

## Spin fluctuations in the ruthenium oxides $\text{RuO}_2$ , $\text{SrRuO}_3$ , $\text{CaRuO}_3$ , and $\text{Sr}_2\text{RuO}_4$ probed by Ru NMR

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By means of Ru NMR, magnetic properties in three-dimensional (3D) perovskites  $\text{SrRuO}_3$  (ferromagnet) and  $\text{CaRuO}_3$  (exchange enhanced paramagnet) were investigated and compared with those in the two-dimensional (2D) layered perovskite  $\text{Sr}_2\text{RuO}_4$  (superconductor),  $\text{RuO}_2$ , and Ru metal (Pauli paramagnet). We found that  $4d$ -spin contributions in the Knight shift and  $^{101}(1/T_1)$  of Ru are predominant in  $\text{SrRuO}_3$ ,  $\text{CaRuO}_3$ , and  $\text{Sr}_2\text{RuO}_4$ , but not in nonmagnetic  $\text{RuO}_2$  and Ru metal. The experimental results that a Stoner factor for  $\text{CaRuO}_3$  is close to 1 and that a correlation factor estimated from modified-Korringa behavior of  $\text{Ru-T}_1$  is much less than 1 indicate that  $\text{CaRuO}_3$  is a nearly ferromagnetic (FM) metal dominated by low-frequency and long-wavelength components of the spin fluctuations (SF). Even though the Stoner factor for  $\text{Sr}_2\text{RuO}_4$  also indicates the closeness to the ferromagnetism, the SF in  $\text{Sr}_2\text{RuO}_4$  are different from those in  $\text{CaRuO}_3$ . The results combined with the previous  $^{17}\text{O}$  NMR study in  $\text{Sr}_2\text{RuO}_4$  indicate that the *in-plane* low-frequency components of SF are exchange enhanced without any significant  $q$  dependence due to 2D electronic character (2D nearly FM), while the *out-of-plane* low-frequency component of SF shows the existence of antiferromagnetic (AFM) SF between layers at low temperature. We propose that this evolution from 3D to 2D nearly FM SF is relevant to the onset of spin-triplet superconductivity in  $\text{Sr}_2\text{RuO}_4$ . The 2D nearly FM SF in the in-plane  $4d_{xy}$ - $p_\pi$  band may play a significant role for the stabilization of parallel spin pairing state within the basal plane among various representations of spin-triplet order parameter in  $\text{Sr}_2\text{RuO}_4$ . [S0163-1829(99)05041-9]

### I. INTRODUCTION

Since the discovery of superconductivity in the copper-free layered perovskite  $\text{Sr}_2\text{RuO}_4$ <sup>1</sup> and the identification of the spin-triplet  $p$ -wave superconductivity in the compound,<sup>2</sup> much attention has been paid to the anomalous magnetic and transport properties of  $\text{Sr}_2\text{RuO}_4$  and related ruthenium oxides. A series of ruthenium oxides  $(\text{Sr,Ca})_{n+1}\text{Ru}_n\text{O}_{3n+1}$  have been known to show rich properties: a ferromagnetic (FM) metal, an antiferromagnetic (AFM) insulator and a superconductor. Especially, understanding of their magnetic properties in these ruthenates allows us to gain insight into the occurrence of the spin-triplet superconductivity in  $\text{Sr}_2\text{RuO}_4$ .

$\text{SrRuO}_3$  and  $\text{CaRuO}_3$ , which are  $n = \infty$  members of the series, have nearly cubic and slightly distorted cubic perovskite structure, respectively. Although both the ruthenates exhibit metallic behavior,<sup>3,4</sup> their magnetic properties are quite different:  $\text{SrRuO}_3$  is a FM metal with the Curie temperature  $T_C = 160$  K,<sup>5,6</sup> whereas  $\text{CaRuO}_3$  does not show any magnetic anomalies even at low temperature ( $T$ ).<sup>7</sup> The Ca substitution for the Sr sites makes the  $\text{RuO}_6$  octahedra tilt slightly from the  $c$  axis and rotates around it to fill the extra space of Sr-shared positions, since an ionic radius of Ca is smaller than of Sr. However, each  $\text{RuO}_6$  octahedron is not distorted, then, the angle of Ru-O-Ru bond connecting octahedra directly influences the bandwidth of  $dp\pi^*$  state. With

increasing the Ca substitution for the Sr sites in  $\text{Sr}_{1-x}\text{Ca}_x\text{RuO}_3$ ,  $T_C$  decreases rapidly and no magnetic order is found in  $x \geq 0.7$ , whereas the Curie constant is nearly independent of the Ca concentration.<sup>8,4</sup> Although the AFM interaction of  $\text{CaRuO}_3$  is inferred from the large negative value of the Weiss temperature in the framework of local moment model, any trace of AFM correlation is not evidenced by experiments. While  $\text{Sr}_{1-x}\text{Ca}_x\text{RuO}_3$  conserves the metallic conductivity down to lowest  $T$  without depending on Ca content,<sup>3,4</sup> the other pseudoternary ruthenates  $\text{Sr}_{2-x}\text{Ca}_x\text{RuO}_4$  ( $n=1$ ) (Ref. 9) and  $\text{Sr}_{3-x}\text{Ca}_x\text{Ru}_2\text{O}_7$  ( $n=2$ ) (Refs. 10 and 11) show a metal-insulator transition with increasing the Ca content. The end members  $\text{Ca}_2\text{RuO}_4$  and  $\text{Ca}_3\text{Ru}_2\text{O}_7$  are the AFM-Mott insulators.<sup>9-11</sup> In contrast, a magnetic ground state of  $\text{CaRuO}_3$  is still not clear to date.

