

Signatures of nearly invisible defects in $\text{PrBa}_2\text{Cu}_3\text{O}_7$ and $\text{Pr}_{2-z}\text{Ce}_z\text{Sr}_2\text{Cu}_2\text{NbO}_{10}$

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Pr_{Ba} and Pr_{Sr} are the defects responsible for the suppression of superconductivity in $\text{PrBa}_2\text{Cu}_3\text{O}_7$ and in $\text{Pr}_{1.5}\text{Ce}_{0.5}\text{Sr}_2\text{Cu}_2\text{NbO}_{10}$, respectively, and are difficult to detect with conventional techniques. Even neutron scattering has difficulty detecting Pr_{Ba} because the scattering lengths of Pr and Ba are so similar. In this paper, we point out how these alkaline-earth-site Pr defects can be readily detected indirectly in fully oxygenated samples, using measurements of the c -axis lengths.

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I. INTRODUCTION

With the demonstration that $\text{PrBa}_2\text{Cu}_3\text{O}_7$ (Fig. 1) superconducts at a critical temperature of roughly 90 K,¹⁻¹² as predicted,^{1,2} it is desirable to know what the conditions are that characterize materials which superconduct. The $\text{PrBa}_2\text{Cu}_3\text{O}_7$ compounds which do superconduct are the ones with few if any Pr-on-Ba-site (Pr_{Ba}) defects,¹³ but these defects are difficult to detect even directly with neutrons, since Pr and Ba have almost the same neutron-scattering lengths.¹⁴ Furthermore, since both Pr and Ba are ions with similar high nuclear charges, x-ray scattering does not discriminate between them easily either.

In this paper, we suggest a way to determine the approximate Pr_{Ba} content in $\text{PrBa}_2\text{Cu}_3\text{O}_7$, by measuring the material's c -axis length with x-ray diffraction. We also argue that a high Néel temperature, the amount of BaCuO_2 impurity phase contained in the sample, the number of O(5) defects, and a short c -axis lattice constant all signal defective material that is unlikely to superconduct. These other quantities, especially the lattice constant, are easier to measure than the number of Pr_{Ba} defects, because the defects are almost invisible even to neutrons.

II. $\text{RBa}_2\text{Cu}_3\text{O}_7$

Flux-grown $\text{PrBa}_2\text{Cu}_3\text{O}_x$ (with $x \approx 7$) (Ref. 15) has a short c -axis lattice constant (and does not superconduct), while the same material grown by the traveling-solvent floating-zone (TSFZ) scheme¹⁵⁻¹⁷ does superconduct and has a longer c axis—near the value predicted by extrapolating data for the other (rare-earth) $\text{Ba}_2\text{Cu}_3\text{O}_7$ compounds (see Fig. 2).^{18,19} The TSFZ material has a critical temperature of 80–85 K,^{15,20} slightly less than the optimal T_c ,⁹ indicating that it still very likely has some Pr_{Ba} defects. Indeed, the prescription for optimizing the critical temperature is both to optimize the oxygen content and to minimize the number of Pr_{Ba} defects. In

this paper, we assume that, to an adequate approximation, oxygen content has been optimized. (We do know that increasing the oxygen content from $x=6$ to $x=7$ leads to contraction of the c -axis length.²¹)

Recently, Araujo-Moreira *et al.*¹² have also reported superconducting $\text{PrBa}_2\text{Cu}_3\text{O}_7$, and their material also has a long c axis, near the line of Fig. 2 and in agreement with TSFZ- $\text{PrBa}_2\text{Cu}_3\text{O}_7$, which also superconducts.

