# **Local detection of the optical magnetic field in the near zone of dielectric samples**

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We present a study of the influence of the probe composition on the formation of constant-height photon scanning tunneling microscope images when observing a dielectric sample. Dramatic effects due to the metallization of the tip are presented and discussed in detail. We show how the recorded images can look quite different when the probe is dielectric or coated with gold. Comparison with numerical calculations indicate that the experimental signals are of electric or magnetic nature depending on the composition of the tip. For well-defined conditions, gold-coated tips provide images of the distribution of the *magnetic field intensity* associated with the optical near field. To get more insight into the origin of this effect, we have performed a careful analysis of the plasmon modes associated with a gold-coated dielectric cylinder. We conclude that the detection of the optical magnetic field is related to the conditions of excitation of *circular symmetry plasmon*, or *ring plasmon*, in the gold-coated tip.

## **I. INTRODUCTION**

In optical near-field devices, $\frac{1}{1}$  the local detection of the optical signal relies on the use of nanometer-sized probes. These probes are generally sharpened optical fibers that are employed in two basic configurations. In the generic scanning near-field optical microscope (SNOM) configuration, the probe acts as a local source of evanescent optical fields, while in the generic photon scanning tunneling microscope  $(PSTM)$  setup,<sup>2</sup> the probe behaves as a local detector of light. In order to achieve a narrower localization of the incident light on the sample surface, SNOM tips are usually coated with a thin metal layer. For this purpose, Al is the most widely used metal, although very few works have been devoted to the influence of various tip compositions when observing a given reference sample using a SNOM setup.<sup>3</sup> By analogy, it was believed that a proper metal coating of the tips would also improve the resolution of the PSTM configuration. However, the first PSTM attempts using Al-coated tips have shown limited improvement due to the concomitant degradation of the signal to noise ratio related to the very low transmission through such a coating. In order to reduce this noise, *fully* gold coated tips (with no resulting apertures at the apex) were recently used. $4$  Surprisingly, it turned out that these probes recorded isointensity images with an inverted contrast relative to the contrast obtained with (uncoated) dielectric tips. These results have clearly indicated that the detected signal may reveal different physical phenomena according to the probe composition. Calculations of magnetic or electric field maps, at constant height above a well-defined sample<sup>4–6</sup> have allowed us to interpret these different kinds of contrasts. While the dielectric tip always collects a signal proportional to the square modulus of the electric near field, the images recorded at the incident wavelength  $\lambda$  = 633 nm, for a well-defined gold thickness on the probe, display the same patterns as the theoretical maps of the square modulus of the *magnetic* field associated with the

optical near field. However, the first experiments suggesting a possible detection of the magnetic field $4.5$  raised several important questions that we intend to answer in the present work.

In this paper, we find the precise conditions for the occurrence of this phenomenon by proceeding to a systematic study of a well-defined dielectric sample in various experimental configurations. In Secs. IV and V, we discuss a series of PSTM images we have obtained with different probe tips (uncoated or fully coated), at two different incident wavelengths and for both transverse magnetic and transverse electric incident polarizations. Our analysis confirms the possibility to detect, in well-defined conditions, the optical magnetic near field with gold-coated tips. Moreover, the results also provide indications about the effective height of detection in PSTM experiments.

A recent hypothesis, given in Ref. 4, suggests that the magnetic field detection could be justified by the existence of plasmon eigenmodes in the fully coated tip, at the red laser frequency ( $\lambda$  = 633 nm) used in the first experiments. More precisely, it was assumed that these plasmons could be able to radiate a net optical energy proportional to the optical magnetic field scattered or confined by the sample structures. Since the excitation of a plasmon depends strongly on geometrical features, we have examined two geometries that could possibly account for this particular detection process. First, we may assume that the red laser frequency excites a small gold particle at the apex of the tip. Alternatively, the gold coating around the dielectric core has a circular symmetry, which may sustain a particular collective motion of the electron gas of the metal. It would then give rise to a circular symmetry plasmon, an expression that we shorten to *ring plasmon*. We have discarded the first hypothesis because the red laser frequency is not a surface plasmon eigenfrequency of a spherical gold particle having the dimensions of the apex of the tip.7,8

To check the second geometry, we have modeled this

apex by a thin dielectric cylinder coated with gold and calculated the dispersion relation of plasmons associated with such a geometry. Section VI demonstrates that the red laser frequency is indeed a plasmon eigenfrequency of this tip model for radii and optical properties corresponding to those of the tips used in the experiments. A first experimental test of this hypothesis appears in Sec. VII A where we present images recorded with ''semicoated'' probes that are obtained by depositing an asymmetric metallic layer around the dielectric core. Indeed, if the detection of the magnetic field is related to the circular symmetry of the collective excitation around the core, it should not occur if the symmetry conditions are broken. We effectively observed that semicoated probes behave like (uncoated) dielectric probes.