Pauli-paramagnetic compound  $\text{RuO}_2$  with the rutile structure<sup>12</sup> is also a good reference compound to understand the magnetic properties in the  $\text{RuO}_6$  octahedron. The electron configuration in the  $\text{RuO}_2$  having the distorted octahedral structure is  $4d^{4+}(t_{2g}^4 e_g^0)$  which is analogous to that in the series of  $(\text{Sr,Ca})_{n+1}\text{Ru}_n\text{O}_{3n+1}$ . Note, however, that the edge sharing of the  $\text{RuO}_6$  octahedra makes conductivity better because of the larger  $4d(t_{2g})-p_\pi$  hybridization through nearly the  $90^\circ$  Ru-O-Ru bridgelike bond<sup>13</sup> than the corner sharing through nearly the  $180^\circ$  Ru-O-Ru linear bond. Consequently,  $\text{RuO}_2$  exhibits a  $T$ -independent susceptibility.<sup>14</sup>

In this paper, we report systematic Ru-NMR studies for  $\text{SrRuO}_3$ ,  $\text{CaRuO}_3$ , and  $\text{RuO}_2$  as well as Ru metal, and compare these results with those reported on the 2D-layered perovskite  $\text{Sr}_2\text{RuO}_4$ .<sup>15</sup> We show that  $\text{CaRuO}_3$  is entitled as a 3D nearly FM metal with a Stoner factor  $\alpha \approx 0.98$ , whereas  $\text{Sr}_2\text{RuO}_4$  as a quasi-2D exchange enhanced metal. We found that spin fluctuations (SF) in  $\text{CaRuO}_3$  are dominated by low-frequency and long-wavelength components, whereas the SF in  $\text{Sr}_2\text{RuO}_4$  reveals a weak wave-number dependence associated with the quasi-2D electronic character. In this sense, it is emphasized that the occurrence of the spin-triplet  $p$ -wave superconductivity in  $\text{Sr}_2\text{RuO}_4$  does not always originate from the 3D-FM SF with analogy to liquid  $^3\text{He}$ . Alternatively, the 2D nearly FM SF in the in-plane  $4d_{xy}-p_\pi$  band may play a significant role for the stabilization of parallel spin pairing state within the basal plane<sup>2</sup> among various representations of spin-triplet order parameter.

## II. EXPERIMENTAL PROCEDURES

Powdered samples of Ru metal (Ru >99.98% purity) and  $\text{RuO}_2$  ( $\text{RuO}_2 > 99.9\%$  purity) were used for NMR measurements.  $\text{SrRuO}_3$  and  $\text{CaRuO}_3$  were prepared by heating appropriate molar ratios of  $\text{SrCO}_3$ ,  $\text{CaCO}_3$ , and  $\text{RuO}_2$  with 3N purity, and calcined at 1223 K for 24 h.<sup>3</sup> After reground, the samples were pressed into pellets again and fired at 1473 K for 24 h. The powdered samples of  $\text{SrRuO}_3$  and  $\text{CaRuO}_3$  were used for magnetization and NMR measurements. The magnetization measurements for  $\text{SrRuO}_3$  and  $\text{CaRuO}_3$  were performed under the magnetic field  $H=1$  kOe, using a superconducting quantum interference device (SQUID) magnetometer. The Curie temperature  $T_C$  of  $\text{SrRuO}_3$  is 160 K and an effective paramagnetic moment  $p_{\text{eff}}$  above  $T_C$  is  $2.68\mu_B$ .  $\text{CaRuO}_3$  has a negative large Weiss temperature  $\theta = -137 \pm 10$  K without exhibiting any magnetic transition down to

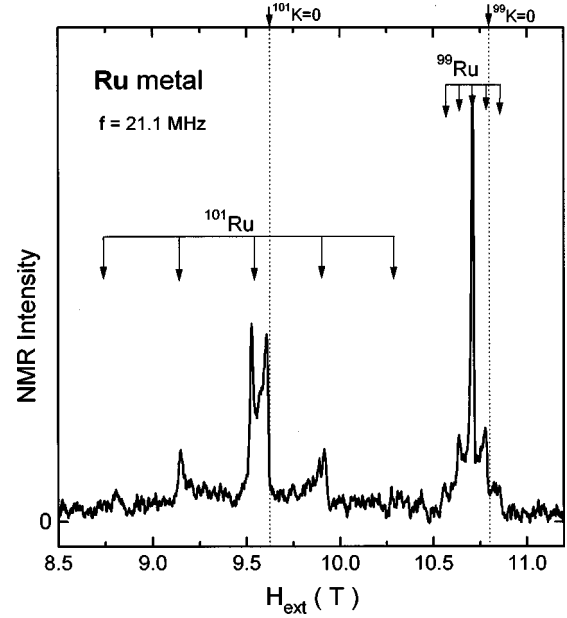


FIG. 1. The Ru-NMR spectrum of hcp Ru metal. Peaks at a lower (higher) field side corresponds to  $^{101}\text{Ru}$ - ( $^{99}\text{Ru}$ -) NMR spectrum articulated by the electric quadrupole interaction.

1.4 K and  $p_{\text{eff}}$  is estimated as  $3.15\mu_B$  in  $T=100-300$  K. These results indicate that the Ru ion is in the tetravalent state  $(4d)^{4+}(t_{2g}^4 e_g^0)$  for the low-spin state ( $S=1$ ), since  $p_{\text{eff}}$ 's for both the ruthenates are close to  $2\mu_B\sqrt{S(S+1)} = 2.83\mu_B$  ( $S=1$ ).

Spin-echo NMR measurements were performed using a conventional phase-coherent-type spectrometer. Nuclear-spin-lattice relaxation time  $T_1$  was obtained by means of the saturation-recovery method.  $T_1$  for all compounds was determined with a single component by fitting the recovery of nuclear magnetization to the following relaxation function for  $I=5/2$ :<sup>16</sup>

$$\frac{M(\infty) - M(t)}{M(\infty)} = 0.028 \exp\left(-\frac{t}{T_1}\right) + 0.178 \exp\left(-\frac{6t}{T_1}\right) + 0.794 \exp\left(-\frac{15t}{T_1}\right). \quad (1)$$

## III. RESULTS AND DISCUSSIONS

### A. Ru metal

Figure 1 indicates the NMR spectrum of  $^{99,101}\text{Ru}$  ( $I=5/2$ ) in Ru metal with the hexagonal close-packed structure. The spectrum at a low- (high-) field side exhibits a typical powder pattern for  $^{101}\text{Ru}$  ( $^{99}\text{Ru}$ ) which is well articulated by the nuclear electric quadrupole (eqQ) interaction. The nuclear quadrupole resonance frequency  $\nu_Q$  of  $^{99}\text{Ru}$  ( $^{101}\text{Ru}$ ) is estimated to be 0.29 (1.68) MHz.

