# Exchange springs in antiferromagnetically coupled DyFe<sub>2</sub>-YFe<sub>2</sub> superlattices

M. Sawicki, G. J. Bowden, P. A. J. de Groot, B. D. Rainford, and J.-M. L. Beaujour Department of Physics and Astronomy, University of Southampton, SO17 1BJ, United Kingdom

R. C. C. Ward and M. R. Wells

Clarendon Laboratory, Oxford University, OX1 3PU, United Kingdom

(Received 13 March 2000)

Molecular beam epitaxy methods have been used to grow single-crystal Laves phase DyFe<sub>2</sub>-YFe<sub>2</sub> superlattice samples with a (110) growth direction. In this paper, magnetization curves for the multilayer samples  $[wDyFe_2/wYFe_2] \times 40$ , with w = 50, 75, 100, 150, and 300 Å, are presented and discussed. Below  $T_C$ , the magnetic moments of the DyFe<sub>2</sub> layers are coupled antiferromagnetically to those of the YFe<sub>2</sub> layers. However, in applied fields, it is possible to generate magnetic exchange springs in the YFe<sub>2</sub> layers, with well-defined bending (onset) fields  $B_B$ . In particular, it is demonstrated, both experimentally and theoretically, that the bending field  $B_B$  is closely proportional to  $1/w^2$ , where w is the thickness of the magnetically soft YFe<sub>2</sub> layer.

#### I. INTRODUCTION

In recent years, research into magnetic exchange springs has received fresh impetus, because it holds out the promise of increasing  $(BH)_{MAX}$  in permanent magnet applications.<sup>1–4</sup> For example, it has been argued that it should be possible to produce magnets with a giant energy product  $(BH)_{MAX}$  of 120 MGOe, by exploiting the exchange-spring mechanism in nanostructured oriented magnets.<sup>3,4</sup> In general, this research has been directed towards sputtered compounds, such as SmCo<sub>5</sub> and Fe, where the hard and soft magnetic layers are coupled ferromagnetically. Such a combination enables the magnetic designer to increase the net magnetization, while maintaining the coercivity associated with the hard layers.

In this paper, we report magnetic measurements on antiferromagnetically coupled hard and soft multilayer samples, grown epitaxially with nanometer control. While antiferromagnetic coupling leads naturally to a decrease in the maximum energy product, it does permits interesting applications. These include engineering magnetic compensation points (in a digital fashion), increasing coercivity, and fabricating magnetic exchange springs. In this paper, we present results for molecular beam epitaxy (MBE) grown, antiferromagnetically coupled, DyFe2-YFe2 superlattice films. In zero field, the larger Dy moments are coupled antiferromagnetically to the weaker Fe moments, and hence to their Fe counterparts in neighboring YFe<sub>2</sub> layers. However, this is not necessarily the case in applied fields above a critical value, known as the bending field  $B_B$ . For fields in excess of  $B_B$ , model exchange springs can be set up in the YFe<sub>2</sub> layers, whose properties are dictated by the thicknesses of the component layers. A schematic drawing of an exchange spring in a single YFe<sub>2</sub> layer can be seen in Fig. 1.

# II. SAMPLE DETAILS, CRYSTAL GROWTH, AND MEASUREMENT

The two magnetic layers in question,  $DyFe_2$  and  $YFe_2$ , belong to the cubic Layes  $O_h^7$ -F3dm MgCu<sub>2</sub>-type intermetallic compound.<sup>5,6</sup> They are both characterized by high Curie temperatures in excess of 600 K, as a result of strong Fe-Fe magnetic exchange. In addition, they also exhibit relatively strong RE-Fe magnetic exchange fields  $\sim 100$  T ( $\sim 100$  K), which gives rise to antiferromagnetic (ferromagnetic) coupling in the heavy (light) RE compounds, respectively. Finally, the direction of easy magnetization is controlled primarily by crystal-field interaction at the RE ion.<sup>7</sup>



FIG. 1. A schematic drawing of an exchange spring in a  $YFe_2$  layer.