As a second experimental check to support the model of coated cylinder, we have repeated the detection of the optical magnetic field at another wavelength  $(\lambda = 543 \text{ nm})$  on the basis of the ring plasmon resonance conditions in the probe coating. From the dispersion relation of the coated cylinder model, we have adjusted the gold-coating thickness in order to excite a ring plasmon at  $\lambda$  = 543 nm. At this wavelength and with the preset value of the gold coating on the tip, we obtained the same contrast as a calculated map of the square modulus of the magnetic field again (Sec. VII B). For very precise experimental parameters, we thus succeeded in reproducing the phenomenon of magnetic field detection from the hypothesis of the existence of a ring plasmon sustained by the gold coating. Moreover, the detection of the optical magnetic field with gold-coated tips was surprisingly found to be equally efficient as the detection of the optical electric field with bare dielectric tips provided that the conditions of plasmon excitation are satisfied.

## **II. EXPERIMENTAL SETUP**

We use a D3000 scanning force microscope (Digital Instruments) in which the atomic force microscope (AFM) cantilever is replaced by a sharpened optical fiber when it is used in the PSTM configuration. This fiber tip is brought piezoelectrically close to the sample surface and behaves like a local probe. The sample is illuminated in total internal reflection and most of the intensity collected by the fiber corresponds to the evanescent part of the light scattered by its surface. Different lasers have been used to observe the influence of the wavelength of the incident light on the recorded images: a red laser (wavelength  $\lambda$  = 633 nm) and a green laser ( $\lambda$ =543 nm). A polarizer is placed between the laser and the prism on which the sample lies.

An AFM image of a typical dielectric sample we have studied appears in Fig. 1. Seven glass pads deposited on a glass substrate are the result of a microfabrication process based on electron beam lithography. Their lateral size is about 130 nm and their height is about 100 nm. The closest distance between the two pads is 900 nm. This pattern is reproduced every 20  $\mu$ m along horizontal lines on the sample surface. This has allowed us to scan on different patterns and explains the differences (defects, incomplete patterns, etc.) that can be observed on the various experimental images reported in this paper. Indeed, in the case of a tip crash, we had to change the zone scanned by the probe. The



FIG. 1. AFM image of the sample. Tracks close to the pads along the scanning direction are due to the presence of water on the sample.

glass substrate has the same index of refraction as the prism on which it lies.

The images have been recorded in constant-height mode  $(512\times512$  pixels), which is possible by tuning the gain of the electronic feedback. The gray scale of the experimental images presented in this paper thus corresponds to the variations of the detected intensity in a plane parallel to the sample surface (no auxiliary force feedback). The amplification of the signal upon using the green laser had to be increased because it was less powerful than the red one. Therefore, the images recorded at  $\lambda$  = 543 nm were somewhat noisy. We have filtered this noise by the Savitzky-Golay algorithm, which allows us to smooth the data with minimal broadening.9 For each series of images, the tip approaches the sample as close as possible until contact occurs. By *series*, we mean that we have used the same tip, the same incident wavelength, and the same polarization of the laser. A series is thus the sequence of images recorded at different set points of the near-field microscope, where each successive set point brings the tip apex at a smaller constant height above the sample surface.

Since, as shown in previous works,  $4,11$  the optical response is not necessarily bright above a pad, we need to know the localization of the pads relatively to the observed optical response. In order to avoid artefacts related to any kind of auxiliary force feedback, $10$  the only reliable way to localize a pad is to note where the tip touches the surface first in the near-field image. Indeed, the tip will crash and destruct into one of the pads as one reduces the constant height of scan above the surface. Most of the images we present here have been recorded presumably a few nanometers above the pads, at the last set point that allowed scanning without crashing into one pad. Any arrow reported in the image of this paper indicates where the tip crashed when scanning at the next smaller height. This procedure relies on a tip production facility delivering well-reproducible tip designs at high rate. The probes we used for this work are multimodes fibers that are sharpened by pulling. Such probes are not so



FIG. 2. Definition of the angles  $\theta$  (angle of incidence) and  $\psi$ (azimuthal angle). In the PSTM experiments presented in this paper, their values are  $\theta$ =60° (total internal reflection) and  $\psi$ =90°, i.e.,  $\widetilde{k_{\parallel}}$  along *y*.

sharp as those used in Refs. 4 and 11, which were obtained by chemical etching, but they are more reproducible. After the pulling, the fiber can be placed in a calibrated evaporator where it is fully coated (no resulting aperture at the apex) with gold while turning around its axis. The deposition process has a 1 nm accuracy determined by a device relying on the use of a quartz weighing apparatus.

# **III. THE GREEN'S DYADIC METHOD AS AN INTERPRETATION TOOL**

The contrast observed in the images can be interpreted as a result of numerical simulations. Indeed, previous PSTM works $^{11,12}$  have established that dielectric tips detect the electric field associated with the optical wave close to the sample surface because the observed contrasts correspond to the square modulus of the electric field distribution, as given by the solution of Maxwell equations *that does not include the tip*. In order to understand the contrasts of the experimental constant-height images, we keep following the principle of finding the relation between the experimental images and the solution of Maxwell equations, as computed in the absence of the tip. For the sake of our demonstration, we just need reliable theoretical constant-height maps of the electric and magnetic near-field distributions that can be considered like the images due to a pointlike detector. For this purpose, we used a numerical solver that computes the electromagnetic near-field distribution in a plane parallel to the sample surface, when it is illuminated in total internal reflection by polarized light. It is based on the Green's dyadic method,  $13-15$  which is proven to be an efficient computation technique for the typical parameters of near-field optics. The input geometry of the computations was given by an AFM data file recorded previously on the sample  $(Fig. 1)$ . These data are made discrete by cubic cells of 30 nm $\times$ 30 nm $\times$ 30 nm. The illumination conditions are chosen as follows:  $\theta$  $=60^{\circ}$  (angle of incidence in the prism) and  $\psi=90^{\circ}$  (azimuthal angle) (Fig. 2). In the experiment, the angle  $\theta$  is fixed but the angle  $\psi$  is not so well controlled since it depends on the initial orientation of the sample on the prism. It may also be modified by a misalignment of the patterns on the substrate. In all the calculations, the detected intensity is calculated in a plane that is located at a constant height  $z_{ref}$  above the sample surface, without accounting for the tip. It is then normalized to the calculated intensity at the same height when there is no pad on the surface of the glass substrate.

