10+\delta}$ contains the electron-doped $T'R_{2-r}Ce_rO_2$ substructure, there is no evidence of the corresponding phonon modes. This is apparent in Fig. 2 where we plot the room-temperature Raman spectra from RuSr₂Gd_{1.4}Ce_{0.6}Cu₂O_{10+ δ}. The four peaks at ~260, ~320, ~440, and ~650 cm⁻¹ are also observed in RuSr₂GdCu₂O₈ and have been attributed to oxygen vibrations arising from the Ru-O-Ru, Cu-O-Ru (out of phase), Cu-O-Cu (in phase), and Ru-O-Cu bonds, respectively.¹⁴ There is no evidence in the Raman spectra for peaks that can be attributed to O(4)vibrations from the R_{2-x} Ce_xO₂ substructure. In the case of $Gd_{2-x}Ce_xCuO_4$, Raman peaks are observed at 347, 492, and



FIG. 2. Plot of the room-temperature Raman spectra from $RuSr_2Gd_{1,4}Ce_{0,6}Cu_2O_{10+\delta}$.

596 cm⁻¹. The peaks in the Gd_{2-x}Ce_xCuO₄ Raman spectra at 347 and 492 cm⁻¹ have been attributed to B_{1g} and E_{g} vibrations of O(4), respectively, while the peak at 596 cm⁻¹ is assigned as a A_{1g*} peak, which may be due to O(4) sites in the structures that have been rotated to be directly above Cu.²⁰ It can be seen in Fig. 2 that there is an additional broad peak near 400 cm⁻¹ in the RuSr₂Gd_{2-x}Ce_xCu₂O_{10+ δ} Raman spectra, however, this peak is not near any of the expected $R_{2-x}Ce_xO_2$ substructure peaks. The absence of O(4) vibrations in the RuSr₂Gd_{2-x}Ce_xCu₂O_{10+ δ} Raman spectra may be due to disorder from a variable Ce content and a variable oxygen content in the R_{2-x}Ce_xO₂ substructure.

It can be seen in Fig. 3 that both the zero resistance, $T_c(0)$, and the initial decrease in the resistance, T_c , vary systematically with increasing Ce concentration. This is clearer in the inset to Fig. 3(b) where we plot $T_c(0)$ (open circles) and T_c (filled circles) against the Ce concentration. We find that $T_c(0)$ and T_c are maximum for 0.6 Ce being 35 K and 50 K for $RuSr_2Gd_{1,4}Ce_{0,6}Cu_2O_{10+\delta}$, respectively. In the case of RuSr₂Eu_{1.4}Ce_{0.6}Cu₂O_{10+ δ}, $T_c(0) = 26$ K and T_c = 49 K. The maximum $T_c(0)$ and T_c values are higher than those reported by Felner *et al.* [\sim 20 and 42 K for x = 0.6 and R = Gd (Ref. 1)] and are comparable to those of Bauernfield, Widder, and Braun [38 and 45 K for x = 0.5 and R = Gd (Ref. 3)]. The T_c values for RuSr₂Gd_{1.4}Ce_{0.6}Cu₂O_{10+ δ} are also comparable to those in RuSr₂GdCu₂O₈ [T_c = 45 K (Refs. 9 and 21)]. However, T_c for RuSr₂Eu_{1.4}Ce_{0.6}Cu₂O_{10+ δ} is significantly higher than that in RuSr₂EuCu₂O₈ [$T_c = 32$ K (Refs. 16 and 21)]. It is interesting to note that the values of $T_c(0)$ and T_c in RuSr₂Gd_{1.4}Ce_{0.6}Cu₂O_{10+ δ} are also significantly higher than those reported in nonmagnetic NbSr₂Eu_{1.4}Ce_{0.6}Cu₂O_{10+ δ} (~13 and ~20 K, respectively⁵). This may suggest that T_c is not being significantly affected by the magnetic order in the RuO_2 layers (e.g., by possible magnetic pairbreaking).