5817

For bulk DyFe<sub>2</sub> the easy direction of magnetization is [001] at all temperatures, whereas for YFe<sub>2</sub> it is [111]. But since the magnetic anisotropy of YFe<sub>2</sub> is very much weaker than that of DyFe<sub>2</sub>, the YFe<sub>2</sub> layers can be considered as magnetically soft. Thus the direction of easy magnetization in the samples is likely to be dictated by the properties of the DyFe<sub>2</sub> layers. Finally, it should be noted that the easy direction of magnetization in an MBE grown (110) DyFe<sub>2</sub> film differs from that of the bulk, because of strain induced during crystal growth. Nevertheless, at low temperatures the direction of easy magnetization in MBE DyFe<sub>2</sub> reverts to [001].<sup>8,9</sup>

All of the above-mentioned features have recently been used to engineer a magnetic compensation point in a  $[25-\text{\AA DyFe}_2/50-\text{\AA YFe}_2] \times 40$  sample, with relatively thin individual layers.<sup>9</sup> Because of the strong Fe-Fe exchange fields, all the Fe atoms, in both the DyFe<sub>2</sub> and YFe<sub>2</sub> layers, are constrained to be parallel to each other. So it is possible to balance the net magnetic moments associated with the Dy and Fe atoms, in a digital fashion.

In this paper, we present results for  $[wDyFe_2/wYFe_2] \times 40$  samples, with w = 50, 75, 100, 150, and 300 Å. In these superlattices, exchange springs can be set up in the magnetically soft YFe<sub>2</sub> layers. This leads to an increase in the saturation magnetization, in applied fields greater than a critical field. We shall refer to this field as the bending field  $B_B$ , after Ref. 10.

The DyFe<sub>2</sub>-YFe<sub>2</sub> superlattice samples were grown by molecular beam epitaxy (MBE) techniques using the Balzers UMS 630 UHV facility at Oxford, following a procedure described in Ref. 8. The samples were grown on epiprepared (11 $\overline{2}0$ ) sapphire substrates with a 1000-Å (110) Nb buffer and a 30-Å layer of Fe. The w = 50-Å sample only was grown with an additional YFe2 seed layer to facilitate crystal growth, as reported in Ref. 9. However, no significant improvement in quality was observed and the additional YFe<sub>2</sub> layer only serves to confuse the magnetic moment analysis. The Laves phase compounds were grown by codeposition of elemental fluxes at a substrate temperature of 400 °C in (110) orientation and with the major axes parallel to those of niobium.<sup>9</sup> Because the bulk lattice parameters for DyFe<sub>2</sub> and YFe<sub>2</sub> are 7.325 and 7.363 Å, respectively, the mismatch at the multilayer interfaces is only  $\sim 0.5\%$ . Ex situ the samples were analyzed by x-ray-diffraction techniques, to confirm their single-crystal nature and check the bilayer repeat distance.

The magnetic measurements reported here were made using an Oxford Instruments Aerosonic 3001 vibrating sample magnetometer (VSM). The temperature range covered was 10–300 K, in applied fields of up to 12 T. Typical in-plane magnetization curves for fields applied along the [001] axis can be seen in Figs. 2(a)-(c). Note that the magnetization is given in terms of magnetic moment per formula unit, which we define as  $Dy_{0.5}Y_{0.5}Fe_2$  for all the samples studied.

It will be observed that there is a small jump in the magnetization, in all the magnetization curves, as the magnetic field passes through zero. This step could be due either to (i) nonepitaxial layers at the bottom of the sample, (ii) slight misorientation of the sample, or (iii) contamination of the sapphire substrate, which could occur during sample shap-



FIG. 2. Selected in plane [001] magnetization curves (magnetic moment per average formula unit  $Dy_{0.5}Y_{0.5}Fe_2$ ) for (a) [150-Å DyFe<sub>2</sub>/150-Å YFe<sub>2</sub>]×40, (b) [100-Å DyFe<sub>2</sub>/100-Å YFe<sub>2</sub>]×40, and (c) [75-Å DyFe<sub>2</sub>/75-Å YFe<sub>2</sub>]×40.

ing, with a diamond/steel cutting wheel. Nevertheless, this annoying feature does not negate any of the principle conclusions reached in this paper. Finally, it should also be acknowledged that while the accuracy of the magnetic moment does not allow us to distinguish between the bulk and epitaxial magnetic moments, the relative high accuracy of the VSM still allows us to follow the temperature dependence of the magnetization accurately.