According to the state of polarization of the incident light and to the composition of the tip, the contrasts of the images change dramatically. Following a procedure detailed recently in Ref. 12, we have sought the value  $z_{ref}$  that results in the best agreement with the experimental images. In order to reproduce their contrasts when they are recorded with dielectric tips, a different value of  $z_{ref}$  is required according to the state of polarization: we found  $z_{ref} = 150$  nm for the TM incident polarization and  $z_{ref}$  around 200 nm for the TE incident polarization. Some of the images recorded with goldcoated tips have been compared to magnetic field intensity maps. For both incident polarizations, the best agreement was found near the observation plane located at  $z_{ref} = 130$ nm.

The short-range parts of the propagators of the electric<sup>22,14</sup> and magnetic<sup>6</sup> fields can be used to understand the origin of the PSTM contrast at the immediate proximity of the dielectric pads. Let us assume that a given pad is discretized by a *single* cell located at  $\vec{r}' = (0,0,z')$ . Within the first Born approximation and with the harmonic time dependence, the total field  $\vec{E}(\vec{r})$  at a point  $\vec{r} = (0,0,z)$  is given by<sup>13</sup> (Gaussian units)

$$
\vec{E}(\vec{r}) = \vec{E}_0(\vec{r}) + \vec{E}_s(\vec{r}) \approx \vec{E}_0(\vec{r}) + \vec{S}^0(\vec{r} - \vec{r}')V(\vec{r}')\vec{E}_0(\vec{r}'),
$$
\n(1)

where  $\vec{E}_0(\vec{r})$  is the electric field incident under the condition of total internal reflection and  $V(\vec{r}')$  is the perturbation expressing the fact that the pad on the surface creates a dielectric function contrast. The constant  $\alpha$  having the dimension of a volume, one can approximate the short-range propagator<sup>14</sup> of the electric field  $\overrightarrow{S}^0(\overrightarrow{r} - \overrightarrow{r})$  as follows:

$$
\overline{S'}^{0}(0,0,z-z')V(\overrightarrow{r'})
$$
\n
$$
\approx \alpha \begin{pmatrix}\n-(z-z')^{-3} & 0 & 0 \\
0 & -(z-z')^{-3} & 0 \\
0 & 0 & (z-z')^{-3}\n\end{pmatrix}.
$$
\n(2)

Therefore, the scattered field  $\vec{E}_s(\vec{r})$  represents the modification of  $\vec{E}_0(\vec{r})$  due to the perturbation  $V(\vec{r}')$ . Table I gives the components of  $\vec{E}_s(\vec{r})$  and the contrasts that are expected to be observed on an experimental PSTM image. For example, when the incident field is TE polarized, the scattered electric field has a negative sign. In the near-field zone, a dark contrast is then associated with the total electric field, which is less intense than the incident field. For a TM polarized field, the magnitude of  $\tilde{E}_{0,y}$  is smaller than  $\tilde{E}_{0,z}$ . The resulting bright near-field contrast is mainly due to the *z* component of the scattered electric field, which turns out to be positive and is enhanced by a factor of 2.

A similar approach may be followed when reasoning on the basis of the magnetic part of the incident optical wave  $\vec{B}_0(\vec{r})$ . In this case, we use once again the first Born approximation. The total magnetic field  $\vec{B}(\vec{r})$  is then given by

TABLE I. When modeling a nanoscopic dielectric pad by a single discretization cell and keeping only the (approximated) short-range part of the electric field propagator, components of the scattered electric field  $\vec{E}_s(\vec{r})$  as a function of the polarization of the incident field  $\vec{E}_0(\vec{r})$  can be found.  $\vec{e}_j$  ( $j=x,y,z$ ) are the unit vectors in Cartesian coordinates such that  $\vec{e}_z$  is perpendicular to the sample surface.

Incident polarization	$E_0(r)$	$\alpha^{-1}\vec{E}_{s}(\vec{r})$	Near-field contrast
TE	$E_{0,x}e_x$	$-(z-z')^{-3}E_{0x}e_{x}$	Dark
TМ	$E_{0,y}e_{y}+E_{0,z}e_{z}$	$-(z-z')^{-3}E_{0y}\vec{e}_y+2(z-z')^{-3}E_{0z}\vec{e}_z$	<b>Bright</b>

$$
\vec{B}(\vec{r}) = \vec{B}_0(\vec{r}) + \vec{B}_s(\vec{r}) \approx \vec{B}_0(\vec{r}) + \vec{Q}^0(\vec{r} - \vec{r}')V(\vec{r}')\vec{E}_0(\vec{r}'),
$$
\n(3)

where  $\vec{Q}^0(\vec{r} - \vec{r}')$  is the short-range mixed propagator.<sup>6</sup> The constant  $\beta$  having the dimension of an area, the short-range approximation leads to

$$
\vec{Q}^0(0,0,z-z')V(\vec{r}') \approx \beta \begin{pmatrix} 0 & -(z-z')^{-2} & 0 \\ (z-z')^{-2} & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}.
$$
\n(4)