The Knight shift  $K_x$ ,  $K_y$ , and  $K_z$  along  $x$ ,  $y$ , and  $z$  axes, is estimated to be +0.64%, +0.64%, and +0.73%, being  $T$  independent in  $T=1.4-20$  K. The isotropic (anisotropic) part of the Knight shift,  $K_{\text{iso}} = (K_x + K_y + K_z)/3$  [ $K_{\text{aniso}} = (2K_z - K_x - K_y)/6$ ], is estimated to be +0.67% (+0.03%). The

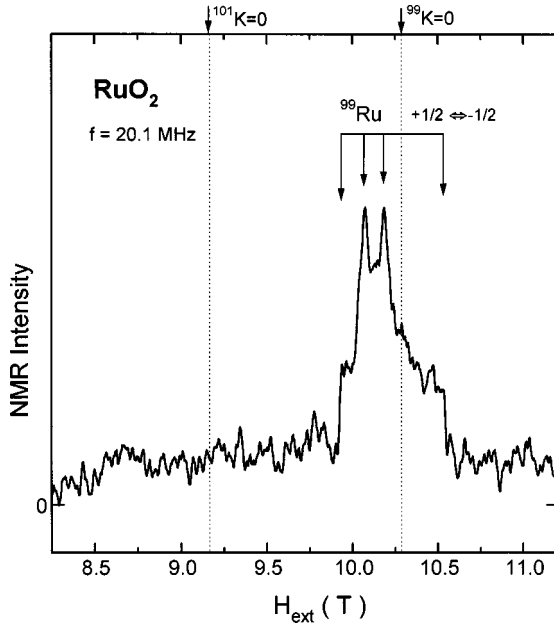


FIG. 2. The Ru-NMR spectrum of  $\text{RuO}_2$  with the rutile structure. This spectrum arises from the  $\phi(+1/2) \leftrightarrow \phi(-1/2)$  transition affected by the nuclear electric quadrupole interaction with a large asymmetric parameter  $\eta$ . Arrows denote resonance fields where two peaks and edges appear in a powder pattern. They are calculated using  $\eta \sim 0.74$  and  ${}^{99}\nu_Q \sim 3.18$  MHz.

$T$ -independent  $K_{\text{iso}}$  with a positive value is due to dominance of the  $4d$  orbital and/or the  $5s$  contributions, consistent with the previous report.<sup>17</sup>

Figure 6 indicates the  $T$  dependence of  ${}^{101}(1/T_1)$  that follows a  $T$ -linear behavior. A constant value of  ${}^{101}(T_1 T)^{-1}$  is two orders of magnitude smaller than that reported in  $\text{Sr}_2\text{RuO}_4$ .<sup>15</sup> Apparently, a dominant relaxation process in the Ru metal is not open to the  $4d$ -spin channel, but to the  $4d$ -orbital and/or the  $5s$ -spin channels.

### B. $\text{RuO}_2$

Figure 2 shows the  ${}^{99}\text{Ru}$ -NMR spectrum arising from the  $\phi(+1/2) \leftrightarrow \phi(-1/2)$  transition affected by the eqQ interaction with a large asymmetric parameter  $\eta$ . Arrows denote resonance fields where two peaks and edges appear in a powder pattern. They are calculated using  $\eta \sim 0.74$  and  ${}^{99}\nu_Q \sim 3.18$  MHz. The articulated spectral structure from other satellite peaks for  ${}^{99}\text{Ru}$  was not observed due to smearing out by large  $\eta$ , and the entire spectrum for  ${}^{101}\text{Ru}$  was not detectable due to the broadening by the large eqQ interaction originating from large nuclear quadrupole moment,  ${}^{101}Q$  of  ${}^{101}\text{Ru}$  ( ${}^{101}Q/{}^{99}Q \sim 5.8$ ). The large value of  $\eta$  is associated with the distorted structure in the  $\text{RuO}_6$  octahedron.<sup>18</sup>

The Knight shift  $K_{\text{obs}}$  is  $T$  independent with a positive value of  $+1.59\%$  in  $T=1.4\text{--}20$  K. It should be noted that  $K_{\text{obs}}=1.59\%$  is comparable to an estimated value of the orbital Knight shift  $K_{\text{orb}} \sim 1.08\%$  in  $\text{Sr}_2\text{RuO}_4$ .<sup>15</sup>  ${}^{99}(T_1 T)^{-1}$  stays constant in  $T=1.4\text{--}20$  K. In Fig. 6,  ${}^{101}(T_1 T)^{-1}$  estimated from the relation of  $({}^{101}\gamma_n/{}^{99}\gamma_n)^2 \cdot {}^{99}(T_1 T)^{-1}$  is plotted, being comparable with the value in Ru metal. Since an orbital contribution in  ${}^{101}(T_1 T)^{-1}$  is negligibly smaller than a value calculated using the density of states,<sup>19</sup>  ${}^{101}(T_1 T)^{-1}$  is

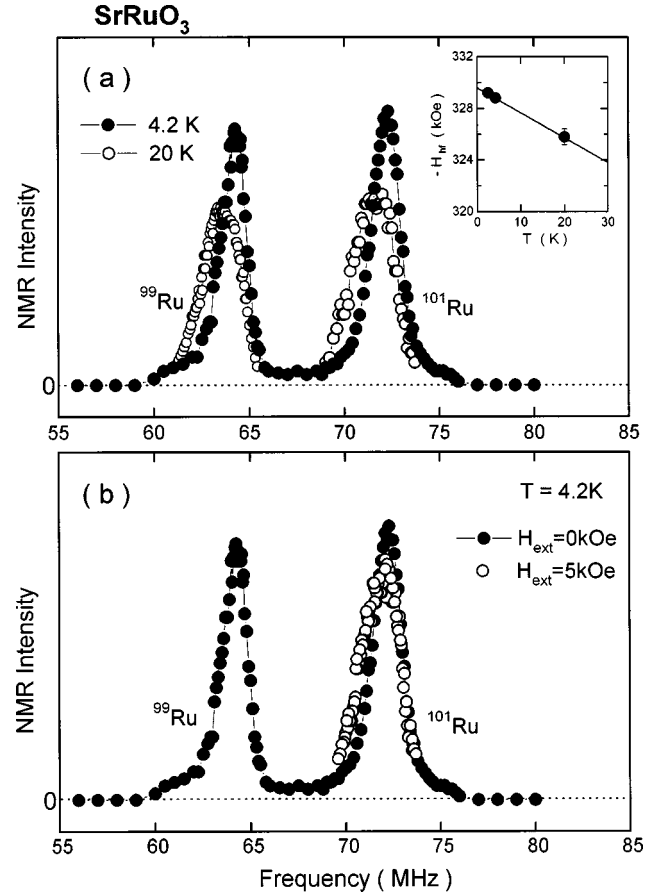


FIG. 3. The Ru-NMR spectra in the ferromagnetic state of  $\text{SrRuO}_3$  at zero field (a) at 4.2 and 20 K. The hyperfine field  $H_{\text{hf}}$  extrapolated to  $T \rightarrow 0$  K is estimated to be  $-329.6$  kOe from  $H_{\text{hf}}$  vs  $T$  plot in the inset. (b) The spectra at the magnetic field  $H_{\text{ext}} = 0$  and 5 kOe. Application of small external field makes the spectrum shift to lower frequency side, which evidences the negative sign of  $H_{\text{hf}}$ .

hence expected to be dominated by the  $5s$ -spin contribution. In  $\text{RuO}_2$ , the  $4d$ -spin contribution is not seen in the Knight shift and  ${}^{101}(1/T_1)$  as well as in Ru metal.