### **III. RESULTS**

From an examination of Figs. 2(a)-(c), it will be observed that all three *M-B* loops show a relatively sharp increase in



FIG. 3. The bending field  $B_B$  as a function of the width of the YFe<sub>2</sub> layer *w*, plotted on a log-log scale.

magnetization, in the positive right-hand quadrant. For example, in Fig. 2(a), the overall increase in magnetization, from 2 to  $4\mu_B$ , commences at the bending field of  $B_B$ = 1.2 T, at 10 K. This increase in magnetization is readily understood in terms of exchange springs. If we ascribe moments of 10 and  $1.5\mu_B$  to the Dy and Fe atoms, respectively, then in the antiferromagnetic state, the net magnetic moment per formula unit  $(Dy_{0.5}Y_{0.5}Fe_2)$  is  $2\mu_B$ . Thus the increase from 2 to  $4\mu_B$  is entirely due to the creation of exchange springs. Furthermore, after saturation, the magnetization curve is found to be reversible if the field is ramped up and down between the coercive field  $-B_C$  and +12 T. This reversibility is a characteristic feature of magnetic exchange springs.<sup>1</sup> Moreover, from an examination of Figs. 2(a)-(c), it is clear that larger bending fields  $B_B$  are required when the thickness of the YFe<sub>2</sub> layers is reduced. This property is highlighted in Fig. 3, which shows the measured bending fields  $B_B$  versus the thickness w of the YFe<sub>2</sub> layer, plotted on a log-log scale. It will be observed that the points fall almost on a straight line. From a least squares fit we find that

$$B_B = k w^n, \tag{1}$$

where

$$n = -1.83 \pm 0.12,$$
  
 $\log_{10}(k) = 4.1 \pm 0.2.$  (2)

This behavior can be explained in terms of a nearestneighbor exchange model, which we outline briefly below.

### **IV. DISCUSSION**

Following Ref. 1, but with minor changes in notation, the total energy for a soft domain wall, with nearest-neighbor interactions only, takes the form

$$E = \sum_{n} \varepsilon(n), \qquad (3)$$

$$\varepsilon(n) = -\mu_{\text{Fe}} B_{\text{APP}} \cos \theta_n - \frac{1}{2} \mu_{\text{Fe}} B_{\text{EX}} [\cos(\theta_n - \theta_{n-1}) + \cos(\theta_{n+1} - \theta_n)].$$
(4)

Note that any anisotropy associated with the YFe<sub>2</sub> layer has been neglected. Also care must be exercised with the spins at the beginning and end of the magnetic exchange spring, which are pinned by the  $DyFe_2$  layers.

For stability, the energy of the entire domain *E* wall must be stable with respect to small partial variations in  $\theta_n$ :

$$\frac{\partial E}{\partial \theta_n} = 0. \tag{5}$$

Proceeding in this fashion, it is possible to determine the set of equilibrium angles  $\{\theta_n\}$ , in an iterative fashion.<sup>11</sup> Moreover, given the equilibrium set  $\{\theta_n\}$ , it is a straightforward matter to calculate the energy of the entire exchange spring and to compare it with the energy of the simple ferromagnetic state (i.e., no exchange spring). In practice, exchange springs will only form when the gain in Zeeman energy outweighs the concomitant loss in magnetic exchange energy. The transition takes place at the bending field  $B_B$ , and from both computer and analytical calculations we find that

$$\frac{B_B}{B_{\rm EX}} = \left(\frac{\pi}{N}\right)^2,\tag{6}$$

where  $B_{\text{EX}}$  is the Fe-Fe exchange field and N is the number of soft YFe<sub>2</sub> monolayers. A more detailed proof of this simple result will be given elsewhere.<sup>11</sup> But for the present we note that  $B_B \propto 1/w^2$ , where w is the thickness of the soft layer. This inverse square law was first derived, many years ago, for bilayer samples.<sup>10</sup> More recently, a similar result has been obtained for the case of a soft magnetic sphere of radius *R*, embedded in a hard magnetic medium.<sup>12</sup>