The components of the scattered magnetic field  $\vec{B}_s(\vec{r})$  are given in Table II, together with the near-field contrasts they produce. For a fixed state of polarization (TE or TM) of the incident field, one notices that an inversion of the contrast right above the pads is expected between an electric and a magnetic field map. Furthermore, the propagator of the electric field  $\overline{S}^0$  decreases as  $(z-z')^{-3}$ , whereas the mixed propagator mixed  $\tilde{Q}^0$  decreases as  $(z-z')^{-2}$ . Thus, at a short distance  $(z-z')$  from the surface, the magnetic intensity decay is smoother than the electric intensity. These results, provided by the examination of the short-range parts of the propagators  $\tilde{S}^0$  and  $\tilde{Q}^0$ , are useful to interpret the experimental images. However, we stress the fact that all short- and long-range terms of the propagators are fully taken into account in all numerical calculations given in the following sections.

### **IV. DIELECTRIC TIPS**

To obtain reference images for later comparisons, we first used uncoated dielectric tips. For TE incident polarization, the Green's dyadic method predicts a negative (dark) optical response above nanoscopic objects (Sec. III, Table I). During

TABLE II. When modeling a nanoscopic dielectric pad by a single discretization cell and keeping only the (approximated) shortrange part of the magnetic field propagator, components of the scattered magnetic field  $\vec{B}_s(\vec{r})$  as a function of the polarization of the incident electric field  $\vec{B}_0(\vec{r})$  can be found.  $\vec{e}_j$  ( $j=x,y,z$ ) are the unit vectors in Cartesian coordinates such that  $\vec{e}_z$  is perpendicular to the sample surface.

Incident polarization	$E_0(r)$	$\beta^{-1}\vec{B}_{s}(\vec{r})$	Near-field contrast
TE.	$E_{0,x}e_x$	$(z-z')^{-2}E_{0x}e_{x}$	<b>Bright</b>
TМ	$E_{0,y}e_{y}+E_{0,z}e_{z}$	$-(z-z')^{-2}E_{0,v}\vec{e}_v$	Dark

an experiment, when the tip was approached a few nanometers closer to the sample to perform a scan at the next lower constant height, a tip crash into one of the pads occurred in the dark parts of the optical response, as indicated by the arrows on Fig. 3(a) ( $\lambda$  = 543 nm) and Fig. 3(c) ( $\lambda$  = 633 nm). This tip crash feature was checked to be reproducible with several tips imaging different seven-pad patterns reproduced on the sample surface. At this stage, two important points must be emphasized. First, these dark contrasts are similar to those already observed by using chemically etched tips scanning the surface in the isointensity mode.<sup>11</sup> Second, in this work, using pulled tips and working in the constant-height mode leads to a significant broadening of the near-field patterns. In particular, the confined peaks close to the pads, reported in Ref. 11, cannot be observed anymore.

In order to interpret the experimental images of Figs.  $3(a)$ and  $3(c)$ , two electric field maps computed in an observation plane  $z_{ref}$ =200 nm are given in Fig. 4. A narrower dark signal and the confined peaks, similar to the isointensity measurements of Ref. 11, emerge from the calculations if the map is computed at a height closer to the sample, i.e., with  $z_{ref} \le 150$  nm. Since the etched tips used in Ref. 11 are sharper than the pulled ones, it thus seems that the mean detection plane is lower for etched tips than for pulled tips. The absence of confined peaks when using pulled tips may be understood by the fact that not only the short-range part but also the other terms of the electric field propagator start to be significant in the calculations when the height of detection  $z_{ref}$  increases to over 150 nm above the sample, involving this slight modification of the near-field contrast. $14,16$ 

For the TM incident polarization, the differences in the images presented in Ref. 11 are limited to a more important broadening when using pulled tips. In this polarization, the tip has touched the bright lobes when it was scanning very close to the surface. It means that the optical responses right over the pads are positive for both wavelengths  $[Figs. 3(b)]$ and  $3(d)$ , as expected from Table I, and as confirmed by the calculated electric field map [Fig.  $4(b)$ ].

Computed field maps for both incident polarizations present different aspects compared to the experimental images: sharper interference patterns and better localization of the optical responses. They are explained by the simplifications that have been done in the calculations. In particular, not including the tip is equivalent to a pointlike detector. In the experiment, the electric intensity is integrated by the finite size of the tip. It results in smoother interference patterns and broader signals above the pads. Moreover, in the calculations, the surface around the pads (inside but also outside the computation window) is assumed to be perfectly flat. In a realistic experiment, there may be many other small struc-



FIG. 3. Experimental constant-height PSTM images recorded with dielectric tips at the last height that allowed scanning without crashing into the sample, for both wavelengths ( $\lambda = 543$  nm and  $\lambda = 633$  nm) and both incident polarizations TE [(a) and (c)] and TM [(b) and (d)]. The arrows indicate where the tips crashed when scanning at the next smaller height.



