

## Stability of trions in strongly spin-polarized two-dimensional electron gases

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Low-temperature magnetophotoluminescence studies of negatively charged excitons ( $X_s^-$  trions) are reported for  $n$ -type modulation-doped ZnSe/Zn(Cd,Mn)Se quantum wells over a wide range of Fermi energy and spin splitting. The magnetic composition is chosen such that these magnetic two-dimensional electron gases are highly spin polarized even at low magnetic fields, throughout the entire range of electron densities studied ( $5 \times 10^{10}$  to  $6.5 \times 10^{11}$  cm $^{-2}$ ). This spin polarization has a pronounced effect on the formation and energy of  $X_s^-$ , with the striking result that the trion ionization energy (the energy separating  $X_s^-$  from the neutral exciton) follows the temperature- and magnetic field-tunable Fermi energy. The large Zeeman energy destabilizes  $X_s^-$  at the  $\nu=1$  quantum limit, beyond which a separate photoluminescence peak appears and persists to 60 T, suggesting the formation of spin-triplet charged excitons.

Magnetic two-dimensional electron gases (2DEGs) represent a relatively new class of semiconductor quantum structure in which an electron gas is made to interact strongly with embedded magnetic moments.<sup>1-4</sup> Typically, magnetic 2DEG's (and 2D hole gases) are realized in modulation-doped II-VI diluted magnetic semiconductor quantum wells in which paramagnetic spins ( $Mn^{2+}$ ,  $S = \frac{5}{2}$ ) interact with the confined electrons via a strong  $J_{s-d}$  exchange interaction.<sup>5</sup> This interaction leads to an enhanced spin splitting of the electron Landau levels which follows the Brillouin-like  $Mn^{2+}$  magnetization, saturating in the range 10–20 meV by a few Tesla. Since the spin splitting can greatly exceed both the cyclotron ( $\hbar\omega_c \sim 1$  meV/T) and Fermi energies, these magnetic 2DEGs consist largely of spin-polarized Landau levels, and serve as interesting templates for studies of quantum transport in the absence of spin gaps.<sup>1</sup> In addition, it has been recognized that this interplay between the cyclotron, Zeeman, and Fermi energies may also be exploited in magneto-optical experiments to gain insights into the rich spectrum of optical excitations found in 2DEGs.<sup>4</sup> The aim of this paper is to use strongly spin-polarized magnetic 2DEGs, containing a wide range of electron densities, to shed light on the spin-dependent properties of negatively charged excitons (or trions).

Predicted in 1958 by Lampert<sup>6</sup> and first observed by Kheng<sup>7</sup> in 1993, the singlet state of the negatively charged exciton (the  $X_s^-$  trion) consists of a spin-up and spin-down electron bound to a single hole.<sup>4</sup> The energy required to remove one of these electrons (leaving behind a neutral exciton  $X^0$ ) is the  $X_s^-$  ionization energy  $\Delta E_X$ , usually defined as the energy between  $X_s^-$  and  $X^0$  features in optical studies.  $\Delta E_X$  is small; typically only  $\sim 1$ ,  $\sim 3$ , and  $\sim 6$  meV in GaAs,<sup>8</sup> CdTe,<sup>7</sup> and ZnSe-based<sup>9</sup> 2DEGs, respectively. The spin-singlet nature of the two electrons in  $X_s^-$  suggests that

$\Delta E_X$ —and hence trion stability—should be sensitive to the Zeeman energy and spin polarization of the 2DEG. Here, we explicitly study highly spin-polarized magnetic 2DEGs to establish empirical correlations between Zeeman energy and trion stability over a broad range of carrier densities. In particular, magnetophotoluminescence (PL) measurements demonstrate the striking result that  $\Delta E_X$  follows the energy of the Fermi surface, which can be tuned independently from the Landau levels via the strong Zeeman dependence on temperature and applied field. The role of the Fermi and Zeeman energies in determining  $\Delta E_X$  is studied for all carrier densities, and qualitative agreement with numerical calculations is found. The giant spin splitting in these systems is found to reduce  $\Delta E_X$ , eventually driving a rapid suppression of  $X_s^-$  by the  $\nu=1$  quantum limit, beyond which the formation of a separate peak in the PL (which persists to 60 T) may signify the formation of spin-triplet charged excitons.