### C. $\text{SrRuO}_3$

Figure 3(a) indicates the Ru-NMR spectra at zero field in the FM state at 4.2 and 20 K. The ratio of two resonance frequencies  $72.3/64.2$  MHz is equivalent to the ratio of the gyromagnetic ratio,  ${}^{101}\gamma_n/{}^{99}\gamma_n = 1.12$ , and an intensity ratio is nearly the same as the ratio of the natural abundance (NA) for the two isotopes,  ${}^{101}\text{NA}/{}^{99}\text{NA} = 1.35$ . Therefore two peaks arise from  ${}^{99}\text{Ru}$  and  ${}^{101}\text{Ru}$  with the same internal hyperfine field  $H_{\text{hf}}$ . Note that their spectral widths are magnetic in origin. If a possible distribution of electric-field gradient were responsible for their spectral broadening, a ratio of width should follow the ratio of nuclear quadrupole moment  ${}^{101}Q/{}^{99}Q = 5.8$ . This is not the case, in fact. Application of small external field makes the spectrum shift to lower frequency side as indicated in Fig. 3(b), which evidences the negative sign of  $H_{\text{hf}}$ . The spectrum slightly shifts to lower frequency side upon heating as indicated in Fig. 3(a). An averaged value of  $H_{\text{hf}}$  is estimated to be  $-329.6$  kOe from an extrapolation to  $T \rightarrow 0$  K as in the inset of the figure.

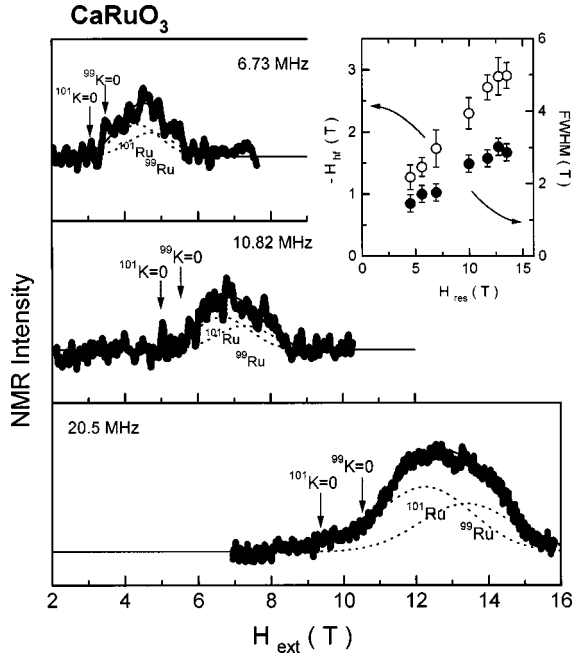


FIG. 4. The Ru-NMR spectra at three frequencies  $f=6.73$ , 10.82, and 20.5 MHz and at 4.2 K. These spectra are widely broadened with a large  $K_{\text{obs}}$ . All the spectra are well reproduced by two Gaussian  $^{99}\text{Ru}$  and  $^{101}\text{Ru}$  spectra as fit by dashed lines. We assumed that the total-intensity ratio and FWHM ratio of the two Gaussians are fixed to  $^{101}\text{NA}/^{99}\text{NA}=1.35$  and  $^{101}\gamma_n/^{99}\gamma_n=1.12$ , respectively. FWHM and  $H_{\text{hf}}$  are fitting parameters. As seen in the inset, the magnitudes of  $H_{\text{hf}}$  and FWHM increase as  $H_{\text{res}}$  increases.

The  $H_{\text{hf}}$  in 4d-transition metals is expressed to be  $H_{\text{hf}}=(A_{\text{hf}}/N_A\mu_B)M_0$ , where  $A_{\text{hf}}$ ,  $N_A$ , and  $M_0$  are the hyperfine coupling constant, the Avogadro's number, and the FM saturation moment, respectively. If we use  $M_0\sim 1.1\pm 0.4\mu_B$  reported in the literatures,<sup>6,20</sup>  $A_{\text{hf}}$  is estimated to be about  $-300\pm 60$  kOe/ $\mu_B$  in the FM state which is close to that for a Ru impurity in the FM state of Fe.<sup>21</sup>

#### D. CaRuO<sub>3</sub>

##### 1. NMR spectrum and Knight shift

Figure 4 indicates the Ru-NMR spectra at three frequencies  $f=6.73$ , 10.82, and 20.5 MHz, which are widely broadened with a large  $K_{\text{obs}}$  at 4.2 K. These spectral widths with no structure increase as frequency  $f$  or magnetic field  $H_{\text{res}}$  increases. Here  $^{99,101}H_{\text{res}}=f/^{99,101}\gamma_n-H_{\text{hf}}$ . This is in contrast to the case for the nonmagnetic Ru metal and RuO<sub>2</sub>. The increase in full width at half maximum (FWHM) with increasing  $H_{\text{res}}$  does not originate from the eqQ interaction, but mainly from  $K_{\text{aniso}}$ . This is because if FWHM originated from the eqQ interaction,  $\text{FWHM}\propto 1/H_{\text{res}}$  should be expected. All the spectra are well reproduced by two Gaussian  $^{99}\text{Ru}$  and  $^{101}\text{Ru}$  spectra as indicated in Fig. 4. The total-intensity ratio and FWHM ratio of the two Gaussians are fixed to  $^{101}\text{NA}/^{99}\text{NA}=1.35$  and  $^{101}\gamma_n/^{99}\gamma_n=1.12$ , respectively. FWHM and  $H_{\text{hf}}$  are fitting parameters. As seen in the inset, the magnitudes of  $H_{\text{hf}}$  and FWHM increase as  $H_{\text{res}}$  increases.