It is apparent in Fig. 3 that the resistance data for all the as-made $RuSr_2Gd_{2-x}Ce_xCu_2O_{10+\delta}$ samples display a semiconductorlike increase for low temperatures. However, in the

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FIG. 3. Plot of the resistance from $\text{RuSr}_2\text{Gd}_{2-x}\text{Ce}_x\text{Cu}_2\text{O}_{10+\delta}$ with (a) x = 0.4, 0.5, 0.6 (b) x = 0.6, 0.7, 0.8 1.0. The arrow indicates increasing Ce concentration. The resistance data have been vertically scaled to the same value at 220 K. Also shown is the resistance from the $\text{RuSr}_2\text{Gd}_{1,4}\text{Ce}_{0,6}\text{Cu}_2\text{O}_{10+\delta}$ sample, which was oxygen loaded at 100 bars [dotted curve, Fig. 4(a)], $\text{RuSr}_2\text{Eu}_{1,4}\text{Ce}_{0,6}\text{Cu}_2\text{O}_{10+\delta}$ [dashed curve, Fig. 4(a)], and $\text{RuSr}_2\text{GdCu}_2\text{O}_8$ [dashed curve, Fig. 4(b) inset: Plot of T_c and $T_c(0)$ against Ce content.

case of RuSr₂Gd_{1.4}Ce_{0.6}Cu₂O_{10+ δ}, which has the smallest increase, the semiconductorlike upturn disappears after oxygen loading at 100 bars as can be seen by the dotted curve in Fig. 3(a). The origin of the semiconductorlike upturn in oxygen-deficient samples is not clear. It may be partly due to oxygen depletion at the grain boundaries. We note that Bauernfeind, Widder, and Braun also observed the progressive development of a low-temperature semiconductorlike upturn with increasing oxygen deficiency.³

The resistance transitions are much broader than those observed in many of the other HTSC. For example, the superconducting transition width is about 14 K for the as-made $RuSr_2Gd_{2-x}Ce_xCu_2O_{10+\delta}$ sample. The superconducting transition width is broader than that observed by Bauernfeind, Widder, and Braun³ and it is comparable to that observed by Felner *et al.*¹ Furthermore, as can be seen in Fig. 3(b), the superconducting transition width is comparable to that observed in $RuSr_2GdCu_2O_8$.²¹ Part of the superconducting transition width may be due to oxygen disorder in $RuSr_2GdCu_2O_8$. However, we note that a broad superconducting transition is also expected within the spontaneous vortex phase model.

Unlike some other dopants in HTSC we find that most of the additional electrons introduced by Ce do not appear to be significantly altering the hole concentration on the CuO_2 planes. This is apparent in the inset to Fig. 3(b) where it can

be seen that an increase in x from 0.4 to 0.8 results in a small increase and then decrease in T_c . If all of the electrons were doped onto the CuO_2 planes then the hole concentration *n* should decrease by 0.2. However, by comparison with other HTSC,²² a decrease in n by 0.2 should result in large changes in T_c . This is apparent by noting that most HTSC have been shown to follow the $T_c(n)$ correlation, $T_c(n) = T_{c,\max}[1]$ $-82.6(n-0.16)^2$ where superconductivity occurs for 0.05 $\leq n \leq 0.27.^{22}$ Thus if RuSr₂ R_{2-x} Ce_xCu₂O_{10+ δ} is underdoped (n < 0.16) then T_c should decrease from 43 K for x = 0.4 to 0 for x > 0.6, which is obviously not the case. On the other hand, if we assume that $RuSr_2Gd_{2-x}Ce_xCu_2O_{10+\delta}$ is overdoped, then by comparison with other HTSC, T_c should dramatically increase and then decrease. It is possible that, similar to $Bi_2Sr_2Ca_{1-x}Y_xCu_2O_{8+\delta}$,²³ the additional electrons introduced by Ce4+ are partially compensated for by an increase in δ . For example, an increase in x from 0.4 to 0.8 could be compensated for by an increase in δ of 0.2. It is also possible that the additional electrons introduced by Ce^{4+} are appearing in the RuO₂ layers. The possible effects of a change in δ or a decrease in the Ru valence can be seen using simple valence counting. In the case of RuSr₂GdCu₂O₈ it has been shown from a x-ray absorption near-edge spectroscopy (XANES) study that the Ru valence is +4.6.²⁴ Thus, from simple valence counting, this gives a Cu valence of p =+2.2, which is close to that of underdoped YBa₂Cu₄O₈ and underdoped YBa₂Cu₃O_{7- δ}. From the similar T_c values of $RuSr_2R_{2-x}Ce_xCu_2O_{10+\delta}$ and $RuSr_2GdCu_2O_8$ we might expect that the Cu valence is also $\sim +2.2$ in $\operatorname{RuSr}_2 R_{2-x} \operatorname{Ce}_x \operatorname{Cu}_2 \operatorname{O}_{10+\delta}$. Thus, using $p = 0.5 + \delta + (y)$ (-x)/2, where 5-y is the average Ru valence, assuming that p = +2.2 and using y=0 for x=0.5²⁵ we find that $\delta = 0.03$ for x = 0.5. It is possible that p = +2.2 is maintained for increasing x by a corresponding increase in δ .