These experiments are performed at the National High Magnetic Field Laboratory, in the generator-driven 60 T long-pulse magnet and a 40 T capacitor-driven magnet (with 2000 and 500 ms pulse duration, respectively), as well as a 20 T superconducting magnet. Light is coupled to and from the samples via single optical fibers (200 or 600  $\mu$ m diameter), and excitation power is kept below 200  $\mu$ W. Thin-film circular polarizers between the fiber and sample permit polarization-sensitive PL studies. In the pulsed magnet experiments, a high-speed charge-coupled device camera acquires complete optical spectra every 1.5 ms, enabling reconstruction of the entire spectra vs field dependence in a single magnet shot.<sup>10</sup> The magnetic 2DEG samples, grown by molecular beam epitaxy, are  $n$ -type modulation-doped 105 Å wide single quantum wells into which  $Mn^{2+}$  are “digitally” introduced in the form of equally spaced fractional monolayers of MnSe. Specifically, the quantum wells are paramagnetic digital alloys of  $(Zn_{1-x}Cd_xSe)_{m-f}(MnSe)_f$  with  $x$

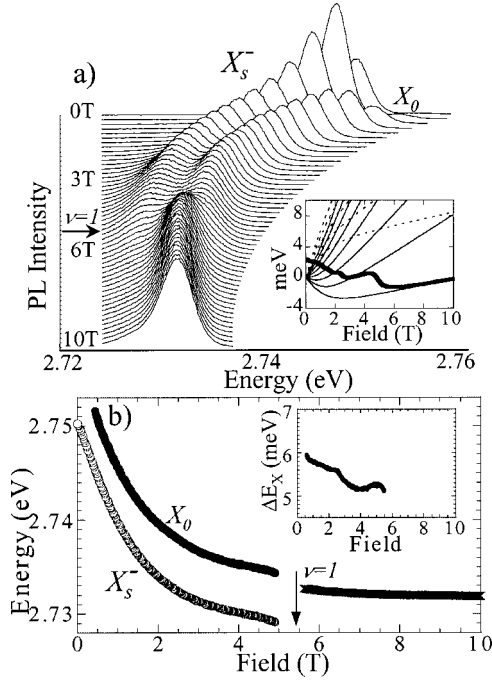


FIG. 1. (a) Characteristic evolution of the PL spectra at 1.5 K in low-density ( $n_e=1.24e^{11} \text{ cm}^{-2}$ ) magnetic 2DEGs showing a collapse of the  $X_s^-$  and  $X_0$  peaks at  $\nu=1$ . Inset: spin-up (dotted) and spin-down (solid) LLs, and Fermi energy in this sample. (b) PL peak energies. Inset: the  $X_s^-$ - $X_0$  energy splitting, which follows the Fermi energy.

$=0.1$  to  $0.2$ ,  $m=5$  and  $f=\frac{1}{8}$  or  $\frac{1}{16}$  effective monolayer thickness.<sup>1</sup> The electron densities, determined from Shubnikov–de Haas (SdH) oscillations in transport, range between  $5 \times 10^{10}$  and  $6.5 \times 10^{11} \text{ cm}^{-2}$ . All samples show a large spin splitting at 1.5 K, with “effective”  $g$  factors in the range  $70 < g_e^{eff}(H \rightarrow 0) < 100$ .

Figure 1(a) shows the evolution of the PL spectra in a magnetic 2DEG with a relatively low carrier density of  $1.24 \times 10^{11} \text{ cm}^{-2}$  and  $g_e^{eff}=73$  at 1.5 K. This sample has a mobility of  $14000 \text{ cm}^2/\text{Vs}$  and exhibits clear SdH oscillations in transport.<sup>11</sup> At  $H=0$ , the data show a strong PL peak at 2.75 eV with a small satellite  $\sim 6$  meV higher in energy. With applied field, the peaks shift rapidly to lower energy in the  $\sigma^+$  polarization due to the large Zeeman energy (the  $\sigma^-$  emission disappears completely at low fields in all the magnetic 2DEGs, much like their undoped counterparts<sup>12</sup>). By 1 T, the satellite develops into a clear peak of comparable amplitude, and as will be verified in Fig. 2, we assign the high- and low-energy PL features to  $X_0$  and  $X_s^-$ . At  $\nu=1$  (5.5 T), the smooth evolution of the PL spectra changes abruptly as the  $X_s^-$  resonance collapses and a strong, single PL peak emerges at an energy between that of  $X_0$  and  $X_s^-$ , as shown. This PL feature persists to 60 T. Figure 1(b) shows the energies of the PL peaks (the data are fit to Gaussians), where the discontinuity at  $\nu=1$  is clearly seen. The  $X_s^-$  ionization energy  $\Delta E_X$  decreases and oscillates with magnetic field [inset, Fig. 1(b)]. Anticipating Figs. 3 and 4, we note that  $\Delta E_X$  qualitatively mimics the Fermi energy in this low-density magnetic 2DEG [plotted in Fig. 1(a) inset].