FIG. 4. Theoretical distribution of  $|\vec{E}|^2$  at  $\lambda = 633$  nm for (a) TE ( $z_{ref} = 200$  nm) and (b) TM ( $z_{ref} = 150$  nm) incident polarizations. The same contrasts are obtained with  $\lambda = 543$  nm. On all the theoretical field maps, a little white square shows the position of the pad that is at the bottom of the pattern. Its coordinates were taken from the discretized AFM data file that have been used for the calculations.



FIG. 5. Experimental constant-height PSTM images recorded with a gold-coated tip ( $d=20$  nm) and  $\lambda=543$  nm: (a) TE incident polarization; (b) TM incident polarization.

tures on the sample surface (protrusions, dusts, etc.). The multiple scattering of the incident surface wave by these structures can also attenuate the interferences of surface waves. We can thus conclude that the near-field feature that can be reliably compared to theoretical maps is the intensity contrast right above the pads.

#### **V. GOLD-COATED TIPS**

Using tips coated with 20 nm of gold provides PSTM images that are sensitive to the incident wavelength. To analyze this singular behavior, two different wavelengths have been considered.

 $(i)$  As shown in Figs. 5 $(a)$  and 5 $(b)$ , when working with a green incident light ( $\lambda$  = 543 nm) we have not observed significant changes relative to the electric field pattern  $|\vec{E}|^2$ , which is detected with a pure dielectric tip. The dependence of the contrast right above the pads on the incident polarization confirms that the detected signal is of electric nature.

(ii) When illuminating the sample with the second wavelength  $\lambda$  = 633 nm, we observed a dramatic evolution of the images for both incident polarizations [Figs.  $6(a)$  and  $7(a)$ ]. For example, in the TE mode, the pads appears now with a



FIG. 6. For  $\lambda = 633$  nm and TE incident polarization: (a) constant-height experimental PSTM image recorded with a goldcoated tip ( $d=20$  nm); (b) theoretical distribution of  $|\vec{B}|^2$  ( $z_{ref}$  $= 130$  nm).

bright contrast and the TM images reveal them with a very neat and dark contrast. In this last case, the dark signal right above the pads is surrounded by two bright lobes located perpendicularly to the direction of propagation of the incident surface wave. The localization of the pads was checked with the tip crash test explained above. Specifically, for TM incident polarization, the tip touched the sample between the two lobes. Thus, for this wavelength  $\lambda$  = 633 nm, the images no longer fit in with the optical electric intensity. Indeed, these images do not agree with the simulations presented in Fig. 4, where the detected intensity was supposed to be proportional to  $|\vec{E}|^2$ .

In order to explain this contrast reversal phenomena, we can make use of the data gathered in Table II, which indicate similar contrast changes when passing from  $|\vec{E}|^2$  to  $|\vec{B}|^2$  intensities. To check this hypothesis, we have therefore calculated the magnetic field maps above the sample, for both polarizations. These maps [Figs.  $6(b)$  and  $7(b)$ ] look quite similar to the images recorded at  $\lambda$  = 633 nm for a tip coated with 20 nm of gold [Figs.  $6(a)$  and  $7(a)$ ]. We have checked that a linear superposition of both electric and magnetic fields, with equal weights, cannot give such strongly varying



FIG. 7. For  $\lambda$ =633 nm and TM incident polarization: (a) constant-height experimental PSTM image recorded with a goldcoated tip ( $d=20$  nm); (b) theoretical distribution of  $|\vec{B}|^2$  ( $z_{ref}$  $= 130$  nm).

contrasts. The squares showing the underlying position of the lower pad on the theoretical maps confirm the inversion of the contrasts. It means that the signal detected in this case is proportional to  $|\vec{B}|^2$ . The magnetic field maps have been calculated at the same height above the sample, i.e.,  $z_{ref} = 130$ nm for both states of polarization. Moreover, the width of the optical responses is as good as that from the images presented in Ref. 4, which had been recorded with etched fibers. Here again, we can interpret this as a result of the considerations given in Sec. III, where we have seen that the shortrange decay of the magnetic near-field intensity follows a  $z^{-2}$  law, while the short-range decay of the electric nearfield intensity follows a  $z^{-3}$  law. The short-range behavior of the intensity of the magnetic field is thus valid on a larger range of *z* values than the short-range behavior of the intensity of the electric field. Therefore, even if the tips do not have the same mean plane of detection according to their different fabrication process (etched in Ref. 4 or pulled in the present work), they provide the same kind of results when detecting the magnetic field because the values of  $z_{ref}$  are not at the validity edge of the short-range approximation of the mixed propagator  $\ddot{Q}_0$ .



FIG. 8. Real part Re $\epsilon(\omega)$  of the dielectric function of gold as a function of  $\omega$  as tabulated in Ref. 21.