$\text{CmBa}_2\text{Cu}_3\text{O}_7$,²² which has not yet been observed to superconduct, appears to be singularly distant from the line in Fig. 2 that defines the c -axis lengths of the superconductors of this class, as is also the case for flux-grown (nonsuperconducting) $\text{PrBa}_2\text{Cu}_3\text{O}_7$. This suggests that “clean” $\text{PrBa}_2\text{Cu}_3\text{O}_7$ material²² (i) will superconduct and (ii) will have a c -axis length about 0.05 Å longer than the c axis of

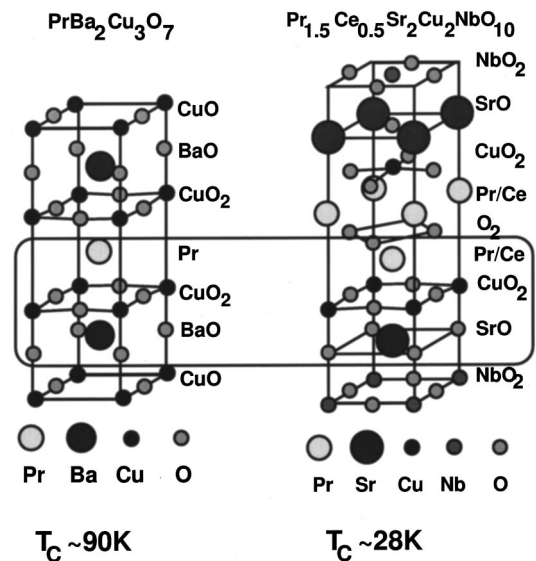


FIG. 1. Crystal structures of (a) $\text{PrBa}_2\text{Cu}_3\text{O}_7$ and (b) $\text{Pr}_{2-z}\text{Ce}_z\text{Sr}_2\text{Cu}_2\text{NbO}_{10}$.

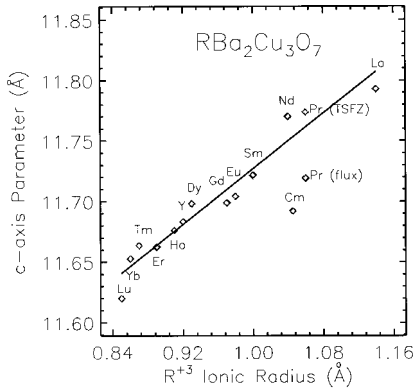


FIG. 2. The c -axis lattice parameter of the $\text{RBa}_2\text{Cu}_3\text{O}_7$, after Ref. 18 versus trivalent rare-earth (R) ionic radius as obtained from Ref. 19. Data for $R = \text{Y}$ and Cm are also included. Two data points are plotted for Pr ; the material with the longer c axis had the lower reported Néel temperature.

the present “dirty” flux-grown material. Certainly the “dirty” $\text{PrBa}_2\text{Cu}_3\text{O}_7$ (and very likely the conventionally prepared $\text{CmBa}_2\text{Cu}_3\text{O}_7$) materials have numerous Pr_{Ba} (and Cm_{Ba}) defects.^{23,24}

III. NÉEL TEMPERATURE

One of the interesting facts about superconducting $\text{PrBa}_2\text{Cu}_3\text{O}_7$ that distinguishes it from nonsuperconducting material is that its Néel temperature is less than 5 K,²⁵ although the Néel temperature of non-superconducting $\text{PrBa}_2\text{Cu}_3\text{O}_7$ is reported to be as high as 17 K for $\text{PrBa}_2\text{Cu}_3\text{O}_7$ (Ref. 26) [and 22 K for $\text{CmBa}_2\text{Cu}_3\text{O}_7$ (Ref. 27)]. We believe that this major reduction in the Néel temperature of superconducting $\text{PrBa}_2\text{Cu}_3\text{O}_7$ samples is due to the absence of Pr_{Ba} defects which occur in contents of order 0.10 in the nonsuperconducting homologues, as in $\text{CmBa}_2\text{Cu}_3\text{O}_7$ (which almost certainly contains Cm_{Ba} de-