Owing to the giant spin splitting in this sample, the “ordinary” Landau level (LL) fan diagram for nonmagnetic

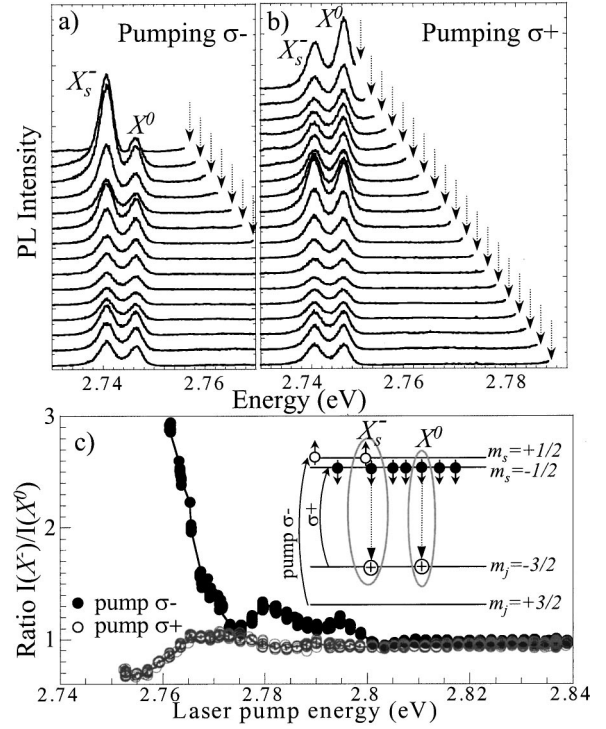


FIG. 2. (a) PL excitation at 2.2 K and 1 T, showing an enhancement of  $X_s^-$  when injecting spin-up electrons on the  $\sigma^-$  resonance. (b) A similar enhancement of the  $X_0$  peak when injecting spin-down electrons. (c) The intensity ratio  $I(X_s^-)/I(X_0)$ , with a schematic of the energy levels and processes involved (the light holes are split off due to quantum confinement effects).

2DEGs (with Landau levels evenly spaced by  $\hbar\omega_c$ , and spin splitting  $\ll \hbar\omega_c$ ) is replaced by that shown in the inset of Fig. 1(a). The LLs are simply calculated as

$$\varepsilon_{l,s} = \hbar\omega_c(l + \frac{1}{2}) + sE_Z B_{5/2}(5g_{\text{Mn}}\mu_B H/2k_B T^*), \quad (1)$$

where  $l$  is the orbital angular momentum index and  $s$  is the electron spin ( $\pm \frac{1}{2}$ ). Here,  $\hbar\omega_c=0.83 \text{ meV/T}$  is the electron cyclotron energy, and the second term is the Zeeman energy:  $B_{5/2}$  is the Brillouin function describing the magnetization of the  $S=\frac{5}{2} \text{ Mn}^{2+}$  moments,  $E_z$  is the saturation value of the electron splitting,  $g_{\text{Mn}}=2.0$ , and  $T^*$  is an empirical “effective temperature” which best fits the low-field energy shifts.<sup>5</sup> We ignore the much smaller contribution to the Zeeman energy arising from the bare electron  $g$  factor. At low fields, the spin-down LLs (solid lines) are Zeeman shifted well below the spin-up LLs (dotted lines), leading to a highly spin-polarized electron gas, e.g., by 1 T, over 95% of the electrons are oriented spin down in this sample. The Fermi energy  $\varepsilon_F$  (thick line) is calculated numerically by inverting the integral

$$N_e = \int_{-\infty}^{\infty} g[\varepsilon, B, T] f[\varepsilon, \varepsilon_F, T] d\varepsilon. \quad (2)$$