## **VI. MODELING GOLD-COATED TIPS**

## **A. Mixed susceptibility**

As already mentioned in the Introduction, the most probable hypothesis able to account for the detection of optical magnetic field intensity relies on the excitation of plasmon resonances in the tip at the wavelength operated in the experiment. Indeed, these plasmons could lead to the excitation of a magnetic moment entering the *mixed susceptibility tensor*  $\hat{Y}_{tip}$  of the tip. In fact, this mixed susceptibility is a dyadic function that describes how the tip responds linearly to the magnetic near–field according to

$$
\vec{\mu}(\vec{r}) = \vec{Y}_{tip} \cdot \vec{B}(\vec{r}),\tag{5}
$$

where  $\vec{\mu}(\vec{r})$  is the fluctuating *electric* moment of the plasmon. Moreover,  $\tilde{Y}_{tip}$  displays resonances for eigenfrequencies of the system, as is well known in the context of molecular physics. $17$  In the present situation, such resonant mixed susceptibility inside the detector could explain our results. To obtain more insight into this complex phenomenon, we will describe the detector with two different model geometries.

#### **B. Small gold sphere**

In this case, it is well known from standard textbooks  $(see, for example, Ref. 8) that the magnetic moment of a$ small spherical particle is proportional to the factor

$$
\Delta(\omega) = \frac{\epsilon(\omega) - 1}{2\epsilon(\omega) + 3},\tag{6}
$$

where  $\epsilon(\omega)$  is the dielectric function of gold and  $\omega$  $=2\pi c/\lambda$  is the angular frequency of light in vacuum. The factor  $\Delta(\omega)$  displays a resonance when  $\epsilon(\omega)$ = -1.5. In the case of gold spheres in vacuum, this resonance occurs around the wavelength  $\lambda$  = 465 nm (Fig. 8). The proximity of the glass substrate is known to induce a redshift of this resonance wavelength. In order to provide an excess value of this effect, we suppose that the gold sphere is fully embedded in glass such that it is easy to find that the resonance is redshifted towards the wavelength  $\lambda$ =502 nm. We may thus conclude that in spite of this overestimated redshift, the



FIG. 9. Model for the gold-coated tip: a cylindrical dielectric core of radius *b* is uniformly coated by a thickness  $d = a - b$  of gold.  $\vec{e}_o$ ,  $\vec{e}_d$ , and  $\vec{e}_z$  are the units vectors in cylindrical coordinates.

shifted resonance wavelength of a spherical particle remains very far from the incident wavelength  $\lambda$  = 633 nm for which the magnetic field detection effect has been observed. Consequently, the model of a resonating particle at the apex of the fully coated tip must be discarded.

#### **C. Gold-coated glass cylinder**

We then assumed a second model based on the approximation of the tip by a gold-coated glass cylinder (Fig. 9). In order to know if the gold-coated tip may sustain a plasmon resonance, we have calculated the dispersion relation of the surface plasmon modes<sup>18</sup> of such a geometry. The goldcoating thickness may be defined by the difference *d* between the outside  $a$  and inside  $b$  radii (Fig. 9). The wavelength-dependent values of the gold dielectric response  $\epsilon(\omega)$  were found in Ref. 21. The validity of this set of data was assessed in Ref. 12 to *predict* the occurrence of plasmon resonances of nanoscopic structures (gold nanowires and nanodots deposited on glass), which were then observed experimentally at the right wavelength and at the right location with a PSTM. The dielectric functions are  $\epsilon_c = 2.25$  in the glass core and  $\epsilon_A = 1$  in the external medium. The time dependence of fields was chosen to be harmonic. The small dimensions of the tips allow us to neglect the retardation effects. According to a standard procedure,<sup>19,20</sup> we solved the Laplace equation for the electric potential in cylindrical coordinates  $(\rho, \phi, z)$  and searched the surface modes, decaying for growing radial distance  $\rho$  and oscillatory as a function of  $z$  and  $\phi$ . We found the dispersion relation of the surface eigenmodes of a gold-coated dielectric cylinder to be

$$
\begin{split}\n&\left(\epsilon_{A} \frac{K'_{m}(ak_{z})}{K_{m}(ak_{z})} - \epsilon(\omega) \frac{I'_{m}(ak_{z})}{I_{m}(ak_{z})}\right) \\
&\times \left(\epsilon_{C} \frac{I'_{m}(bk_{z})}{I_{m}(bk_{z})} - \epsilon(\omega) \frac{K'_{m}(bk_{z})}{K_{m}(bk_{z})}\right) \\
&= \frac{I'_{m}(bk_{z})K'_{m}(ak_{z})}{I_{m}(ak_{z})K_{m}(bk_{z})} \left[\epsilon(\omega) - \epsilon_{A}\right] \left[\epsilon(\omega) - \epsilon_{C}\right].\n\end{split} \tag{7}
$$



FIG. 10. For the geometry of a glass cylinder of radius *b* coated with a thickness  $d=a-b$  of gold, dispersion curves are shown for the  $m=0,1,2,3$  branches of plasmon modes for the ratios  $a/b$  $=1.3$  and  $a/b=1.4$ . As *m* increases, the branches converge to a horizontal line (not drawn) defined by  $\omega/c = \omega_s/c$ , where  $\omega_s$ is such that  $\epsilon_C = -\epsilon(\omega_s)$ , corresponding to the nonretarded dispersion relation of a flat glass-gold interface. The straight lines  $(- \cdot \cdot \cdot -)$  are guides for the eyes in order to locate the two laser frequencies easily (here converted in units of wavelength in vacuum) for the experiments reported in this paper.