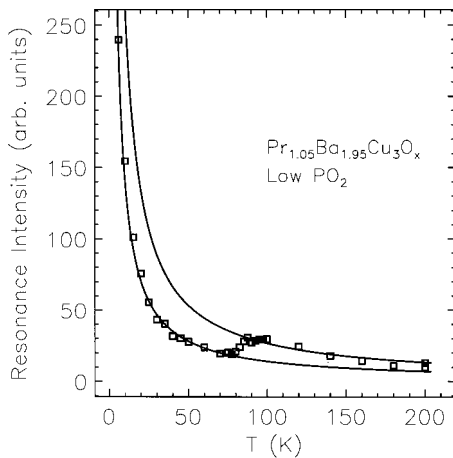


FIG. 3. Cu electron spin resonance intensity (in arbitrary units) versus temperature (in K) of $\text{Pr}_{1.05}\text{Ba}_{1.95}\text{Cu}_3\text{O}_x$ with $x \approx 7$. Note that as the temperature drops through $T \approx 92$ K the number of resonating spins decreases to about half of the number of spins above T_c . This is evidence of a mesoscopic Meissner effect.

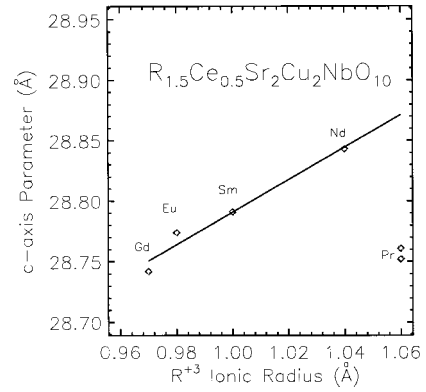


FIG. 4. The c -axis lattice parameter of the $\text{R}_{1.5}\text{Ce}_{0.5}\text{Sr}_2\text{Cu}_2\text{NbO}_{10}$, after Refs. 33 and 34 versus trivalent rare-earth ionic radius as obtained from Ref. 19. Two data points are plotted for Pr ; the material with the longer c axis had the lower Néel temperature.

fects). These Pr_{Ba} (and Cm_{Ba}) defects, in a sense, provide additional coupling between the rare-earth ions Pr_{Pr} (and Cm_{Cm}) by reducing the average distance between them, and hence cause the Néel temperature to increase by increasing the *effective* $\text{Pr}_{\text{Pr}}\text{-Pr}_{\text{Pr}}$ interaction.

IV. BaCuO₂ DEFECTS

When Pr occupies Ba sites, an impurity phase of BaCuO_2 occurs,²⁸ because of the extra material left over. This phase can be detected by Cu electron-spin resonance in *granular* $\text{Pr}_{1+u}\text{Ba}_{2-u}\text{Cu}_8\text{O}_x$ (with $x \approx 7$) (see Ref. 4 for a discussion of sample preparation). The resonance signal varies as NT^{-1} , where T is the temperature and N is the number of resonating spins. Since some of the spins are screened in superconducting material ($T_c \approx 92$ K) by a local Meissner effect (which causes about half of the Cu spins to stop resonating), the number of resonating spins N drops [by almost a factor of 2 for the sample of Fig. 3 (Ref. 4)] when the temperature is decreased through T_c .

V. O(5) DEFECTS

To facilitate substitution of Pr_{Ba} , namely Pr^{+3} on a Ba^{+2} site, some O(5) oxygen forms.²⁹ In all likelihood, about one O(5) for two Pr_{Ba} defects forms to balance charge.³⁰ Therefore the three defects, O(5), BaCuO_2 , and Pr_{Ba} , act as signatures of the formation of imperfect $\text{PrBa}_2\text{Cu}_3\text{O}_7$. Normally the imperfect material does not superconduct, because it contains too many Cooper pair-breaking defects Pr_{Ba} .