In general, magnetization under magnetic field  $H$ ,  $M_{\text{obs}}(H)$  consisting of 5s-spin, 4d-orbital, and 4d-spin

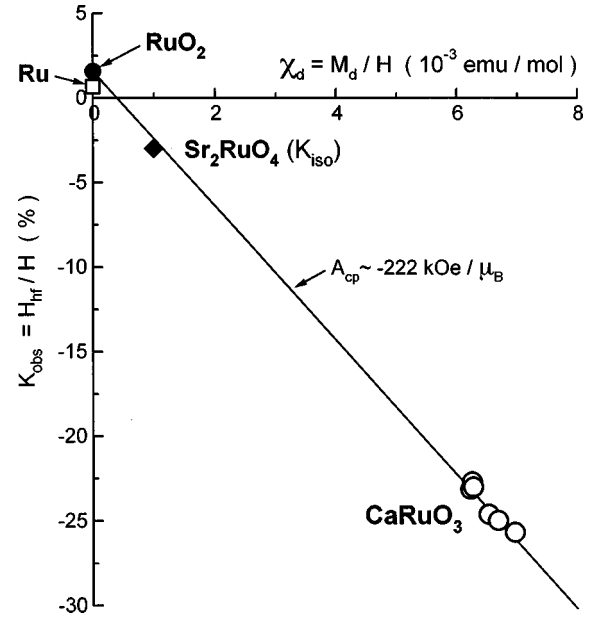


FIG. 5. Knight shift vs susceptibility  $[M_d(H)/H]$  with an implicit parameter of the external field  $H$ . The hyperfine coupling constant due to the inner core polarization  $A_{\text{cp}}\approx -222\pm 50$  kOe/ $\mu_B$  is estimated from a slope of linear line when  $K_{5s}+K_{\text{orb}}$  is assumed to be the same value as  $K_{\text{obs}}=+1.59\%$  in RuO<sub>2</sub>. This value is close to  $A_{\text{hf}}\sim -300\pm 60$  kOe/ $\mu_B$  in the FM state of SrRuO<sub>3</sub>. Note that the Knight shift for Sr<sub>2</sub>RuO<sub>4</sub> lies on the same line of  $K_{\text{obs}}$  vs  $\chi_{\text{obs}}$  plot as that for CaRuO<sub>3</sub>.

( $M_d$ ) contributions is given by

$$M_{\text{obs}}(H)=(\chi_{5s}+\chi_{\text{orb}})H+M_d(H). \quad (2)$$

The hyperfine field  $H_{\text{hf}}$  at the Ru site is also expressed by the sum of the 5s-spin ( $H_{5s}$ ), the 4d-orbital ( $H_{\text{orb}}$ ), and the 4d-spin ( $H_d$ ) contributions as

$$H_{\text{hf}}=H_{5s}+H_{\text{orb}}+H_d=\left(\frac{A_{5s}}{N_A\mu_B}\chi_{5s}+\frac{A_{\text{orb}}}{N_A\mu_B}\chi_{\text{orb}}\right)H \\ +\frac{A_{\text{cp}}}{N_A\mu_B}M_d(H)=(K_{5s}+K_{\text{orb}})H+\frac{A_{\text{cp}}}{N_A\mu_B}M_d(H), \quad (3)$$

where  $K_i=(A_i/N_A\mu_B)\chi_i$  ( $i=5s$ , orb, and  $d$ ), and the hyperfine-coupling constant  $A_{\text{cp}}$  is due to the inner-core polarization induced by 4d spins. From Eq. (3), the Knight shift  $K_{\text{obs}}$  at the Ru site is given by

$$K_{\text{obs}}=\frac{H_{\text{hf}}}{H}=K_{5s}+K_{\text{orb}}+\frac{A_{\text{cp}}}{N_A\mu_B}\frac{M_d(H)}{H}. \quad (4)$$

As shown in Fig. 5,  $K_{\text{obs}}$  is plotted against  $M_d(H)/H$  for CaRuO<sub>3</sub> with an implicit parameter of  $H$ . Here  $\chi_{5s}+\chi_{\text{orb}}$  is assumed to be  $T$ -independent part in Curie-Weiss behavior [ $\chi_0\sim 0.7\times 10^{-3}$  (emu/mol) (Ref. 4)], and then  $M_d(H)$  is estimated by subtracting  $\chi_0H$  from the observed magnetization  $M_{\text{obs}}$  (Ref. 4) in Eq. (2). If we assume  $K_{5s}+K_{\text{orb}}$  in Eq. (4) to be the same value as  $K_{\text{obs}}=+1.59\%$  in RuO<sub>2</sub>,  $A_{\text{cp}}\approx -222\pm 50$  kOe/ $\mu_B$  is estimated from a slope in Fig. 5. This value is between  $-345$  kOe/ $\mu_B$  (Pd metal) and



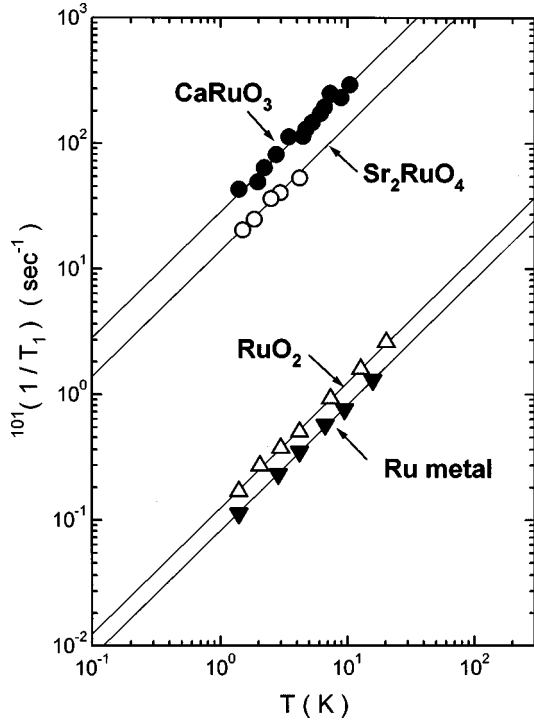


FIG. 6.  $T$  dependence of  $^{101}(1/T_1)$  for Ru metal,  $\text{RuO}_2$ , and  $\text{CaRuO}_3$  together with that for  $\text{Sr}_2\text{RuO}_4$  (Ref. 15).  $^{101}(1/T_1)$  in  $\text{RuO}_2$  is estimated from the experimental values of  $^{99}(1/T_1)$  using the relation of  $(^{101}\gamma_n/^{99}\gamma_n)^2 \cdot ^{99}(1/T_1)$ .  $^{101}(1/T_1)$  in  $\text{Sr}_2\text{RuO}_4$  is the isotropic component of  $^{101}(1/T_1)_{\text{ab,c}}$  (Ref. 15).  $^{101}(T_1T)^{-1}$ 's in  $\text{CaRuO}_3$  and  $\text{Sr}_2\text{RuO}_4$  are two orders of magnitude larger than those values in Ru metal and  $\text{RuO}_2$ .