In this expression,  $I_m$  and  $K_m$  are the modified Bessel functions of the first and second kinds, respectively, while  $I'_m$  and  $K'_m$  are their first derivatives.  $k_z$  is the projection of the wave vector along the longitudinal  $(z)$  axis of the cylinder. The angular dependence of the solutions is  $exp(im\phi)$ . Since dispersion relations describe ideal, undamped, normal modes, the roots of the above equation are computed, as usual, by zeroing the imaginary part of the dielectric function of the metal  $[\epsilon(\omega)]$ , i.e., by taking only the real part of  $\epsilon(\omega)$  into account. The results of such a computation are zero-width dispersion curves for each value of  $m$  (Fig. 10). Finite lifetime effects related to the imaginary part of  $\epsilon(\omega)$  broaden these dispersion curves. Therefore, when two curves related to different values of *m* are sufficiently close to each other, the described broadening related to the imaginary part of  $\epsilon(\omega)$  allows us to consider both curves as overlapping.

In the dispersion relation above, the argument of the Bessel functions depends implicitly on the ratio *a*/*b*. Dispersion curves have been computed systematically for *a*/*b* ratios covering ranges of values that are relevant to the context of this paper. For values of  $k_7a$  smaller than 1 or close to 1 (which correspond to the range of validity of the nonretarded approximation), this systematic study brings to the fore the main difference between gold cylinders  $(b=0)$  and glass cylinders coated with gold  $(b \neq 0)$ . In the dispersion relation of gold cylinders (not shown), the  $m=0$  curve alone enters the range of red frequencies and an important frequency gap separates this  $m=0$  curve from the  $m \ge 1$  curves, which arise at higher frequencies. For glass cylinders coated with gold, it turns out that according to the value of the ratio *a*/*b*, the *m*  $=0$  and  $m=1$  curves may both enter the range of red frequencies  $(Fig. 10)$ . Since the abscissas of the dispersion curves is the product of  $k_z$  multiplied by the outside radius  $a$ , such dispersion curves actually describe a *discrete* spectrum for each specific gold-coated glass cylinder defined by the radii *a* and *b*. Due to this discrete nature of the plasmon spectrum and since the photons are well known to carry unit spins that are exchanged in interactions of light with matter, the elastic coupling of red light to the plasmon field requires that both  $m=0$  and  $m=1$  curves do virtually overlap each other.

We therefore searched which ratio  $a/b$  results in  $m=0$ and  $m=1$  curves sufficiently close to each other at the angular frequency of the red He-Ne laser (wavelength in vacuum  $\lambda$  = 633 nm) so that they are practically overlapping by virtue of the above-mentioned broadening effect. This occurs for  $a/b = 1.3$ , which sets  $a = 100$  nm and  $d = 23$  nm (Fig. 10). These values are in good agreement with the dimensions of the real tips: indeed, according to the fabrication parameters, the gold-coating thickness was about 20 nm in the experiment while the mean radius at the tip apex was around 100 nm. But for the green laser ( $\lambda$ =543 nm in vacuum), the dispersion curve for the ratio  $a/b = 1.3$  implies that  $a=146$  nm and  $d=33$  nm. According to this model, the tips coated with  $d=20$  nm, leading to the same contrast on the images than the purely dielectric tips, do not sustain any plasmon resonance at  $\lambda$  = 543 nm.

For the actual dimensions of the tips ( $a \approx 100$  nm and *d*  $\approx$  20 nm), we can conclude from the dispersion curves that, at  $\lambda$ =633 nm, a plasmon excitation associated to the ring geometry can be sustained by the gold coating. We postulate that the mixed polarizability  $Y_{tip}$  of this nanoscopic ring could be resonant in our experiment. The plasmon could then radiate proportionally to the optical magnetic field, thereby leading to an image pattern that is proportional to  $|\vec{B}|^2$ . At  $\lambda$  = 543 nm, the conditions of plasmon resonance are not fulfilled and the optical magnetic field detection should not occur if  $d=20$  nm. However, the cylinder-shaped tip being a rough model, we decided to check experimentally the dependence of the optical magnetic field detection on the circular symmetry plasmons associated with the cylinder geometry.

## **VII. EXPERIMENTAL CONFIRMATION OF CIRCULAR SYMMETRY PLASMONS**

#### **A. Semicoated tips**

For each ratio *a*/*b*, a family of ring plasmons can be excited and these particular modes depend basically on the *circular symmetry* of the metallic coating. Now, a ''semicoated'' tip, obtained by the evaporation of a dissymmetric gold layer on the dielectric core, not only downgrades the effective ratio *a*/*b* but additionally breaks the circular symmetry. If a ring plasmon is involved in the detection of the



FIG. 11. Sketch of the two lightning conditions of the semicoated tips used in this work. The  $\vec{e}_i$  ( $i=x,y,z$ ) are the units vectors in Cartesian coordinates, which are consistent with the coordinate system of the experimental images introduced in Fig. 2.  $\vec{k}_{\parallel}$  is the component of the incident wave vector that is parallel to the sample surface.