VI. LATTICE CONSTANT OF $\text{R}_{1.5}\text{Ce}_{0.5}\text{Sr}_2\text{Cu}_2\text{NbO}_{10}$

An effective way to search for Pr_{Ba} defects in $\text{PrBa}_2\text{Cu}_3\text{O}_7$ is via the c -axis lattice parameter, which is known to be anomalously short in all but the purest materials—and becomes shorter when Pr_{Ba} is present.³¹ The lattice parameter of $\text{Pr}_{1.5}\text{Ce}_{0.5}\text{Sr}_2\text{Cu}_2\text{NbO}_{10}$ is also known to be anomalously short: 28.72 Å (Ref. 32) or 28.75 Å,^{33,34} instead of the 28.87 Å expected by plotting the c -axis parameter versus the triva-

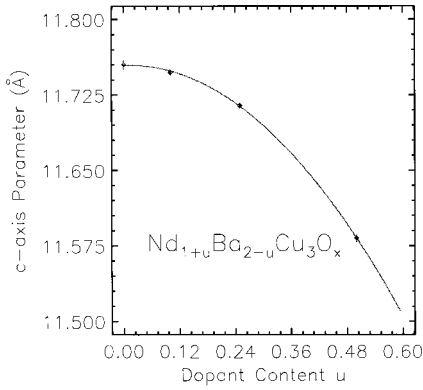


FIG. 5. The c -axis lattice parameter of $\text{Nd}_{1+u}\text{Ba}_{2-u}\text{Cu}_3\text{O}_x$ with $x \approx 7$ versus Pr_{Ba} dopant content u , based on data from Ref. 35. The data are plotted with error bars that are five times as large as they should be (to make them visible).

lent rare-earth radii for all rare-earth ions (Fig. 4). In the case of $\text{Pr}_{1.5}\text{Ce}_{0.5}\text{Sr}_2\text{Cu}_2\text{NbO}_{10}$ (Fig. 1), there is sufficient neutron contrast between Pr and Sr, so that neutrons easily determine that there are about 23% (+7%/-8%) (Ref. 30) Pr_{Sr} defects in the samples we have measured. These defects are also responsible for the short lattice constant.

The Néel temperature of $\text{Pr}_{1.5}\text{Ce}_{0.5}\text{Sr}_2\text{Cu}_2\text{NbO}_{10}$ is apparently controversial. Felner *et al.*³² suggest that the Pr sublattice does not order at all, while Goodwin *et al.* claim that T_N depends on the sample, having reported it to be both 10 K (Ref. 33) and 17 K (Ref. 34). This may be symptomatic of an effect due to Pr_{Sr} defects: The 10 K sample (Fig. 4) has a longer c axis than the 17 K sample, as would be expected for fewer Pr_{Sr} defects.

The authors of Ref. 33 have argued that the mechanism for the suppression of superconductivity in $\text{Pr}_{1.5}\text{Ce}_{0.5}\text{Sr}_2\text{Cu}_2\text{NbO}_{10}$ is the same as in $\text{PrBa}_2\text{Cu}_3\text{O}_7$, and we agree. The mechanism is pair breaking by Pr_{Sr} defects in $\text{Pr}_{1.5}\text{Ce}_{0.5}\text{Sr}_2\text{Cu}_2\text{NbO}_{10}$ (or by Pr_{Ba} in $\text{PrBa}_2\text{Cu}_3\text{O}_7$). By analogy with $\text{PrBa}_2\text{Cu}_3\text{O}_7$, if the Néel temperature is indeed in the range of 10–17 K, as Goodwin *et al.* claim, we suggest that the Néel temperature of $\text{Pr}_{1.5}\text{Ce}_{0.5}\text{Sr}_2\text{Cu}_2\text{NbO}_{10}$ should drop to about 2 K or less if the Pr_{Sr} defects are removed, in which case the material should exhibit bulk superconductivity.