We show later that there are significant changes in the low-field magnetization data commencing between 70 and 130 K, depending on the Ce concentration. If the RuO₂ layers contributed significantly to the normal-state conductivity then we might expect the magnetic ordering in the RuO₂ layers to be mirrored by a decrease in the resistance. This is observed in other ruthenate compounds.²⁶⁻²⁸ For example, there is a decrease in the SrRuO3 resistance near the ferromagnetic-ordering temperature (160 K).²⁶ However, it is clear in Fig. 3 that it is not observed in $RuSr_2Gd_{1,4}Ce_{0,6}Cu_2O_{10+\delta}$, even after the 100-bar anneal, and it is also not observed in $RuSr_2RCu_2O_8$.^{9,12,21} In the case of RuSr₂RCu₂O₈ the effect of the RuO₂ layers is observed indirectly by magnetoresistance measurements.^{12,21} It is therefore possible that the RuO_2 layers in $RuSr_2Gd_{1,4}Ce_{0,6}Cu_2O_{10+\delta}$ do not contribute directly to the normal-state conductivity (i.e., $\sigma_{\text{RuO}_2} \ll \sigma_{\text{CuO}_2}$).

We show in Fig. 4 that the thermopower also changes with increasing Ce concentration. It can be seen in the inset to Fig. 4(a) that the room-temperature thermopower initially decreases and then increases with increasing Ce concentration (filled circles). It had previously been argued in the case of RuSr₂GdCu₂O₈ that the room-temperature thermopower S(300 K) of RuSr₂GdCu₂O₈($\sim 60 \,\mu$ V/K) is indicative of a



FIG. 4. (a) Plot of thermopower against temperature from $RuSr_2Gd_{2-x}Ce_xCu_2O_{10+\delta}$ with x=1.0 (open up triangles), 0.8 (open down triangles), 0.6 (open circles), and x = 0.4 (filled circles). Also included is the thermopower from $RuSr_2Gd_{1,4}Ce_{0,6}Cu_2O_{10+\delta}$ that had been annealed at 600 $^{\circ}\mathrm{C}$ in 0.1% O_{2} (solid curve). Inset: against Ce fraction for Plot of *S*(300 K) as-made $RuSr_2Gd_{2-x}Ce_xCu_2O_{10+\delta}$ (filled circles) from $RuSr_2Gd_{1.4}Ce_{0.6}Cu_2O_{10+\delta}$ that had been annealed at 600 °C in 0.1% O₂ (open circle) and from RuSr₂Gd_{1.4}Ce_{0.6}Cu₂O_{10+ δ} that had been oxygen loaded at 100 bars (cross). (b) Plot of the thermopower against temperature for $RuSr_2Gd_{1.4}Ce_{0.6}Cu_2O_{10+\delta}$ (open circles), $RuSr_2Eu_{1.4}Ce_{0.6}Cu_2O_{10+\delta}$ (filled squares), and $La_{1.87}Sr_{0.13}CuO_4$ (plus symbols). Inset: Plot of the thermopower derivative against temperature for $RuSr_2Gd_{1,4}Ce_{0,6}Cu_2O_{10+\delta}$ (open circles) and RuSr₂GdCeCu₂O_{10+ δ} (open up triangles).