–162 kOe/ $\mu_B$  (Rh metal), being close to  $A_{\text{hf}} \sim -300 \pm 60$  kOe/ $\mu_B$  in the FM state of  $\text{SrRuO}_3$ .

Using the spin part of Knight shift  $K_d \approx -25\%$  at 4.2 K and  $A_{\text{hf}}$  in  $\text{CaRuO}_3$ , it should be noted that a ratio of  $\chi_d/\chi_{\text{band}} = 1/(1-\alpha) \approx 58.8$  is strongly exchange enhanced. Here  $\chi_d$  and  $\chi_{\text{band}}$  are the spin susceptibility estimated from  $K_d$  and the one calculated from the band calculation result,<sup>22</sup> respectively. A Stoner factor  $\alpha \approx 0.98$  for  $\text{CaRuO}_3$  is close to 1, entitling it as a nearly FM material.

It is noteworthy that the Knight shift for  $\text{Sr}_2\text{RuO}_4$  lies on the same line of  $K_{\text{obs}}$  vs  $\chi_{\text{obs}}$  plot as that for  $\text{CaRuO}_3$  (Fig. 5). It suggests that  $4d$  spins play vital roles on the magnetic and transport properties not only in  $\text{SrRuO}_3$  and  $\text{CaRuO}_3$  but also in  $\text{Sr}_2\text{RuO}_4$ .

## 2. Nuclear-spin-relaxation rate $1/T_1$

Figure 6 displays the  $T$  dependence of  $^{101}(1/T_1)$  for  $\text{CaRuO}_3$  at  $H_{\text{res}} = 12.6$  T in  $T = 1.4$ –11 K together with the results for  $\text{Sr}_2\text{RuO}_4$ , Ru metal, and  $\text{RuO}_2$ .  $^{101}(1/T_1)$  proportional to  $T$  has a large value of  $^{101}(T_1T)^{-1} = 28$  ( $\text{s}^{-1}\text{K}^{-1}$ ). The constant values of  $^{101}(T_1T)^{-1}$  for  $\text{CaRuO}_3$  and  $\text{Sr}_2\text{RuO}_4$  (Ref. 15) are two orders of magnitude larger than in the nonmagnetic Ru metal and  $\text{RuO}_2$ .

$(T_1T)^{-1}$  in ruthenium oxides is generally decomposed by the  $5s$ -spin, the  $4d$ -orbital, and the  $4d$ -spin contribution by the following relation:

$$\left(\frac{1}{T_1T}\right)_{\text{obs}} = \left(\frac{1}{T_1T}\right)_s + \left(\frac{1}{T_1T}\right)_{\text{orb}} + \left(\frac{1}{T_1T}\right)_d. \quad (5)$$

A sum of  $(T_1T)_s^{-1}$  and  $(T_1T)_{\text{orb}}^{-1}$  is anticipated to be comparable to  $^{101}(T_1T)_{\text{obs}}^{-1} = 0.12$  ( $\text{s}^{-1}\text{K}^{-1}$ ) in  $\text{RuO}_2$ , which is much smaller than  $^{101}(T_1T)_{\text{obs}}^{-1} = 28$  ( $\text{s}^{-1}\text{K}^{-1}$ ). Furthermore, we estimate a value  $^{101}(T_1T)_{\text{orb}}^{-1} \sim 0.18$  ( $\text{s}^{-1}\text{K}^{-1}$ ) for  $\text{CaRuO}_3$  from the following equation:

$$\left(\frac{1}{T_1T}\right)_{\text{orb}} = \pi k_B \gamma_n^2 \hbar A_{\text{orb}}^2 N_d^2(E_F) \frac{2}{3} f \left(2 - \frac{5}{3} f\right), \quad (6)$$

where  $N_d(E_F) \sim 4.06$  (states/eV/cell/spin) from the band calculation,<sup>22</sup>  $A_{\text{orb}} = 2\mu_B \langle r^{-3} \rangle = 385$  kOe/ $\mu_B$  from the Hartree-Fock calculation of  $\langle r^{-3} \rangle = 4.2$  (a.u.) for free  $\text{Ru}^{4+}$  with the reduction factor of  $\xi = 3/4$ ,<sup>23</sup> and the fractional factor  $f$  due to the occupation of the  $t_{2g}$  orbitals at the Fermi surface is  $f = 1$  in this case. Therefore it is evident that  $(T_1T)_{\text{obs}}^{-1}$  for  $\text{CaRuO}_3$  is dominated by the  $4d$ -spin contribution  $(T_1T)_d^{-1}$ .

In terms of the random-phase approximation (RPA),  $(T_1T)_d^{-1}$  is described as

$$\left(\frac{1}{T_1T}\right)_d = \pi k_B \gamma_n^2 \hbar K_d^2 \left(\frac{1}{3} f^2 + \frac{1}{2} (1-f^2)\right) R, \quad (7)$$

where  $R$  is the correlation factor in a modified Korringa (MK) relation for exchange enhanced metals.<sup>24,25</sup> This factor is given by<sup>26</sup>

$$R = \left\langle \frac{(1-\alpha_0)^2}{(1-\alpha_{q_0})^2} \right\rangle_{FS}, \quad (8)$$

where  $\alpha_0 = I\chi_0/2$ ,  $\alpha_{q_0} = I\chi_0(\mathbf{q}_0, 0)/2$ , and  $\langle \dots \rangle_{FS}$  means the average over the Fermi surface. Here  $I = U/N_0$  with the intra-atomic Coulomb integral  $U$  and number of sites  $N_0$ ,  $\chi_0$ , and  $\chi_0(\mathbf{q}_0, \omega)$  is the noninteracting spin and dynamical susceptibility at  $\mathbf{q} = 0$  and  $\mathbf{q} = \mathbf{q}_0$ , respectively. The value reflects intimately the  $\mathbf{q}$  dependence of  $\chi(\mathbf{q}, 0)$ . In the case that ferromagnetic SF are significant with  $\alpha_0 \sim 1$ ,  $R \ll 1$ . In the case that antiferromagnetic SF play a crucial role,  $R \gg 1$  for  $\alpha_{\mathbf{Q}}$  close to 1 where  $\mathbf{Q}$  is the AF wave vector. In 2D exchange enhanced Pauli paramagnets where  $\chi(\mathbf{q}, 0)$  exhibits a weak  $\mathbf{q}$  dependence,  $R \sim 1$  without depending on  $\alpha_0$ .