VII. LATTICE CONSTANT OF $\text{PrBa}_2\text{Cu}_3\text{O}_7$

Likewise, we expect a short c axis in defective $\text{PrBa}_2\text{Cu}_3\text{O}_7$, and shall assume that in perfect material

$$c(\text{PrBa}_2\text{Cu}_3\text{O}_7) = c(\text{NdBa}_2\text{Cu}_3\text{O}_7) + \Delta c,$$

where we have $\Delta c = 0.0115 \text{ \AA}$, the difference in the c -lattice constants of $\text{PrBa}_2\text{Cu}_3\text{O}_7$ and $\text{NdBa}_2\text{Cu}_3\text{O}_7$ obtained from the line of Fig. 2.

Consequently we can obtain for $\text{Pr}_{1+u}\text{Ba}_{2-u}\text{Cu}_3\text{O}_7$ a c -axis length as a function of Pr_{Ba} defect content u . Using the fit to the c -axis lattice constants of the $\text{R}\text{Ba}_2\text{Cu}_3\text{O}_7$ compounds (the straight line in Fig. 2), and the dependence on (rare-earth) $_{\text{Ba}}$ antisite defect dopant concentration u found by Kramer *et al.* (Fig. 5),³⁵ we obtain the approximate expression for the (properly oxygenated) c -axis parameter of $\text{Pr}_{1+u}\text{Ba}_{2-u}\text{Cu}_3\text{O}_x$ compounds (where $x \approx 7$) to be

$$c(\text{Pr}_{1+u}\text{Ba}_{2-u}\text{Cu}_3\text{O}_x) = \Delta c + D - Eu - Fu^2,$$

where we have $D = 11.754 \text{ \AA}$, $E = 0.017439 \text{ \AA}$, and $F = 0.72118 \text{ \AA}$.

One thing is clear: the researchers^{7,12} who have fabricated $\text{PrBa}_2\text{Cu}_3\text{O}_7$ with a c axis longer than 11.76 \AA have also observed bulk superconductivity, while those who have found $c < 11.72 \text{ \AA}$ have not observed superconductivity.^{36–38} Clearly the nonsuperconducting materials have short c axes and hence about $u > 0.23$ undetected pair-breaking Pr_{Ba} defects—more than enough to destroy the superconductivity. Ba_{Pr} defects cannot explain the changes in the c -axis length because Ba does not dissolve on rare-earth sites in (rare-earth) $\text{Ba}_2\text{Cu}_3\text{O}_7$ compounds.³⁹

Moreover, it is well known that La easily occupies Ba sites in $\text{LaBa}_2\text{Cu}_3\text{O}_7$, and several researchers have recently shown that there are indeed numerous Pr_{Ba} defects in conventionally prepared $\text{PrBa}_2\text{Cu}_3\text{O}_7$ material.^{40,41} Not only does $\text{NdBa}_2\text{Cu}_3\text{O}_7$ have some Nd_{Ba} defects,⁴² but the Ba site of $\text{PrBa}_2\text{Cu}_3\text{O}_7$ also has some Pr defects, as noted first by Nutley *et al.*⁴³ and more recently by Shukla *et al.*¹¹ The solubility of Pr_{Ba} defects should be between the solubilities of La_{Ba} in $\text{LaBa}_2\text{Cu}_3\text{O}_7$ and Nd_{Ba} in $\text{NdBa}_2\text{Cu}_3\text{O}_7$.

VIII. CONCLUSION

The approximate formula above for the c -axis length can be used to estimate the concentration u of antisite Pr_{Ba} defects, and to infer the quality of $\text{PrBa}_2\text{Cu}_3\text{O}_7$ samples—so that improved sample-preparation procedures can be readily developed. That way, one can determine if the $\text{PrBa}_2\text{Cu}_3\text{O}_7$ is sufficiently defect-free that it is likely to superconduct—or nearly superconduct.

Furthermore, measurements of the BaCuO_2 and the O(5) defect concentrations should confirm the general conclusions drawn from the c -lattice constants, and should facilitate the development of “clean” superconducting $\text{PrBa}_2\text{Cu}_3\text{O}_7$.

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