optical magnetic field, breaking this fundamental symmetry should not lead to detection  $|\vec{B}|^2$ . On the contrary, if a semicoated tip still detects the same signal, we should conclude that this particular detection is related to another process. The semicoated tips are fabricated in the same manner as described in Sec. II, but they are not rotated in the evaporator, while the deposition time is reduced in order to coat only one side of the tip with 20 nm of gold. With this procedure, in spite of some gold atoms diffusion effects on the other side of the tip, the resulting metal layer is always highly dissymmetric. To ensure that no particular effect due to this dissymmetry could happen, we recorded the images with two orientations of the gold-coated side with respect to  $k_{\parallel}$  (see Fig. 11). At  $\lambda$  = 633 nm, for the TM incident polarization, the contrast is the same with both orientations  $(Fig. 12)$ . Moreover, the images look as if they were recorded with a purely dielectric tip. They reveal the same contrast as in Fig.  $3(b)$ with a signal proportional to  $|\vec{E}|^2$ . These results support our hypothesis: the circular symmetry of the gold coating being broken, the semicoated probes do not collect a magnetic signal anymore. This definitely discards the excitation of a single gold particle as the possible cause of the detection of



FIG. 12. Experimental constant-height PSTM image recorded with a semicoated tip in the configuration  $(a)$  presented on Fig. 11  $(\lambda = 633$  nm, TM incident polarization). The configuration (b) of Fig. 11 leads to the same contrast.





FIG. 13. Experimental constant-height PSTM image recorded with a gold-coated tip ( $d=30$  nm) at  $\lambda=543$  nm: (a) TE incident polarization; (b) TM incident polarization.

the optical magnetic field. Incidentally, we can notice that the broadening of the bright spots is reduced with these tips  $(Fig. 12)$ , relative to the use of dielectric tips  $[Fig. 3(b)]$ : the resolution, defined relative to the distribution of  $|\vec{E}|^2$ , is thus improved by semicoated tips.

### **B.** Optical magnetic field detection at  $\lambda$  = 543 nm

The next attempt we made to confirm the role of ring plasmons in detecting a magnetic signal with a PSTM was to reproduce the phenomenon at another incident wavelength. We chose to determine the conditions leading to a plasmon excitation at  $\lambda$  = 543 nm for another value of the ratio *a*/*b*. For  $a/b = 1.4$ , we notice (Fig. 10) that the  $m=0$  and  $m=1$ curves are well separated in the range of red frequencies but start to overlap each other for a value of the frequency corresponding to the wavelength in vacuum  $\lambda$  = 543 nm. The intersection of both  $m=0$  and  $m=1$  curves with the straight line  $\lambda$  = 543 nm defines the values *a* = 96 nm and *d* = 29 nm. This is not so far from the estimated value of the outside radius  $a=100$  nm, which was the basis of our modeling in Sec. VI. The fibers used in this section have then been placed in the evaporator for a longer time, in order to obtain a layer of 30 nm of gold around the dielectric core. The images



FIG. 14. Experimental constant-height PSTM image recorded with a gold-coated tip ( $d=35$  nm) at  $\lambda=543$  nm for a TM incident polarization.

recorded with this kind of probe, while the sample was illuminated with the green laser, are presented in Fig. 13. The contrasts right above the pads obtained with both incident polarizations are the same as those recorded at  $\lambda$  = 633 nm using a probe coated with 20 nm of gold  $[Figs. 6(a)$  and  $7(a)$ , that is, *the same as on the theoretical magnetic field*  $maps$  presented in Figs.  $6(b)$  and  $7(b)$ . When the wavelength of the incident light is changed to be 633 nm, other experiments (not shown) have checked that such tips coated with 30 nm of gold do not detect a signal proportional to  $|\vec{B}|^2$ anymore but collect a signal proportional to  $|\vec{E}|^2$ .

The gold-coated glass cylinder model of the tip turns out to be sufficient to define the conditions leading to the detection of the optical magnetic field with another design of the PSTM probe. The hypothesis of the excitation of a ring plasmon is thus relevant to account for the process of detecting optical magnetic fields. Furthermore, we can state that a magnetic signal is collected by the tip only for very accurate parameters. Indeed, we have finally fabricated a coated tip by evaporating 35 nm of gold. It means that the gold layer around the tip was 5 nm thicker than on the tip used to record Fig. 13. For TM incident polarization and at  $\lambda = 543$ nm again, the pads have appeared in bright contrast  $(Fig. 14)$ , in the same way as with a dielectric tip [Fig. 1(a)]. The conditions of resonance have thus been broken by the addition of only a few nanometers of gold.

## **VIII. CONCLUSION**

The experiments presented in this paper confirm that the composition of a PSTM probe may influence dramatically the nature of the detected signals. Specifically, for welldefined wavelengths and precise coating thicknesses, gold coated glass tips allow signals proportional to the optical magnetic field intensity to be detected in the near-field zone.

A theoretical analysis based on an elementary model of coated cylindrical glass tip indicates the possible excitation of *ring plasmons* in the metal layer surrounding the dielectric core. In each situation where the detection of the optical magnetic field occurs, these *circular symmetry* plasmon modes are active.

As proven by the utilization of ''semicoated'' tips, the circular symmetry of the gold coating appears to be fundamental for observing the phenomenon. The experimental evidence thus suggests that plasmons associated with a ring geometry might set up significant dynamical magnetic field detection processes that can mask the more common electric field detection mechanisms. Through the above-mentioned resonant phenomena, ring plasmons could radiate energy proportional to the incident optical *magnetic* field intensity, thereby explaining the observations reported in this paper.

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This work thus calls for a deeper theoretical analysis of the properties of plasmons in nanoscopic rings.

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