Using  $K_d \sim -25\%$  at  $H_{\text{res}} = 12.6$  T,  $^{101}R \approx 0.15$  is obtained from Eq. (7). Various characteristic parameters in  $\text{CaRuO}_3$  are summarized in Table I and compared with those in a nearly FM metal  $\text{YCo}_2$ .  $\alpha \approx 0.98$  and  $^{101}R \approx 0.15$  indicate that  $\text{CaRuO}_3$  is closer to the FM instability than  $\text{YCo}_2$  ( $\alpha = 0.95$  and  $^{59}R = 0.30$ ).<sup>27</sup> Note that  $N_d(E_F)$  is smaller for  $\text{CaRuO}_3$  than for  $\text{YCo}_2$ , whereas  $\alpha = I \cdot N_d(E_F)$  is larger for the former than for the latter. It is concluded that the electron correlation in  $\text{CaRuO}_3$  is stronger than in  $\text{YCo}_2$ . One may suppose that the large negative  $\theta$  value in  $\text{CaRuO}_3$  suggests a strong AFM interaction. Contrary to this expectation, a much smaller  $^{101}R \approx 0.15$  and  $\alpha \approx 0.98$  close to 1 evidence that  $\text{CaRuO}_3$  is the 3D nearly FM metal dominated by SF with low frequencies and long-wavelength components.

## E. Comparison with the magnetic properties in the superconducting $\text{Sr}_2\text{RuO}_4$

The NMR results for  $\text{CaRuO}_3$  are compared with those for  $\text{Sr}_2\text{RuO}_4$  (Ref. 15) with the similar  $\text{RuO}_6$  octahedron.

TABLE I. Various characteristic parameters in  $\text{Sr}_2\text{RuO}_4$  and  $\text{CaRuO}_3$ , together with those values of liquid  $^3\text{He}$  at 27 bars (Ref. 30) and the nearly ferromagnetic  $\text{YCo}_2$  (Ref. 27). The 2D nearly FM SF in  $\text{Sr}_2\text{RuO}_4$  are distinguished from the 3D nearly FM SF with dominant low frequencies and long-wavelength components in  $\text{CaRuO}_3$ ,  $\text{YCo}_2$ , and liquid  $^3\text{He}$ .

	$\text{Sr}_2\text{RuO}_4$	$\text{CaRuO}_3$	$^3\text{He}$ (Ref. 30)	$\text{YCo}_2$ (Ref. 31)
$N_d(E_F)$ (state/eV)	4.36 (Ref. 31)	4.06 (Ref. 22)		5.55
$\gamma_{\text{exp}}$ (mJ/mol K <sup>2</sup> )	39 (Ref. 1)	73 (Ref. 4)		36
$\gamma_{\text{band}}$ (mJ/mol K <sup>2</sup> )	10.3	9.54		13.0
$\gamma_{\text{exp}}/\gamma_{\text{band}}$	3.8	7.65	5.26	2.8
$\chi_{d,\text{exp}}$ ( $10^{-4}$ emu/mol) $_{T \rightarrow 0}$	9.7	77		35.4
$\chi_{d,\text{band}}$ ( $10^{-4}$ emu/mol)	1.41	1.31		1.79
$\chi_{d,\text{exp}}/\chi_{d,\text{band}}$	6.9	58.8	21	19.8
Wilson ratio; $R_W$	1.8	7.7	4	7.1
Stoner factor; $\alpha$	0.86	0.98	0.95	0.95
$^{101}R_{ab}$	2.1	0.15		$^{59}R=0.30$
$^{101}R_c$	4.2	0.15		$^{59}R=0.30$
$^{17}R_{\parallel,\perp}$	0.8 (Ref. 26)			
$^{17}R_c$	11 (Ref. 26)			

The respective Stoner factors are  $\alpha \approx 0.98$  and  $\approx 0.86$  for  $\text{CaRuO}_3$  and  $\text{Sr}_2\text{RuO}_4$ , indicating that the magnetic susceptibility is more significantly enhanced than a respective value based on the band calculation. A substantial difference appears in  $^{101}R$  as shown in Table I. Extremely small value of  $^{101}R \approx 0.15$  and  $\alpha \approx 0.98$  reveal that  $\text{CaRuO}_3$  is a 3D nearly FM metal. By contrast,  $^{101}R_{ab} \approx 2.1$  and  $^{101}R_c \approx 4.2$  in  $\text{Sr}_2\text{RuO}_4$  are even larger than 1, even though its Stoner factor points to the closeness to ferromagnetism. Here the  $c$ -axis component  $^{101}R_c$  is about twice larger than the  $ab$ -plane component  $^{101}R_{ab}$ , suggesting that SF in  $\text{Sr}_2\text{RuO}_4$  might be anisotropic. The result that  $^{101}R_{ab,c}$  for  $\text{Sr}_2\text{RuO}_4$  is larger than 1 demonstrates that the SF in  $\text{Sr}_2\text{RuO}_4$  is different from those in the 3D nearly FM  $\text{CaRuO}_3$  and/or liquid  $^3\text{He}$ . It is also suggested from the fact that  $R_W$  in  $\text{Sr}_2\text{RuO}_4$  is much smaller than in the 3D nearly ferromagnetic materials indicated in Table I.

Recently,  $^{17}\text{O}$ -NMR studies in  $\text{Sr}_2\text{RuO}_4$  clarified that there exists anisotropic SF in the  $\text{RuO}_2$  plane.<sup>26</sup> At low temperatures, the in-plane components of the correlation factor  $^{17}R_{\perp} \approx ^{17}R_{\parallel} \approx 0.8$  are lower than and/or close to 1, whereas  $\text{CaRuO}_3$  dominated by 3D-FM SF shows quite smaller than 1. The result indicates that the *in-plane* low-frequency components of the dynamical spin susceptibility  $^{17}\chi''(q, \omega)_{\parallel,\perp}$ , which is dominated by  $d_{xy}$  orbital character, are exchange enhanced with weak  $q$  dependence (2D nearly FM) as described in the above section. By contrast, its out-of-plane component  $^{17}R_c \approx 11$  is one order of magnitude larger than in-plane components, indicating that the *out-of-plane* low-frequency component of the dynamical spin susceptibility  $^{17}\chi''(q, \omega)_c$ , which is dominated by  $d_{xz,yz}$  orbital character, shows the development of AFM SF upon cooling below  $T^* \sim 130$  K where the  $c$ -axis resistivity shows a metallic behavior.<sup>26</sup> Consequently, we concluded that 2D nearly FM SF is dominant in the  $\text{RuO}_2$  plane, whereas interlayer AFM SF along the  $c$  axis below  $T^*$ . We propose that  $^{101}R_{ab,c} > 1$  may reflect some average on this highly anisotropic SF revealed by the  $^{17}\text{O}$ -NMR measurements. This is because the  $H_{\text{hf}}$  at the Ru site is produced mainly by the isotropic inner-