very underdoped high-temperature superconductor (HTSC) $[n \sim 0.065 \text{ (Ref. 9)}]$. This was based on the S(300 K) holeconcentration correlation,²⁹ which has been found for most of the HTSC's. A similar interpretation of S(300 K) for $RuSr_2Gd_{14}Ce_{06}Cu_2O_{10+\delta}$ would imply that $RuSr_2Gd_{2-x}Ce_xCu_2O_{10+\delta}$ is a hole-doped HTSC and the maximum hole concentration is ~ 0.10 for x = 0.6. However, there is a problem because according to the S(300 K) vs hole-concentration correlation, *S*(300 K) for $RuSr_2Gd_{2-x}Ce_xCu_2O_{10+\delta}$ should systematically increase with increasing Ce concentration (i.e., decreasing hole concentration). It may be that like $La_{2-x}Sr_{x}CuO_{4}$,³⁰ $RuSr_2Gd_{2-r}Ce_rCu_2O_{10+\delta}$ does not follow the S(300 K) vs hole-concentration correlation or the electrons introduced by Ce^{4+} are partially compensated for by an increase in δ .

The effect of oxygen unloading is to increase S(300 K)while oxygen loading decreases S(300 K) as can be seen in Fig. 4(a) inset for the RuSr₂Gd_{1.6}Ce_{0.4}Cu₂O_{10+ δ} sample. The decrease in oxygen content for the oxygen unloaded sample corresponds to a maximum decrease in the hole concentration in the CuO₂ planes of 0.10. It might be expected that a decrease in δ of 0.10 is equivalent to a 0.20 increase in the Ce content. However, this does not appear to be the case because S(300 K) for the oxygen-reduced sample is even higher than that for the 1.0 Ce sample. We show later that changes in the magnetic order correlate with a decrease in δ of 0.10 corresponding to an increase in x of 0.20.

The temperature dependence of the thermopower for $\operatorname{RuSr}_2 R_{2-x} \operatorname{Ce}_x \operatorname{Cu}_2 \operatorname{O}_{10+\delta}$ has features similar to those found in $\operatorname{RuSr}_2 R \operatorname{Cu}_2 \operatorname{O}_8^{.9,21}$ In particular, S(T) is flat or initially increases with decreasing temperature. At a lower temperature of ~170 K, S(T) begins to decrease for all the samples studied. This is clearer in the inset to Fig. 4(b) where we plot dS/dT against temperature for RuSr₂Gd_{1.4}Ce_{0.6}Cu₂O_{10+ δ} (open circles). The normal-state temperature dependence of the derivative is essentially the same for all the superconducting $RuSr_2R_{2-x}Ce_xCu_2O_{10+\delta}$ samples and is only different for nonsuperconducting RuSr₂RCeCu₂O_{10+ δ} (open up triangles). Although there is no generally accepted model for the thermopower in the HTSC, we believe that the thermopower is dominated by the CuO₂ layers. In two of the other HTSC's, which contain CuO₂ planes and conducting CuO chains or CuO ribbons, it has been shown that the thermopower can be modeled as $S(T) = (\sigma_{CuO_2}/\sigma_T)S_{CuO_2}$ $+(\sigma_{\rm CuO}/\sigma_T)S_{\rm CuO}$, where $\sigma_{\rm CuO_2}$ is the conductivity from the ${
m CuO_2}$ planes, $\sigma_{
m CuO}$ is the conductivity from the CuO chain or ribbons, σ_T is the total conductivity, S_{CuO_2} is the thermopower from the CuO₂ planes, and S_{CuO} is the thermopower from the CuO chain or ribbons.^{30–32} Thus, the interpretation of the RuSr₂ R_{2-x} Ce_xCu₂O_{10+ δ} resistance data in terms of $\sigma_{\rm RuO_2} \ll \sigma_{\rm CuO_2}$ can lead to the thermopower being dominated by the CuO₂ layers.