Here,  $N_e$  is the known electron density,  $f[\varepsilon, \varepsilon_F, T]$  is the Fermi-Dirac distribution, and  $g[\varepsilon, B, T]$  is the density of states, taken to be the sum of Lorentzian LLs of width  $\Gamma = \hbar/2\tau_s$ ,<sup>13</sup> centered at the energies  $\varepsilon_{ls}$  given in Eq.(1). The

electron scattering time  $\tau_s$  is obtained from analyzing SdH oscillations, or alternatively from the measured mobility.

Typically, identification of  $X^0$  and  $X_s^-$  relies on their polarization properties in reflection or absorption<sup>4,7</sup>—measurements which directly probe the available density of states. However, in these magnetic 2DEGs, the huge Zeeman splitting and the relatively broad spectral linewidths (resulting from the high  $\text{Mn}^{2+}$  concentration) complicate these standard analyses. While reflectivity studies in these samples *do* confirm the presence of two bound states at zero field (as expected for  $X^0$  and  $X_s^-$ ), we rely on spin-polarized PL excitation measurements to verify the peaks in finite field, shown in Fig. 2. At fixed field and temperature, we record the PL while tuning the energy and helicity of the excitation laser (a frequency-doubled cw Ti:sapphire laser). Since the PL is entirely  $\sigma^+$  polarized, it must arise from the recombination of a spin-down ( $m_s = -\frac{1}{2}$ ) electron with a  $m_j = -\frac{3}{2}$  valence hole [see diagram, Fig. 2(c)]. If that  $m_s = -\frac{1}{2}$  electron is part of an  $X_s^-$  trion, emission will occur at the  $X_s^-$  energy. Thus, the probability of forming  $X_s^-$  is related to the number of spin-up ( $m_s = +\frac{1}{2}$ ) electrons present in the system. By specifically injecting spin-up electrons at the  $\sigma^-$  resonance, we do indeed observe an enhancement of the  $X_s^-$  intensity [Fig. 2(a)]. In contrast, injecting spin-down electrons with  $\sigma^+$  light can (and does) only favor the  $X^0$  intensity [Fig. 2(b)]. The amplitude ratio,  $I(X_s^-)/I(X^0)$ , is plotted in Fig. 2(c), where the effects of pumping spin-up and spin-down electrons are more easily seen. Of related interest, no difference in this ratio is observed when exciting above the ZnSe barriers (2.8 eV)—evidence that the injected spin is scrambled when the electrons spill into the well from the barrier regions.

With the aid of the diagram in Fig. 2(c), the evolution of the PL spectra in Fig. 1 may be interpreted as follows:  $X_s^-$  and  $X^0$  are competing channels for exciton formation, with  $X_s^-$  dominating at zero field. With small applied field, the large spin splitting drives a rapid depopulation of the spin-up electron bands, reducing the probability of  $X_s^-$  formation and thus increasing  $X^0$  formation, as observed. With increasing field and Zeeman energy,  $X_s^-$  continues to form, with reduced binding energy, until it is no longer energetically favorable to bind a spin-up electron—in this case, evidently, at  $\nu=1$  when the Fermi energy falls to the lowest LL. The PL peak which forms at  $\nu=1$  (and persists to 60 T), with an energy *between* that of  $X_s^-$  and  $X^0$ , represents formation of a new stable ground state. A likely candidate is the spin-triplet state of the negatively charged exciton ( $X_t^-$ ), wherein both bound electrons are oriented spin down. The  $X_t^-$  trion, which must be the only stable trion in the limit of infinite Zeeman energy, may be forming stably with this energy in these spin-polarized magnetic 2DEGs, due to the large Zeeman energy. Indeed, the very recent calculations of Wojs *et al.*<sup>14</sup> reveal the presence of a stable “bright” triplet trion with energy between that of  $X_s^-$  and  $X^0$  at high magnetic fields, as seen here and in recent high-field studies of trions in GaAs-based 2DEGs.<sup>15</sup>