core polarization induced by  $4d$  spins, which averages the SF at the Ru site. On the other hand, the  $H_{\text{hf}}$  at the O(1) site originates from the dipole interaction with spins on the  $p\pi_{\perp}$  and  $p\pi_c$  orbitals hybridized with the  $d_{xy}$  and  $d_{xz,yz}$ , respectively. This orbital dependent anisotropic hyperfine interaction at the O(1) sites enables us to probe the anisotropic SF. The existence of the *in-plane* FM SF is also evidenced by the identical  $T$  dependence between  $^{17}(1/T_1)$  at the O(1) site and  $^{101}(1/T_1)$  at the Ru site studied by Imai *et al.*<sup>28</sup>

Soon after the discovery of the superconductivity in  $\text{Sr}_2\text{RuO}_4$ , Rice and Sigrist proposed that  $\text{Sr}_2\text{RuO}_4$  is the spin-triplet superconductor with analogy to the superfluid  $^3\text{He}$ ,<sup>29</sup> where the 3D-FM SF mediates a spin-triplet pair. However, as discussed above, the SF in  $\text{Sr}_2\text{RuO}_4$  should be distinguished from the 3D-FM SF with dominant low frequencies and long-wavelength components, since exhibiting remarkable anisotropic SF. This anisotropic SF may be relevant to an orbital dependent electronic structure. The 2D nearly FM SF in the in-plane  $4d_{xy}$ - $p\pi$  band may play a significant role for the stabilization of parallel spin pairing state within the basal plane<sup>2</sup> among various representations of spin-triplet order parameter.

#### IV. CONCLUSIONS

We reported systematic Ru-NMR studies on the ferromagnetic  $\text{SrRuO}_3$  and exchange enhanced paramagnetic  $\text{CaRuO}_3$  as well as nonmagnetic Ru metal and  $\text{RuO}_2$ , and compared the obtained results with those in spin-triplet  $p$ -wave superconductor  $\text{Sr}_2\text{RuO}_4$ . The results for  $\text{RuO}_2$  and Ru metal reveal that the Knight shift  $K_{\text{obs}}$  with a positive value of  $\sim +1\%$  and the small nuclear-spin-lattice relaxation rate  $^{101}(1/T_1)$  are not affected by the  $4d$ -spin contribution, but dominated by the  $4d$ -orbital and/or the  $5s$ -spin contributions. In  $\text{SrRuO}_3$ , the internal field at the Ru site in the ferromagnetic (FM) state below  $T_C = 160$  K is  $-329.6$  kOe at  $T \rightarrow 0$ , and the negative hyperfine coupling constant  $A_{\text{hf}} \sim -300 \pm 60$  kOe/ $\mu_B$  originates mainly from the inner-core polarization effect. In  $\text{CaRuO}_3$  that is proved

to remain paramagnetic down to 1.4 K, the field  $H$  dependence of Knight shift  $K_{\text{obs}}(H)$  is well scaled to the measured susceptibility with  $A_{\text{hf}} \approx -222 \pm 50$  kOe/ $\mu_B$  through the inner-core polarization. The spin susceptibility  $\chi_d$  deduced from the Knight shift in CaRuO<sub>3</sub> is nearly two orders of magnitude larger than the value  $\chi_{\text{band}}$  obtained from the band calculation. The Stoner factor  $\alpha \approx 0.98$  is estimated from the ratio of  $\chi_d/\chi_{\text{band}} \approx 58.8$ , entitling CaRuO<sub>3</sub> as the nearly FM metal. The  $^{101}(1/T_1)$  in CaRuO<sub>3</sub> comparable to that in Sr<sub>2</sub>RuO<sub>4</sub> is two orders of magnitude larger than those values in Ru metal and RuO<sub>2</sub>. This enhancement is due to the FM spin fluctuations (SF). From the modified-Korringa relation, the correlation factor  $^{101}R \approx 0.15$  was deduced to be very small. CaRuO<sub>3</sub> was shown to be in the nearly FM regime, dominated by low-frequencies and long-wavelength SF components.

The anisotropic correlation factor ( $^{101}R_{\text{ab}} \approx 2.1$  and  $^{101}R_{\text{c}} \approx 4.2$ ) in Sr<sub>2</sub>RuO<sub>4</sub> are one order of magnitude larger than  $^{101}R \approx 0.15$  in CaRuO<sub>3</sub>, nevertheless the Stoner factors for both materials point to the closeness to ferromagnetism. The results combined with the previous  $^{17}\text{O}$  NMR study indicate that the *in-plane* low-frequency components of the dynamical spin susceptibility, which is dominated by  $d_{xy}$  orbital character, are exchange enhanced without any significant  $q$  dependence due to 2D electronic character (2D nearly-FM), by contrast, the *out-of-plane* low-frequency component of the dynamical spin susceptibility, which is dominated by

$d_{xz,yz}$  orbital character, shows the existence of AFM SF between the layers at low temperature. Therefore we reinforce that the 2D nearly FM SF in Sr<sub>2</sub>RuO<sub>4</sub> should be distinguished from the 3D low frequencies and long-wavelength FM SF in CaRuO<sub>3</sub>. In this sense, the occurrence of spin-triplet  $p$ -wave superconductivity in Sr<sub>2</sub>RuO<sub>4</sub> does not always originate from the 3D-FM SF with analogy to liquid  $^3\text{He}$ . Alternatively, the 2D nearly FM SF in the in-plane  $4d_{xy}$ - $p$   $\pi$  band may play a significant role for the stabilization of parallel spin pairing state within the basal planes among various representations of spin-triplet order parameter. These characteristic SF's provide an interesting scenario for the spin-triplet  $p$ -wave superconductivity in Sr<sub>2</sub>RuO<sub>4</sub> that is mediated by the *in-plane* short-range SF with 2D nearly FM character based on the Hund's rule coupling between the  $d_{xy}$  and  $d_{yz,zx}$  orbitals.

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