It is important to note that the decrease in the thermopower below ~170 K does not imply that the decrease is somehow related to the magnetic order. This is apparent in Fig. 4(b) where we also plot the thermopower from underdoped La_{1.87}Sr_{0.13}CuO₄ (crosses). It can be seen that La_{1.87}Sr_{0.13}CuO₄ displays general features similar to those seen in RuSr₂Gd_{2-x}Ce_xCu₂O_{10+ δ}, except that the decrease in *S*(*T*) occurs at a lower temperature (~130 K). Furthermore, as we show later, the peak in the zero-field-cooled magnetization and the saturation magnetization systematically increase with increasing Ce concentration. However, this is not reflected by changes in the temperature dependence of the thermopower.

The rapid decrease in S(T) for RuSr₂ R_{2-x} Ce_xCu₂O_{10+ δ} at low temperatures signals the onset of superconductivity. We find that the zero-thermopower temperature (49 K for R=Gd and 41 K for R=Eu for x=0.6) is close to T_c as determined from the resistance data. Similar behavior is observed in RuSr₂GdCu₂O₈, where zero thermopower occurs at ~49 K, the resistance begins to decrease below 45 K, and a specific-heat jump is observed at 45 K.^{9,21}

It is apparent in Fig. 5(a) that there are systematic changes in the low-field zero-field-cooled (ZFC) magnetization M_{ZFC} from RuSr₂Gd_{2-x}Ce_xCu₂O_{10+ δ} with increasing Ce concentration. In particular, there is a peak in M_{ZFC} at a temperature T_p , which increases in temperature with increasing Ce concentration, and for higher temperatures there is a gradual decrease in M_{ZFC} with increasing temperature. Furthermore,



FIG. 5. (a) Plot of the zero-field-cooled magnetization at 50 G from RuSr₂Gd_{2-x}Ce_xCu₂O_{10+ δ} with x = 0.4, 0.6, 0.8, and 1.0. The arrow indicates increasing Ce fraction. (b) Plot of zero-field-cooled magnetization from RuSr₂Gd_{1.4}Ce_{0.6}Cu₂O_{10+ δ} with H = 50, 250, and 1000 G. The arrow indicates increasing H. Inset: Plot of the maximum zero-field-cooled magnetization temperature at 50 G, T_p , for RuSr₂Gd_{2-x}Ce_xCu₂O_{10+ δ} (filled circles) and RuSr₂Eu_{2-x}Ce_xCu₂O_{10+ δ} (filled up triangles). Also shown is T_p for the RuSr₂Gd_{1.4}Ce_{0.6}Cu₂O_{10+ δ} sample annealed at 600 °C in 0.1% O₂ (open circle) and at 100 bars (cross).

this peak disappears with increasing magnetic field as can be seen in Fig. 5(b). Similar features were observed in $RuSr_2Eu_{2-x}Ce_xCu_2O_{10+\delta}$ for x=0.5 and x=0.6 where the data was interpreted in terms of localized Ru moment magnetic ordering at 180 K, slight spin canting below ~170 K, and Ru-Ru and/or Gd-Ru interactions at lower temperatures.^{1,19} However, as we show later, the saturation magnetization data at 9500 G can be interpreted in terms of itinerant ferromagnetism in the RuO₂ layers. Unfortunately, there are no reports of neutron diffraction or very-high-field magnetization measurements, which would provide a better understanding of the magnetic order in $\text{RuSr}_2R_{2-x}\text{Ce}_x\text{Cu}_2O_{10+\delta}$. In the absence of such data, we associate T_p with the ferromagnetic ordering in the RuO₂ layers. We note again that there was no evidence of SrRuO₃ (magnetic-ordering temperature of 160 K) in the XRD pattern. There was some evidence of Gd₂SrRuO₆ and Eu₂SrRuO₆ but these phases do not magnetically order above 100 K.