We turn now to results from high-density samples. Figure 3 shows PL spectra and energy shifts observed in a high-density magnetic 2DEG [ $n_e = 4.2 \times 10^{11} \text{ cm}^{-2}$ , mobility = 2700  $\text{cm}^2/\text{Vs}$ , and  $g_e^{\text{eff}}(H \rightarrow 0) = 95$  at 1.5 K]. These data

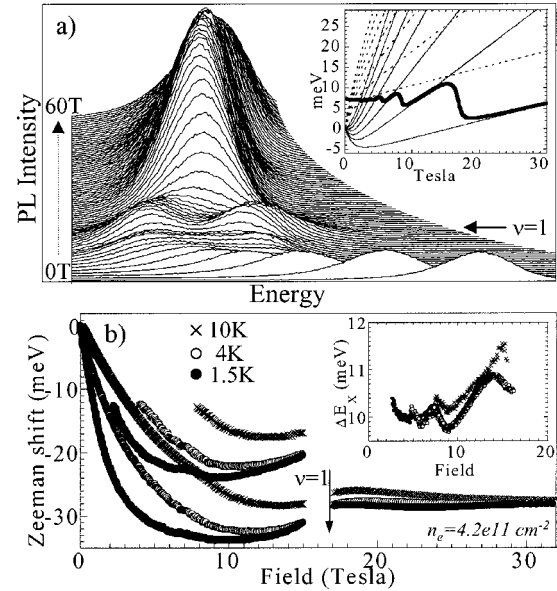


FIG. 3. (a) Characteristic evolution of the PL spectra in high-density magnetic 2DEGs, with calculation of the LLs and Fermi energy (inset). (b) Energies of the observed PL peaks at different temperatures, with the  $X_s^-$ - $X^0$  energy splitting (inset).

are characteristic of that obtained in samples with  $n_e$  up to  $6.5 \times 10^{11} \text{ cm}^{-2}$ , the highest density studied. Again, we observe a dominant PL peak at  $H=0$ , which shifts rapidly down in energy with applied field. However, in contrast with the low-density 2DEGs, the high-energy satellite peak does not appear until  $\sim 2$  T (at 1.5 K). This satellite grows to a peak of comparable amplitude by 12 T, and exhibits similar sensitivity to the energy and helicity of the pump laser, as seen in Fig. 2; therefore, we again assign these features to  $X_s^-$  and  $X^0$ . At  $\nu=1$  (17 T), these resonances collapse and are again replaced by a strong emission at an intermediate energy which persists to 60 T. The energy of the observed PL peaks at 1.5, 4, and 10 K are plotted in Fig. 3(b), along with  $\Delta E_X$  (inset). Several features are notable. First, the  $X^0$  peak only becomes visible at a particular *spin splitting*—not field—in support of the assertion that  $X^0$  forms readily only when the spin-up electrons subbands depopulate to a particular degree. In addition, the collapse of the  $X^0$  and  $X_s^-$  peaks occurs at  $\nu=1$  *independent* of temperature, again indicating that the drop of the Fermi energy to the lowest LL destabilizes  $X_s^-$ . Finally,  $\Delta E_X$  again follows the calculated Fermi energy in this sample, exhibiting oscillations in phase with the Fermi edge.

This latter behavior is unexpected but appears to be true in all our samples. In contrast with studies in nonmagnetic 2DEGs, these data clearly demonstrate the relevance of both the Zeeman energy and the Fermi energy in determining the trion ionization energy  $\Delta E_X$ . In Fig. 4 we explicitly study this behavior and reveal the surprising result that  $\Delta E_X$  closely follows the energy of the Fermi surface *regardless* of electron density, temperature, and applied field. Figure 4(a) shows the measured field dependence of  $\Delta E_X$  in six magnetic 2DEGs with electron densities from  $\sim 5 \times 10^{10}$  to  $\sim 2.5 \times 10^{11} \text{ cm}^{-2}$ . The data are plotted from the field at which distinct  $X^0$  and  $X_s^-$  PL peaks first appear, until the collapse of the PL spectra.  $\Delta E_X$  is seen to decrease rapidly