As noted earlier, the experimentally determined exponent of w falls slightly below that of -2. However, we believe that the experimentally determined figure of  $-1.83\pm0.12$  is acceptable, given the uncertainties associated with spin pinning at the edges of the YFe<sub>2</sub> layer. In this regard, preliminary TEM measurements show that the surface roughness of the interfaces could be as high as  $\pm 5$  Å.<sup>13</sup>

Finally, we can use Eq. (6), and the bending fields shown in Figs. 2(a)–(c), to make an estimate of the magnetic exchange field. For example, for the w=100-Å sample, the effective number of Fe monolayers N is ~55, where we have assumed that there are four Fe layers per unit cell. Thus on using  $B_B=3.0$  T, we find  $B_{\rm EX}$ ~910 T. This figure is in excess of the figure of 680 T, given by Ref. 6 and may reflect the inadequacies of the nearest-neighbor effective-field model.

### **V. CONCLUSIONS**

We have presented magnetization results for MBE grown DyFe<sub>2</sub>-YFe<sub>2</sub> superlattice samples, with antiferromagnetic coupling between the two component layers. The results show the existence of model exchange springs in the magnetically soft YFe<sub>2</sub> layers, pinned at their edges by the mag-

where

netically hard DyFe<sub>2</sub> layers. These exchange springs are characterized by well-defined bending (onset) fields  $B_B$ , which are proportional to  $1/w^n$ , where the experimentally determined exponent *n* is almost 2.

# ACKNOWLEDGMENTS

This work has been supported by the Advanced Magnetics Program of the EPSRC, and DERA-Farnborough, UK. We also acknowledge useful discussions with G. J. Tomka.

- <sup>1</sup>E. E. Fullerton, J. S. Jiang, M. Grimsditch, C. H. Sowers, and S. D. Bader, Phys. Rev. B 58, 12 193 (1998).
- <sup>2</sup>E. E. Fullerton, J. S. Jiang, and S. D. Bader, J. Magn. Magn. Mater. **200**, 392 (1999).
- <sup>3</sup>J. M. D. Coey and R. Skomski, Phys. Scr. **T49**, 315 (1993).
- <sup>4</sup>R. Skomski and J. M. D. Coey, IEEE Trans. Magn. **29**, 2860 (1993).
- <sup>5</sup>For a review, see K. H. J. Buschow, Rep. Prog. Phys. **40**, 1179 (1977).
- <sup>6</sup>J. J. M. Franse and R. J. Radwanski, in *Handbook of Magnetic Materials*, edited by K. H. J. Buschow (North-Holland, Amsterdam, 1993), Vol. 7.
- <sup>7</sup>G. J. Bowden, D. St. P. Bunbury, A. P. Guimaraes, and R. E.

Snyder, J. Phys. C 1, 1376 (1968).

- <sup>8</sup>V. Oderno, C. Dufour, K. Dumesnil, Ph. Bauer, Ph. Mangin, and G. Marcal, Phys. Rev. B 54, R17 375 (1996).
- <sup>9</sup>M. Sawicki, G. J. Bowden, P. A. J. de Groot, B. D. Rainford, R. C. C. Ward, and M. R. Wells, J. Appl. Phys. **87**, 6839 (2000).
- <sup>10</sup>E. Goto, N. Hayashi, T. Miyashita, and K. Nakagawa, J. Appl. Phys. **36**, 2951 (1965).
- <sup>11</sup>G. J. Bowden, P. A. J. de Groot, B. D. Rainford, and M. Sawicki (unpublished).
- <sup>12</sup>R. Skomski and J. M. D. Coey, *Permanent Magnetism* (IOP Publishing Ltd., Bristol, 1999), p. 178.
- <sup>13</sup>E. Grier (private communication).