We show in the inset to Fig. 5(b) that T_p at 50 G increases systematically with increasing Ce concentration and there is no significant change for R = Gd (filled circles) or R = Eu(filled up triangles). It is not clear if the increase in T_p is due to the additional holes going onto the RuO₂ layers or structurally induced changes in the RuO₂ layer band structure. A similar increase in the magnetic-ordering temperature has



FIG. 6. Plot of the magnetization against H for (a) RuSr₂Gd_{1.2}Ce_{0.8}Cu₂O_{10+ δ} with T=17, 37, 57, 77, 117, and 118 K; (b) RuSr₂Eu_{1.2}Ce_{0.8}Cu₂O_{10+ δ} with T=17, 37, 56, 77, 98, and 121 K. The lower-temperature loops have larger hysteresis. The initial increase in H has been removed for clarity.

been observed in $Ca_{1-x}Sr_xRuO_3$ with increasing x for x > 0.3.^{27,33} However Ca and Sr have the same 2+ valence and hence the increase in T_n with increasing Ca concentration is not due to a simple doping effect. It is interesting to note that the removal of oxygen (i.e., the removal of holes) from $RuSr_2R_{2-r}Ce_rCu_2O_{10+\delta}$ has the same effect on T_n as an increase in Ce concentration (i.e., the removal of holes). This can be seen in the inset to Fig. 5(b) where we plot the data for the RuSr₂ $R_{1,4}$ Ce_{0.6}Cu₂O_{10+ δ} sample, which had been annealed at 600 °C in 0.1% O_2 gas resulting in a decrease in δ by 0.10 (open circle) or an equivalent increase in the Ce content of 0.20. Also shown in the inset to Fig. 5(b) is T_p for the RuSr₂ $R_{1,4}$ Ce_{0.6}Cu₂O_{10+ δ} sample annealed at 100 bars (cross symbol), which results in an increase in the oxygen content of 0.07. It can be seen that T_p decreases in a manner consistent with an equivalent decrease in the Ce content of 0.14.

We show in Fig. 6 that both $\operatorname{RuSr_2Gd_{2-x}Ce_xCu_2O_{10+\delta}}$ and $\operatorname{RuSr_2Eu_{2-x}Ce_xCu_2O_{10+\delta}}$ display similar magnetic hysteresis with increasing applied magnetic field. Here we plot the magnetization against magnetic field for x=0.8. The larger gradient observed for Gd is due to the large Gd moment. It can be seen that both the remanent magnetization and the coercive field decrease with increasing temperature. The resultant remanent magnetization is plotted in Fig. 7 for fully loaded $\operatorname{RuSr_2Gd_{2-x}Ce_xCu_2O_{10+\delta}}$ (solid symbols) and $\operatorname{RuSr_2Eu_{1.2}Ce_{0.8}Cu_2O_{10+\delta}}$ (solid curve). We find that the remanent magnetization from $\operatorname{RuSr_2Gd_{2-x}Ce_xCu_2O_{10+\delta}}$ falls onto a common curve for $0.6 \le x \le 1.0$ and is still finite for temperatures up to 100 K. Oxygen removal for x=0.6 has no significant effect on the remanent magnetization as can be seen by the open circles in Fig. 7.



FIG. 7. Plot of the remanent magnetization against temperature for RuSr₂Gd_{2-x}Ce_xCu₂O_{10+ δ} with x=0.4 (filled down triangles), 0.6 (filled circles), 0.8 (filled up triangles), and 1.0 (filled diamonds). Also included is the remanent magnetization from $RuSr_2Eu_{1,2}Ce_{0,8}Cu_2O_{10+\delta}$ (solid curve) and the $RuSr_2Gd_{1,4}Ce_{0,6}Cu_2O_{10+\delta}$ sample that had been annealed at 600 °C in 0.1% O₂ (open circles). Inset: Plot of the magnetization at 9500 G and 16 K from $RuSr_2Gd_{2-x}Ce_xCu_2O_{10+\delta}$ (filled circles) and $RuSr_2Eu_{2-x}Ce_xCu_2O_{10+\delta}$ (filled up triangles). The Gd^{3+} Curie-Weiss contribution was subtracted from the $RuSr_2Gd_{2-x}Ce_xCu_2O_{10+\delta}$ data. Also shown is the corresponding remanent magnetization (open symbols).