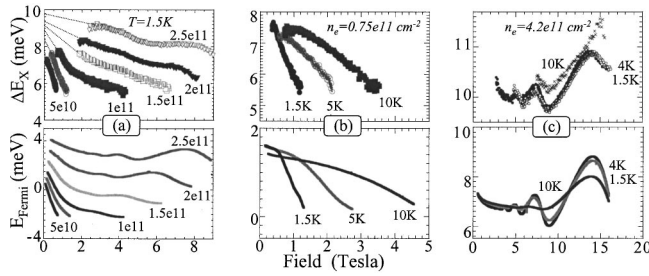


FIG. 4. Explicit dependence of the trion ionization energy  $\Delta E_X$  on (a) carrier density in otherwise identical magnetic 2DEGs, and on temperature in (b) low- and (c) high-density samples, all showing marked similarity to numerical calculation of the Fermi energy.

with field at the lowest densities, but remain roughly constant and exhibit weak oscillations at high densities. Further, a rough extrapolation (dotted lines) reveals that  $\Delta E_X$  at zero field increases from  $\sim 7$  to 10 meV with carrier density. Aside from a  $\sim 7$  meV difference in overall magnitude, these features are qualitatively reproduced by the numerical computation of the Fermi energy in these samples, plotted in the lower graph. It is natural to associate 7 meV with the “bare” ( $n_e \rightarrow 0$ )  $X_s^-$  binding energy, in reasonable agreement with earlier studies in low-density, nonmagnetic ZnSe-based 2DEGs.<sup>9</sup> Thus, at least at zero field,  $\Delta E_X$  reflects the “bare”  $X_s^-$  binding energy *plus* the Fermi energy, in agreement with a recent viewpoint<sup>16</sup> wherein the ionization process requires removing one electron from  $X_s^-$  to the top of the Fermi sea.

In nonzero field, the Zeeman energy reduces the  $X_s^-$  ionization energy. The explicit temperature dependence of  $\Delta E_X$  in the low-density magnetic 2DEG is particularly telling [Fig. 4(b)]: Here, the small Fermi energy should play a minimal role ( $\varepsilon_F \sim 1.5$  meV  $\ll$  9 meV total spin splitting), and the data should directly reveal the  $X_s^-$  ionization energy. At different temperatures,  $\Delta E_X$  decreases from its zero-field value of  $\sim 7.5$  meV *at a rate which depends on the Brillouin-like spin splitting*. In this sample, the 2DEG is almost immediately completely spin-polarized—no gas of “spin-up” electrons remains—and thus the drop in  $\Delta E_X$  must reflect the

influence of the Zeeman energy. Physically, the energy of the spin-up electron in  $X_s^-$  increases with spin splitting, becoming more weakly bound, reducing  $X_X$  by roughly half of the total Zeeman splitting until the  $\Delta E_s^-$  destabilizes. Within this scenario, however, the rolloff in the slope of the data towards zero field is puzzling, possibly indicating that the energy *between* the Fermi edge and the spin-up subbands (rather than the Zeeman energy itself) may be the relevant parameter, as the calculated Fermi energy shows precisely the same behavior. No theoretical framework for this behavior exists at present. Alternatively, Fig. 4(c) shows typical data from the high electron density sample where the Fermi energy (7.7 meV) is comparable to the total spin splitting (12.6 meV). Here, the measured  $\Delta E_X$  clearly follows the oscillations of the calculated Fermi energy, with no clear indication of the role played by the Zeeman energy. We pose these questions for future theoretical models for  $X_s^-$  formation, which must necessarily include the Zeeman energy and the influence of a finite Fermi energy.

In conclusion, we have presented a systematic study of charged exciton formation in strongly magnetic 2DEGs, wherein the giant spin splitting dominates the cyclotron energy and the electron gas is highly spin polarized. The trion ionization energy  $\Delta E_X$  tracks the energy of the Fermi edge regardless of electron density, temperature or applied field, highlighting the important roles played by both the Fermi- and Zeeman energies. With increasing electron density, the data suggest that  $\Delta E_X$ —at least at zero magnetic field—reflects the “bare”  $X_s^-$  ionization energy of  $\sim 7$  meV *plus* the Fermi energy. Studies in low density samples show that the “bare”  $X_s^-$  binding energy is reduced by an amount proportional to the increasing Zeeman energy until the  $X_s^-$  destabilizes and no longer forms, and in high density samples  $\Delta E_X$  follows the oscillations of the Fermi surface as it moves between Landau levels. Quantitative interpretation of these data must await a more complete theory of  $X_s^-$  formation in electron gases.

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