We show in Fig. 8 that the magnetization saturates for moderate magnetic fields (~2500 G) after which the magnetization increases slowly with increasing magnetic field. Here we plot the magnetization $RuSr_2Eu_{2-x}Ce_xCu_2O_{10+\delta}$ from [Fig. 8(a)] and $RuSr_2Gd_{2-x}Ce_xCu_2O_{10+\delta}$ [Fig. 8(b)] at 16 K. The linear saturation of the magnetization observed in RuSr₂ R_{2-x} Ce_xCu₂O_{10+ δ} for magnetic fields above ~2500 G and at 16 K can be contrasted with RuSr₂EuCu₂O₈ [dashed curve in Fig. 8(a) and at 25 K (Ref. 16)], where the magnetization has not saturated for magnetic fields as high as 60 000 G. The magnetization for $RuSr_2Gd_{2-r}Ce_rCu_2O_{10+\delta}$ has a slope that is much greater than that of $RuSr_2Eu_{2-x}Ce_xCu_2O_{10+\delta}$, which is due to the Gd^{3+} moment. In the case of $RuSr_2Eu_{2-x}Ce_xCu_2O_{10+\delta}$, the Van Vleck paramagnetism from Eu³⁺ at 16 K is too small to account for the increase in the magnetization above ~ 2500 G. To characterize the saturation magnetization with increasing Ce concentration, we plot the magnetization at 9500 G and 16 K from $RuSr_2Eu_{2-x}Ce_xCu_2O_{10+\delta}$ in the inset to Fig. 7 (solid up triangles). Also plotted is the magnetization at 9500 G and 16 K from $RuSr_2Gd_{2-x}Ce_xCu_2O_{10+\delta}$ (filled circles) after subtraction of the Curie-Weiss term attributed to the Gd³⁺ moment, which is assumed to be $7\mu_B/\text{Gd}$ (Ref. 2) in $RuSr_2GdCu_2O_8$. It can be seen that the saturation magnetization increases consistently for both



FIG. 8. (a) Plot of the magnetization against *H* at 16 K for RuSr₂Eu_{2-x}Ce_xCu₂O_{10+ δ} with *x*=0.4, 0.6, 0.8, and 1.0. The arrow indicates increasing Ce fraction. The dashed curve is for RuSr₂EuCu₂O₆ and at 25 K.¹⁶ (b) Plot of the magnetization against *H* at 16 K for RuSr₂Gd_{2-x}Ce_xCu₂O_{10+ δ} with *x*=0.6, 0.8, and 1.0. The arrow indicates increasing Ce fraction. The initial increase in *H* has been removed for clarity.

 $RuSr_2Eu_{2-x}Ce_xCu_2O_{10+\delta}$ and $RuSr_2Gd_{2-x}Ce_xCu_2O_{10+\delta}$. Also shown in the inset to Fig. 7 is the corresponding remanent magnetization at 16 K (open symbols).

There are a number of similarities between the magnetic and electronic behavior of the RuO₂ layers in SrRuO₃, RuSr₂*R*Cu₂O₈, and RuSr₂*R*_{2-x}Ce_xCu₂O_{10+ δ}. For example, the octahedral crystal field results in the $4d^4$ band splitting to become a triplet (t_{2g}) state and a higher-energy doublet (e_{o}) valence band. Thus for Ru⁴⁺, the ground state should have S=1 and hence the saturation moment should be $2.0\mu_B/\text{Ru}$. However, in the case of SrRuO₃ and RuSr₂EuCu₂O₈ the saturation moment at 60 kG and 5 K is only $\sim 1.3 \mu_B/\text{Ru}$ (Ref. 27) and $\sim 1 \mu_B / \text{Ru}$ (Ref. 16), respectively. Interestingly, the moment per Ru in SrRuO₃ has not saturated for magnetic fields as high as 300 kG [$\sim 1.4 \mu_B$ /Ru at 300 kG and 50 K (Ref. 27)]. In the case of SrRuO₃ it is now believed that SrRuO₃ is an itinerant ferromagnetic metal as well as a "bad" metal with a very small mean free path.26,27,33 It is therefore possible that the RuO₂ layers in both RuSr₂RCu₂O₈ and $RuSr_2R_{2-x}Ce_xCu_2O_{10+\delta}$ display itinerant magnetic behavior. This interpretation is different from that suggested by a recent XANES study on RuSr₂RCu₂O₈ where the data was interpreted in terms of a mixture of Ru⁴⁺ and Ru⁵⁺ ferrimagnetism and it was suggested that there is a double-exchange interaction in the RuO₂ layers.²⁴ The double-exchange mechanism³⁴ has been invoked to explain the ferromagnetic transition in $La_{1-x}Sr_xMnO_3$, where the ordering is accompanied by a dramatic decrease in the resistivity.³⁵ For the double-exchange mechanism to be valid in RuSr₂RCu₂O₈ and RuSr₂ R_{2-x} Ce_xCu₂O_{10+ δ} we would expect a mixture of $t_{2g}^3 e^1$ (Ru⁴⁺) and t_{2g}^3 (Ru⁵⁺) with S=2 and S=3/2, respectively. Therefore, we might expect the saturation magnetization to be between $4\mu_B/\text{Ru}$ and $3\mu_B/\text{Ru}$. However, as mentioned above, the saturation magnetization at 9500 G and 16 K for RuSr₂ R_{2-x} Ce_xCu₂O_{10+ δ} is less than $1\mu_B/\text{Ru}$. Furthermore, the saturation magnetization at 60 000 G and 5 K for RuSr₂EuCu₂O₈ is only $\sim 1\mu_B/\text{Ru}$.

interpretation The itinerant ferromagnetic for $RuSr_2R_{2-x}Ce_xCu_2O_{10+\delta}$ conveniently explains why the saturation magnetization is less than that expected within a local moment model and why the saturation magnetization varies systematically with increasing Ce concentration. A similar increase in both the saturation magnetization and the magnetic-ordering temperature is observed in $Ca_{1-r}Sr_rRuO_2$ for x > 0.3 where, as mentioned earlier, the substitution of Sr^{2+} for Ca^{2+} is not expected to result in a simple doping effect. The changes observed in $Ca_{1-r}Sr_rRuO_3$ have been interpreted in terms of band effects where the underlying interaction is assumed to be ferromagnetic.^{26,27,33} The lowfield antiferromagnetic order of RuSr₂RCu₂O₈ and the spinflip transition for higher applied fields indicates that the interactions more complex in are $RuSr_2RCu_2O_8$. Antiferromagnetic order is observed in another ruthenate, Sr₂GdRuO₆, but this ruthanate is also an insulator.

CONCLUSION

We have shown that the $\text{RuSr}_2R_{2-x}\text{Ce}_x\text{Cu}_2\text{O}_{10+\delta}$ transport data can be interpreted in terms of the CuO₂ layers dominating the electrical conductivity and the thermopower. There is possibly exchange coupling from the carriers in the RuO₂ layers to the conduction-band carriers in the CuO₂ layers, as is observed in RuSr₂RCu₂O₈. There is a low-field peak in the zero-field-cooled magnetization and the saturation magnetization increases with increasing Ce concentration. However, there is no direct correlation between these increases and the superconducting transition temperature, which may indicate that pairbreaking via coupling to the RuO_2 layers is weak. Although the temperature dependence of the magnetization is complex we show, by comparing the saturation magnetization with that from other ruthenate compounds, that the magnetic order in the RuO₂ layers can be interpreted in terms of itinerant ferromagnetism. The roomtemperature Raman spectra display the same modes found in $RuSr_2RCu_2O_8$ and there is no evidence of O(4) Raman modes that are observed in the electron-doped T'HTSC. This may be due to O(4) site disorder in the R_{2-x} Ce_xO₂ layers, which could arise from a variable oxygen content in the R_{2-x} Ce_xO₂ layers.

ACKNOWLEDGMENTS

Funding support was provided by the New Zealand Marsden Fund and the Alexander von Humboldt Foundation. We acknowledge helpful discussions with H. J. Trodahl and S. Krämer. We thank R. Fairlie for oxygen loading and measuring one of the samples.

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